

national Symposium on Electron and Photon Interactions at High Energies, Bonn, W. Germany, 1973, edited by H. Rollnik and W. Pfeil (North-Holland, Amsterdam, 1974).

¹⁶For a review see M. K. Gaillard, B. W. Lee, and J. L. Rosner, Fermilab Report No. PUB-74/86-THY, 1974 (unpublished).

¹⁷Y. Nambu, unpublished lectures; P. Goddard, J. Goldstone, C. Rebbi, and C. B. Thorn, Nucl. Phys. **B56**, 109 (1973), and references therein.

¹⁸If the force between c and \bar{c} may be approximated by a harmonic oscillator potential then the first radial excitation with $L=0$ is degenerate in energy with the lowest state with $L=2$.

¹⁹We note that the decay $\psi \rightarrow J + \eta$, which might otherwise be expected to be a strong competitor with $\psi \rightarrow J + 2\pi$, should be suppressed because the available phase space is limited and the decay takes place only in the P wave. Moreover the process violates SU(3) symmetry.

COMMENTS

Intermediate Boson in the Fermion-Current Model of Neutral Currents*

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The intermediate-boson version of the earlier proposed fermion-current model of neutral currents is discussed. In particular I speculate on the possibility that the recently discovered 3.105-GeV particle may be identified with the intermediate boson of the fermion-current model.

Shortly after the discovery of neutrino-induced neutral-current reactions it was proposed that the hadronic piece of the neutral current be identified with the unitary singlet baryon current.¹ In the same paper I also speculated that all neutral-current phenomena are due to an extremely simple universal Fermi interaction of the form

$$\mathcal{L}_{\text{eff}} = (G\lambda/\sqrt{2}) j_\lambda^{(F)} j_\lambda^{(F)}, \quad (1)$$

with

$$j_\lambda^{(F)} = i[\bar{e}\gamma_\lambda e + \bar{\mu}\gamma_\lambda \mu + \bar{\nu}_e\gamma_\lambda \nu_e + \bar{\nu}_\mu\gamma_\lambda \nu_\mu + \bar{u}\gamma_\lambda u + \bar{d}\gamma_\lambda d + \bar{s}\gamma_\lambda s], \quad (2)$$

where the notation of the uncolored quark model is used for hadrons. In view of the recently reported evidence for a narrow-width boson in e^+e^- production² and in e^+e^- annihilation,³ it is of some interest to make a few comments on the intermediate-boson version of the "fermion-current model."

I propose that the effective interaction (1) applicable to low- q^2 phenomena arises from a more fundamental intermediate-boson coupling as fol-

lows:

$$\mathcal{L} = gZ_\mu j_\mu^{(F)}, \quad (3)$$

where Z_μ is a neutral spin-1 field of mass m_Z .

Clearly we have

$$g^2/4\pi = 2(\lambda/4\pi)(G/\sqrt{2})m_Z^2, \quad (4)$$

where the factor 2 is necessary because the interaction (1) represents the product of two identical currents so that a typical term like $(\bar{e}e)(\bar{u}u)$ appears twice.⁴ The partial decay width for the Z boson decaying into a lepton pair can easily be calculated to be

$$\begin{aligned} \Gamma(Z \rightarrow e^+e^-) &= \Gamma(Z \rightarrow \mu^+\mu^-) = \frac{1}{3}(g^2/4\pi)m_Z \\ &\simeq (10^{-5}/\sqrt{2})(\lambda/6\pi)(m_Z^3/m_p^2). \end{aligned} \quad (5)$$

As for the hadronic decay modes of the Z boson, let us first observe that the quantum numbers of the final states are characterized by

$$J^{PC} = 1^{--}, \quad I^G = 0^-. \quad (6)$$

This quantum number assignment leads to numerous predictions some of which will be discussed

later.

We now proceed to estimate the hadrons-to-lepton-pair ratio

$$R_Z \equiv \Gamma(Z \rightarrow \text{hadrons}) / \Gamma(Z \rightarrow \mu^+ \mu^-) \quad (7)$$

using the quark-parton model. Just by counting the number of quark pairs we find that this ratio is 3 in the uncolored quark model and 9 in the triply colored quark model. As is well known, the quark-parton model, with or without coloring, makes a disastrous prediction for the hadrons-to-lepton-pair ratio in e^+e^- annihilation. We may, however, take the point of view that the symmetry relations inferred from the quark-parton model are far more general than the model itself. We can then derive that

$$R_Z = \frac{9}{2} R \quad (8)$$

with or without coloring, where R stands for the ratio of hadrons to lepton pairs in e^+e^- annihilation right outside the Z -peak region.⁵

Very recently a boson with $m = 3.105$ GeV of a very narrow width has been reported in

$$p + \text{Be} \rightarrow e^+ + e^- + \text{anything}, \quad (9)$$

$$e^+ + e^- \rightarrow e^+ + e^-, \mu^+ + \mu^-, \text{hadrons}, \quad (10)$$

by two different groups.^{2,3} It is amusing to speculate on whether we can identify the observed 3.105-GeV particle with the Z boson.

To compute the partial decay width for the lepton-pair mode we must first know the neutral-current coupling constant λ . This constant has previously been estimated from the deep inelastic neutrino data to be $\lambda^2 \simeq 0.2$ within perhaps $\pm 30\%$.^{6,7} I therefore predict that

$$\Gamma(Z \rightarrow e^+e^-) = \Gamma(Z \rightarrow \mu^+\mu^-) = 4.8-6.5 \text{ keV}. \quad (11)$$

As for the hadrons-to-lepton-pair ratio for the Z boson, the corresponding ratio in e^+e^- annihilation in the vicinity of $s = 3.0-3.2$ GeV is known to be 2.5-3.0⁸; hence my prediction for this ratio is given by

$$R_Z = \Gamma(Z \rightarrow \text{hadrons}) / \Gamma(Z \rightarrow \mu^+\mu^-) \simeq 11-14. \quad (12)$$

The partial decay widths, $\Gamma(Z \rightarrow \text{hadrons})$ and $\Gamma(Z \rightarrow \mu^+\mu^-)$, can be extracted from the colliding-beam data by using (after appropriate radiative corrections)

$$\int_{\text{peak}} \sigma(e^+e^- \rightarrow \text{hadrons}) ds = \frac{12\pi^2 \Gamma(Z \rightarrow e^+e^-) \Gamma(Z \rightarrow \text{hadrons})}{m_Z^4 \Gamma_{\text{tot}}} \quad (13)$$

and the analogous formula with "hadrons" re-

placed by $\mu^+\mu^-$. In (13) Γ_{tot} must include the contributions from $\Gamma(Z \rightarrow \nu_{e,\mu} + \bar{\nu}_{e,\mu})$ predicted in our model to be equal to $\Gamma(Z \rightarrow e^+e^-)$. The data of Ref. 3 appear to be roughly consistent with both (11) and (12); however, for more quantitative comparisons we must await more complete data.^{9,10}

There are other more or less obvious suggestions we can make for the experimentalists:

(i) Attempts should be made to examine whether reactions

$$e^+ + e^- \rightarrow Z \rightarrow 2\pi^+ + 2\pi^-, 3\pi^+ + 3\pi^- \quad (14)$$

are indeed forbidden, as required in the present model. This is a good test of the G -parity assignment because appreciable signals for $4\pi^+$ and $6\pi^+$ have been observed outside the peak region.⁸

(ii) If there is a measurable cross section for $\rho + \pi$ in the Z -peak region, we can check the isospin assignment as follows:

$$\begin{aligned} \Gamma(\rho^0 + \pi^0) &= \Gamma(\rho^+ + \pi^-) = \Gamma(\rho^- + \pi^+) \text{ for } I=0, \\ \Gamma(\rho^0 + \pi^0) &= 0 \text{ for } I=1. \end{aligned} \quad (15)$$

(iii) We can think of other reactions that might be helpful in determining the isospin and C parity. For example, the final states of

$$e^+ + e^- \rightarrow Z \rightarrow f + \omega, \quad (16a)$$

$$e^+ + e^- \rightarrow Z \rightarrow \rho^0 + \omega, \quad (16b)$$

are both characterized by odd G parity but the present model allows (16a) and forbids (16b).

(iv) A careful study of the shape of $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ is worthwhile; I predict that the interference between the background and the Z boson is destructive below the peak and constructive above the peak. However, the same feature is expected in a large class of spin-1 models with μe universality.

The main virtue of my interpretation for the 3.105-GeV particle is that it makes many specific predictions some of which are quite quantitative.¹¹ I conclude this short note by listing two obvious defects of the interpretation. (i) We have no simple way of accommodating possible higher-mass peaks now being rumored.¹² (ii) With a Z -boson mass as low as 3.1 GeV it is somewhat strange that there is not much variation observed in the neutral-current-to-charged-current ratio as we go from CERN energies to Fermi National Accelerator Laboratory energies.¹³

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¹J. J. Sakurai, Phys. Rev. D 9, 250 (1974).

²J. J. Aubert *et al.*, Phys. Rev. Lett. 33, 1404 (1974).

³J.-E. Augustin *et al.*, Phys. Rev. Lett. 33, 1406 (1974).

⁴Note also that in computing the cross sections for neutrino-induced reactions we have to be careful with another factor of 2 arising from the replacement $\bar{\nu}\gamma\lambda\nu \rightarrow \frac{1}{2}\bar{\nu}\gamma\lambda(1+\gamma_5)\nu$ which we can freely make for reactions induced by left-handed accelerator neutrinos.

⁵Those who are skeptical of arguments based on the quark-parton model may be interested to know that the result (8) can be obtained in an equally convincing manner by using nonet symmetry for the low-lying vector mesons together with Q^2 duality [of the kind discussed by M. Greco, Nucl. Phys. B63, 393 (1973); and J. J. Sakurai, University of California at Los Angeles Report No. UCLA/73/TEP/90 (to be published)].

⁶G. Rajasekaran and K. V. L. Sarma, Pramana 2, 62 (1974); J. J. Sakurai, in *Neutrinos—1974*, edited by C. Baltay, AIP Conference Proceedings No. 22 (American Institute of Physics, New York, 1974), p. 57.

⁷This value of λ^2 is consistent with other ν scattering data. See J. J. Sakurai and F. Urrutia, Phys. Rev. D (to be published).

⁸B. Richter, SLAC Report No. SLAC-PUB-1478 (to be published).

⁹In attempting to deduce R_Z from Ref. 3 it is important to keep in mind that detection-efficiency corrections have been applied to Fig. 1(a) but not to Figs. 1(b) and 1(c). For a detector that covers the angular region

$|\cos\theta| < 0.7$ the purely geometric efficiency is 0.61 for $\mu^+\mu^-$ final states expected to exhibit a $1 + \cos^2\theta$ distribution.

¹⁰To be able to deduce the absolute magnitude of $\Gamma(Z \rightarrow e^+e^-)$, etc., from the data our knowledge of the neutrino spectrum must be complete. Our crude estimate was made under the assumption that there are no "neutrinos" other than ν_e and ν_μ , e.g., no neutrinos associated with heavy leptons.

¹¹Needless to say, similar speculations can be made by using other models of neutral currents. If the 3,105-GeV particle indeed turns out to be the mediator of neutral-current interactions, it will be relatively easy to devise stringent tests for the various neutral-current models proposed so far. For example, the "electromagnetic-current model" of the kind discussed by M. A. B. Bég and A. Zee [Phys. Rev. Lett. 30, 675 (1973)] predicts $R_Z = R$; the " $I=1$ $V-A$ model" of S. L. Adler and S. F. Tuan [Phys. Rev. D (to be published)] predicts a $(1 + \cos\theta)^2$ distribution with a huge front-back asymmetry in $e^+e^- \rightarrow \mu^+\mu^-$ in the Z -peak region. Both models give sizable signals for $Z \rightarrow 4\pi^\pm, 6\pi^\pm$. More tests along these lines will be left as an exercise for the interested reader with his own pet model of neutral currents.

¹²Perhaps a single Z field can correspond to many (an infinite sequence of ?) weak boson states.

¹³F. J. Hasert *et al.*, Phys. Lett. 46B, 138 (1973); B. Aubert *et al.*, Phys. Rev. Lett. 32, 1457 (1974); B. C. Barish and F. J. Sciulli, private communication.