

ability must roughly double for such a transition to occur. Further calculations of more polarizable molecules should prove valuable in this regard.

<sup>1</sup>R. G. Brewer and C. H. Lee, preceding Letter [Phys. Rev. Letters **20**, 267 (1968)].

<sup>2</sup>All calculations reported in this paper were performed with Program No. 104 available from the Quantum Program Exchange, Indiana University, Bloomington, Ind. This program is described and documented by A. D. McLean and M. Yoshimine, IBM J. Res. Develop. **12**, 206 (1968).

<sup>3</sup>G. Herzberg, Molecular Spectra and Molecular Structure (D. Van Nostrand Company, Inc., New York, 1957), 2nd ed., p. 522.

<sup>4</sup>A. D. Buckingham and B. J. Orr, Quarterly Rev. (London) **21**, 195 (1967).

<sup>5</sup>C. A. Coulson, A. Maccoll, and L. E. Sutton, Trans. Faraday Soc. **48**, 106 (1952), have taken a different approach by treating benzene as a two-level system, but there appears to be a serious error in this paper. Examination of their expression for the induced dipole moment [Eq. (4)] shows that the effective polarizability  $\mu/F$  decreases with increasing field. This is just opposite to the thesis of that paper. Only after thermal averaging of the moment over the molecular orientation angle does  $\mu/F$  increase with increasing field. The purely electronic distortion should be independent of temperature, however. The reason this averaging masks the previous error is that the principal polari-

zation direction closest to that of the electric field is favored, i.e., the molecular-orientational Kerr effect was inadvertently derived rather than an electronic distortion.

<sup>6</sup>A. D. McLean and M. Yoshimine, J. Chem. Phys. **47**, 1927 (1967).

<sup>7</sup>McLean and Yoshimine, Ref. 2, "Tables of Linear Molecule Wave Functions" (supplement); available on request to the authors.

<sup>8</sup>A. D. McLean and M. Yoshimine, J. Chem. Phys. **46**, 3682 (1967).

<sup>9</sup>C. A. Burrus, J. Chem. Phys. **28**, 427 (1958); I. Ozier, Pon-nyong Yi, A. Khosla, and N. F. Ramsey, J. Chem Phys. **46**, 1530 (1967).

<sup>10</sup>J. O. Hirschfelder, C. F. Curtis, and R. B. Bird, Molecular Theory of Gases and Liquids (John Wiley & Sons, Inc., New York, 1954), p. 950.

<sup>11</sup>J. R. Oppenheimer, Phys. Rev. **13**, 66 (1928).

<sup>12</sup>L. V. Keldysh, Zh. Eksperim. i. Teor. Fiz.—Pis'ma Redakt. **47**, 1945 (1964) [translation: Soviet Phys.—JETP **20**, 1307 (1965)].

<sup>13</sup>M. H. Rice and R. H. Good, Jr., J. Opt. Soc. Am. **52**, 239 (1962).

<sup>14</sup>F. H. Field and J. L. Franklin, Electron Impact Phenomena and the Properties of Gaseous Ions (Academic Press, Inc., New York, 1957), p. 110.

<sup>15</sup>R. W. Terhune, P. D. Maker, and C. M. Savage, Phys. Rev. Letters **14**, 681 (1965); P. D. Maker, in Physics of Quantum Electronics, edited by P. L. Kelley, B. Lax, and P. E. Tannenwald (McGraw-Hill Book Company, Inc., New York, 1966), p. 60.

<sup>16</sup>C. Kittel, Introduction to Solid State Physics (John Wiley & Sons, Inc., New York, 1967), 3rd ed., p. 401.

## VORTEX-RING FORMATION BY NEGATIVE IONS IN He II UNDER PRESSURE\*

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It was previously shown that at temperatures  $\geq 0.36^\circ\text{K}$  and pressures  $> 12$  atm negative ions in He II could be accelerated until they emitted rotons at velocities of about 50 m/sec. We find that at temperatures  $\leq 0.3^\circ\text{K}$  negative ions produce only vortex rings at pressures up to 16 atm.

At temperatures  $\geq 0.36^\circ\text{K}$  negative ions in superfluid helium produce quantized vortex rings at low pressures, but surprisingly at pressures above 12 atm they can be accelerated to the Landau critical velocity of  $\sim 50$  m/sec at which they produce rotons.<sup>1,2</sup> We have found that at temperatures  $\leq 0.3^\circ\text{K}$  negative ions, like positive ions, produce only vortex rings, even at 16 atm and in the presence of an excess of He<sup>3</sup> impurities.

Our experimental cell, which was initially intended for other experiments, contained a Po<sup>210</sup> source of  $\sim 5$   $\mu\text{Ci}$ , several regions separated by grids, and a collector. In the present experi-

ments the charge carriers were accelerated in a 6-mm long space adjacent to the radioactive source. Their velocity was then measured by gating in a second 6-mm long space in an adaptation of the method analyzed in detail by Tanner.<sup>3</sup> The cell was refrigerated by a He<sup>3</sup>/He<sup>4</sup> dilution refrigerator.<sup>4</sup>

At a pressure of 16 atm (the limit of our apparatus) and  $T \approx 0.5^\circ\text{K}$ , our results are completely consistent with those of Rayfield: Vortex rings comprise only a minor fraction of the total current drawn from the source. However, as the temperature is reduced, rings comprise an

increasing fraction of the total current, until at all  $T \leq 0.3^\circ\text{K}$  the current consists of vortex rings only. At  $T \sim 0.05^\circ\text{K}$  the current consists entirely of rings even after the addition of  $3 \times 10^{-5}$  mole fraction  $\text{He}^3$ , although this causes significant energy losses for the rings.

It has been suggested that the creation of a vortex ring and its capture of the ion is a discontinuous process.<sup>5,6</sup> In such a case, conservation of energy and momentum require that the ion of mass  $m^*$  reach a critical velocity  $v_c = P_0/2m^* + E_0/P_0$ , in which  $P_0$  is the impulse of the ring<sup>7</sup> and  $E_0$  its energy. As pointed out by Pines,<sup>6</sup> this requires a  $v_c$  greater than the Landau critical velocity for creation of rotons. He attributes the difficulty to the use of improper expressions for  $E_0$  and  $P_0$ . However, Rayfield<sup>8</sup> interprets his experimental evidence as showing that, at least in the presence of  $\text{He}^3$  scattering, the formation of the ring from the positive ion is a continuous process. We feel that our results also support the model of ring formation extended over some time, since they show that the critical velocity which a negative ion must achieve before demonstrating a ringlike dispersion relation is temperature dependent as well as pressure dependent. These results suggest that negative ions under pressure at  $T \geq 0.36^\circ\text{K}$  undergo sufficient scattering by phonons and rotons so that during acceleration of the ion the formation of a quantized ring is perturbed, and many of the ions can reach the

Landau critical velocity. At  $T < 0.3^\circ\text{K}$ , however, rings can always be formed at a negative-ion velocity less than the roton critical velocity, as is always the case for positive ions. A  $\text{He}^3$  concentration of  $3 \times 10^{-5}$  mole fraction does not provide enough scattering to prevent the formation of rings.

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<sup>1</sup>Lothar Meyer and F. Reif, *Phys. Rev.* **123**, 727 (1961).

<sup>2</sup>G. W. Rayfield, *Phys. Rev. Letters* **16**, 934 (1966).

<sup>3</sup>D. J. Tanner, *Phys. Rev.* **152**, 121 (1966). See especially p. 123.

<sup>4</sup>A comprehensive treatment is given by Ray Radebaugh, Natural Bureau of Standards Technical Note No. NBS-362 (unpublished).

<sup>5</sup>G. W. Rayfield and F. Reif, *Phys. Rev.* **136**, A1194 (1964).

<sup>6</sup>D. Pines, in *Quantum Fluids*, edited by D. F. Brewer (North-Holland Publishing Company, Amsterdam, The Netherlands, 1966), p. 328.

<sup>7</sup>It seems permissible to use  $I = \pi\rho\kappa R^2$  for the impulse of a ring of radius  $R$ , circulation  $\kappa$ , in a fluid of density  $\rho$  since formation of a ring by an ion is similar to the dissolving membrane model discussed by Elisha R. Huggins, *Phys. Rev. Letters* **17**, 1284 (1966).

<sup>8</sup>G. W. Rayfield, *Phys. Rev. Letters* **19**, 1371 (1967).