to provide interesting relations between magnetic moments and axial quantities. It can also be shown that it leads to an accurate prediction for the  $\pi^0$  lifetime (L. Maiani and G. Preparata, to be published).

<sup>10</sup>N. Cabibbo and H. Ruegg, Phys. Letters <u>22</u>, 85 (1966); R. Gatto, L. Maiani, and G. Preparata, to be published.

<sup>11</sup>R. F. Peierls, Phys. Rev. <u>118</u>, 325 (1960); H. De-Staebler, E. F. Erickson, A. C. Hearn, and C. Schaerf, Phys. Rev. <u>140</u>, B336 (1965). <sup>12</sup>R. H. Dalitz and D. G. Sutherland, Phys. Rev. <u>146</u>,

1180 (1966).

<sup>13</sup>T. Janssens, R. Hofstadter, E. B. Hughes, and M. R. Yearian, Phys. Rev. <u>142</u>, 922 (1966).

## DECAY PROPERTIES OF THE $A_2(1310)$ MESON\*

Suh Urk Chung,<sup>†</sup> Orin I. Dahl, Lyndon M. Hardy,<sup>‡</sup> Richard I. Hess,<sup>§</sup> Janos Kirz, and Donald H. Miller

Lawrence Radiation Laboratory and Department of Physics, University of California, Berkeley, California (Received 9 December 1966)

The properties of the  $A_2$  enhancement are determined from the  $K\overline{K}$  and  $\pi\rho$  decay modes independently. The characteristics of both systems are consistent with the decay of a particle having  $I^G J^P = 1^- 2^+$ .

Existence of a strong  $\pi \rho$  enhancement between 1.0 and 1.4 BeV was discovered by Goldhaber et al. in a study of the reaction  $\pi^+ + p \rightarrow \pi^+ + \pi^+$  $+\pi^-+p$  at 3.65 BeV/c.<sup>1</sup> The Aachen-Berlin-Birmingham-Bonn-Hamburg-London(I.C.)-München Collaboration<sup>2</sup> and Chung et al.<sup>3</sup> demonstrated that the enhancement consisted of two peaks: the  $A_1$  at 1080 MeV and the  $A_2$  at 1310 MeV. In addition, Chung et al. reported evidence for existence of a  $K\overline{K}$  peak at 1310 MeV; the assignment  $I^G J^P = 1^- 2^+$  was deduced on the assumption that the  $\pi\rho$  and  $K\overline{K}$  peaks represented alternative decay modes of the  $A_2(1310)$ . In several recent studies of the  $\pi\rho$  system alone, the assignment  $J^P = 2^+$  has been favored for the  $A_2(1310)$ .<sup>4-6</sup> In others, however, assignments  $J^P = 1^+$  or  $2^-$  have appeared more like- $1y^{7-9}$ ; in this case, the  $K\overline{K}$  peak represents the decay of a new particle. In the present Letter we attempt to resolve this question by determining quantum numbers independently for the  $K\overline{K}$  and  $\pi\rho$  peaks; the analysis supports the original assumption of Chung et al.<sup>3</sup>

The film was obtained in the course of a systematic study of  $\pi^- p$  interactions near 3.2 and 4.2 BeV/c in the Lawrence Radiation Laboratory's 72-inch hydrogen bubble chamber. The experimental details are given by Hess<sup>10</sup> and Chung.<sup>11</sup> The observed numbers of events and corresponding cross sections are given in Table I.

The  $K\overline{K}$  system has been studied in both  $pK^-K_1^0$ and  $nK_1^0K_1^0$  final states where the decays  $K_1^0 \rightarrow \pi^+ + \pi^-$  were observed; all successfully fitted events in the fiducial volume were used. In contrast, the  $A_2(1310)$  represents less than 10% of the  $\pi^+\pi^-\pi^-p$  final state, so that useful comparisons are possible only after imposition of stringent selection criteria. For subsequent analysis,  $\pi^-\rho^0 p$  events are defined as those with at least one  $M(\pi^+\pi^-)$  combination in the interval 0.66 to 0.84 BeV. Background due to the sequence  $\pi^- + p \rightarrow \pi^- + \pi^- + N^{*++}(1238) \rightarrow \pi^ + \pi^- + \pi^+ + p$  has been minimized by rejecting events with 1.12 BeV  $\leq M(\pi^+p) \leq 1.32$  BeV and  $\Delta_b \pi^{+2} \leq 1.5$  (BeV/c)<sup>2</sup>. In addition, events were

	Number of events		Cross section (µb)	
Final state	3.2 BeV/c	4.2 BeV/ $c$	3.2 BeV/c	4.2 BeV/c
$p\pi^{+}\pi^{-}\pi^{-}$ $pK^{0}K^{-}$ $nK_{1}^{0}K_{1}^{0}$	$6318 \\ 228^{a} \\ 201^{b}$	$2986 \\ 95^{a} \\ 68^{b}$	$1910 \pm 80 \\ 65.1 \pm 5.3 \\ 45.3 \pm 4.1$	$1920 \pm 100 \\ 65.7 \pm 7.9 \\ 36.6 \pm 5.1$

Table I. Final states analyzed.

 ${}^{a}K_{1}{}^{0} \rightarrow \pi^{+} + \pi^{-}$  decay was observed for these events. The cross sections were corrected for this detection efficiency ( $\epsilon \approx \frac{1}{3}$ ).

<sup>b</sup>Decay of both  $K_1^0 \rightarrow \pi^+ + \pi^-$  was observed for these events. The cross sections were corrected for this detection efficiency ( $\epsilon \approx 4/9$ ).

rejected if they fell into the region where the Deck mechanism<sup>12</sup> is strongest,  $\Delta_{p\pi} - {}^2 \le 0.55$   $(\text{BeV}/c)^2$  and  $\hat{p}_p \cdot \hat{p}_0 = \cos \theta_p \le -0.8$ . Here  $\vec{p}_p$  is the momentum of the outgoing proton and  $\vec{p}_0$  is the beam direction in the  $p\pi^-$  rest frame.<sup>13</sup>

The effective-mass distributions,  $M(K\overline{K})$ , for the  $K\overline{K}$  systems are shown in Fig. 1(a); the  $M(\pi^-\rho^0)$  distribution is shown in Fig. 1(d) for events with  $\Delta_p^2 \leq 0.65$  (BeV/c)<sup>2</sup>. In both cases a good fit is provided by a Breit-Wigner resonance, with  $M_0 = 1310 \pm 20$  MeV and  $\Gamma = 65 \pm 20$ MeV, above a smooth background. The  $\Delta_N^2$ distributions for events in the  $A_2$  interval, 1.24 to 1.38 BeV, are shown separately for  $K\overline{K}$  events [Figs. 1(b) and 1(c)] and  $\pi^-\rho^0$  events [Figs. 1(e) and 1(f)]. After comparison with control regions we conclude that, within statistics, contributions from the 1310-MeV peak are similar in all cases.

Possible quantum numbers for the  $K\overline{K}$  peak at 1310 MeV are readily deduced. Since the decay  $K_1^{0}K_1^{0}$  is observed, *C* is +1 and  $J^P$  is (even)<sup>+</sup>. Histograms of decay cosine ( $\cos\theta_K$ in the  $K\overline{K}$  rest frame) and Treiman-Yang angle are plotted in Fig. 2. The decay cosine distributions for both the  $K^-K_1^{0}$  and  $K_1^{0}K_1^{0}$  events contain strong  $\cos^2\theta$  components, so that *J* is not equal to zero. Since *I* is 1 for  $K^-K_1^{0}$ , we conclude that  $G = (-1)^{J+I} = -1$ . Consequently,  $I^G$  is 1<sup>-</sup> and  $J^P$  is 2<sup>+</sup>, 4<sup>+</sup>, etc. for the  $K\overline{K}$  peak



FIG. 1. (a) Effective-mass histogram for the  $K\overline{K}$  systems at 3.2 and 4.2 BeV/c. (b), (c) Histograms of  $\Delta_N^2$  at 3.2 and 4.2 BeV/c for  $K\overline{K}$  events in the  $A_2$  region. (d) Effective-mass histogram for the  $\pi^-\rho^0$  system at 3.2 and 4.2 BeV/c. Selections are discussed in the text. (e), (f) Histograms of  $\Delta_p^2$  at 3.2 and 4.2 BeV/c for the  $\pi\rho$  events in the  $A_2$  region.



FIG. 2. Histograms of decay cosine  $(=\hat{p}_{K}, \hat{p}_{0})$  in the  $A_{2}$  rest frame) and the Treiman-Yang angle for  $K\overline{K}$  events in the  $A_{2}$  region. The  $A_{2}^{-}$  histogram is shown in (a) and (b) and the  $A_{2}^{0}$  in (c) and (d). In (c) and (d) two points have been plotted per event.

## at 1310 MeV.

In deducing possible quantum numbers for the  $\pi\rho$  system, we note first that the decay  $A_2(1310) - \pi + \rho$  is allowed, consequently G is -1; in addition, Abolins <u>et al.</u> have shown that  $I=1.^{14}$  To determine the spin and parity, we consider the decay correlations in the  $A_2$  rest frame; we define  $\bar{q}$  as the relative momentum of the  $\pi^+\pi^-$  pair forming the  $\rho^0$ ,  $\bar{p}$  as the momentum of the third pion, and  $\cos\beta = \hat{q} \cdot \hat{p}$ . For collinear decays, corresponding to points on the boundary of the Dalitz plot, we have  $\cos\beta$  $=\pm 1$ . For these decays  $\psi(3\pi)$  is proportional to  $Y_J^M(\hat{q})$ , so that P is  $-(-1)^J$ ; consequently, for  $3\pi$  systems with  $P = (-1)^J$ , collinear decays are not allowed.<sup>15</sup> Since the parity of the  $3\pi$ system can be deduced only from the density on the Dalitz plot near the boundaries, a precise estimate of background is crucial; for systems with  $P = (-1)^J$ , a small residual background of collinear events can lead (erroneously) to the opposite parity assignment.

The  $\cos\beta$  distributions are shown in Figs. 3(b), 3(c), and 3(d) for events in the  $A_2$  region and control regions; the strong contribution from the decay  $A_2 \rightarrow \pi + \rho$  produces the peak at  $\cos\beta \approx 0.2$  in Fig. 3(b). Events in the interval 1.24 to 1.38 BeV may be identified as (1)  $A_2$   $\rightarrow \pi + \rho$ , (2)  $\pi\rho$  background, or (3)  $3\pi$  background. We designate the fraction of events of each type by  $\epsilon_i$ . The smooth curve in Fig. 1(d) suggests that  $\epsilon_2 + \epsilon_3 = 0.6 \pm 0.1$ ; the  $M(\pi^+\pi^-)$  distribution for the events in the  $A_2$  interval gives  $\epsilon_3 = 0.4 \pm 0.1$ .

For comparison with the experimental data, theoretical  $\cos\beta$  distributions<sup>16</sup> for possible  $J^P$  assignments were modified by addition of noninterfering background. To examine the dependence of each  $J^P$  assignment on background,  $\epsilon_2 + \epsilon_3$  was varied from 0 to 1. The  $\pi\rho$  background was calculated using the matrix element for an *s*-wave  $\pi\rho$  interaction (i.e.,  $J^P = 1^+$  appropriately symmetrized)<sup>17</sup>; a uniform distribu-



FIG. 3. (a) Variations of  $\chi^2$  (19 degrees of freedom) for various  $J^P$  assignments for the  $A_2$  as a function of the background level. (b) The  $\cos\beta$  distribution in the  $A_2$  region. See text for explanation of the curves. (c) The  $\cos\beta$  distribution for the region below the  $A_2$  (1.0 to 1.14 BeV). (d) The same distribution for the region above the  $A_2$  (1.48 to 1.62 BeV).

tion in  $\cos\beta$  was assumed for the  $3\pi$  background. The behavior of  $\chi^2$  (for 19 degrees of freedom) is shown in Fig. 3(a) as a function of the assumed background level; the slopes are discontinuous, since we have arbitrarily set  $\epsilon_2 = 0$  for  $\epsilon_1 \ge 0.6$ . We note that when background is ignored, the most likely assignments are  $J^P = 1^+(l=0)$  and  $J^P = 2^{-}(l=1)$ . However, for a realistic back-ground level of 40 to 70%,  $J^P = 2^+$  represents the only assignment (of those considered) compatible with the data<sup>18</sup>: The fitted distribution is shown in Fig. 3(b) for  $\epsilon_1 = 0.4$ . Consequently, for a model with noninterfering background, parsimony requires that we identify the  $\pi\rho$  and  $K\overline{K}$  peaks as alternative decay modes of an  $I^{G}J^{P} = 1^{-2^{+}}$  state at 1310 MeV; production cross sections are given in Table II. The combined data give  $\Gamma(A_2 \rightarrow K + \overline{K}) / \Gamma(A_2 \rightarrow \pi + \rho) = 0.05$  $\pm 0.02$ ; a factor of  $\frac{1}{2}$  has been included for the unobserved  $\pi^{0}\rho^{-}$  decays. The decay  $A_{2} \rightarrow \pi + \eta$ is allowed; some evidence for a peak near 1310 MeV has been reported. We have examined the  $M(\pi^-\eta)$  distribution from the  $\pi^-(\pi^+\pi^-\pi^0)p$ final state and (after correcting for unobserved decays) estimate  $\Gamma(A_2 \rightarrow \pi + \eta) / \Gamma(A_2 \rightarrow \pi + \rho)$  $=0.12 \pm 0.08$ .

Since  $A_2$  events are concentrated at low  ${\Delta_N}^2$ and the decay  $A_2 - \pi + \rho$  is dominant, it is likely that production occurs through  $\rho$  exchange. Unmodified, this model predicts a distribution  $\cos^2\theta_K \sin^2\theta_K (1 + a \cos 2\varphi)$  for the  $K\overline{K}$  decay mode, where  $\varphi$  is the Treiman-Yang angle; the  $\cos\theta_K$ distributions in Fig. 2 are in strong disagreement with this prediction. Similarly, the model does not account for the observed correlation between the beam direction and the normal to the  $\pi\rho$  decay plane.<sup>11</sup> Analogous discrepancies in other reactions involving  $\rho$  exchange have been explained by absorption effects.<sup>19</sup>

We wish to thank the scanning and measuring staff for their untiring efforts in bringing this experiment to a successful completion. It is a pleasure to acknowledge the encouragement and support of Professor Luis Alvarez throughout the course of this experiment. \*Work done under the auspices of the U. S. Atomic Energy Commission.

<sup>†</sup>Present address: Brookhaven National Laboratory, Upton, New York.

<sup>‡</sup>Present address: TRW Systems, Incorporated,

1 Space Park, Redondo Beach, California.

§Present address: Logicon, Incorporated, 205 Avenue I, Redondo Beach, California.

<sup>1</sup>G. Goldhaber, J. L. Brown, S. Goldhaber, J. A.

Kadyk, B. C. Shen, and G. H. Trilling, Phys. Rev. Letters <u>12</u>, 336 (1964).

<sup>2</sup>Aachen-Berlin-Birmingham-Bonn-Hamburg-London (I.C.)-München Collaboration, Phys. Letters <u>10</u>, 226 (1964).

<sup>3</sup>S. U. Chung, O. I. Dahl, L. M. Hardy, R. I. Hess, G. R. Kalbfleisch, J. Kirz, D. H. Miller, and G. A. Smith, Phys. Rev. Letters 12, 621 (1964).

<sup>4</sup>J. Alitti, J. P. Baton, B. Deler, M. Neveu-René, J. Crussard, J. Ginestet, A. H. Tran, R. Gessaroli, and A. Romano, Phys. Letters <u>15</u>, 69 (1965).

<sup>5</sup>R. L. Lander, Maris Abolins, D. D. Carmony, T. Hendricks, Nguyen-huu Xuong, and P. M. Yager, Phys. Rev. Letters <u>13</u>, 346 (1964), and Ref. 2 report that the  $J^P = 2^+$  assignment is consistent with their data, although other  $J^P$  assignments cannot be ruled out.

<sup>6</sup>G. Benson, L. Lovell, E. Marquit, B. Roe, D. Sinclair, and J. Vander Velde, Phys. Rev. Letters <u>16</u>, 1177 (1966).

<sup>7</sup>V. E. Barnes, W. B. Fowler, K. W. Lai, S. Orenstein, D. Radojicic, M. S. Webster, A. H. Bachman, P. Baumel, and R. M. Lea, Phys. Rev. Letters <u>16</u>, 41 (1966).

<sup>8</sup>N. M. Cason, Phys. Rev. <u>148</u>, 1282 (1966).

<sup>9</sup>Aachen-Berlin-CERN Collaboration, reported by D. R. O. Morrison, in Proceedings of the Thirteenth International Conference on High Energy Physics, Berkeley, California, 1966 (unpublished). See G. Goldhaber, in Proceedings of the Thirteenth International Conference on High Energy Physics, Berkeley, California, 1966 (unpublished).

<sup>10</sup>R. I. Hess, thesis, University of California Radiation Laboratory Report No. UCRL-16832, 1966 (unpublished).

<sup>11</sup>S. U. Chung, thesis, University of California Radiation Laboratory Report No. UCRL-16981, 1966 (unpublished).

<sup>12</sup>R. T. Deck, Phys. Rev. Letters <u>13</u>, 169 (1964). <sup>13</sup>This cut reduces the number of events in the mass region below the  $A_2$ , but eliminates few events in the  $A_2$  region itself. The analysis was also carried out without this cut, and the conclusions remained un-

Table II. Cross section for  $A_2$  production.

	Cross section (µb)	
Reaction	3.2 BeV/c	4.2 BeV/c
$\pi^+ + p \rightarrow A_2^- + p; A_2^- \rightarrow K^0 + K^-$	$18 \pm 4$	$17 \pm 5$
$\pi^{-} + p \rightarrow A_2^{0} + n;  A_2^{0} \rightarrow K + \overline{K}$	$36 \pm 10$	$18 \pm 9$
$\pi^- + p \rightarrow A_2^- + p; \ A_2^- \rightarrow \rho^0 + \pi^-$	$150 \pm 50$	$175 \pm 45$

changed. See Ref. 11 for a detailed account.

<sup>14</sup>M. A. Abolins, D. D. Carmony, R. L. Lander, O. Piccioni, Ng. H. Xuong, and P. M. Yager, Phys. Letters 21, 584 (1966).

<sup>15</sup>R. H. Dalitz, <u>Strange Particles and Strong Interac-</u> <u>tions</u> (Oxford University Press, New York, 1962), p. 40.

<sup>16</sup>We have used a computer program written by R. Diebold, CERN/TC/PROG 64-25, modified for our purpose. As an alternative method for taking background into account, varying amounts of the  $\cos\beta$  distribution in the control region were subtracted from the distribution in the  $A_2$  interval. A comparison of the resulting distribution with theoretical curves for various  $J^P$  assignments yielded similar results; see Ref. 11 for details.

<sup>17</sup>We thank Dr. Vanya Cocconi (private communication) for informing us that calculated distributions for events produced through the Deck mechanism resemble closely those for a  $J^P = 1^+$  system.

<sup>18</sup>Benson <u>et al.</u> (Ref. 6) in their study of the  $\pi^+d$  interactions, reached similar conclusions for the neutral  $A_2$ , assuming that the background consisted entirely of the  $3\pi$  phase space.

<sup>19</sup>J. D. Jackson, J. T. Donohue, K. Gottfried, R. Keyser, and B. E. Y. Svensson, Phys. Rev. <u>139</u>, B428 (1965).