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 6 So long as the magnetic pole carries no electric charge or electric charge $\ll 137e$, the constant force (3) leads to linear acceleration along magnetic field lines. This rectilinear acceleration leads to electromagnetic radiation at the negligible rate

$$P_{1oss} = \frac{2}{3} \frac{g^2}{c^3} \left(\frac{gB}{M}\right)^2 = \frac{2}{3} \frac{g^2}{(Mc^2)^2} gBP_{in} \ll P_{in}.$$

If the pole carries a large electric charge ~137*e*, it spirals about magnetic field lines. The radiation due to transverse acceleration, γ^2 times larger than that due to rectilinear acceleration, is still negligible for any but the lightest magnetic poles.

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Splitting and Structure of the Giant Quadrupole Resonances in Deformed Nuclei

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We have performed microscopic calculations of the low-lying and high-lying $K^{\pi} = 0^+$, 1⁺, and 2⁺ states in deformed rare-earth nuclei. The centroids of the isoscalar giant quadrupole resonance in ¹⁶⁰Dy, ¹⁷⁰Yb, and ¹⁸⁴W are at 11.58, 11.44, and 11.22 MeV, respectively. A broadening of these resonances due to the deformation is predicted which varies appreciably in the different nuclei. About 20% of the monopole strength is found in the same energy range.

In the last two years giant resonances of multipolarity different from the well-known dipole resonance have been detected experimentally by inelastic electron and proton scattering.¹ A review of this field may be found in Satchler.² Until now most of the experimental work has been done on spherical nuclei. The isoscalar giant quadrupole resonance (GQR), e.g., has been found at an excitation energy which agrees qualitatively with the prediction of Bohr and Mottelson.³ In the special cases of doubly closed-shell nuclei random-phase-approximation (RPA) calculations^{4, 5} give semiquantitative agreement with the experimental data.

Very recently the GQR has also been found experimentally in deformed rare-earth nuclei.⁶⁻⁸ In these experiments the width of the GQR was found to be broader than in the spherical isotopes. In the case of the giant dipole resonances this is an experimentally well established and also theoretically understood phenomenon. The situation, however, is controversial for the GQR: The dynamic collective model predicts⁹ a splitting into five levels as a result of the deformation. In a schematic calculation using the harmonic-oscillator model and a quadrupole-quadrupole interaction one gets a splitting into three different levels and a broadening of 6 or 2 MeV depending on the quadrupole-quadrupole force used. Neither the transition probability nor the absolute energies are reported in Ref. 8.

In this Letter we present results of a realistic microscopic calculation within the quasiparticle-RPA of the low-lying and high-lying $K^{\pi} = 0^+$, 1^+ , and 2^+ (intrinsic) states. We used data for the low-lying states to check the input data of our theory such as single-particle energies, effective particle-hole and particle-particle interactions, and the size of the configuration space. This is a generalization of previous calculations in spherical nuclei.⁴ For the effective interactions density-dependent zero-range forces have been used. The force parameters and the singleparticle wave functions are the same as in a recent analysis of isotope shifts and $K^{\pi} = 0^+$ excitations.¹⁰ We do not repeat here the well-known formulas of the quasiparticle-RPA theory, which may be found in Ref. 10. We used the single-particle level schemes given in Ogle et al.¹¹ A diagonalization in a space which includes all particle-hole pairs within an energy range of $2\hbar\omega_0$ above and below the Fermi surface is not yet possible with our computing facilities. Therefore the following procedure for selection of pairs was chosen: (i) Any combination within the interval $\epsilon_{p} \pm \hbar \omega_{0}$ is included; (ii) the particle-hole pairs outside this energy interval are included in the order of decreasing absolute value of the single-particle matrix elements. This procedure

TABLE I. Energies and transition probabilities of ¹⁶⁰Dy, ¹⁷⁰Yb, and ¹⁸⁴W. In general only the most collective state of the low-lying levels of each K^{π} combination is given. In the case of the GQR we give the energy of the most collective state and the total strength which generally is distributed over a few levels within an interval of 1 MeV.

Nucleus	кπ	E [MeV]		B(E2,0 ⁺ +2 ⁺) [e ² fm ⁴]		B(EO) [e ² fm ⁴]	
		th	exp	th	exp	th	exp
160 _{Dy}	0+	1.38	1.26	354	220±70 ^a	211	
		10.5		873		921	
	1+	1.58		55			
		11.7		1222			
	2*	1.27	0.97	468	1050±80 ^b		
		13.7		665			
170 _{Yb}	o *	1.14	1.07	394	240±30 ^a	202	
		1.32	1.23	47	190±60 ^a	16	
		9.7		1223		1165	
	1+	2.28		46			
		11.9		1067			
	2*	1.41	1.14	242	940 [°]		
-		13.4		842			
¹⁸⁴ W	o +	1.23	1.00	41	50±5 ^d	42	1.9 0.4 ^a
		1.40	1.32	36			
		9.7		1013		867	
	1	1.82		98			
		11.4		1316	a		
	2	0.94	0.90	154	1250±50 ^u		
		1.45	1.39	198	210±20 ⁴		
		12.6		938			
⁻ Ref. 12. ^b Ref. 13.					~Ref. 14. ^d Ref. 15.		

works well for the $K^{\pi} = 0^+$ case. For the 1^+ and 2^+ levels the restriction is somewhat more stringent.

It should be mentioned that we obtain spurious 0^+ states at zero energy as a result of the consistent use of the particle-particle interaction.¹⁰ A spurious 1^+ state is also reasonably close to zero (e.g., $E_{1+}^2 = -0.1 \text{ MeV}^2$ for ¹⁶⁰Dy).

A summary of our results is given in Table I and in Fig. 1. In the table we give in general only the most collective state of the low-lying levels of each K^{π} combination. In Fig. 1 the $B(E\lambda)$ values have been summed in intervals of 0.5 MeV. The three peaks between 10 and 14 MeV correspond to the $K^{\pi} = 0^+$, 1^+ , and 2^+ components of the quadrupole vibration. Coinciding with the K^{π} $=0^+$ peak there is also a peak in B(E0) since the $K^{\pi} = 0^+$ intrinsic states can be populated or depopulated by monopole transitions, too. The distributions for $^{170}\mathrm{Yb}$ and $^{184}\mathrm{W}$ are very similar. It is important to point out that no effective charges are used. The agreement for $K^{\pi} = 0^+$ is in general better than for $K^{\pi} = 2^+$. It is the effect of the truncation of the configuration space which makes the interaction in the 2^+ case appear to be too weak. A slight renormalization, i.e., increase of the interaction strength, improves the agreement of energy and B(E2) values with experiment. Therefore our present B(E2) values of the giant resonances should be taken as lower limits. The centroids of the GQR are in Dy, Yb, and W at 11.58, 11.44, and 11.22 MeV, respec-



FIG. 1. Distribution of B(E2) strength (solid line) and B(E0) strength (dotted line) for ¹⁶⁰Dy. The $B(E\lambda)$ values have been summed in intervals of 0.5 MeV. The exact locations of the resonance maxima are indicated by arrows.

tively, and the corresponding B(E2) strengths exhaust the energy-weighted sum rule (EWSR) for isoscalar E2 states to 57%, 57%, and 53%, respectively. These values might be compared with the results of several experiments in that region, using hadronic probes, 7,8 which give the GQR around 12 MeV. The experimental B(E2)strength varies from 80% up to 150% of the EWSR. In a (e, e') experiment⁶ the GQR in ¹⁵⁰Nd was found at 11.2 ± 0.2 MeV and the B(E2) value exhausts 85% of the EWSR. If one compares the experimental B(E2) values with the theoretical results one always has to add the B(E0) contribution since present experiments do not distinguish between 0^+ and 2^+ . This gives another 10% of the EWSR. On the other hand these high-lying (intrinsic) states can be excited also by any 2^{λ} transition, especially E4. This might be one reason why different experiments give such strongly differing B(E2) values. To clarify this point one has to perform a distorted-wave Born-approximation analysis similar to that in ²⁰⁸Pb using microscopic wave functions.¹⁶

In our model the width of the giant resonances is not calculated. Therefore one has to assume a shape and a width for each line in order to deduce a broadening of the GQR from our results. If we take Gaussian shapes with a full width at half-maximum of 3.9 MeV as measured⁸ in ¹⁴⁴Sm, we get a broadening of 1.0, 2.3, and 1.4 MeV in Dy, Yb, and W, respectively. If we take a full width at half-maximum of 2.8 MeV as measured⁷ in ¹⁴²Nd, the corresponding numbers are 1.3, 2.9, and 1.4 MeV. These results might be compared with two experimental values: In ¹⁵⁰Nd the broadening measured with electrons⁷ is about 2 MeV, whereas the broadening in ¹⁵⁴Sm measured with α particles is 1 MeV.

In order to get more insight into the structure of the GQR in deformed nuclei we calculated the transition density of these levels into the ground state. This corresponds most closely to the density change of a classical vibration at maximum elongation. In Fig. 2 the microscopically calculated transition densities of the high-lying $K^{\pi} = 0^+$, 1^+ , and 2^+ states are shown. The $K^{\pi} = 0^+$ pattern looks very similar to a classical β vibration. But instead of being small inside the nucleus, the transition density has an appreciable value there as one would expect from a classical breathing mode. Also the $K^{\pi} = 1^+$ and 2^+ excitations show the features of high collectivity, i.e., the microscopic transition densities are very similar to a vibrating liquid drop (γ vibration) with little addi-



FIG. 2. Microscopically calculated transition densities $\rho_K(\mathbf{r})$ of the $K^{\pi} = 0^+$, 1^+ , and 2^+ giant resonances in ¹⁶⁰Dy in units of 10^{-4} fm⁻³. From top to bottom, $K^{\pi} = 0^+$, 1^+ , and 2^+ components of the resonance. Since ρ_K has the same reflection symmetry and dependence on the angle φ as $Y_{2,K}(\theta, \varphi)$, only one quadrant of the *x*-*z* plane is shown. The dash-dotted line indicates the boundary of the nucleus where the density has fallen to half its inside value.

tional structure. This behavior is typical for all nuclei investigated so far. The low-lying collective $K^{\pi} = 0^+$ and 2^+ states, however, deviate strongly from that classical picture.

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Population of High-Lying Three-Nucleon-Cluster States in ¹⁹F and ¹⁹Ne[†]

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The analog reactions ${}^{16}O({}^{10}B, {}^{7}Li) {}^{19}Ne$ and ${}^{16}O({}^{10}B, {}^{7}Be) {}^{19}F$ at 100 MeV have been utilized to study high-excitation, three-nucleon-cluster states in ${}^{19}Ne$ and ${}^{19}F$. Deformed-model calculations have been made in order to predict the energies of such high-lying states in terms of rotational bands with one or more particles in the fp shell. These show that the high-lying levels seen in the data can be explained by $(sd)^2(fp)^1$ and $(fp)^3$ configurations outside an ${}^{16}O$ core.

The mass-19 nuclei, particularly ¹⁹F and ¹⁹Ne, are among the most extensively studied in the light-mass region, both experimentally and theoretically. However, these studies have mainly concentrated on the low-lying positive- and negative-parity states which are now well understood in terms of "bands" arising from $(sd)^3$ and $(p)^{-1}$ $\times (sd)^4$, $(p)^{-3}(sd)^6$, etc. configurations about an ¹⁶O core. It has now become possible to explore more exotic configurations with one or more nucleons in higher shells by using heavy-ion-induced multinucleon transfer reactions. It has been well established^{1,2} that such reactions tend to enhance high-spin transitions to high excitations. Furthermore, the states populated can be explained in terms of the nucleons being transferred as a cluster into configurations with maximum spatial symmetry.

The present study utilizes ¹⁰B-induced threenucleon transfer reactions on ¹⁶O to populate exotic states in the high-excitation region which could have up to three nucleons in the 0f-1p shell, leaving the *sd* shell partially or even totally vacant. Since there is no theoretical information available for such states, a simple rotational model³ has been used to predict energies of excited bands in ¹⁹F based on removing one nucleon from various excited bands in ²⁰Ne. The results, as will be discussed, show that bands based on $(sd)^2(fp)^1$ and $(fp)^3$ configurations outside ¹⁶O can start at surprisingly low excitations and can account for the high-lying unknown levels seen in the data.

The experimental study was performed using a 100-MeV ¹⁰B beam from the Texas A&M University cyclotron and an ¹⁶O gas target. Reaction products were detected and identified by a standard ΔE -E solid-state counter telescope. The typical energy resolution in the ⁷Li and ⁷Be channels was 250-300 keV. Energy calibrations were obtained from known transitions in various outgoing channels. The resulting uncertainty for excitation energies in the high-excitation region is \pm 100 keV.

Figure 1 shows the analog spectra obtained for ¹⁹F and ¹⁹Ne. Below 8 MeV only the $\frac{9+}{2}$ and $\frac{13}{2}$ ⁺ members of the ground-state (g.s.) bands are populated strongly as a result of the spin selectivity of the reactions. The direct-transfer nature of the reactions is evident from the fact that the high-spin members of the $K^{\pi} = \frac{1}{2}$ band, arising from a 0p-shell hole, are seen only very weakly. The weak population of the low-spin members of the g.s. band can be explained by applying the semiclassical theory due to Brink. ^{1,4} The relative transition strengths for the known members of the g.s. band, calculated assuming cluster transfer and using SU(3) (6,0)-symmetry