

(1968).

<sup>8</sup>K. Tajima, J. Phys. Soc. Jpn. **31**, 441 (1971).<sup>9</sup>B. G. Wybourne, Phys. Rev. **148**, 317 (1966).<sup>10</sup>T. P. Das and M. Pomerantz, Phys. Rev. **123**, 2070 (1961); B. Bleaney, in *Magnetic Properties of Rare Earth Metals*, edited by R. J. Elliot (Plenum, London

and New York, 1972), p. 405.

<sup>11</sup>P. J. Unsworth, J. Phys. B: Proc. Phys. Soc., London **2**, 122 (1969).<sup>12</sup>A. Narath, Phys. Rev. **179**, 359 (1969).<sup>13</sup>D. L. Uhrich and R. G. Barnes, Phys. Rev. **164**, 428 (1967).

## Cross Section Ratios for ( $\pi^\pm, \pi N$ ) Reactions on $^{16}\text{O}$ near the $\Delta(1236)$ Resonance\*

B. J. Lieb

*George Mason University, Fairfax, Virginia 22030*

and

H. S. Plendl

*Florida State University, Tallahassee, Florida 32306*

and

H. O. Funsten and W. J. Kossler

*College of William and Mary, Williamsburg, Virginia 23185*

and

C. E. Stronach

*Virginia State College, Petersburg, Virginia 23803*

(Received 22 January 1975)

Ratios of cross sections for 200-MeV  $\pi^\pm$  reactions on  $^{16}\text{O}$  leading to mirror levels in  $^{15}\text{O}$  and  $^{15}\text{N}$ , observed by their  $\gamma$  decays, were measured and compared. For the first  $\frac{3}{2}^-$  levels, the ratios are  $(^{15}\text{O}/^{15}\text{N})_{\pi^-} = 1.7 \pm 0.4$  and  $(^{15}\text{O}/^{15}\text{N})_{\pi^+} = 1/(1.8 \pm 0.4)$ , indicating charge symmetry.

The one-step quasifree (OSQF) mechanism for ( $\pi, \pi N$ ) nuclear reactions, in which the incident pion scatters from an individual nucleon, appeared to be a good approximation<sup>1</sup> until Chivers *et al.*<sup>2</sup> reported that the activation-cross-section ratios  $(A + \pi^- \rightarrow A - 1)/(A + \pi^+ \rightarrow A - 1)$  on  $^{12}\text{C}$ ,  $^{14}\text{N}$ , and  $^{16}\text{O}$  near the  $\Delta(1236)$  pion-nucleon resonance are close to 1 and not to 3, as originally expected from the behavior of the pion-nucleon cross section. Similar cross-section ratios have also been determined for a variety of even- and odd-mass targets from  $^4\text{He}$  to  $^{64}\text{Zn}$  at incident energies ranging from 30 to 360 MeV.<sup>2-9</sup> A recent remeasurement at Los Alamos<sup>10</sup> of  $\pi^\pm$  activation of  $^{11}\text{C}$  from  $^{12}\text{C}$  yielded  $\pi^+$  cross sections somewhat lower than those in Ref. 2. Nearly all ratios were found to be considerably less than 3; the Los Alamos measurement yielded, at  $E_\pi = 180$  MeV,  $\sigma_{\pi^-}/\sigma_{\pi^+} = 1.5$ . Various mechanisms have been proposed to explain these results. Besides OSQF processes, final-state interactions between the struck nucleon and the residual nucleus and in-

elastic pion scattering to unbound levels have been suggested.<sup>2,11-17</sup>

In order to test the ( $\pi, \pi N$ ) nuclear reaction mechanism in a different way from previous experiments, we determined, for incident  $\pi^+$  near the  $\Delta(1236)$  resonance energy on a water target, the ratio of  $\pi^+$  cross sections,

$$R(\pi^+) \equiv \frac{\sigma(\pi^+, ^{15}\text{O}^*(6.18, \frac{3}{2}^-))}{\sigma(\pi^+, ^{15}\text{N}^*(6.32, \frac{3}{2}^-))},$$

producing the first  $\frac{3}{2}^-$  excited levels in the residual mirror nuclei  $^{15}\text{O}$  and  $^{15}\text{N}$ . We then compared the result with a previously obtained ratio<sup>18</sup> of  $\pi^-$  cross sections,

$$R(\pi^-) \equiv \frac{\sigma(\pi^-, ^{15}\text{O}^*(6.18, \frac{3}{2}^-))}{\sigma(\pi^-, ^{15}\text{N}^*(6.32, \frac{3}{2}^-))},$$

leading to the same excited residual-nucleus levels. These ratios were determined by observing the prompt de-excitation  $\gamma$  rays from individual bound levels of these residual nuclei. Since the decay schemes for  $^{15}\text{O}$  and  $^{15}\text{N}$ <sup>19</sup> permit an un-

ambiguous determination of the extent to which the first  $\frac{3}{2}^-$  levels are populated directly from the reactions rather than from  $\gamma$ -ray feeding, a major uncertainty inherent in the prompt- $\gamma$ -ray method was avoided.

These  $\frac{3}{2}^-$  levels have a predominant  $(p_{3/2})^{-1}$  hole configuration. Hence they should be strongly excited if the reaction proceeds by a direct process. In the previous  $^{16}\text{O}-\pi^-$  experiment, these levels were indeed strongly excited. However,  $R(\pi^-)$  was found to be  $1.7 \pm 0.4$ , i.e., below the OSQF value of 3 but larger than the value of  $1.03 \pm 0.09$  given by Chivers *et al.*<sup>2</sup> for the ratio of activation cross sections,

$$\sigma(^{16}\text{O} + \pi^- \rightarrow ^{15}\text{O}) / \sigma(^{16}\text{O} + \pi^+ \rightarrow ^{15}\text{O}),$$

to all bound levels in the residual nucleus  $^{15}\text{O}$ . If the reaction proceeds predominantly by an isospin-symmetric process, such as OSQF or a final-state mechanism, then  $R(\pi^+)$  should equal  $1/R(\pi^-)$ . Hence a comparison of these ratios is suggestive of the reaction mechanism.

The experiments were performed with  $\pi^-$  and  $\pi^+$  beams from the Space Radiation Effects Laboratory synchrocyclotron.<sup>20</sup> The 230-MeV  $\pi^-$  beam was momentum-selected by a bending magnet from pions produced on an internal carbon target, deflected out of the cyclotron by its fringing field, and focused by a quadrupole pair.<sup>18</sup> The 190-MeV  $\pi^+$  beam was focused and momentum-selected by a beam channel<sup>21</sup> from pions produced by the external proton beam in a  $\text{CH}_4$  target; protons in the  $\pi^+$  beam were stopped in Plexiglas before the last bending magnet. The intensity for both beams, as determined with a counter telescope in front of the experimental target, was of the order of  $2 \times 10^5$  particles/sec. The lepton contribution was  $(15 \pm 7)\%$  in the  $\pi^-$  beam<sup>18</sup> and  $(8 \pm 5)\%$  in the  $\pi^+$  beam,<sup>4</sup> as determined by time-of-flight measurements. The  $\text{H}_2\text{O}$  targets were made as thick as possible without causing excessive  $\gamma$ -ray absorption and pion-energy degradation (15 and 10 g/cm<sup>2</sup>, respectively, for  $\pi^-$  and  $\pi^+$  beams). The water was kept in rectangular, 0.1-mm-thick brass containers. The average energy in the targets,  $(E_{\text{in}} + E_{\text{out}})/2$ , was 215 MeV for the  $\pi^-$  beam and 180 MeV for the  $\pi^+$  beam. (Pion excitation curves for  $^{16}\text{O}$  vary by  $<7\%$  over the interval  $180 \leq E_\pi \leq 215$  MeV.<sup>2</sup>)

Gamma rays were detected with a 40-cm<sup>3</sup> Ge(Li) detector at approximately 90° with respect to the beam; events coincident with the beam telescope and anticoincident with a scintillator surrounding the Ge(Li) detector (to discriminate

against charged particles) were energy-analyzed and stored in the first half of a multichannel analyzer. Background and random contributions to a spectrum were identified by recording in the second half of the analyzer an additional spectrum consisting of events in the Ge(Li) detector that were delayed by  $\sim 50$  nsec relative to beam-telescope events. Overall system resolution was  $\sim 5$  keV at 1 MeV. Further details are given in Ref. 18.

In the resulting  $\gamma$ -ray spectra, approximately twenty peaks were seen and identified with transitions in residual nuclei. The first excited  $\frac{3}{2}^-$  mirror levels in  $^{15}\text{O}$  and  $^{15}\text{N}$ , together with the 6.131-MeV,  $3^-$ ,  $T=0$  level in  $^{16}\text{O}$ , the 3.945-MeV,  $1^+$ ,  $T=0$  level in  $^{14}\text{N}$ , and the 4.439-MeV,  $2^+$ ,  $T=0$  level in  $^{12}\text{C}$ , were the most strongly excited ones in both the  $\pi^-$ - and the  $\pi^+$ -induced reactions. Portions of the spectra containing the  $\frac{3}{2}^-$ -level photopeaks are shown in Fig. 1. The width of these peaks is due to Doppler recoil broadening in the target.

From the decay schemes for  $^{15}\text{O}$  and  $^{15}\text{N}$ ,<sup>19</sup> it is evident that  $\gamma$  feeding from higher excited levels does not contribute significantly to the excitation of the first  $\frac{3}{2}^-$  mirror levels. In  $^{15}\text{O}$ , the three bound levels above the  $\frac{3}{2}^-$  level at 6.177 MeV have no reported  $\gamma$  branch to that level, and the small  $\gamma$  widths of the unbound  $^{15}\text{O}$  levels cannot contrib-

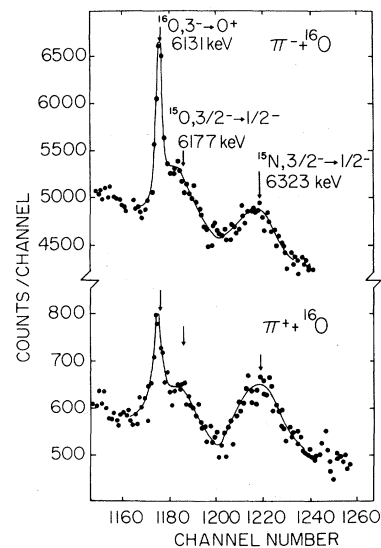


FIG. 1. Portions of the prompt- $\gamma$ -ray spectra from interactions of 215-MeV  $\pi^-$  and of 180-MeV  $\pi^+$  with  $^{16}\text{O}$ , containing the photopeaks due to ground-state transitions from the  $^{15}\text{O}$  and  $^{15}\text{N}$  mirror levels near 6 MeV. Arrows indicate nominal photopeak positions; the solid lines are intended to guide the eye.

TABLE I. Experimental cross sections for 215-MeV  $\pi^-$  and 180-MeV  $\pi^+$  interactions with  $^{16}\text{O}$ .

Product	$E_{\text{exc}}$ (MeV)	$J^\pi$	$\sigma(\pi^-)$ (mb) <sup>a</sup>	$\sigma(\pi^+)$ (mb) <sup>b</sup>
$^{15}\text{N}$	6.323	$(3/2)^-$	$9.1 \pm 2.5$	$17.3 \pm 4.6$
$^{15}\text{O}$	6.177	$(3/2)^-$	$15.6 \pm 3.8$	$9.9 \pm 2.8$
$^{15}\text{N}$	5.271	$(5/2)^+$	$4.2 \pm 1.1$ <sup>c</sup>	$4.8 \pm 1.4$ <sup>c</sup>
$^{15}\text{O}$	5.242	$(5/2)^+$	$2.9 \pm 0.8$ <sup>c</sup>	$2.3 \pm 0.7$ <sup>c</sup>
$^{16}\text{O}$	6.131	$3^-$	$12.5 \pm 2.8$	$9.0 \pm 2.3$

<sup>a</sup> Ref. 18.<sup>b</sup> Present work.<sup>c</sup> Probably includes feeding from higher bound levels; see text.

ute significantly to the excitation of that level. In  $^{15}\text{N}$ , there are thirteen bound levels above the  $\frac{3}{2}^-$  level at 6.323 MeV. While two of these levels do have branches to the  $\frac{3}{2}^-$  level (<25% each), no significant transitions from these two levels were found in the  $\gamma$ -ray spectra. Of the remaining bound levels, six have  $\gamma$  branches of less than 5%, and five have no reported branching to the  $\frac{3}{2}^-$  level. The observed strong excitation of the first  $\frac{3}{2}^-$  level is, therefore, attributed primarily to excitation from the reactions rather than to feeding from higher excited levels.

The only other  $^{15}\text{O}$  and  $^{15}\text{N}$  levels for which transitions could be identified in both the  $\pi^+$  and  $\pi^-$  spectra were the first excited  $\frac{5}{2}^+$  mirror levels near 5 MeV. Although none of the bound negative-parity levels have significant  $\gamma$  branches to these levels, several higher-energy positive-parity bound levels have significant branching to these  $\frac{5}{2}^+$  levels.<sup>19</sup> Since the lifetimes of these higher positive-parity levels are short enough (<0.1 psec) to produce Doppler-broadened  $\gamma$  peaks possibly obscured by spectrum background, the amount of excitation directly to the first  $\frac{5}{2}^+$  levels could not be determined.

Cross sections were determined and corrected for target  $\gamma$ -ray absorption, detector efficiency assuming isotropic  $\gamma$  emission, and feeding from higher levels which were found to be excited. The values determined from photopeaks were consistent with values determined from escape peaks. The results are shown in Table I for the first  $\frac{3}{2}^-$  and  $\frac{5}{2}^+$  levels in  $^{15}\text{O}$  and  $^{15}\text{N}$  and for the  $3^-$  level in  $^{16}\text{O}$ . In Table II, cross-section ratios for the first  $\frac{3}{2}^-$  levels are shown. The cross-section errors include both statistical and systematic contributions. In the ratios, transitions of similar

TABLE II. Cross-section ratios,  $R(\pi^\pm)$ , for  $\pi^\pm + ^{16}\text{O} \rightarrow ^{15}\text{O}, ^{15}\text{N}$  6-MeV  $\frac{3}{2}^-$  states at  $E_\pi$  near the  $\Delta(1236)$  resonance.

Reactions	OSQF	Expt.
$\frac{\sigma(\pi^+, ^{15}\text{O}^* [6.18, (3/2)^-])}{\sigma(\pi^+, ^{15}\text{N}^* [6.32, (3/2)^-])}$	$\frac{1}{3}$	$\frac{1}{1.8 \pm 0.4}$
$\frac{\sigma(\pi^-, ^{15}\text{O}^* [6.18, (3/2)^-])}{\sigma(\pi^-, ^{15}\text{N}^* [6.32, (3/2)^-])}$	3	$1.7 \pm 0.4$

energy are compared, so that most systematic error contributions cancel out.

The cross sections for excitation of the first  $\frac{3}{2}^-$  levels in  $^{15}\text{O}$  and  $^{15}\text{N}$  are large, in qualitative agreement with the OSQF prediction. Furthermore, these cross sections display, within error limits,  $T_z$  symmetry; i.e.,  $\sigma(\pi^-)$  for  $^{15}\text{O}$  equals  $\sigma(\pi^+)$  for  $^{15}\text{N}$ , and  $\sigma(\pi^+)$  for  $^{15}\text{O}$  equals  $\sigma(\pi^-)$  for  $^{15}\text{N}$ . Hence, within error limits,  $R(\pi^+) = 1/R(\pi^-)$  for the first  $\frac{3}{2}^-$  levels. It should be noted that these ratios differ by ~50% from the OSQF prediction. Differences of this magnitude have, in fact, been expected from distortion and other effects of the nucleus on the interacting pion and nucleon.<sup>12-14,17</sup>

Relative to the  $\frac{3}{2}^-$  cross sections, the cross sections for excitation of the first  $\frac{5}{2}^+$  levels are considerably larger than expected from OSQF processes—the experimental  $\sigma_{(5/2)^+}/\sigma_{(3/2)^-}$  ratios range from 0.2 to 0.5 (Table I). In a OSQF process, the cross sections would be proportional to the spectroscopic factors for nucleon removal; i.e.,  $\sigma_{(5/2)^+}/\sigma_{(3/2)^-} = S_{(5/2)^+}/S_{(3/2)^-} < 0.1$ .<sup>18,22</sup> (These  $\frac{5}{2}^+$  and  $\frac{3}{2}^-$  states are predominantly two-hole, one-particle and one-hole states, respectively.<sup>23</sup>) Even with the previously mentioned possibility of unmeasured  $\frac{5}{2}^+$  feeding from higher positive-parity levels, having comparably small spectroscopic factors, the measured ratios are larger than expected from OSQF. A final-state process<sup>13,15</sup> could produce the two-hole, one-particle state needed for the positive-parity states. The stronger excitation of  $^{15}\text{N}$   $\frac{5}{2}^+$  relative to  $^{15}\text{O}$   $\frac{5}{2}^+$  may be due to the presence of about four bound  $^{15}\text{N}$  positive-parity levels that appreciably branch to the  $\frac{5}{2}^+$  whereas  $^{15}\text{O}$  has only one such level.

Estimated ground-state cross sections added to the measured  $^{15}\text{O}$  excited-state  $\gamma$  cross sections for  $\pi^- + ^{16}\text{O}$  agreed (Ref. 18, Section IV-A) with the  $\pi^- - ^{16}\text{O}$  activation cross sections of Chivers *et al.*<sup>2</sup> Similar agreement is obtained in the present  $\pi^+ - ^{16}\text{O}$  ac-

tivation cross section is lowered by  $\approx 30\%$ , as indicated by the Los Alamos  $\pi^+ -^{12}\text{C}$  remeasurement.<sup>10</sup>

The cross sections for excitation of the 6.131-MeV,  $3^-$  level in  $^{16}\text{O}$  are nearly equal, as expected for inelastic scattering from a  $T=0$  target.

\*Work supported by the National Science Foundation, the National Aeronautics and Space Administration, and the Southern Regional Education Board.

<sup>1</sup>See, e.g., the work reviewed by D. S. Koltun, in *Advances in Nuclear Physics*, edited by M. Baranger and E. Vogt (Plenum, New York, 1969), Vol. 3, Chap. 2.

<sup>2</sup>D. J. Chivers, E. M. Rimmer, B. W. Allardyce, R. C. Witcomb, J. J. Domingo, and N. W. Tanner, *Phys. Lett.* **26B**, 573 (1968), and *Nucl. Phys.* **A126**, 129 (1969).

<sup>3</sup>Y. A. Budagov, P. F. Ermolov, E. A. Kushnivenski, and V. I. Moskalev, *Zh. Eksp. Teor. Fiz.* **42**, 1191 (1962) [*Sov. Phys. JETP* **15**, 824 (1962)].

<sup>4</sup>P. J. Karol, A. A. Caretto, R. L. Klobuchar, D. M. Montgomery, R. A. Williams, and M. V. Yester, *Phys. Lett.* **44B**, 459 (1973).

<sup>5</sup>K. R. Hogstrom, B. W. Mayes, L. Y. Lee, J. C. Alldred, C. Goodman, G. S. Mutchler, C. R. Fletcher, and G. C. Phillips, *Nucl. Phys.* **A215**, 598 (1973).

<sup>6</sup>M. A. Moinester, M. Zaider, J. Alster, D. Asheri, S. Cochavi, and A. L. Yavin, *Phys. Rev. C* **8**, 2039 (1973).

<sup>7</sup>D. Asheri, M. Zaider, Y. Shamai, S. Cochavi, M. A. Moinester, A. L. Yavin, and J. Alster, *Phys. Rev. Lett.* **32**, 993 (1974).

<sup>8</sup>M. Zaider, J. Alster, D. Ashery, S. Cochavi, M. A. Moinester, and A. L. Yavin, *Phys. Rev. C* **10**, 938 (1974).

<sup>9</sup>H. S. Plendl, H. O. Funsten, A. Richter, V. G. Lind, B. J. Lieb, and C. J. Umbarger, to be published.

<sup>10</sup>B. J. Dropesky *et al.*, *Phys. Rev. Lett.* **34**, 821 (1975).

<sup>11</sup>D. Wilkinson, *Comments Nucl. Particle Phys.* **1**, 169 (1967).

<sup>12</sup>V. M. Kolybasov, *Phys. Lett.* **27B**, 3 (1968); V. M. Kolybasov and N. Ya. Smorodinskaya, *Phys. Lett.* **30B**, 11 (1969).

<sup>13</sup>P. W. Hewson, *Nucl. Phys.* **A133**, 659 (1969).

<sup>14</sup>R. Seki, *Nuovo Cimento* **9A**, 235 (1972).

<sup>15</sup>D. Robson, *Ann. Phys. (New York)* **71**, 277 (1972).

<sup>16</sup>G. L. Strobel, *Nucl. Phys.* **A232**, 502 (1974).

<sup>17</sup>M. M. Sternheim and R. R. Silbar, *Phys. Rev. Lett.* **34**, 824 (1975).

<sup>18</sup>B. J. Lieb, Ph.D. dissertation, College of William and Mary, 1971 (unpublished); B. J. Lieb and H. O. Funsten, *Phys. Rev. C* **10**, 1753 (1974).

<sup>19</sup>F. Ajzenberg-Selove, *Nucl. Phys.* **A152**, 1 (1970).

<sup>20</sup>The Space Radiation Effects Laboratory is supported by the National Science Foundation, the National Aeronautics and Space Administration, and the Commonwealth of Virginia.

<sup>21</sup>W. Risk, private communication.

<sup>22</sup>K. H. Purser, W. P. Alford, D. Cline, H. W. Fulbright, H. E. Gove, and M. S. Krick, *Nucl. Phys.* **A132**, 75 (1969).

<sup>23</sup>S. Lie and T. Engeland, *Nucl. Phys.* **A169**, 617 (1971).

## ( $^6\text{Li}, d$ ) Reaction on $fp$ -Shell Nuclei and Alpha-Transfer Distorted-Wave Born-Approximation Analysis

U. Strohmusch\* and G. Bauer

*Fakultät für Physik, Universität Freiburg, Freiburg, Germany*

and

W. W. Fulbright†

*Nuclear Structure Research Laboratory, University of Rochester, Rochester, New York 14627*

(Received 6 January 1975)

Strongly structured ( $^6\text{Li}, d$ ) angular distributions exhibiting systematic variations with  $A$  for  $A=40$  to  $A=90$  target nuclei are well reproduced by  $\alpha$ -stripping calculations using a single set of potential parameters. Zero-range and finite-range distorted-wave Born-approximation results are found very similar both in the shapes of the angular distributions and in the relative magnitudes. The question of nuclear-structure dependence in the angular distributions is discussed.

The ( $^6\text{Li}, d$ ) reaction has been studied on a series of  $fp$ -shell nuclei at the University of Rochester.<sup>1,2</sup> In this note we want to demonstrate the capability of the  $\alpha$ -transfer distorted-wave Born

approximation (DWBA), in a very simple parameterization, to reproduce the highly structured angular distributions for the full range of nuclei investigated. Exact recoil finite-range calcula-