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Evidence for the Isoscalar Giant Quadrupole Resonance in ^{16}O

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The spectra of 146-MeV α particles scattered inelastically from ^{16}O exhibit a giant-resonance-type structure between excitation energies of 15.9 and 27.3 MeV. The analysis of angular distributions shows its quadrupole nature and yields a strength exhausting about 65% of the isoscalar $E2$ energy-weighted sum rule.

Recently, several experimental¹⁻⁵ and theoretical⁶⁻¹¹ investigations have been published concerning giant quadrupole resonances (GQR) in ^{16}O . Some of these papers deal especially with the question of an isoscalar ($T=0$) GQR excited in (α, γ_0) capture² and inelastic scattering,^{4,5} however, without arriving at completely conclusive results.¹² The (α, γ_0) investigation suffered mainly from the fact that only one decay channel was studied. The ^3He inelastic scattering,⁴ on the

other hand, is not completely isospin selective. A recent study of inelastic α -particle scattering⁵ at 97 MeV which was not subjected to these restrictions has only been able to exclude the existence of a resonance at $63A^{-1/3} = 25$ MeV predicted by the hydrodynamical model.¹¹ Recent theoretical investigations⁷⁻¹⁰ expect the isoscalar GQR in the energy range between 20- and 25-MeV excitation energy. In this Letter we present results from an $^{16}\text{O}(\alpha, \alpha')$ experiment at 146

MeV showing a large concentration of isoscalar $E2$ strength centered at 21 MeV with a width [full width at half-maximum (FWHM)] of about 7 MeV. This observation was possible mainly because of a reduced and flatter background compared to that of the 97-MeV experiment.

The experiments have been performed with the unanalyzed 146-MeV α beam from the Jülich cyclotron. Natural oxygen gas was contained in a gas cell with 2-mg/cm² Havar windows at a pressure of about 200 Torr. Reaction products were detected and identified with cooled ΔE - E telescopes consisting of four 2-mm Si surface-barrier counters. The beam energy spread, straggling in the target, and reaction kinematics limited the overall energy resolution to 350–650 keV depending on the scattering angle. Spectra were taken at lab angles from 5° to 40° mostly in steps of 1°. At extreme forward angles, where the gas target presented some difficulties, supplementary normalization runs were performed with a 350- μ g/cm² Mylar target yielding an overall resolution of 220 keV. The absolute cross sections of the two measurements agreed within the estimated error of 10%. In order to exclude the possibility that the interesting structures were produced by slit scattering, check runs were made with hydrogen and helium fillings of the gas target.

The spectra of scattered α particles show strong groups which are attributed to the excitation of known¹³ levels at 6.13 MeV ($J^\pi = 3^-$),¹⁴ 6.92 MeV (2^+),¹⁵ 8.87 MeV (2^-),¹⁶ and 11.52 MeV (2^+). The groups at 13.1 and 15 MeV arise from several unresolved levels. The 18.4 ± 0.05 -MeV peak probably corresponds to the 18.3-MeV (2^+) resonance of Ref. 2 and the 18.5-MeV (2^+) group of Ref. 3. The most interesting feature of Fig. 1 is the gross structure between 16 and 27 MeV which clearly stands out against the background and persists at all angles with minor changes of shape. We have evaluated the angular distribution of this structure by subtracting a linear background, as indicated in Fig. 1 (dashed lines). The endpoints are well defined at all angles by a minimum at 15.9 MeV and an abrupt change of the slope at 27.3 MeV. A parabolic background shape which one might prefer could reduce the peak area by about 20%; on the other hand, the peak area would increase by 25% if one were to completely remove the remaining oscillatory structure of the background angular distribution (see Fig. 2).

The resulting angular distribution of the structure between 15.9 and 27.3 MeV together with

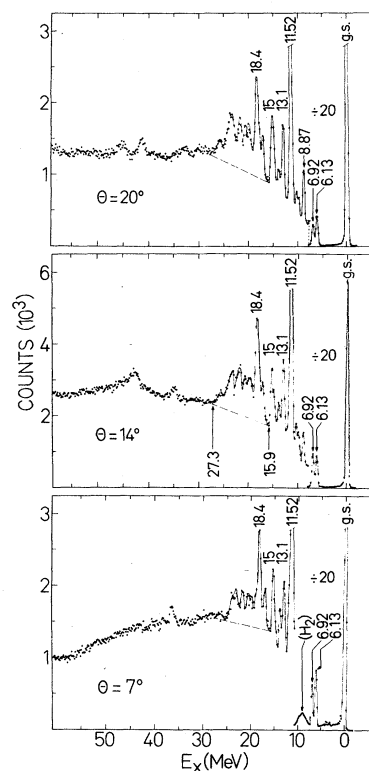


FIG. 1. Spectra of the $^{16}\text{O}(\alpha, \alpha')$ scattering at 146 MeV. The isoscalar GQR between 15.9 and 27.3 MeV clearly stands out against the background at all angles. The smooth curves have been drawn to guide the eye.

those of the strongest α groups are shown in Fig. 2. The cross section of the strong 18.4-MeV group has been evaluated separately (background line taken between the minima) to demonstrate the similarity of both patterns. For c.m. angles less than 30° well-structured angular distributions have been found which allow a straightforward determination of the angular momentum transfer L . Very good fits to the data are obtained by distorted-wave Born approximation (DWBA) calculations using collective form factors¹⁷ with complex coupling, if one assumes $L = 3$ transfer for the 6.13-MeV group and $L = 2$ for all the others, neglecting possible $E0$ contributions. Even the less pronounced structure and the less rapid falloff of the angular distributions of higher excited states, which we had suspected as being due to contributions of other L values, are readily reproduced by the DWBA calculations (Fig. 2). Concerning the gross structure between 16 and 27 MeV, statistics and resolution of the spectra are not adequate to evaluate the individu-

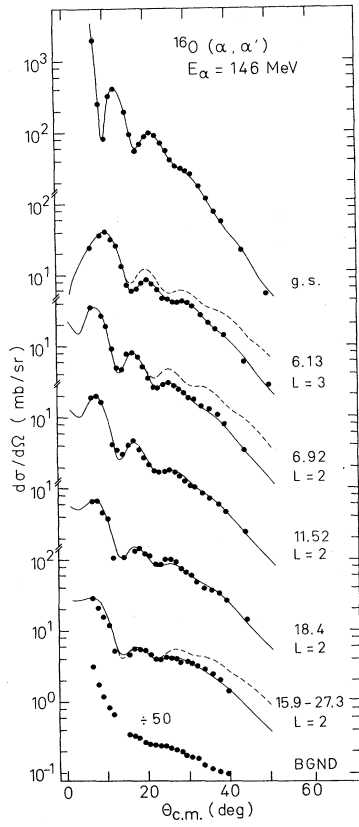


FIG. 2. Angular distributions of the strongest α groups and of the structure above the background (dashed line in Fig. 1) between 16 and 27 MeV. The cross section of the 18.4-MeV states has been subtracted from the latter. The solid curves represent complex-coupling DWBA calculations. The dashed lines are typical examples of real-coupling DWBA calculations. The angular distribution of the background between 16 and 27 MeV is also shown.

al fine-structure peaks with the aim to definitely exclude small contributions from other L values. The optical-model parameters of the assumed Woods-Saxon potential ($V=109.7$ MeV, $r_v=1.16$ fm, $a_v=0.82$ fm, $W=14.7$ MeV, $r_w=1.80$ fm, $a_w=0.77$ fm) were derived from a least-squares fit to the elastic cross sections (see Fig. 2).

Deformation parameters $\beta_L = [d\sigma(\theta)_{\text{exp}}/d\sigma(\theta)_{\text{DW}}]^{1/2}$ and the corresponding deformation lengths $\beta_L R$ have been extracted (see Table I) using real-coupling DWBA calculations¹⁸ which gave fits of comparable quality in the diffraction region (see Fig. 2). In this way we avoided the ambiguities in the deformation lengths $\beta_L R$ arising from the largely different real and imaginary radii. Fractions of the isoscalar $E2$ energy-weighted sum rule (EWSR)

TABLE I. Deformation lengths $\beta_L R$ and corresponding fractions $S(\text{IS})$ of the isoscalar energy-weighted sum rule in comparison with values $S(\text{EM})$ from electromagnetic transition rates.

E_x (MeV)	J^π ($T=0$)	$\beta_L R$ (fm)	$S(\text{IS})$ (%)	$S(\text{EM})$ (%)
6.13	3^-	1.41	8	13 ± 2^a
6.92	2^+	0.95	11	11 ± 1^a
11.52	2^+	0.75	11	13 ± 2^a
13.1	2^+	0.37^b	$\leq 3^b$	$6, \leq 8^c$
18.4	2^+	0.52	9	$11, 4^d$
15.9 to 27.3	2^+	1.22^e	58 ± 25^e	21 ± 9^f

^aRef. 13.

^bWith contributions from the 13.02- (2^+) and 13.14-MeV (2^+) levels. We give an upper limit only to allow for a possible contribution from the 13.13-MeV (3^-) level.

^cRefs. 2, 20.

^dRefs. 2, 3.

^eWith the strength of the 18.4-MeV group subtracted.

^fRef. 3; $E2$ strength in the region of 20–30 MeV excitation energy.

have been calculated accounting for Fermi mass distributions through the application of method II from Bernstein.¹⁹ For the low-lying states, Table I shows a satisfactory agreement between our isoscalar strengths and the electromagnetic values. This is very gratifying since all trivial criticism of the applied procedure (e.g., choice of the optical potential, real or complex coupling) would lead only to a simultaneous renormalization of all transition strengths. Therefore, unless the use of the identical collective form factors for all transitions is questioned, reasonable confidence can be attached to the value of $(67 \pm 25)\%$ of the ($T=0$) $E2$ EWSR found in the isoscalar GQR region (Table I). The errors are estimated from the uncertainties of the absolute cross sections and of the background subtraction.

This strength is not at variance with previous experiments. It seems to indicate, however, that most of the $E2$ strength observed in the (p, γ_0) channel¹ is isoscalar. This has already been suggested on the basis of inelastic ^3He scattering⁴ where, however, a $T=1$ contribution could not be ruled out. An attempt to disentangle the dipole and quadrupole strength excited in this reaction has led to an estimate⁴ of 75% of the isoscalar EWSR for $L=2$ in the region between 17 and 27 MeV. Only an analysis of electron-scattering

data,³ which are also affected by the presence of the GQR, has yielded noticeably smaller $E2$ strength exhausting $(27 \pm 10)\%$ of the EWSR between 16 and 30 MeV.

In conclusion, for the first time a large concentration of isoscalar $E2$ strength has been located definitely between 16 and 27 MeV of excitation energy in ^{16}O , centered at 20.7 MeV with a width (FWHM) of 7.5 ± 1 MeV. Because of the high selectivity of the (α, α') reaction and a background which is less important than in the 97-MeV experiment⁵ this strength is directly visible in the spectra as a giant resonance with appreciable fine structure. The total observed isoscalar $E2$ strength exhausts about 90% of the $(T=0)$ $E2$ EWSR.

Theoretically the semiempirical resonance analysis⁶ of scattering data yields a maximum of the $E2$ strength (isoscalar and/or isovector) at 24 MeV with a width (FWHM) of about 5 MeV. It is remarkable that three calculations^{7,8,10} of the isoscalar GQR predicted the position correctly within 1 MeV even if the strengths are overestimated and the widths (if any) are underestimated.

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