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## SUBMILLIMETER CYCLOTRON RESONANCE IN TELLURIUM

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We report cyclotron resonance measurements in high-purity tellurium at submillimeter wavelength confirming that the isoenergetic surfaces involved at low magnetic fields are ellipsoids grouped by pairs symmetrical with respect to the Brillouin-zone corners. We explain the violent perturbation of the Landau levels at high magnetic field by assuming the ellipsoids to coalesce into dumb-bell surfaces, as for the Shubnikov-de Haas effect.

A recent band-structure calculation<sup>1</sup> for tellurium predicts near the corner  $M$  of the Brillouin zone a valence band of the shape depicted in Fig. 1(a). Near the maximum of the valence band the isoenergetic surfaces are ellipsoids, of revolution around the trigonal axis  $c$ , centered in  $N$  and  $N'$  symmetrical with respect to  $M$  [surfaces  $S_{E_1}$  in Fig. 1(b)]. When the energy increases up to  $E_S$  these ellipsoids coalesce into a "dumb-bell" shaped surface (surface  $S_{E_2}$ ). Such a model, with the assumption of a constant quadratic dependence of  $E$  with  $k \perp c$ , allowed the interpretation of Shubnikov-de Haas results.<sup>2,3</sup> Previous cyclotron resonance experiments at magnetic

fields lower than ours<sup>4-6</sup> showed ellipsoidal isoenergetic surfaces

$$E(k) = \hbar^2 \left[ \frac{k_x^2 + k_y^2}{2m_1} + \frac{k_z^2}{2m_3} \right],$$

with

$$m_1 = (0.119 \pm 0.006)m_0, \quad m_3 = (0.25 \pm 0.01)m_0$$

(Ref. 4);

$$m_1 = (0.109 \pm 0.003)m_0, \quad m_3 = (0.264 \pm 0.008)m_0$$

(Ref. 5).

Our experiment has been realized with high-

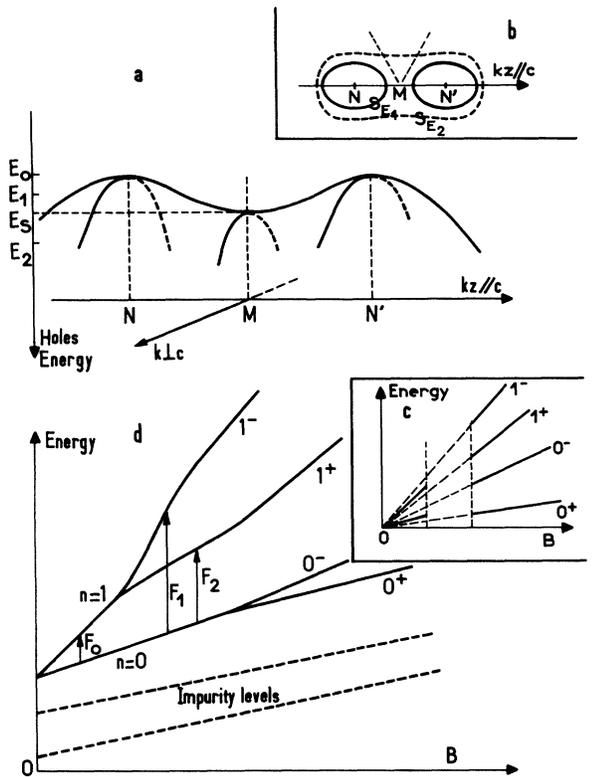


FIG. 1. (a) Shape of the valence band near the Brillouin-zone corner. The maximum  $E_0$  of the valence band is shifted from the trihedral vertex along the side edge of the prism. (b) Section of the isoenergetic surfaces cut by a plane parallel to the  $c$  axis.  $SE_1$  corresponds to  $E_1$  close to  $E_0$ ;  $SE_2$  to  $E_2 > E_S$ . (c) Scheme of the Landau levels at low and high magnetic field deduced from a Bohr-Sommerfeld argument. (d) Scheme of the Landau levels deduced from a quantum calculation.

purity  $p$ -type samples<sup>7</sup>  $n_p \sim 10^{13}$  carriers/cm<sup>3</sup>,  $\mu \sim 100\,000$  cm<sup>2</sup>/V sec at  $T \sim 4^\circ$ . For our experimental frequencies  $\nu > 300$  GHz, we have  $\omega\tau > 10$  and  $\omega/\omega_p > 4$ . Working at  $\omega > \omega_p$  allows the use of a transmission technique.<sup>4</sup>

The frequency band 280-740 GHz is covered by five CSF carcinotrons. The microwaves are transmitted through oversized waveguides. An Allen-Bradley bolometer is used to measure the transmitted power. The direction of the magnetic field  $\vec{B}$  is either parallel or perpendicular to the trigonal axis  $c$  of the crystal.

$\vec{B} \parallel c$ . - The cyclotron resonance is an intense absorption line ( $F_c$ ) for which the relation between frequency and magnetic field is linear up to  $B = 28$  kG. Some other absorption lines show up at these high frequencies, probably related to the existence of impurity levels: (i) A doublet of

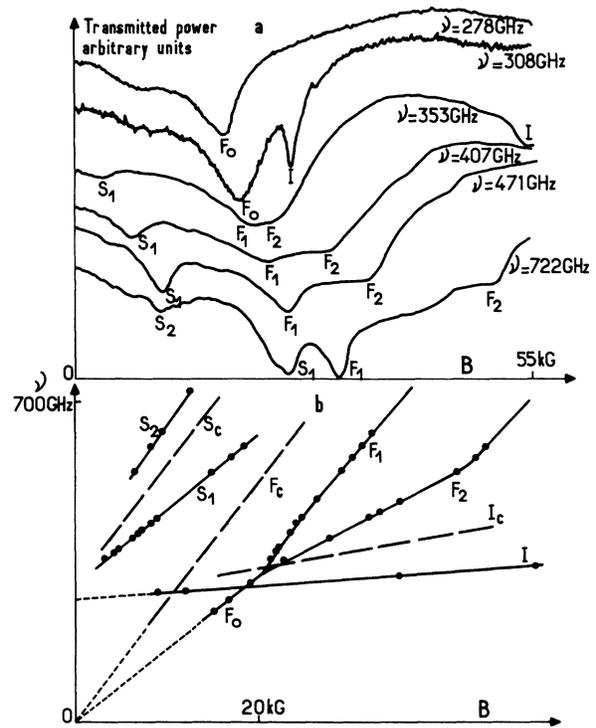


FIG. 2. (a)  $\vec{B} \perp c$ : Experimental recordings (at various frequencies) of the transmitted microwave power as a function of the magnetic field. The main absorption line  $F_0$  (cyclotron resonance) splits into  $F_1$  and  $F_2$  at  $B \sim 20$  kG,  $\nu \sim 320$  GHz. The secondary lines are labeled  $I$ ,  $S_1$ ,  $S_2$ . (b) Plot of the frequency versus magnetic field for the absorption lines. Solid lines,  $\vec{B} \perp c$ ; dashed lines,  $\vec{B} \parallel c$ .

sharp lines  $I_c$  shows up with a small magnetic field dependence (it disappears when the microwave is exactly polarized with its electric field perpendicular to  $\vec{B}$ ). (ii) A secondary line  $S_c$  appears for  $\nu > 300$  GHz; in an  $\omega(B)$  diagram the corresponding experimental points fall on a straight line which extrapolates to  $(B=0, \nu=300$  GHz).

$\vec{B} \perp c$ . - At the lower frequencies  $\nu \sim 300$  GHz the cyclotron resonance shows up on the recording [Fig. 2(a)] as a broad, intense absorption line  $F_0$  at a magnetic field proportional to  $\omega$  [Fig. 2(b)]. At higher frequencies  $\nu > 330$  GHz the cyclotron resonance line  $F_0$  splits into two lines  $F_1$  and  $F_2$  behaving differently with the increase of the frequency. Also, some new secondary absorption lines show up which will be related to the existence of impurity levels: (i) A sharp absorption peak  $I$  at a frequency depending weakly on the magnetic field. (ii) Two secondary lines  $S_1 S_2$  appear at low  $B$ . The position of  $S_1$  in the  $\omega(B)$  diagram can be extrapolated to  $B=0, \nu=300$  GHz.

For decreasing values of the angle between  $\vec{B}$  and  $c$ ,  $F_0$  transforms itself continuously into  $F_C$ ,  $S_1$  into  $S_{1C}$ , and  $I$  into  $I_C$ .

**Discussion.**—The tellurium sample used in these experiments is nondegenerate and at  $\nu = 300$  GHz,  $\hbar\omega_C \sim 1.24$  meV,  $\hbar\omega_C \gg kT$  for  $T = 1.8^\circ\text{K}$ . Hence the sample is in the extreme quantum limit. We first treat the fundamental cyclotron absorption lines  $F_0$ ,  $F_1$ ,  $F_2$ , and  $F_C$ .

(i) At low field, the carriers stay around points  $N$  or  $N'$  in the Brillouin zone. Where the energy has the usual quadratic  $k$  dependence, they occupy normal Landau levels with energies  $E_n = (n + \frac{1}{2})\hbar\omega_C$ ,  $\omega_C$  proportional to  $B$ . The observed transition between  $n = 0$  and  $n = 1$  gives the ellipsoid effective masses

$$m_1 = (0.109 \pm 0.001)m_0, \quad m_3 = (0.29 \pm 0.02)m_0.$$

(ii) At high field the behavior depends on the magnetic field direction. For  $\vec{B} \parallel c$ , the energy is still quadratic in  $k_\perp$  and leads to a normal Landau quantization. The absorption frequency  $\nu$  is proportional to  $B$ . For  $\vec{B} \perp c$ , the  $E(k)$  relation becomes more complicated and the previous Landau scheme is no longer valid. A qualitative discussion can be based on semiclassical arguments. The carrier orbits in reciprocal space should enclose quantized areas  $A_n$  given by the Bohr-Sommerfeld condition,

$$\partial A_n = A(E_{n+1}) - A(E_n) = 2\pi eH/\hbar c. \quad (1)$$

At low fields (1) involves the elliptic sections of the isoenergetic surfaces  $S_{E_1}$  (Fig. 1) and leads to the Landau levels of case (i). At higher field the orbit dimensions must increase and the orbits now belong to the type  $S_{E_2}$  surfaces which result from the coalescence of two  $S_{E_1}$  ellipsoids. Hence an energy difference  $E_{n+1} - E_n$  roughly twice smaller than for case (i) is now large enough to meet condition (1) [Fig. 1(c)].

As a result, the energy level quantization will be deeply modified from case (i) to case (ii), and the transition between these two regimes can be described only through a more detailed quantum mechanical calculation (for instance, in the effective-mass approximation). One can show<sup>8</sup> that each low-field Landau level splits into two levels,  $n = 0 \rightarrow 0^+$ ,  $0^-$ ;  $n = 1 \rightarrow 1^+$ ,  $1^-$  [Fig. 1(d)]; the splitting occurs when the level energy comes close to

$E_S$ . This scheme accounts for the observed fundamental absorption curves  $F_0$  ( $n = 0 \rightarrow n = 1$ ) giving rise to  $F_1$  ( $0 \rightarrow 1^-$ ) and  $F_2$  ( $0 \rightarrow 1^+$ ), when the  $n = 1$  level diverges at  $\nu \sim 320$  GHz (the fields used here are not high enough to reveal the  $n = 0 \rightarrow 0^+$ ,  $0^-$  splitting). One gets for  $E_S$  at  $\nu_C \sim 320$  GHz,  $E_S \sim \frac{3}{2}\hbar\omega_C \sim 2$  meV.

The secondary lines  $S_1, S_2, S_C, I, I_C$  can be related to transitions involving impurity states.<sup>9</sup> A transition between two impurity levels can account for the sharp lines  $I$  and  $I_C$ . The  $S_C$  and  $S_1$  lines occur for frequencies which for a given  $B$  are very nearly those of the fundamental absorption plus a constant ( $\sim 300$  GHz). They can be ascribed to transitions from an impurity level (1.8 meV beneath the first Landau level  $n = 0$ ) towards the second ( $n = 1$ ) Landau level.  $S_2$  might be a harmonic of  $S_1$  corresponding to a final level  $n = 2$ . The precise study of impurity levels<sup>10</sup> is presently in progress.

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