

find  $|G_Y|^2 < 0.02 |G_F|^2$ .

In conclusion, we see no evidence for a charged positive heavy muon (lepton number = +1) coupled to muon neutrinos. It now appears, in contrast to very simple gauge models, that if such a heavy lepton exists it either is very massive or has a small effective coupling constant.

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<sup>7</sup>Heavy leptons produced by neutrinos would have predominantly negative helicity. The  $\mu^+$  from a  $V-A$  decay interaction have smaller laboratory acceptance than from  $V+A$  decay. For example, if  $M_Y = 8 \text{ GeV}/c^2$ , the  $V+A$  decay assumption would produce a factor of 1.25 increase in the expected number of detected  $\mu^+$ .

<sup>8</sup>Preliminary result reported by B. Richter at the Conference on Lepton Induced Reactions, Irvine, California, 7-8 December 1973 (unpublished).

## Approximate Scaling of Multiplicity Distributions as a Function of Missing Mass

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Data from  $p+p \rightarrow p+X$  at 102, 205, and 405 GeV and from  $\pi^-+p \rightarrow p+X$  at 205 GeV exhibit an approximate scaling property in the charged-prong multiplicity distributions as a function of the missing mass for the range  $5 \leq M_X \leq 13 \text{ GeV}$ .

A well-known empirical fact<sup>1</sup> is the approximate scaling of the charged-particle multiplicity cross sections  $\sigma_N(s)$  in the reaction  $p+p \rightarrow X$ :

$$P_N(s) = \frac{\sigma_N(s)}{\sigma(s)} \cong \frac{1}{\langle N(s) \rangle} \psi \left( \frac{N}{\langle N(s) \rangle} \right), \quad (1)$$

where  $\sigma(s)$  is the inelastic cross section and  $\langle N(s) \rangle$  the average charged multiplicity. Although the variation of the scaling function  $\psi$  with the center-of-mass energy  $\sqrt{s}$  is definite,<sup>2-4</sup> it is small, hence the usefulness of Eq. (1). Based upon a geometrical picture,<sup>5</sup> Barshay and Yama-

guchi<sup>6</sup> suggested looking for a more difficult scaling behavior in the reaction  $p+p \rightarrow p+X$ . In particular they suggested looking for scaling of multiplicity distributions as a function of the missing mass of  $X$ , hereafter denoted by  $M$ :

$$P_n(M^2, s) = \frac{\sigma_n(M^2, s)}{\sigma(M^2, s)} \cong \frac{1}{\langle n(M^2, s) \rangle} \tilde{\psi} \left( \frac{n}{\langle n(M^2, s) \rangle}, s \right). \quad (2)$$

Here  $n$  is the associated multiplicity,  $n = N - 1$ .

We have examined data on associated charged-prong multiplicities as a function of missing mass from  $pp$  and  $\pi^-p$  interactions in the energy range 102 to 405 GeV. Details of event identification in the reactions  $p(\pi^-)+p \rightarrow p+X$  are given by Chapman *et al.*,<sup>7</sup> Barish *et al.*,<sup>8</sup> and Winkelmann *et al.*<sup>9</sup> We give results from 205-GeV  $pp$  interactions for all multiplicities and for the  $M^2$  interval  $0 < M^2 < 150 \text{ GeV}^2$ . We use published results for multiplicities  $n < 10$  in the  $M^2$  interval  $0 < M^2 < 70 \text{ GeV}^2$  for  $pp$  interactions at 102 and 405 GeV,<sup>7</sup> and  $0 < M^2 < 120 \text{ GeV}^2$  for  $\pi^-p$  interactions at 205 GeV.<sup>9</sup> In all cases  $M^2$  is below the value where experimental losses set in as a result of detection inefficiency of the slow proton. Where not given, the experimental errors for  $\langle n(M^2, s) \rangle \times P_n(M^2, s)$  are estimated from the known microbarn equivalents of the experiments and the published  $d\sigma_n/dM^2$  distributions. The  $M^2$  bins are chosen such that statistical errors are about the same.

Figure 1 shows  $\langle n(M^2) \rangle P_n(M^2, s)$  for the  $pp$  data. An approximate scaling behavior as in Eq. (2) is exhibited. There is no marked  $s$  dependence. As has been noted,<sup>10</sup> the scaling function in  $p+p \rightarrow X$  [Eq. (1)] is not very sensitive to details of the

multiplicity distributions. We therefore give in Table I the values of various moments of the multiplicity distributions in different  $M^2$  bins for the 205-GeV  $pp$  data. If Eq. (2) holds,

$$C_k = \langle n^k(M^2) \rangle / \langle n(M^2) \rangle^k$$

must be independent of  $M^2$ . Except for the low-mass bin, the data are consistent with such a trend. It would be valuable to study the low-mass region more differentially. Note that  $\langle n(M^2) \rangle$  varies by more than a factor of 2 over the  $M^2$  region studied.

In Fig. 2 we show the 205-GeV data on  $\pi^-+p \rightarrow p+X$ . The curve represents the  $pp$  data from Fig. 1. The distributions are quite similar.

It has been noted<sup>8,11</sup> that the  $M^2$  dependences of  $\langle n(M^2) \rangle$  and  $\langle n^2(M^2) \rangle$  in  $p+p \rightarrow p+X$  are similar to the  $s$  dependences of  $\langle [N(s) - 1] \rangle$  and  $\langle [N(s) - 1]^2 \rangle$  in  $p+p \rightarrow X$ , provided one postulates<sup>11</sup> a suitable relation between  $M$  and an "equivalent"  $\sqrt{s}$ . We emphasize however, that approximate scaling properties for  $P_{(n-1)}(s)$  and  $P_n(M^2)$  are independent empirical results since at any *given*  $s$  one sums over *all*  $M^2$ .

We conclude that the multiplicity distributions

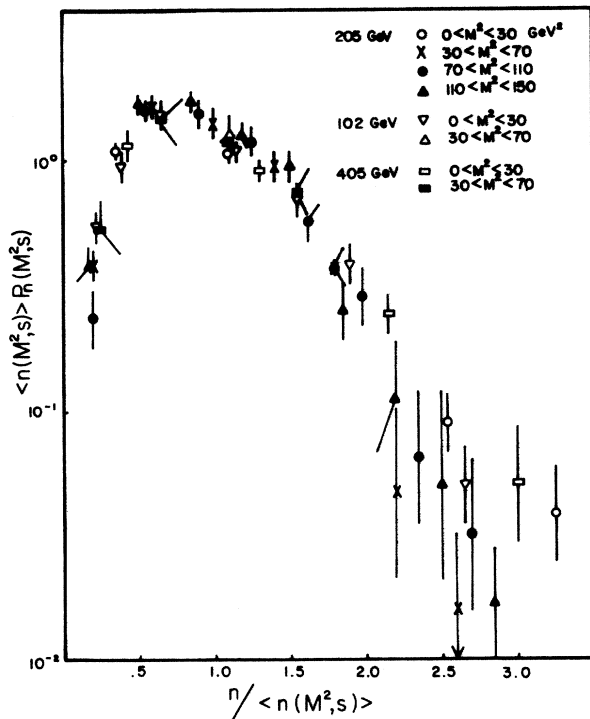


FIG. 1.  $\langle n(M^2, s) \rangle P_n(M^2, s)$  versus  $n / \langle n(M^2, s) \rangle$  for  $p+p \rightarrow p+X$  in  $M^2$  bins and at laboratory momenta as indicated.

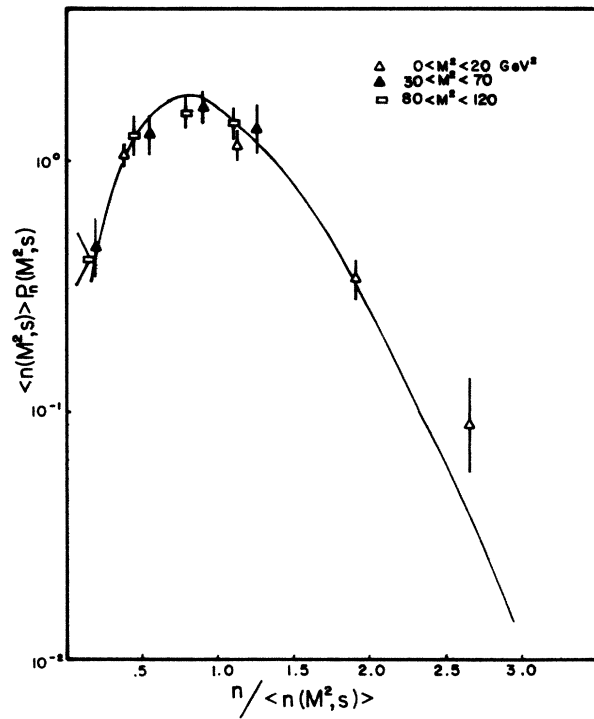


FIG. 2. Data for  $\pi^-+p \rightarrow p+X$  at 205 GeV plotted as in Fig. 1. The curve represents the data in Fig. 1.

TABLE I. The average associated multiplicity  $\langle n \rangle$  and the moments  $C_k$  of the multiplicity distribution in different  $M^2$  bins for the 205-GeV data.

$M^2$ range (GeV <sup>2</sup> )	$\langle n \rangle$	$C_2$	$C_3$	$C_4$
0-30	2.74 ± 0.09	1.41 ± 0.03	2.54 ± 0.17	5.54 ± 0.69
30-70	4.85 ± 0.13	1.22 ± 0.02	1.71 ± 0.06	2.66 ± 0.18
70-110	5.55 ± 0.14	1.23 ± 0.02	1.77 ± 0.07	2.87 ± 0.20
110-150	6.03 ± 0.15	1.23 ± 0.02	1.73 ± 0.06	2.70 ± 0.18

$P_n(M^2, s)$  in the reactions  $p(\pi^-) + p \rightarrow p + X$  exhibit an approximate scaling behavior over a wide range of missing mass  $5 < M < 13$  GeV. This feature does not change markedly with  $s$  (as shown for  $p + p \rightarrow p + X$ ). We note that our empirical result would follow from (a) the existence (for given  $s$ ) of multiplicity distributions at each four-momentum transfer to the proton  $\sqrt{-t}$ , of the form

$$P_n(\sqrt{-t}, M^2) = \frac{\sigma_n(\sqrt{-t}, M^2)}{\sigma(\sqrt{-t}, M^2)} \approx \frac{1}{\langle n(\sqrt{-t}, M^2) \rangle} \Phi\left(\frac{n}{\langle n(\sqrt{-t}, M^2) \rangle}, \sqrt{-t}\right),$$

with the *only*  $M^2$  dependence coming through the average associated multiplicity  $\langle n(\sqrt{-t}, M^2) \rangle$ ; and (b) approximate factorization of  $\langle n(\sqrt{-t}, M^2) \rangle$  and  $\sigma(\sqrt{-t}, M^2)$ .<sup>6</sup> It would be useful to investigate these properties with high-statistics data.<sup>12,13</sup>

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