

Fig. 1.

(3) The cross sections at 102 and 405 GeV for  $M^2 < 10 \text{ GeV}^2$  are, respectively,  $4.5 \pm 0.4$  and  $3.5 \pm 0.5 \text{ mb}$  (after multiplying by 2).<sup>8</sup> Taking into account differences in background we conclude that this low-mass diffraction-dissociation region contributes about half of the total "diffractive" component of 6–7 mb.

In Fig. 3 we show the invariant cross section versus  $x$  for various  $P_T^2$  slices of the data. Where possible we have made comparison with the NAL<sup>4</sup> and IST<sup>9</sup> counter data and find good agreement within the limited statistical accuracy.

In Fig. 4 we show the invariant cross section versus  $P_T^2$  for various  $x$  slices of the data. The  $P_T^2$  dependences do not show any marked variation with  $x$  or  $s$ . In the  $P_T^2$  region where our data overlap the ISR data the agreement is good. We see no evidence for turnovers or dips at small  $P_T^2$ .

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†Present address: Nevis Laboratory, Columbia University, New York, N. Y. 10027.

‡A. P. Sloan Fellow.

<sup>1</sup>See the reviews by J. C. Sens, in the Proceedings

of the Conference on Recent Advances in Particle Physics, New York, New York, 15–17 March 1973 (to be published); and by P. Slattery, in *Experiments on High Energy Particle Collisions*, AIP Conference Proceedings No. 12, edited by R. S. Panvini (American Institute of Physics, New York, 1973).

<sup>2</sup>For 205-GeV/c  $\pi^-p$  data, see F. C. Winkelmann *et al.*, Lawrence Berkeley Laboratory–NAL Report No. LBL-2113 (unpublished); G. S. Abrams *et al.*, Lawrence Berkeley Laboratory Report No. LBL-2112 (unpublished).

<sup>3</sup>We estimate the overall systematic uncertainties in the cross sections for the inelastic two-pronged channels in the region  $x < -0.99$  to be  $\pm 10\%$  at 102 GeV and  $\pm 25\%$  at 405 GeV. The separation between elastic and inelastic events is particularly questionable for momentum transfers below 200 MeV/c. See C. Bromberg *et al.*, University of Michigan–University of Rochester Report No. UMBC 73-18 and UR-459 (to be published).

<sup>4</sup>K. Abe *et al.*, Phys. Rev. Lett. **31**, 1527, 1530 (1973); F. Sannes *et al.*, Phys. Rev. Lett. **30**, 766 (1973).

<sup>5</sup>Data from the ISR on  $p+p \rightarrow n + \text{anything}$  [L. Foà, Rapporteurs talk in Second International Aix-en-Provence Conference on Elementary Particles, Aix-en-Provence, France, 6–12 September 1973 (to be published)] indicate that the nucleon background in the region  $x < -0.9$  from nondiffractive events is small.

<sup>6</sup>Summary talk by J. Whitmore, APS Division of Particles and Fields Meeting, Berkeley, California, 13–17 August 1973 (to be published); S. J. Barish *et al.*, Phys. Rev. Lett. **31**, 1080 (1973).

<sup>7</sup>For recent experimental summaries of the triple-Regge subject see D. W. G. S. Leith, SLAC Report No. SLAC-PUB-1330, 1973 (unpublished); and Foà, Ref. 5.

<sup>8</sup>At 205 GeV the corresponding cross section for  $M^2 < 10 \text{ GeV}^2$  is  $3.4 \pm 0.5 \text{ mb}$  (Ref. 6; S. Barish, private communication).

<sup>9</sup>M. G. Albrow *et al.*, Nucl. Phys. **B54**, 6 (1973).

## Evidence for the $\omega\pi\pi$ Decay Modes of the $A_2$ and $\omega(1675)$

J. Díaz,\* F. A. DiBianca, W. J. Fickinger, J. A. Malko, D. K. Robinson, and C. R. Sullivan†  
Case Western Reserve University, Cleveland, Ohio 44106‡

and

J. C. Anderson, A. Engler, R. W. Kraemer, S. Toaff,§ and F. Weisser||  
Carnegie-Mellon University, Pittsburgh, Pennsylvania 15213¶

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We present evidence for the decay  $A_2^0 \rightarrow \omega\pi^+\pi^-$  with a branching ratio  $\Gamma(A_2 \rightarrow \omega\pi\pi)/\Gamma(A_2 \rightarrow \rho\pi) = 0.28 \pm 0.09$  and for the decay  $\omega(1675) \rightarrow \omega\pi^+\pi^-$  with a branching ratio  $\Gamma(\omega(1675) \rightarrow \omega\pi^+\pi^-)/\Gamma(\omega(1675) \rightarrow \rho\pi) = 0.47 \pm 0.18$ . Evidence is given for an intermediate  $B(1235)\pi$  state in the  $\omega(1675)$  decay.

We present evidence for enhancements in the  $\omega\pi^+\pi^-$  mass spectrum in the 1.3- and 1.65-GeV regions, which we identify as decay modes of the

$A_2$  and the  $\omega(1675)$ , respectively. Enhancements in these regions have been reported in several experiments.<sup>1–6</sup> In addition, we give evidence

for the cascade decay of the  $\omega(1675)$  through the  $B(1235)$ , i.e.,  $\omega(1675) \rightarrow B\pi$ ,  $B \rightarrow \omega\pi$ .

The data are from a 930 000-picture exposure of the Argonne National Laboratory 30-in deuterium bubble chamber to a 6.0-GeV/c  $\pi^+$  beam at the zero-gradient synchrotron. The five- and six-prong and three- and four-prong events were fitted with

$$\pi^+d \rightarrow p_s p \pi^+ \pi^- \pi^+ \pi^- \pi^0 \quad (1)$$

and

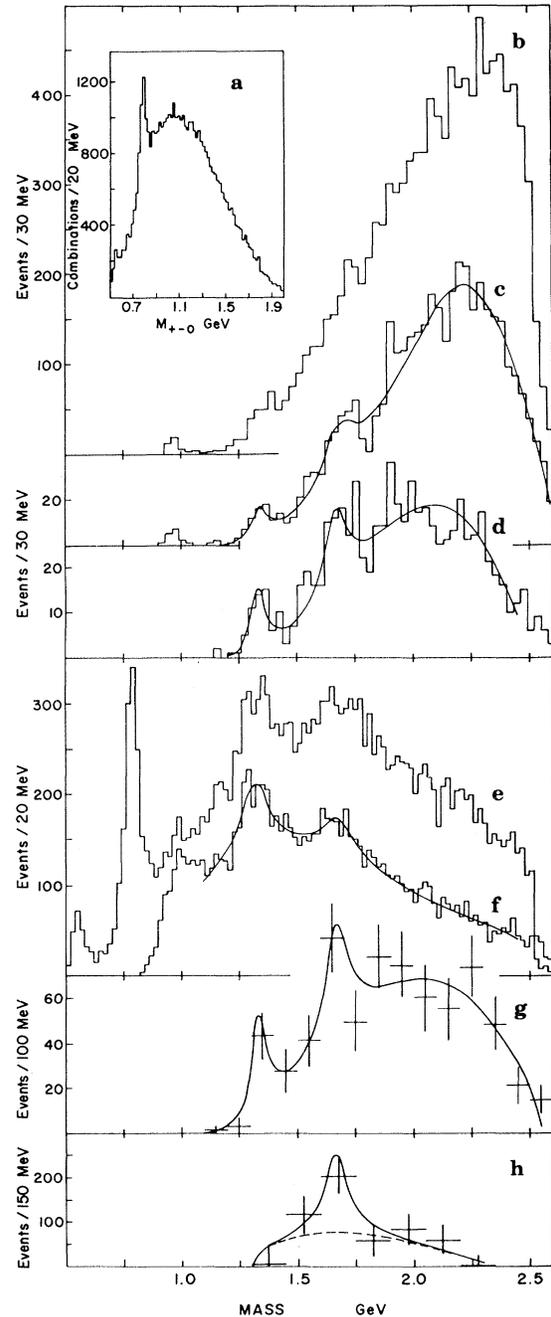
$$\pi^+d \rightarrow p_s p \pi^+ \pi^- \pi^0, \quad (2)$$

respectively, where  $p_s$  refers to the spectator proton. Ionization information was used in selecting the fits. Ambiguities between fits with and without a neutral pion were resolved in favor of the latter. Ambiguities among fits with neutral particles were resolved in favor of the fit with the highest  $\chi^2$  probability. The data were subjected to the following cuts: spectator momentum  $< 0.250$  GeV/c,  $-0.4 \leq (MM)^2 < 0.3$  GeV<sup>2</sup>,  $\chi^2$  probability  $\geq 0.01$  for events with  $(MM)^2 < M_{\pi^0}^2$ , and  $\chi^2$  probability  $> 0.1$  for events with  $(MM)^2 > M_{\pi^0}^2$ , where  $(MM)^2$  is the square of the missing mass. After the above cuts the sample consists of 15 816 fits with Reaction (1) and 18 619 fits with Reaction (2). We have further selected events with  $t' < 1.5$  (GeV/c)<sup>2</sup>, where  $t' = |t - t_{\min}|$ , with  $t$  the square of the four-momentum transfer to the outgoing multipion system and  $t_{\min}$  the minimum  $t$  for a given multipion effective mass. Cross sections have been calculated for this  $t'$  interval.

Figure 1(a) shows the  $\pi^+\pi^-\pi^0$  mass distribution

FIG. 1. (a)  $\pi^+\pi^-\pi^0$  mass distribution from Reaction (1) (four combinations per event). (b)  $5\pi$  mass distribution from Reaction (1). (c) Same as (b) but for six-prong data only. (d)  $5\pi$  mass distribution from Reaction (1) for six-prong events having at least one neutral  $3\pi$  combination in the  $\omega$  region. (e)  $3\pi$  mass distribution from Reaction (2). (f)  $3\pi$  mass distribution from Reaction (2) for events having at least one  $2\pi$  combination in the  $\rho$  region. (g) Fitted number of  $\omega$  events above background as a function of the  $5\pi$  mass for Reaction (1) (six-prong events). (h) Fitted number of  $B$  events above background as a function of the  $5\pi$  mass from Reaction (1). The curves on (c), (d), (f), and (g) are fits to the data using an incoherent sum of two Breit-Wigner terms plus a modified phase-space background; in (c), (d), and (f) we used free mass and width parameters; in (g) the fit was obtained using masses and widths fixed at the values obtained in the fit to (d). The solid curve in (h) is a fit with one Breit-Wigner term plus modified background; the background is indicated by the dashed curve.

from the  $5\pi$  channel (four combinations per event). A fit of a Gaussian function to this histogram for the  $\omega$  meson with phase space modified by a polynomial yielded  $2709 \pm 110$   $\omega$  events above background.<sup>7</sup> Figures 1(b) and 1(c) show the  $5\pi$  mass distributions from Reaction (1) for the total sample and the six-prong subsample, respectively. There are suggestions of enhancements in the 1.3- and 1.65-GeV regions, which are seen more clearly in the more tightly constrained six-prong



data. An  $\eta'$  signal is evident near 0.96 GeV. We then select events for which at least one neutral  $3\pi$  mass combination is in the region  $750 \leq M_{3\pi} < 825$  MeV and plot the resulting  $5\pi$  mass distribution for the six-prong data in Fig. 1(d). Fits to the distributions in Fig. 1 are described in the caption. The enhancements at 1.3 and 1.65 GeV are again clearly visible, but this does not prove that the effects correspond to  $\omega\pi\pi$  decays, since there is a high probability for any low-mass  $5\pi$  system to have at least one  $3\pi$  combination in the above-defined  $\omega$  region. Therefore, we show in Fig. 1(g) the  $\omega$  signal as a function of the  $5\pi$  mass for the six-prong events.<sup>8</sup> There are distinct peaks in the spectrum in the 1.3- and 1.65-GeV regions. A fit to this spectrum using masses and widths fixed at values found in the fit to Fig. 1(d) gives our best estimates for the number of true  $\omega\pi\pi$  decays for the two enhancements.

Figures 1(e) and 1(f) show for Reaction (2) the total  $\pi^+\pi^-\pi^0$  mass distribution and the  $\pi^+\pi^-\pi^0$  mass distribution for events with at least one dipion mass combination in the  $\rho$  mass region ( $0.68 < M_{\pi\pi} < 0.84$  GeV).<sup>9</sup> Identification of the 1.3- and 1.65-GeV  $\omega\pi\pi$  enhancements with decays of the  $A_2$  and  $\omega(1675)$  mesons is supported by the observation of strong  $A_2$  and  $\omega(1675)$  signals in these distributions. The  $A_2$  and the  $\omega(1675)$  signals in the separate  $\rho^+$ ,  $\rho^-$ , and  $\rho^0$  selections (not shown) are consistent with the expected branching ratios for the  $I=1$  and  $I=0$  states.

The fits in Figs. 1(c), 1(d), and 1(g) yield  $57 \pm 15$ ,  $62 \pm 16$ , and  $57 \pm 17$   $A_2$  events, consistent with the interpretation that this  $A_2$  decay proceeds entirely through the  $\omega\pi\pi$  channel. Masses and widths obtained from the fits to Figs. 1(c) and 1(d) are consistent with the values obtained from the fit to the  $3\pi$  mass distribution of Fig. 1(f). Our best estimates of the masses and widths from fits to the  $A_2$  peaks are listed in Table I. After a 10.4% correction for unobserved decay modes of the  $\omega$ , we obtain the branching ratio  $\Gamma(A_2 \rightarrow \omega\pi\pi)/\Gamma(A_2 \rightarrow \rho\pi) = 0.28 \pm 0.09$ .<sup>10</sup> From Reaction (2) we obtain the cross section  $\sigma(\pi^+n \rightarrow A_2^0 p, A_2^0 \rightarrow \rho\pi) = 65 \pm 11 \mu\text{b}$ .

In Figs. 2(a) and 2(c) we show the  $t'$  distributions for the  $A_2 \rightarrow \rho\pi$  and  $A_2 \rightarrow \omega\pi\pi$  events. The numbers of resonant events above background were obtained from fits to the mass plots for each  $t'$  interval. These distributions are compatible with two decay modes of the same state. Fits of the data in Figs. 2(a) and 2(c) with the form  $Ae^{-bt'}$  give slopes  $b = 2.0 \pm 0.6$  and  $b = 2.7 \pm 0.5$ , respectively. Studies of the decay angles

TABLE I. Masses, widths, and branching ratios for decay modes of the  $A_2$  and  $\omega(1675)$ . The  $A_2$  branching ratio is normalized to the  $\rho^+\pi^0$  mode; the  $\omega(1675)$  branching ratios are normalized to the  $\rho^+\pi^0$  mode. In the table the notation  $5\pi$  means  $\pi^+\pi^+\pi^-\pi^-\pi^0$ .

Decay mode	$M$ (MeV)	$\Gamma$ (MeV)	Branching ratio (%)
$A_2 \rightarrow \omega\pi^+\pi^-$	$1325 \pm 9$	$74 \pm 20$	$28 \pm 9$
$\rightarrow \rho^+\pi^0$	$1313 \pm 8$	$135 \pm 21$	...
$\omega(1675) \rightarrow 5\pi$	...	...	$97 \pm 28$
$\rightarrow \omega\pi^+\pi^-$	$1660 \pm 13$	$122 \pm 39$	$47 \pm 18$
$\rightarrow B^+\pi^0$	...	...	$32 \pm 16$
$\rightarrow \rho^+\pi^0$	$1678 \pm 14$	$167 \pm 40$	...

and their moments gave no further information about the  $\omega\pi\pi$  decay of the  $A_2$ .

In a previous experiment,<sup>1</sup> the  $\omega\pi\pi$  decay of the  $A_2$  was reported to be associated with an  $\omega\pi$  resonance having a mass and width of  $1040 \pm 5$  and  $\sim 55$  MeV. We have studied the  $\omega\pi^+$  mass plot [Fig. 2(e)] for events in the region  $1.24 \leq M_{\omega\pi\pi} < 1.38$  GeV and observe no confirmation of this effect. Unmodified phase space (smooth curve) gives a good fit to the distribution ( $\chi^2 = 4.2$  for 11 degrees of freedom).

We associate the  $5\pi$  enhancement in the 1.65-GeV region [Figs. 1(b)–1(d)] with the  $\omega(1675)$  meson.<sup>11</sup> The  $\rho\pi$  decay modes of this state are clearly visible in the  $3\pi$  mass plot of Fig. 1(e) and the  $\rho$ -selected distribution of Fig. 1(f). From the fits to the  $3\pi$  and  $5\pi$  mass distributions we obtain estimates for the mass and width of the resonance in the  $\rho\pi$  and  $\omega\pi\pi$  decay modes (see Table I). From the fits to the mass spectra of Figs. 1(c), 1(d), and 1(g) we obtain  $204 \pm 40$ ,  $115 \pm 27$ , and  $90 \pm 31$  as estimates for the number of events in the  $\omega(1675)$  resonance. A comparison of the first and last of these numbers implies that there is a direct  $5\pi$  decay of the  $\omega(1675)$ . We therefore list separately in Table I the  $5\pi/\rho\pi$  and the  $\omega\pi\pi/\rho\pi$  branching ratios, where the  $5\pi$  mode includes submodes. Using the fits to Figs. 1(f) and 1(g), we find the branching ratio  $\Gamma(\omega(1675) \rightarrow \omega\pi^+\pi^-)/\Gamma(\omega(1675) \rightarrow \rho\pi) = 0.47 \pm 0.18$ . From Reaction (2) we obtain the cross section  $\sigma(\pi^+n \rightarrow \omega(1675)p, \omega(1675) \rightarrow \rho\pi) = 60 \pm 13 \mu\text{b}$ . The  $t'$  distributions for the  $\omega(1675)$  for the two decay channels [Figs. 2(b) and 2(d)] were fitted with the form  $Ae^{-bt'}$  and yield slopes  $b = 3.3 \pm 0.9$  and  $2.8 \pm 0.5$ . These distributions are consistent with alternative decay modes of the same state, as are the

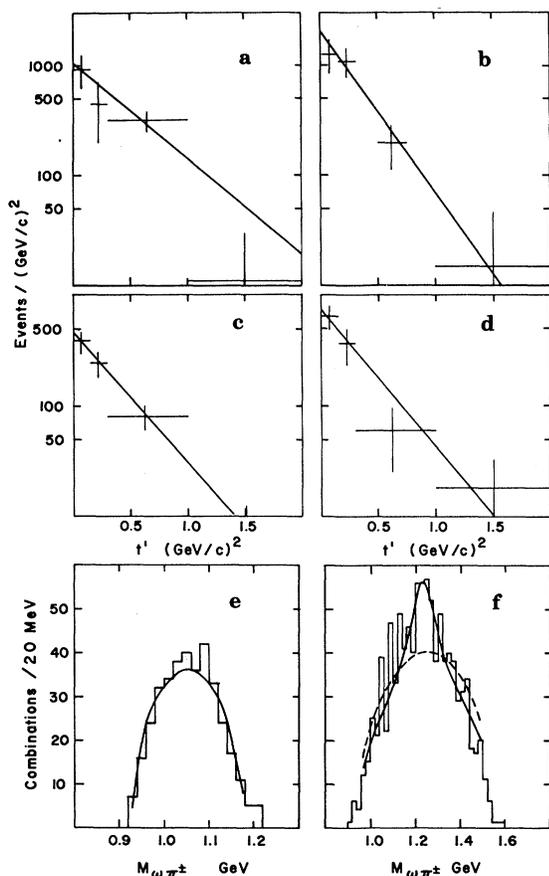


FIG. 2. (a) Background-subtracted  $t'$  distributions for the  $A_2 \rightarrow \rho^\pm \pi^\mp$  events from Reaction (2). (b) Same as (a) but for  $\omega(1675) \rightarrow \rho^\pm \pi^\mp$ . (c) Background-subtracted  $t'$  distributions for the  $A_2 \rightarrow \omega \pi^+ \pi^-$  events from Reaction (1). (d) Same as (c) but for  $\omega(1675) \rightarrow \omega \pi^+ \pi^-$ . (e)  $\omega \pi^\pm$  mass distribution in the  $A_2$  region from Reaction (1). (f)  $\omega \pi^\pm$  mass distribution in the  $\omega(1675)$  region from Reaction (1). The lines in (a)-(d) are fits to the data of the form  $Ae^{-bt'}$  in the range  $0 \leq t' \leq 2.0$  ( $\text{GeV}/c$ )<sup>2</sup>. Curve in (e), fit with unmodified phase space. Solid curve in (f), fit with unmodified phase space plus one Breit-Wigner term having fixed mass and width; dashed curve in (f), fit with unmodified phase space.

masses and widths listed in Table I.

A study of the  $\omega \pi^\pm$  mass plot [Fig. 2(f)] for the  $\omega(1675)$  region ( $1.60 < M_{\omega \pi^\pm} < 1.75$  GeV) indicates that a fraction of the  $\omega(1675)$  decays into  $B^\pm \pi^\mp$ . The possibility of this decay mode has been suggested by Matthews *et al.*<sup>12</sup> The solid and dashed curves in Fig. 2(f) correspond to fits of unmodified phase space with and without a Breit-Wigner resonance form for the  $B(1235)$ , and give  $\chi^2 = 31$  for 25 degrees of freedom and  $\chi^2 = 57$  for 26 degrees of freedom, respectively.<sup>13</sup> We show in Fig. 1(h) the number of  $B\pi$  events above back-

ground as a function of  $M_{5\pi}$ . A fit to this plot gives  $201 \pm 91$  events in the  $\omega(1675)$  resonance, corresponding to a branching ratio<sup>14</sup>  $\Gamma(\omega(1675) \rightarrow B^\pm \pi^\mp) / \Gamma(\omega(1675) \rightarrow \rho \pi) = 0.32 \pm 0.16$ . A study of the decay angles and moments for the  $B\pi$  and  $\omega \pi \pi$  modes of the  $\omega(1675)$  gave no further information. If  $J^P = 1^+$  for the  $B$  meson, the observation of both a  $\rho \pi$  and a  $B\pi$  decay mode requires  $J \geq 1$  for the  $\omega(1675)$ .

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\*Presently at Junta de Energía Nuclear, Madrid, Spain.

†Deceased.

‡Work supported by the National Science Foundation.

§Presently at Technion, Haifa, Israel.

||Presently at Bell Laboratories, Whippany, N.J. 07981.

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<sup>1</sup>C. Defoix, L. Dobrzynski, P. Espigat, A. Nascimente, J. O'Neill, P. Rivet, and J. Slaud, Phys. Lett. **43B**, 141 (1973).

<sup>2</sup>Lawrence Berkeley Laboratory Group A, as reported by S. M. Flatté, in *Proceedings of the Sixteenth International Conference on High Energy Physics, The University of Chicago and National Accelerator Laboratory, 1972*, edited by J. D. Jackson and A. Roberts (National Accelerator Laboratory, Batavia, Ill., 1973), Vol. 1, p. 132.

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<sup>4</sup>J. A. Danysz, B. R. French, and V. Simak, Nuovo Cimento **51A**, 801 (1967).

<sup>5</sup>G. P. Yost, G. B. Yodh, M. Einschlag, T. B. Day, and R. G. Glasser, as reported by B. French, in *Proceedings of the Fourteenth International Conference on High Energy Physics, Vienna, Austria, 1968*, edited by J. Prentki and J. Steinberger (CERN Scientific Information Service, Geneva, 1968), p. 91.

<sup>6</sup>V. E. Barnes, S. U. Chung, R. L. Eisner, E. Flaminio, P. Guidoni, J. B. Kinson, and N. P. Samios, Phys. Rev. Lett. **23**, 142 (1969).

<sup>7</sup>The data for Reaction (1) exhibit  $\Delta(1236)$  production. Since the results obtained are insensitive to a  $\Delta$  cut,  $\Delta$  events have not been removed.

<sup>8</sup>For each 100-MeV-wide  $5\pi$  mass interval the  $3\pi$  mass distribution was fitted with modified phase space plus  $\omega$  Gaussian functions for the  $\eta$  and  $\omega$ . The numbers of  $\omega$  events from these fits are shown in Fig. 1(g).

<sup>9</sup>To remove  $\pi\pi \rightarrow \rho\Delta$  events from Reaction (2), we exclude events with  $|t - t_{\min}| < 0.1$  ( $\text{GeV}/c$ )<sup>2</sup> and 1.16

$\leq M_{p\pi^-,0} < 1.32$  GeV, where  $t$  is the square of the momentum transfer between the beam pion and the outgoing di-pion system.

<sup>10</sup>Previous measurements (Refs. 1-3) of this branching ratio gave the values  $0.23 \pm 0.07$ ,  $0.08 \pm 0.05$ , and  $0.10 \pm 0.05$ , where the first value (Ref. 1) was obtained from an assumed cascade decay  $A_2 \rightarrow B_1(1040)\pi \rightarrow \omega\pi\pi$  and where  $B_1(1040)$  is a new enhancement reported in Ref. 1. The weighted average of these three branching ratios is  $0.11 \pm 0.03$ . With our measurement the new weighted average is  $0.14 \pm 0.03$ .

<sup>11</sup>An  $A_3$  interpretation is disfavored since the reactions considered in this report are charge exchange, whereas the  $A_3$  is usually seen in non-charge-exchange reactions. Furthermore, we see no  $A_3 \rightarrow f\pi$  in Reaction (2). To check for an  $I=1$  interpretation for the 1.65-

GeV  $\omega\pi\pi$  state, we have looked for a  $\rho^0\omega$  contribution by examining the  $\rho^0$  signal as a function of  $M_{\omega\pi\pi}$  (not shown). We find a smoothly varying  $\rho^0\omega$  signal across the 1.65-GeV region consistent with no  $\rho^0\omega$  contribution.

<sup>12</sup>J. A. J. Matthews, J. D. Prentice, T. S. Yoon, J. T. Carroll, M. W. Firebaugh, and W. D. Walker, Phys. Rev. D **3**, 2561 (1971).

<sup>13</sup>The mass and width of the  $B(1235)$  were fixed at 1.237 and 0.118 GeV. T. A. Lasinski *et al.*, Rev. Mod. Phys., Suppl. **45**, S1 (1973).

<sup>14</sup>In Figs. 1(c), 1(d), and 1(g) we have used the high-resolution six-prong events only; in Figs. 1(h) and 2(c) through 2(f) we have used the five- and six-prong events. For the  $3\pi$  channel, three- and four-prong events have been used throughout. Appropriate corrections have been applied to the branching ratios.

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## ERRATA

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EXCITATION OF GIANT RESONANCES IN  $^{58}\text{Ni}$  VIA INELASTIC SCATTERING OF POLARIZED PROTONS. D. C. Kocher, F. E. Bertrand, E. E. Gross, R. S. Lord, and E. Newman [Phys. Rev. Lett. **31**, 1070 (1973)].

In Fig. 2, the DWBA predictions for the analyzing power were inadvertently plotted with the wrong sign. The data points are plotted correctly. Thus, we find that the analyzing power in the region  $E_x \approx 14.6-16.7$  MeV gives better agreement with the  $E0$  prediction than with the  $E2$  prediction, while the cross section in the region  $E_x \approx 12.7-23.7$  MeV (see Fig. 3) shows a preference for an  $E2$  assignment. We are currently investigating possible causes of this ambiguity.

The authors are indebted to G. R. Satchler for bringing this error to our attention.

DIFFERENTIAL CROSS SECTIONS IN  $\pi^-p \rightarrow K^0\Lambda^0$  AND  $\pi^-p \rightarrow K^0\Sigma^0$  FROM 3 TO 6 GeV/c. C. E. W. Ward, I. Ambats, A. Lesnik, W. T. Meyer, D. R. Rust, and D. D. Yovanovitch [Phys. Rev. Lett. **31**, 1149 (1973)].

In Ref. 5, read "A. Bashian *et al.* . . .," instead of "A. Abashian *et al.* . . . ."