

DYNAMICS OF OXIDATION-REDUCTION PROCESSES IN RARE-EARTH-DOPED  $\text{CaF}_2$ 

Z. J. Kiss and D. L. Staebler

RCA Laboratories, Princeton, New Jersey  
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The effects of high-energy radiation on single crystals of alkaline halides have been studied in great detail, and a number of color centers have been identified in these systems.<sup>1</sup> The corresponding situation in the alkaline earth fluorides is much more complex.<sup>2</sup> The latest evidence indicates that all coloration in  $\text{CaF}_2$  is associated with impurities, and very pure crystals are not noticeably affected by  $\gamma$  irradiation.<sup>3</sup> We have studied the oxidation-reduction processes associated with rare-earth-doped  $\text{CaF}_2$  crystals subjected to  $\gamma$  irradiation. Under the influence of high-energy radiation, some of the trivalent rare earths ( $\text{RE}^{3+}$ ) convert to the divalent state ( $\text{RE}^{2+}$ ),<sup>4,5</sup> leaving an unidentified hole behind. The divalent rare earth produced is not stable; it reoxidizes to the trivalent state accompanied by luminescence characteristic of the trivalent rare earth.

In this note we wish to report on the mechanism of this reversion, triggered either by heat or by infrared radiation. The reoxidation is accompanied by both luminescence and photoconductivity,<sup>6</sup> and the excitation spectra of the two phenomena are identical. The luminescence spectrum is characteristic of the trivalent rare-earth ion in a cubic environment. The IR-triggered reversion rate is faster than  $10^{-6}$  sec.

To study the thermoluminescence, single crystals of  $\text{CaF}_2$  containing trivalent rare earth of 0.02-1.0 molar percent were irradiated at 78°K using  $\gamma$  irradiation from a spent reactor fuel rod and dosages of the order of  $10^6$  rad. The  $\text{RE}^{2+}$  concentration was monitored by recording the  $4f-5d$  absorption bands<sup>5</sup> of the ions. The crystals were warmed to room temperature, while the luminescence spectra were photographed with a Bausch and Lomb 2-m grating spectrograph having an effective resolution of  $1 \text{ cm}^{-1}$ . All the rare-earth-doped samples were found to emit some radiation, but only the Dy and Tm systems were investigated in detail.

Figure 1(a) shows a densitometer trace of a photograph of the thermoluminescence spectrum accompanying the  $\text{Dy}^{2+}-\text{Dy}^{3+}$  conversion. The lines correspond to the  ${}^6F_{11/2} \rightarrow {}^6H_{15/2}$  transition of  $\text{Dy}^{3+}$ .<sup>7</sup> Figure 1(b) shows a fluores-

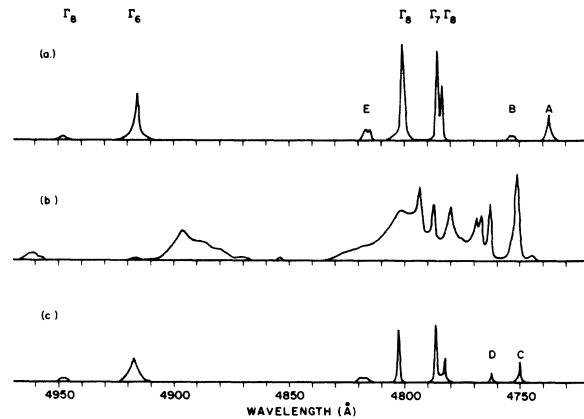


FIG. 1. (a) Thermoluminescence spectrum of 0.1 mole %  $\text{CaF}_2:\text{Dy}$ ,  $\gamma$ -irradiated at 78°K and warmed to 300°K. The transition is between  ${}^6F_{11/2} \rightarrow {}^6H_{15/2}$  states of  $\text{Dy}^{3+}$ . (b) Fluorescence spectrum of 0.1 mole %  $\text{CaF}_2:\text{Dy}^{3+}$  before  $\gamma$  irradiation at 78°K. (c) Luminescence spectrum of  $\text{CaF}_2:\text{Dy}$  at 78°K when the crystal is excited with light of longer wavelength ( $\lambda_{\text{exc}} > 5000 \text{ \AA}$ ) than the emission lines ( $\lambda_{\text{E}} = 4900 \text{ \AA}$ ). The crystal was irradiated with  $\gamma$  rays at 78°K and was kept at this temperature. (The line, A, is emission from the excited thermalized state of  ${}^6F_{11/2}$ . B and E are possible vibronic compounds. C and D are some "noncubic" lines excited.)

cence spectrum of the crystal before irradiation. While the two spectra cover the same frequency range and originate from the same groups of transitions, we suggest that the simpler thermoluminescence spectrum of Fig. 1(a) is characteristic of  $\text{Dy}^{3+}$  in a cubic site. The evidence for this suggestion is as follows: (1) While the fluorescence spectrum of  $\text{Dy}^{3+}$  is strongly concentration dependent, the thermoluminescence spectrum is concentration independent. (2) The positions of the five crystal-field components of the  ${}^6H_{15/2}$  level (indicated by symbols  $\Gamma_i$ ) as deduced from Fig. 1(a) can be well fitted by a cubic field description.<sup>8</sup> (3) The first excited crystal-field level of the ground state  $\Gamma_7$  is  $8.3 \text{ cm}^{-1}$  above the ground  $\Gamma_8$  level [Fig. 1(a)], and this level has been observed in paramagnetic resonance,<sup>9</sup> and identified as originating from  $\text{Dy}^{3+}$  in cubic sites. We conclude that the luminescing Dy ion is undergoing the  $\text{Dy}^{2+}-\text{Dy}^{3+}$  reversion process. This is corroborated by previous observations

that  $\gamma$  irradiation only reduces  $\text{RE}^{3+}$  ions in a cubic site,<sup>10</sup> and that  $\text{RE}^{2+}$  ions remain in a cubic site.<sup>5</sup>

We have found that the  $\text{RE}^{2+}$  can be reconverted to  $\text{RE}^{3+}$  with visible and infrared radiation, and that this photo-oxidation process is accompanied by the same cubic-site  $\text{RE}^{3+}$  emission as found in the thermoluminescence [Fig. 1(c)]. The system behaves as an IR-stimulable phosphor, where, for example [Fig. 1(c)], the 4900Å emission can be triggered by IR photons (up to  $\lambda \leq 9000$  Å). The excitation spectrum of a trivalent thulium luminescence is shown in Fig. 2(b). The spectrum was taken by monitoring the intensity of the 4500Å emission line of  $\text{Tm}^{3+}$ , corresponding to the transition  ${}^1G_4 \rightarrow {}^3H_6$ , while the crystal was excited through a second monochromator using a tungsten lamp. The absorption spectrum of the same crystal is shown on Fig. 2(a), showing the characteristic  $4f-5d$  bands of  $\text{CaF}_2:\text{Tm}^{2+}$ .<sup>5</sup> While the peaks of the  $\text{Tm}^{3+}$  excitation spectrum of Fig. 2(c) occur at the same wavelength as the  $5d$  bands of  $\text{Tm}^{2+}$ , it increases very rapidly with increasing frequency. The crystals are also photoconductive while irradiated with IR light,<sup>6</sup> and the frequency response of the photoconductivity is shown in Fig. 2(b). It can be noted that the excitation spectrum of the  $\text{Tm}^{3+}$  luminescence reflects closely the photoconductive response curves.

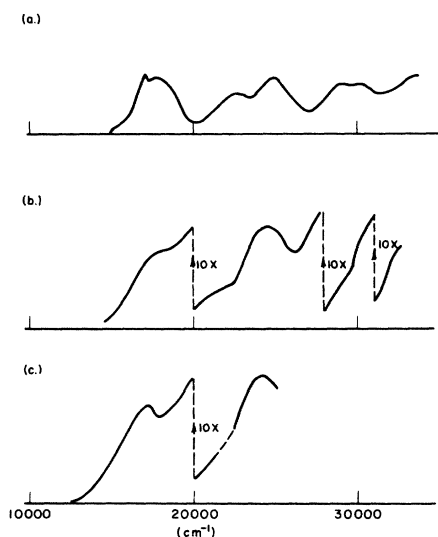


FIG. 2. (a) The absorption spectrum of  $\text{CaF}_2:\text{Tm}$  irradiated with  $\gamma$  rays at 78°K. (b) The photoconductivity response of  $\text{CaF}_2:\text{Tm}^{2+}$  as a function of excitation frequency. (c) The excitation spectrum of the 4500Å  $\text{Tm}^{3+}$  emission when the  $\gamma$ -irradiated crystal is excited with the light  $\lambda_{\text{exc}} > 4500$  Å.

In an attempt to measure the rate of photo-oxidation, we have recorded the time dependence of the 4900Å  $\text{Dy}^{3+}$  emission, after the crystal was excited with a light pulse of 3- $\mu$ sec duration and having wavelengths longer than 5000 Å. The  $\text{Dy}^{3+}$  emission showed no resolvable rise time, indicating that the reversion rate is faster than the time resolution of the instrument, which was  $10^{-6}$  sec. The luminescence then decays in two steps. First there is a fast, exponential decay measurable for about 50 msec, having a lifetime of  $\tau = 1.9$  msec at 78°K. This is the right order of magnitude for the lifetime of a magnetic-dipole transition which would be expected between states of  $\text{Dy}^{3+}$  in cubic site. Following this fast exponential decay, there is luminescence of much lower intensity which persists for minutes, and has a complex time dependence. The number of photons emitted during the short exponential decay is of the same order of magnitude as the total number of photons emitted during the much weaker but longer persistent luminescence.

We cannot yet fit all the observations on the oxidation-reduction processes into a consistent picture, but the above observations elucidate points not previously understood. From previous observations,<sup>10</sup> we know that  $\gamma$  radiation converts only  $\text{RE}^{3+}$  in a cubic site to  $\text{RE}^{2+}$ . This presumably occurs by taking an electron from an interstitial charge compensator  $\text{F}^-$ , which is distant from the  $\text{RE}^{3+}$  by more than a few lattice sites. We now suggest that the  $\text{F}^0$  left behind is not stable and may combine with a second  $\text{F}^0$  to form nonparamagnetic  $\text{F}_2$  molecular complexes as the stable hole. Each  $\text{RE}^{2+}$  is in a cubic site, and it will remain  $\text{RE}^{2+}$  until one of two mechanisms triggers the reversion: (1) The absorption of a photon lifts one of the  $\text{RE}^{2+}$  electrons into the conduction band. This conduction electron is trapped by an electron trap, presumably the hole created by  $\gamma$  irradiation, thus leaving a  $\text{RE}^{3+}$  excited ion in the cubic site which returns to the ground state by the observed characteristic cubic-site fluorescence. (2) The reversion is triggered by thermal energy freeing the trapped hole. As this trapped hole approaches a  $\text{RE}^{2+}$ , it will capture one of the electrons of  $\text{RE}^{2+}$ , leaving again an excited  $\text{RE}^{3+}$  ion. Whether the mechanism of this trapping is by tunneling or by some other process is not yet known.

The existence of the  $\text{F}_2$  molecule as the hole would qualitatively explain the time dependence

of the IR-triggered luminescence. First the IR photons will free the electron, leading to photoconductivity. This electron is trapped by the  $F_2$ , breaks up the molecular complex, leaving an interstitial  $F^-$  charge compensator and a nonstable  $F^0$ . The second long part of the luminescence could correspond to the capture by this  $F^0$  of one of the electrons of the  $RE^{2+}$ . This is in qualitative agreement with the observation that the number of photons emitted during the "slow" process is the same order of magnitude as during the "fast" process.

In summary, we have found that the luminescence associated with the reversion of  $RE^{2+} - RE^{3+}$  in  $CaF_2$  is characteristic of  $RE^{2+}$  ions in a cubic site. We would like to emphasize the importance and the ease of this technique for studies of the cubic  $RE^{3+}$  spectra in the fluoride hosts. This study is very difficult by the ordinary absorption and emission techniques, since it is always overlapped by a much more intense concentration-dependent noncubic spectrum. The  $RE^{2+}$  can be photo-oxidized, and the process leads to photoconductivity. The photo-oxidized reversion triggers luminescence with two different time dependences.

We wish to point out the possibility of laser action in the  $RE^{3+}$  emission associated with the  $RE^{2+} - RE^{3+}$  reversion process.

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<sup>7</sup>See, e.g., G. H. Dieke and S. Singh, J. Opt. Soc. Am. **46**, 495 (1956).

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## RELATIVISTIC ENERGY BANDS FOR TUNGSTEN\*

T. L. Loucks

Institute for Atomic Research and Department of Physics, Iowa State University, Ames, Iowa  
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In this Letter the results of an *ab initio* relativistic calculation of the electronic structure of tungsten are presented. The predicted splitting of the energy bands is in complete agreement with the experimental results obtained from size effect measurements.<sup>1</sup>

The method used in these calculations was developed by the author and has recently been submitted for publication.<sup>2</sup> It can be thought of as a relativistic generalization of the augmented plane wave (APW) method of Slater.<sup>3</sup>

The basic function consists of a Dirac plane wave in the outer region of the unit cell and an expansion of Dirac central-field orbitals inside the APW sphere. The expansion coefficients are chosen such that the upper (large) components of the wave function are continuous on the sphere. The lower (small) components are, in general, discontinuous on this surface. A variational expression, which is appropriate for this type of trial function, is developed. The resulting matrix elements have the following form:

$$M \begin{pmatrix} NM \\ nm \end{pmatrix} = (k_N^2 - E) \Omega_{nN} \delta_{mM} + 4\pi R^2 \sum_{\kappa} D_{\kappa} \begin{pmatrix} NM \\ nm \end{pmatrix} j_l(k_n R) \left\{ j_l(k_N R) \left( \frac{c_{\kappa}^f(R, E)}{g_{\kappa}(R, E)} \right) - j_l(k_N R) k_N S_{\kappa} \right\}, \quad (1)$$

where

$$\Omega_{nN} = \Omega_{nN} \delta_{nN} - 4\pi R^2 \frac{j_1(|\vec{k}_N - \vec{k}_n| R)}{|\vec{k}_N - \vec{k}_n|}, \quad (2)$$