Lifetime Measurements in ⁸⁰Kr and ⁸¹Rb⁺

H.-G. Friederichs, A. Gelberg, B. Heits, K. P. Lieb, M. Uhrmacher, K. O. Zell,

and P. von Brentano

Institut für Kernphysik der Universität zu Köln, 5 Köln, Germany

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We measure the lifetimes of excited states in ⁸¹Rb and in the core nucleus ⁸⁰Kr. Ratios of reduced transition probabilities in ⁸⁰Kr are consistent with those given by the rotational model. The B(E2) of the $\frac{13}{2}$ state in ⁸¹Rb is in agreement with the particle-plus-rotor value and inconsistent with the weak-coupling prediction. The B(E2) values of the $\frac{17}{2}$ and $\frac{21}{2}$ states lie much higher than predicted by several models.

The coupling of a $g_{9/2}$ proton to an even-even core can lead to high-spin states which one may describe in terms of relatively simple concepts, e.g., weak coupling $(W)^1$ or Coriolis mixed wave functions.²⁻⁴ Since the knowledge of electromagnetic matrix elements is often an efficient tool for distinguishing between different models, measurements of lifetimes and possibly of g factors are highly desirable. The purpose of this paper is to present and discuss results of lifetime measurements in ⁸¹Rb and in the core nucleus ⁸⁰Kr. We will briefly summarize the existing information on both nuclei.

The excited levels of ⁸⁰Kr, and in particular those belonging to the yrast sequence, have been extensively studied^{5,6} by means of $(\alpha, xn\gamma)$ reactions, and the spin assignments are unambiguous (Fig. 1). The levels of ⁸¹Rb populated by β decay have been investigated by Broda *et al.*⁷; these are mainly low-spin, negative-parity states. High-spin, positive-parity states in ⁸¹Rb, produced by ⁷⁹Br(α , 2n), have been investigated by Friederichs *et al.*⁸ γ - γ coincidence measurements showed the existence of a 623-875-1024keV cascade feeding the 86.4-keV $\frac{9}{2}$ + isomeric state. Subsequent angular-distribution measurements suggested a quadrupole character of the cascade γ 's, thus favoring the spin sequence $\frac{9}{2}$ - $\frac{13}{2}$ $-\frac{17}{2}$ $-\frac{21}{2}$ (Fig. 1). A closer look at the level schemes shows that the excitation energies in the band built upon the $\frac{9}{2}$ tate in ⁸¹Rb are very close to the corresponding values in ⁸⁰Kr. This relationship is characteristic of the strongly Coriolisdecoupled states 2,4 and, to a certain extent, of weak-coupling states. A careful search for other possible transitions depopulating the $\frac{17}{2}^+$ and $\frac{21}{2}^+$ states, besides those given in Fig. 1, has been unsuccessful.

The investigated nuclei have been produced in the reactions ${}^{65}Cu({}^{18}O, p2n){}^{80}Kr$ and ${}^{65}Cu({}^{19}F, p2n){}^{81}Rb$ by using a 52.5-MeV ${}^{18}O$ beam and a 50-

MeV ¹⁹F beam of the Köln tandem accelerator, respectively. Lifetimes of the low-lying states have been measured by means of the recoil-distance Doppler-shift (RDDS) technique. The selfsupporting, $1-2-\mu m$ thick, ⁶⁵Cu targets have been mounted in a plunger system described elsewhere.⁹ Recoil nuclei and beam were stopped in a stretched 20- μ m Ta foil. The flight distance was varied by means of a micrometer screw with an accuracy of 1 μ m. The evenness of the Cu targets, which was checked under a microscope, turned out to be better than 1 μ m. γ rays were measured at 0° by Ge(Li) detectors having an energy resolution of 2.1-3.2 keV at 1.33 MeV. Spectra were accumulated for 24 different flight distances ranging from 0 to 1 mm. The data were analyzed according to the method described by Lieb *et al.*¹⁰ The spectra were normalized by means of the strong 301-keV peak due to Coulomb excitation in the ¹⁸¹Ta stopper.

A few lifetimes (Table I) have been measured by the Doppler-shift attenuation method (DSAM); the targets have been evaporated on an Au back-

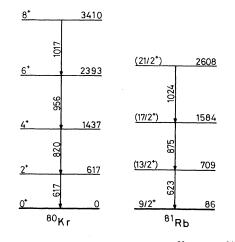


FIG. 1. Partial level schemes of ⁸⁰Kr and ⁸¹Rb.

TABLE I. Lifetimes and reduced transition probabilities. RA, rotation aligned; M, Mottelson (Ref. 4); W, Weak coupling.

	80 _{Kr}					
I	E	$ au_{ ext{exp}}$	B(E2)exp	B(E2) _{Rot}	B(E2)vibr	
_	(keV)	(ps)	(fm^4e^2)			
2 ⁺	617	12.7 <u>+</u> 0.7 ^a	722 <u>+</u> 40	722 <u>+</u> 40	722 <u>+</u> 40	
4 ⁺	820	2.4 <u>+</u> 0.2 ^a	921 <u>+</u> 77	1031 <u>+</u> 57	1444 <u>+</u> 80	
6+	956	0.75 <u>+</u> 0.2 ^b	1369 <u>+</u> 364	1137 <u>+</u> 63	2166 <u>+</u> 120	
8 ⁺	1017	0.6 ^b	1256	1188 <u>+</u> 66	2888 <u>+</u> 160	
			81	Rb		
I	Е	τ_{exp}	B(E2)exp	B(E2) _{RA}	в(Е2) _М	в(Е2)
13/2+	623	8.7 <u>+</u> 0.5 ^a	1004 <u>+</u> 58	1010 <u>+</u> 60	1030 <u>+</u> 60	722 <u>+</u> 40
17/2+	876	0.31±0.04 ^b	5125 <u>+</u> 660	1138 <u>+</u> 68	1140 <u>+</u> 68	1031 <u>+</u> 57
21/2+	1024	0.16 <u>+</u> 0.03 ^b	4550 <u>+</u> 850	1172 <u>+</u> 62	1180 <u>+</u> 70	1135 <u>+</u> 63
^a RDDS.				^b DSAM.		

ing. Spectra were taken at five angles between 0° and 90° . From the angular dependence of the centroid, lifetimes were evaluated using a code written by J. Naser. This program uses the Blaugrund approximation taking into account both electronic and nuclear stopping power.¹¹

The intensities of the unshifted peak and of the Doppler-shifted peak for several transitions are plotted versus recoil distance in Fig. 2. Delayed-cascade feeding was taken into account only in the analysis of the $2^+ \rightarrow 0^+$ transition in 80 Kr and of the $\frac{13}{2}^+ \rightarrow \frac{9}{2}^+$ transition in 81 Rb. Since the life-times of the 4^+ and $\frac{17}{2}^+$ states are shorter, it has been more convenient to extract them from the shifted peaks. Only an upper limit $\tau_{17/2} = 0.65$ psec was obtained in this way. The value obtained from DSAM is $\tau_{17/2} = 0.31 \pm 0.06$ psec. The lifetimes of the 2^+ and 4^+ states in 80 Kr are in agreement with results obtained by Nolte *et al.*¹²

The experimental results are compared in Table I with the predictions of several models. All the theoretical B(E2) values have been normalized to that of the 2⁺ level in ⁸⁰Kr. The B(E2)values in ⁸⁰Kr are in satisfactory agreement with the rotational ones and lie far from the vibrational ones; this is consistent with the conclusions drawn by McCauley and Draper⁵ from excitationenergy systematics. It would, of course, be in-

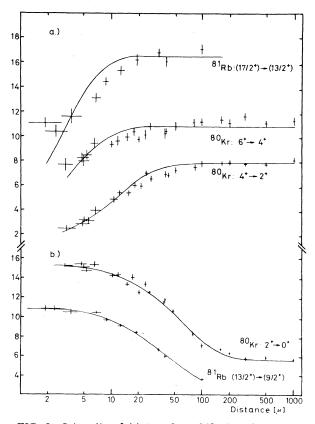


FIG. 2. Intensity of (a) Doppler-shifted peaks and of (b) unshifted peaks versus recoil distance.

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teresting to extend lifetime measurements to other even Kr isotopes. If we assume that we are dealing with a K=0 rotational band, the deformation corresponding to the lifetime of the 2⁺ state is $\delta = 0.261 \pm 0.007$. The reduced transition probabilities in a rotor-plus-particle nucleus is given by

$$B(E2; I_i \rightarrow I_f) = (5e^2/16\pi Q_0^2) \times |\sum_{\Omega} c_{\Omega}^2 \langle I_i 2\Omega 0 | I_f \Omega \rangle|^2,$$

where Q_0 is the core intrinsic quadrupole moment and c_{Ω} is the amplitude of the $|I\Omega\rangle$ component in the wave function. Only Ω -diagonal contributions are taken into account.

The amplitudes c_{Ω} can be calculated in the rotation-aligned (RA) model by the simple approximate formula³

 $c_{\Omega} = d_{i\Omega}^{j}(\pi/2).$

This approximation should be valid when the deformation is around $\delta = \pm 0.2$. The corresponding B(E2) values are given in Table I under the heading RA.

Mottelson⁴ has shown that it is possible to calculate the amplitudes c_{Ω} in a simple way without imposing a restriction on the deformation; this calculation should be valid for relatively-highspin states ($j \gg 1$). A linear recursion formula for c_{Ω} is rewritten as a second-order differential equation which is similar to that of a one-dimensional linear oscillator; the independent variable is Ω . The lowest oscillator state in Ω space has a width Ω_0 which is a function of the deformation and of the core moment of inertia. The amplitude c_{Ω} has the simple form

$$c_{\Omega} = [\Omega_0(2\pi)^{1/2}]^{-1} \exp[-\Omega^2/(2\Omega_0^2)].$$

If we use the deformation calculated above for 80 Kr and assume that it remains unchanged through the coupling with the particle, we obtain B(E2) values represented in Table I under the heading M.

One sees that the experimental B(E2) of the $\frac{13}{2}^+$ - $\frac{9}{2}^+$ transition is in agreement with both rotorplus-particle calculations with strong-Coriolisforce calculations. The hypothesis of weak coupling can be ruled out. As regards the higher $\frac{17}{2}^+$ and $\frac{21}{2}^+$ states, their lifetimes are much shorter than predicted, suggesting a drastic change of structure.

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