

of the components in the oven are Pyrex—there does not appear to be any physical reason why the technique could not be extended to high temperatures.

Optical pumping utilizing the alkalis has in the past provided very precise values for free-atom hfs and g_J values. The high precision is especially useful in looking for effects caused by higher order multipole interactions. The present technique will make possible the pumping of a considerable number of new elements—As, Sb, Bi, Cr, Mn, Mo, Tc, Re, Cu, Ag, Au, Eu, and Am all have orbital S states with $J \neq 0$ and therefore can potentially be polarized by spin-exchange collisions.

Several aspects of interatomic interactions have been studied with optical pumping. These include pressure shifts of hfs¹⁰ and g_J values,¹¹ spin-exchange cross sections,²⁻⁵ spin-relaxation cross sections, and diffusion coefficients.¹² The ability to measure these quantities over an extended temperature range should greatly assist in their understanding. Of particular interest is the energy dependence of the electron-alkali spin-exchange cross section.¹³ It is also possible that the utility of optical pumping in chemistry may be increased.

We would like to thank Dr. Harry Hall for his

assistance.

*Work supported in part by the National Science Foundation.

¹A. Kastler, *J. Phys. Radium* **11**, 255 (1950).

²H. G. Dehmelt, *Phys. Rev.* **109**, 381 (1958).

³R. Novick and H. E. Peters, *Phys. Rev. Letters* **1**, 54 (1958).

⁴P. A. Franken, R. Sands, and J. Hobart, *Phys. Rev. Letters* **1**, 316 (1958).

⁵L. W. Anderson, F. M. Pipkin, and J. C. Baird, Jr., *Phys. Rev. Letters* **1**, 229 (1958).

⁶C. S. Hayne and H. G. Robinson, *Bull. Am. Phys. Soc.* **5**, 411 (1960).

⁷A different method for controlling alkali densities at high temperatures has recently been reported by A. Gallagher, *Phys. Rev.* **172**, 88 (1968). For nonalkalis see B. Carnac and G. Lemeignan, *Compt. Rend.* **264**, 1850 (1967).

⁸R. H. Lambert and J. J. Wright, *Rev. Sci. Instr.* **38**, 1385 (1967).

⁹H. Dahmen and S. Penselin, *Z. Physik* **200**, 256 (1967).

¹⁰P. L. Bender, E. C. Beaty, and A. R. Chi, *Phys. Rev. Letters* **1**, 311 (1958); M. Arditì and T. R. Carver, *Phys. Rev.* **109**, 1012 (1958).

¹¹R. M. Herman, *Phys. Rev.* **175**, 10 (1968).

¹²W. Franzen, *Phys. Rev.* **115**, 850 (1959).

¹³L. C. Balling, R. J. Hanson, and F. M. Pipkin, *Phys. Rev.* **133**, A607 (1964).

DETERMINATION OF MUONIUM HYPERFINE STRUCTURE INTERVAL THROUGH MEASUREMENTS AT LOW MAGNETIC FIELDS*

P. A. Thompson, J. J. Amato, P. Crane, V. W. Hughes, R. M. Mobley, G. zu Putlitz, and J. E. Rothberg
Gibbs Laboratory, Physics Department, Yale University, New Haven, Connecticut
(Received 17 December 1968)

The ground-state hyperfine structure interval $\Delta\nu$ of muonium has been remeasured with significantly improved accuracy through the observation of transitions between hfs states at low magnetic fields. The formation of muonium has been observed for the first time in krypton and the fractional pressure shift of $\Delta\nu$ has been measured in this gas. The average value of $\Delta\nu$ obtained from these measurements is $\Delta\nu = 4463.26 \pm 0.04$ Mc/sec.

The hyperfine structure interval $\Delta\nu$ of the muonium atom (μ^+e^-) in its ground state has been remeasured with improved accuracy through the observation of transitions between magnetic sublevels at weak magnetic field (about 3 G)¹ and at very weak magnetic field (about 10 mG). Compared with the earlier high-field experiment,^{2,3} these measurements involve some different ex-

perimental techniques and thus provide an independent determination of $\Delta\nu$. The more accurate value for $\Delta\nu$ can be used to obtain a value for the fine structure constant α , or to determine a value for the muon magnetic moment, μ_μ , free from uncertainties of magnetic shielding.⁴

In a low external static magnetic field H , the relative energies of the sublevels of muonium are

given with adequate accuracy in frequency units by the equations³

$$\nu_{F=0, M_F=0} = 0, \quad \nu_{1,1} = \Delta\nu + z,$$

$$\nu_{1,0} = \Delta\nu, \quad \nu_{1,-1} = \Delta\nu - z,$$

where the Zeeman term is $z = (g_J\mu_0^e + g_\mu\mu_0^\mu)H/2h$ in which g_J = electron g value and g_μ = muon g value. Under weak-field conditions ($H \approx 3$ G) the transitions $(F, m_F) = (1, 1) \leftrightarrow (0, 0)$ and $(1, -1) \leftrightarrow (0, 0)$ are experimentally well resolved, since $z \approx 4$ Mc/sec. At very weak field ($H \approx 10$ mG) these transitions are unresolved since $z \approx 0.01$ Mc/sec and the observed resonance linewidth is greater than 0.5 Mc/sec. The smallness of the Zeeman term at low magnetic field provides a distinct experimental advantage over measurements at a high magnetic field.

The theory of the resonance line shape for the weak-field case involves only two levels and has been given.^{2,3} In the very weak field case, the line-shape theory must consider the three levels $(F, m_F) = (1, 1), (1, -1),$ and $(0, 0)$. Solutions have been obtained for the state amplitudes in this case. The resulting line shapes are Lorentzian with increased widths and heights as compared with the two-level case. The level $(F, m_F) = (1, 0)$ does not enter the calculation under the assump-

tion that the time-varying magnetic field is perpendicular to the static field.

The experimental method is similar in principle to that of the high-field experiment. Polarized muonium is formed by stopping muons from the Nevis synchrocyclotron in a high-pressure noble-gas target (See Fig. 1). The microwave-induced changes in the populations of the magnetic levels are observed through the resulting change in the angular distribution of the decay positrons. A structure consisting of three large Moly-Permalloy shields surrounding a solenoid and associated correction coils was used to generate the necessary static fields of 2.85 and 0.010 G. For the very weak-field case the solenoid and coils were disconnected, and the outer shield was equipped with Mumetal end caps. The maximum instability and inhomogeneity of the field over the target region were ± 1 and ± 3 mG, respectively. At weak field the static magnetic field was mapped and monitored with a Rb⁸⁵ optical-pumping magnetometer. At very weak field a fluxgate magnetometer was used. The microwave frequency was harmonically generated from a crystal oscillator with a frequency stability of better than 1 part in 10^7 . After amplification this signal was used to drive a high- Q cavity in the TM₂₂₀ mode in which the time-dependent magnetic field was perpendicular to the static field H . A fast feedback system

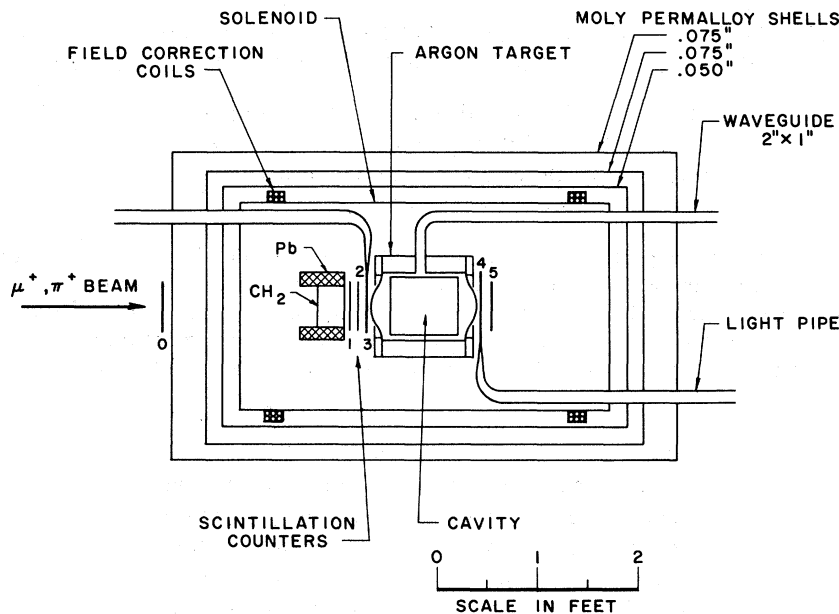


FIG. 1. Schematic diagram of experimental arrangement for observing muonium hfs transitions at low magnetic fields.

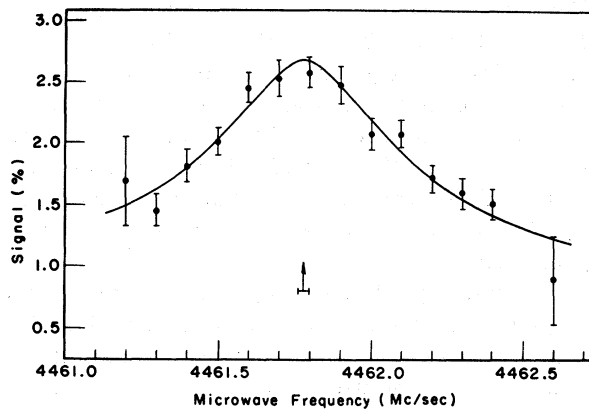


FIG. 2. Resonance curve observed at $H=0.010$ G for the unresolved transitions $(F, M_F) = (1, -1) \leftrightarrow (0, 0)$ and $(1, 1) \leftrightarrow (0, 0)$ in krypton buffer gas at 32 800 Torr. The error bars (1 standard deviation) are due to counting statistics. The solid curve is a best fit to a theoretical Lorentzian line shape. The fitted center is 4461.779 ± 0.017 Mc/sec.

was used to stabilize the microwave power level to 2%. The resonance line was observed by varying the microwave frequency. The temperature and pressure of the buffer gas were monitored continuously with uncertainties of $\pm 0.5^\circ\text{C}$ and ± 1 psi, respectively.

Data were taken with both argon and krypton at two different pressures. Figure 2 shows an observed resonance curve at very weak magnetic field obtained in about 100 h of beam time. The experimental data fit Lorentzian line shapes very well. Increasing the gas density increases both the stopping rate and the uncertainty introduced by the pressure-shift extrapolation; for these reasons pressures in the range 20-60 atm were used. Figure 3 shows a plot of all the weak- and very weak-field data.

A value for the fractional pressure shift (FPS) [$\text{FPS} = (1/\Delta\nu)\partial\Delta\nu/\partial P$] may be obtained from the slope of the straight-line fit to the observed points. The values may be compared with the FPS values for hydrogen in the same buffer gases. For muonium⁵ in argon at high field the FPS = -4.05 ± 0.49 ; at low field the FPS = -4.07 ± 0.25 . For hydrogen in argon⁶ the FPS = -4.78 ± 0.03 . For muonium in krypton the FPS = -10.4 ± 0.30 . For hydrogen in krypton⁷ the FPS = -10.4 ± 0.20 . All FPS values are in units of $10^{-9}/(\text{Torr at } 0^\circ\text{C})$. The apparent difference between the FPS values for muonium and hydrogen in Ar may be evidence of an isotope dependence of the FPS⁸ or of a non-linearity in the density dependence of $\Delta\nu$. There is excellent agreement between the FPS values

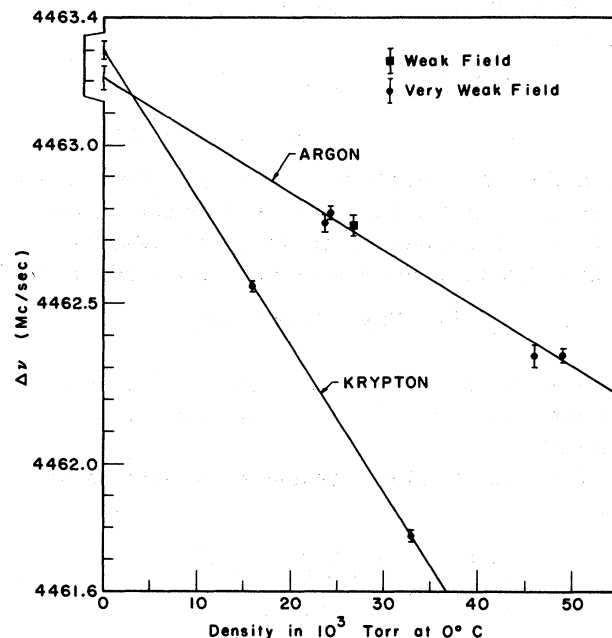


FIG. 3. Observed values of $\Delta\nu$ versus gas density for Ar and Kr. The solid curves are straight lines fitted to the data. The density has been corrected for the departure from ideal-gas behavior. The points at zero density are the extrapolated intercepts and not measured values.

for muonium and hydrogen in Kr.

A value of $\Delta\nu$ for free muonium is obtained from the intercept of the straight-line fit to the data. The results are

$$\Delta\nu = 4463.302 \pm 0.027 \text{ Mc/sec (from Kr data),}$$

$$\Delta\nu = 4463.220 \pm 0.033 \text{ Mc/sec (from Ar data)}$$

in which the errors (1 standard deviation) are statistical counting errors. The sources of systematic errors considered and estimates (at least 1 standard deviation) of their effect on the determination of $\Delta\nu$ are as follows: (1) uncertainty in microwave power level in cavity, 5 kc/sec; (2) uncertainty in microwave frequency, 0.1 kc/sec; (3) instability and inhomogeneity of static magnetic field, 3 kc/sec; (4) uncertainties in buffer-gas pressure and temperature, 3 kc/sec; and (5) approximations in derivation of theoretical line shape, 3 kc/sec. These errors are negligible compared with the counting errors.

The value of $\Delta\nu$ from the previous high-field measurement is²

$$\Delta\nu = 4463.15 \pm 0.06 \text{ Mc/sec.}$$

A weighted average of the three measurements

(high-field Ar, low-field Ar, and low-field Kr) gives

$$\Delta\nu = 4463.255 \pm 0.020 \text{ Mc/sec}$$

(1 standard deviation).

The difference of about 2 standard deviations between the Ar and Kr measurements may be evidence of a nonlinearity in the argon pressure shift. To allow for this we take as a final number

$$\Delta\nu_{\text{expt}} = 4463.26 \pm 0.04 \text{ Mc/sec,}$$

where the error (1 standard deviation) assigned is the variance of the three values about their mean.

The theoretical expression for $\Delta\nu$ may be written³

$$\Delta\nu = \left(\frac{16}{3} \alpha^2 c R_{\infty} \frac{\mu_{\mu}}{\mu_0} \frac{m_e}{m_{\mu}} \right) \left(1 + \frac{m_e}{m_{\mu}} \right)^{-3} \times (1 + \frac{3}{2} \alpha^2 + a_e + \epsilon_1 + \epsilon_2 + \epsilon_3 - \delta_{\mu}) \quad (1)$$

in which

$$a_e = \frac{\alpha}{2\pi} - 0.328 \frac{\alpha^2}{\pi^2}, \quad \epsilon_1 = \alpha^2 (\ln 2 - \frac{5}{2}),$$

$$\epsilon_2 = \frac{8\alpha^3}{3\pi} \ln \alpha (\ln \alpha - \ln 4 + \frac{281}{480}), \quad \epsilon_3 = \frac{\alpha^3}{\pi} (18.4 \pm 5),$$

$$\delta_{\mu} = \frac{3\alpha}{\pi} \frac{m_e m_{\mu}}{m_{\mu}^2 - m_e^2} \ln(m_{\mu}/m_e).$$

A value for the fine-structure constant α can be obtained by equating $\Delta\nu_{\text{theor}}$ to $\Delta\nu_{\text{expt}}$. Accepted values^{3,9} are used for the constants appearing in the expression for $\Delta\nu_{\text{theor}}$. Only the value for the ratio of the magnetic moment of the muon to that of the proton, μ_{μ}/μ_p , requires special comment because the uncertainty with which it is known contributes significantly to the error in the determination of α . The value taken is

$$\mu_{\mu}/\mu_p = 3.183\,355 \pm 0.000\,048$$

(± 15 ppm, 1 standard deviation).

The basic experimental measurement¹⁰ was the ratio of the muon precession frequency in water to the proton precession frequency in water. The value quoted is the average of two values for μ_{μ}/μ_p . One is based on a model in which the muon and the proton in water experience the same magnetic field shielding (giving $3.183\,38 \pm 13$ ppm).

The other is based on a specific model⁴ in which the shielding is different (giving $3.183\,33 \pm 13$ ppm). The error given takes into account the error of the experiment and also the uncertainty in the shielding correction. The value obtained for α is $\alpha^{-1} = 137.0368 \pm 0.0012$ (± 9 ppm, 1 standard deviation), in which the uncertainty comes principally from the uncertainty in the muon magnetic moment.

Alternatively, if one accepts a value for α , the experimental value of $\Delta\nu$ can be used to determine the muon magnetic moment (or the muon mass).¹¹ With the use of the ac Josephson value¹² $\alpha^{-1} = 137.0359 \pm 0.0004$ one obtains

$$\mu_{\mu}/\mu_p = 3.183\,314 \pm 0.000\,034$$

(11 ppm, 1 standard deviation).

From the relation

$$\frac{m_{\mu}}{m_e} = \frac{\mu_p}{\mu_{\mu}} \frac{\mu_e g_{\mu}}{\mu_p g_e}$$

in which g_e and μ_e are the electron g value and magnetic moment, one can obtain a more precise value for the muon mass.¹³ The value we obtain after inserting accepted values^{3,9,14} for μ_e/μ_p and g_{μ}/g_e is

$$m_{\mu}/m_e = 206.770 \pm 0.002$$

(11 ppm, 1 standard deviation).

*Research supported in part by the U. S. Air Force Office of Scientific Research (at Yale) and the National Science Foundation (at Columbia).

¹P. A. Thompson, J. J. Amato, V. W. Hughes, R. M. Mobley, and J. E. Rothberg, *Bull. Am. Phys. Soc.* **12**, 75 (1967).

²W. E. Cleland, J. M. Bailey, M. Eckhause, V. W. Hughes, R. M. Mobley, R. Prepost, and J. E. Rothberg, *Phys. Rev. Letters* **13**, 202 (1964).

³V. W. Hughes, *Ann. Rev. Nucl. Sci.* **16**, 445 (1966).

⁴M. A. Ruderman, *Phys. Rev. Letters* **17**, 794 (1966).

⁵The muonium measurements were made at 19°C. The hydrogen measurements were typically at 30 to 40°C. The density has been corrected to 0°C. No attempt has been made to correct for a possible temperature dependence of the FPS.

⁶R. A. Brown, L. A. Balling, and F. M. Pipkin, *Bull. Am. Phys. Soc.* **11**, 328 (1966); R. A. Brown and F. M. Pipkin, *Phys. Rev.* **174**, 48 (1968).

⁷E. S. Ensberg and C. L. Morgan, *Phys. Letters* **28A**, 106 (1968).

⁸G. A. Clarke, *J. Chem. Phys.* **36**, 2211 (1962).

⁹E. R. Cohen and J. W. M. DuMond, *Rev. Mod. Phys.* **37**, 537 (1965).

¹⁰D. P. Hutchinson, J. Menes, G. Shapiro, and A. M. Patlach, *Phys. Rev.* **131**, 1351 (1963).

¹¹Since the Hamiltonian for muonium contains both $\Delta\nu$ and μ_μ , we can obtain both quantities from measurements of transition frequencies at two different magnetic fields (Ref. 3). If we take the value of $\Delta\nu$ from our present low-field measurement, then we can determine μ_μ from the previous measurement (Ref. 2) of a transition at high field without any ambiguity about magnetic

shielding. The result is 3.1852 ± 0.0014 (440 ppm, 1 standard deviation).

¹²W. H. Parker, B. N. Taylor, and D. N. Langenberg, *Phys. Rev. Letters* **18**, 287 (1967).

¹³G. Feinberg and L. M. Lederman, *Ann. Rev. Nucl. Sci.* **13**, 431 (1963).

¹⁴J. Bailey, W. Bartl, G. von Bochmann, R. C. A. Brown, F. J. M. Farley, H. Jostlein, E. Picasso, and R. W. Williams, "Precision Measurement of the Anomalous Magnetic Moment of the Muon" (to be published); A. Rich, *Phys. Rev. Letters* **20**, 967 (1968).

DEPENDENCE OF NUCLEAR POLARIZED Fe⁵⁷ MÖSSBAUER SPECTRA ON THE MAGNITUDE AND SIGN OF THE HYPERFINE FIELD

P. Reivari

Department of Technical Physics, Technical University of Helsinki, Otaniemi, Finland
(Received 6 December 1968)

The Mössbauer spectra of Fe⁵⁷, with the Co⁵⁷ source in iron and palladium matrices, respectively, have been measured in a He³/He⁴ dilution refrigerator. Both the magnitude and sign of the effective field at Co⁵⁷ can be determined from nuclear polarization effects in the spectra, without recourse to an external magnetic field. Experimental data are also presented on the Kapitza thermal boundary resistance which, together with radioactive self-heating, prevents the source from cooling below 0.15°K.

The possibility of observing nuclear polarization by using the Mössbauer effect was first suggested by Dash *et al.*,¹ who also made the first quantitative measurements on Co⁵⁷ nuclei in an iron matrix.²⁻⁴ Later experiments^{5,6} in our laboratory, employing a He³/He⁴ dilution refrigerator, extended this work to considerably lower temperatures. The present paper discusses similar measurements made on Co⁵⁷ in a Pd matrix and shows that the intensity ratios of the Mössbauer lines can give not only the magnitude but also the sign of the hyperfine field on the parent Co⁵⁷ nucleus.

When we study the nuclear polarization of Co⁵⁷ by the Mössbauer effect we have to take into account several nuclear levels.² The Co⁵⁷ ground state with spin $I_3 = \frac{7}{2}$ (the subscript refers to the nuclear level in question) decays by electron capture to the Fe⁵⁷ 136-keV level with spin $I_2 = \frac{5}{2}$ and mean lifetime 9×10^{-9} sec. This state decays principally by the emission of a 123-keV gamma ray to the first excited state of Fe⁵⁷, with $I_1 = \frac{3}{2}$ and lifetime 1.1×10^{-7} sec. The well known 14.4-keV Mössbauer gamma transition occurs between this state and the Fe⁵⁷ ground state, $I_0 = \frac{1}{2}$.

If the degeneracy of the long-lived Co⁵⁷ parent ground state is lifted by a negative magnetic hy-

perfine field, as in an iron matrix,⁴ then the sublevel with magnetic quantum number $m_3 = -\frac{7}{2}$ will become preferentially populated at low enough temperatures. When the Co⁵⁷ decays, the selection rules operate in such a way that some polarization will be preserved right through the decay chain to the 14.4-keV state of iron to give for instance more $m_1 \rightarrow m_0 = -\frac{3}{2} \rightarrow -\frac{1}{2}$ than $\frac{3}{2} \rightarrow \frac{1}{2}$ gamma transitions, i.e., the line of most negative velocity in the Mössbauer spectrum will be more intense than the corresponding positive velocity line. If H_{eff} at the parent nucleus is positive the situation is reversed.

We can assume that the nuclear spin populations of the two intermediate states 1 and 2 remain constant during the decay process because their lifetimes are short compared with estimates of the nuclear relaxation time.² We thus need only the nuclear magnetic moment of Co⁵⁷ in its ground state, the appropriate Clebsch-Gordan coefficients, and the temperature for calculating the hyperfine field at the Co⁵⁷ nucleus from the intensity ratios of the Mössbauer spectrum. Whether the most enhanced line is at the positive or negative end of the velocity spectrum gives the sign of the field. This conclusion relies on our assumption that there is no significant change