Magicity versus Superfluidity around ²⁸O viewed from the Study of ³⁰F

J. Kahlbow⁽⁰⁾,^{1,2,*} T. Aumann,^{1,3,4} O. Sorlin,⁵ Y. Kondo,⁶ T. Nakamura,⁶ F. Nowacki,⁷ A. Revel,^{5,8} N. L. Achouri,⁸ H. Al Falou,⁹ L. Atar,¹ H. Baba,² K. Boretzky,³ C. Caesar,^{1,3} D. Calvet,¹⁰ H. Chae,¹¹ N. Chiga,² A. Corsi,¹⁰ F. Delaunay,⁸ A. Delbart,¹⁰ Q. Deshayes,⁸ Z. Dombrádi,¹² C. A. Douma,¹³ Z. Elekes,¹² I. Gašparić,^{14,2} J.-M. Gheller,¹⁰ J. Gibelin,⁸ A. Gillibert,¹⁰ M. N. Harakeh,^{3,13} A. Hirayama,⁶ M. Holl,^{1,3} A. Horvat,^{1,3} Á. Horváth,¹⁵ J. W. Hwang,¹⁶ T. Isobe,² N. Kalantar-Nayestanaki,¹³ S. Kawase,¹⁷ S. Kim,¹⁶ K. Kisamori,² T. Kobayashi,¹⁸ D. Körper,³ S. Koyama,¹⁹ I. Kuti,¹² V. Lapoux,¹⁰ S. Lindberg,²⁰ F. M. Marqués,⁸ S. Masuoka,²¹ J. Mayer,²² K. Miki,²³ T. Murakami,²⁴ M. Najafi,¹³ K. Nakano,¹⁷ N. Nakatsuka,²⁴ T. Nilsson,²⁰ A. Obertelli,¹⁰ N. A. Orr,⁸ H. Otsu,² T. Ozaki,⁶ V. Panin,² S. Paschalis,¹ D. M. Rossi,^{1,3} A. T. Saito,⁶ T. Saito,¹⁹ M. Sasano,² H. Sato,² Y. Satou,¹⁶ H. Scheit,¹ F. Schindler,¹ P. Schrock,²¹ M. Shikata,⁶ K. Shimada,⁶ Y. Shimizu,² H. Simon,³ D. Sohler,¹² L. Stuhl,^{25,2} S. Takeuchi,⁶ M. Tanaka,²⁶ M. Thoennessen,²⁷ H. Törnqvist,^{1,3} Y. Togano,⁶ T. Tomai,⁶ J. Tscheuschner,¹ J. Tsubota,⁶ T. Uesaka,² H. Wang,² Z. Yang,² M. Yasuda,⁶ and K. Yoneda²

Z. Yang,² M. Yasuda,⁶ and K. Yoneda²

(SAMURAI21-NeuLAND Collaboration)

¹Institut für Kernphysik, Technische Universität Darmstadt, 64289 Darmstadt, Germany

²RIKEN Nishina Center, Hirosawa 2-1, Wako, Saitama 351-0198, Japan

³GSI Helmholtzzentrum für Schwerionenforschung, 64291 Darmstadt, Germany

⁴Helmholtz Forschungsakademie Hessen für FAIR, 64291 Darmstadt, Germany

⁵Grand Accélérateur National d'Ions Lourds (GANIL), CEA/DRF-CNRS/IN2P3, Bvd Henri Becquerel, 14076 Caen, France

⁶Department of Physics, Tokyo Institute of Technology, 2-12-1 O-Okayama, Meguro, Tokyo 152-8551, Japan

⁷Université de Strasbourg, CNRS, IPHC UMR7178, 23, F-67000 Strasbourg, France

⁸Université de Caen Normandie, ENSICAEN, CNRS/IN2P3, LPC Caen UMR6534, F-14000 Caen, France

⁹Lebanese University, Beirut, Lebanon

¹⁰Irfu, CEA, Université Paris-Saclay, 91191 Gif-sur-Yvette, France

¹IBS, 55, Expo-ro, Yuseong-gu, Daejeon 34126, Korea

¹²HUN-REN Institute for Nuclear Research, HUN-REN ATOMKI, 4001 Debrecen, Hungary

¹³ESRIG, University of Groningen, Zernikelaan 25, 9747 AA Groningen, The Netherlands

¹⁴Ruđer Bošković Institute, HR-10002 Zagreb, Croatia

¹⁵Eötvös Loránd University, Pázmány Péter Sétány 1/A, H-1117 Budapest, Hungary

¹⁶Department of Physics and Astronomy, Seoul National University, 1 Gwanak-ro, Gwanak-gu, Seoul 08826, Republic of Korea

¹⁷Department of Advanced Energy Engineering Science, Kyushu University, Kasuga, Fukuoka 816-8580, Japan

¹⁸Department of Physics, Tohoku University, Miyagi 980-8578, Japan

¹⁹Unversity of Tokyo, Tokyo 1130033, Japan

²⁰Institutionen för Fysik, Chalmers Tekniska Högskola, 412 96 Göteborg, Sweden

²¹Center for Nuclear Study, University of Tokyo, 2-1 Hirosawa, Wako, Saitama 351-0198, Japan

²²Institut für Kernphysik, Universität zu Köln, 50937 Köln, Germany

²³National Superconducting Cyclotron Laboratory, Michigan State University, East Lansing, Michigan 48824, USA ²⁴Department of Physics, Kyoto University, Kyoto 606-8502, Japan

²⁵Center for Exotic Nuclear Studies, Institute for Basic Science, Daejeon 34126, Republic of Korea

²⁶Department of Physics, Osaka University, Osaka 560-0043, Japan

²⁷Facility for Rare Isotope Beams, Michigan State University, East Lansing, Michigan 48824, USA

(Received 11 September 2023; revised 30 January 2024; accepted 24 June 2024; published 23 August 2024)

The neutron-rich unbound fluorine isotope ${}^{30}F_{21}$ has been observed for the first time by measuring its neutron decay at the SAMURAI spectrometer (RIBF, RIKEN) in the quasifree proton knockout reaction of ³¹Ne nuclei at 235 MeV/nucleon. The mass and thus one-neutron-separation energy of ³⁰F has been

^{*}Contact author: jkahlbow@mit.edu

Present address: Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA.

Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI.

determined to be $S_n = -472 \pm 58(\text{stat}) \pm 33(\text{sys})$ keV from the measurement of its invariant-mass spectrum. The absence of a sharp drop in $S_n({}^{30}\text{F})$ shows that the "magic" N = 20 shell gap is not restored close to ${}^{28}\text{O}$, which is in agreement with our shell-model calculations that predict a near degeneracy between the neutron *d* and *fp* orbitals, with the $1p_{3/2}$ and $1p_{1/2}$ orbitals becoming more bound than the $0f_{7/2}$ one. This degeneracy and reordering of orbitals has two potential consequences: ${}^{28}\text{O}$ behaves like a strongly superfluid nucleus with neutron pairs scattering across shells, and both ${}^{29,31}\text{F}$ appear to be good two-neutron halo-nucleus candidates.

DOI: 10.1103/PhysRevLett.133.082501

Introduction—A fundamental question in nuclear physics is to understand which extreme combinations of protons and neutrons can form a bound nucleus [1,2]. While nucleons in stable nuclei are bound by several megaelectronvolts (MeV), adding neutrons to a given isotopic chain progressively reduces their binding energy, until reaching the so-called drip line, beyond which neutrons drip out of the nuclear potential and cannot be bound anymore. Irrespective of experimental efforts carried out to produce nuclei with larger neutron-to-proton imbalance, the location of the neutron drip line is so far only known up to the Ne (Z = 10) isotopic chain [3,4].

The study of asymmetric nuclei and their emerging phenomena serve as a critical testing ground for nuclear theories, both in terms of nuclear interactions and manybody methods [5–7]. The study of a given isotopic chain of light nuclei up to the proton and neutron drip lines offers the opportunity to understand nuclear structure, magic numbers, and shell evolution, as well as effects related to their weak binding energy, such as halo or cluster formation [8,9]. Additionally, the reduction of traditional shell gaps far from stability may lead to a transition into superfluid character in which the scattering of pairs of neutrons is enhanced. This superfluid phase would change from stable to neutron drip-line nuclei, i.e., from a regime of Bardeen-Cooper-Schrieffer (BCS)-like pairs where nucleons have large correlation distances, to a Bose-Einstein condensate (BEC)-like phase of nuclear matter, where dineutron condensates form in a low-density environment [10–12]. The heavy fluorine isotopes (Z = 9)discussed here are highly interesting as most of the effects mentioned above likely contribute [13–17].

The F isotopic chain extends up to ³¹F, with the odd-*N* isotopes of ^{28,30}F being unbound. This is as much as six neutrons further as compared to the O chain, where ²⁴O is the last bound isotope. There exist thus far complementary signatures for the breakdown of "magicity" at the neutron number N = 20 in the F isotopic chain and in the doubly magic candidate nucleus ²⁸O. First, the presence of a low-lying (1/2⁺) excited state at 1080 keV in ²⁹F [18] is suggestive of the coupling of a single $d_{5/2}$ proton with a low-energy 2⁺ excitation of the core nucleus ²⁸O. Second, the study of the ²⁹F(*p*, *pn*) reaction [19] proves the dominant ground-state occupancy of the valence neutron

 $\ell = 1, 1p_{3/2}$ orbital, rather than the normally filled $0d_{3/2}$ orbital and the small occupancy of the $\ell = 3, 0 f_{7/2}$ orbital in ²⁹F. This demonstrates the erosion of the N = 20 gap between the $0d_{3/2}$ and fp orbitals and an inversion between the f and p orbitals. Third, the observed increase of reaction cross section in ²⁹F, as compared to ²⁷F, is compatible with a substantial amount of intruder pstates [13] as found in a microscopic model that agrees with experiment and predicts an occupancy of the $0f_{7/2}$ and $1p_{3/2}$ orbits by 2.19 and 1.26, respectively, for ²⁹F. Fourth, the combined facts that $S_{2n}(^{29}\text{F}) = 1130(540) \text{ keV} [20,21]$ is small and ³¹F is bound imply a rather weak decrease of the two-neutron separation energy S_{2n} after having passed N = 20 [20]. Fifth, the measured ${}^{29}\text{F}(p, 2p){}^{28}\text{O}$ cross section is, when compared to theory, suggestive of a similar structure between ²⁹F and ²⁸O [22], meaning that the N = 20 shell is not closed in ²⁸O either.

The present experimental work aims at studying for the first time the spectroscopy and the neutron separation energy S_n of ${}^{30}F_{21}$, which lies one neutron beyond N = 20. The combined experimental results for the F and O chains in comparison to state-of-the-art shell model calculations will introduce the discussion related to the vanishing N = 20 gap, superfluidity, and possible halo appearance in this region of the chart of nuclides.

Technically, as for ²⁸F [19], we make use of the fact that ³⁰F is unbound to deduce its spectroscopy and neutron separation energy from the reconstructed ²⁹F + *n* invariantmass spectrum, produced in ³¹Ne(p, 2p)³⁰F quasifree proton knockout reactions. The incident ³¹Ne displays features characteristic of a deformed nucleus with a $3/2^-$ ground state having a significant *p*-wave halo component [23–26]. Consequently, negative parity states are expected to be populated in ³⁰F with this reaction, as protons are likely removed from the *sd* orbitals.

Experimental procedure—A secondary beam of ³¹Ne (1.7 particles/s, 235 MeV/nucleon) was produced at the Radioactive Isotope Beam Factory (RIBF) of the RIKEN Nishina Center by fragmentation of a 345 MeV/nucleon ⁴⁸Ca beam (~600 pnA) on a 15-mm-thick Be target, and selected using the BigRIPS fragment separator [27]. The ³¹Ne nuclei were identified via their energy loss and time of flight (TOF) using thin plastic scintillators.

The ³¹Ne secondary beam was tracked toward the SAMURAI superconducting dipole-magnet setup [28] to perform the invariant-mass measurement of ³⁰F following the proton knockout reaction in the MINOS liquid hydrogen target of 1.14 g/cm^2 [29], using the same detector configuration as in Refs. [19,22]. The MINOS target cell was surrounded by a time-projection chamber (TPC), which allowed for the reconstruction of the (p, 2p) reaction vertex with a precision of 3.5 mm (σ_z) in the beam direction. The DALI2 detector array [30] placed around the target, composed of 120 NaI(Tl) crystals, detects in-flight γ rays with an efficiency of $\varepsilon_{\gamma} = 13.8\%$ at 1.173 MeV. The ²⁹F residues were detected at the dispersive focal plane of the SAMURAI spectrometer and identified by means of their TOF and energy loss information from a segmented scintillator hodoscope. Their momentum was obtained with a resolution of $p/\Delta p \approx 625$ (1 σ) based on their bending in the SAMURAI magnet.

Beamlike decay neutrons were detected at forward angles using the segmented plastic-scintillator detectors NeuLAND demonstrator (400 modules) [31] and NEBULA (2×60 modules) [28,32,33]. These three walls with 40 cm, 24 cm, and 24 cm thickness, each accompanied by chargedparticle veto detectors in front and separated by $\sim 2 \text{ m}$ and 1 m, were placed downstream of the magnet. The response of the neutron detectors was evaluated in a dedicated experiment using a quasi-monoenergetic neutron beam of 251 MeV, produced in the charge-exchange reaction $^{7}\text{Li}(p,n)^{7}\text{Be}(g.s. + 430 \text{ keV})$. A one-neutron detection efficiency of 27.4(10)% is obtained with the present NeuLAND demonstrator configuration, which agrees within 1% with simulation. The overall one-neutron detection efficiency of the total array amounts to $\varepsilon_n = 54\%$ for decay energies below 1 MeV, and decreases to 30% at 3.5 MeV.

Analysis and results-³⁰F is produced in the quasifree ³¹Ne(p, 2p) proton-knockout reaction, in which the scattered protons show coplanar kinematics with an opening angle of about 77°, as measured with the MINOS TPC. Being unbound, the ³⁰F nucleus immediately decays into ²⁹F and one neutron, potentially followed by γ -ray emission if ²⁹F is populated in an excited state. As shown in Fig. 1(b) (and Supplemental Material [34] Fig. S1) for the Doppler-corrected γ -ray energy spectrum in coincidence with ${}^{29}\text{F} + n$, this hypothesis has been rejected based on the nonobservation of a γ -ray peak, specifically at 1080(18) keV which corresponds to the decay of the only excited state reported so far in ²⁹F [18]. The emitted neutron is registered as the first hit in TOF in one of the neutron detectors, in coincidence with the incoming ³¹Ne nucleus, two scattered protons, and the (Z - 1, A - 2) fragment ²⁹F. The momentum of each decay neutron was derived from its TOF between the reaction vertex in the target and the hit position and time measured by the NeuLAND demonstrator or NEBULA [33].



FIG. 1. (a) Relative-energy spectrum of 30 F reconstructed in the ³¹Ne $(p, 2p)^{29}$ F + n reaction. The data (points with 1σ stat uncertainty) are corrected for efficiency and acceptance of the neutron detection. The full red curve depicts a fit with one resonance at $E_{fn}^r = 472 \pm 58(\text{stat}) \pm 33(\text{sys})$ keV, while the dashed line describes unresolved resonant contributions. The overall gray curve shows the total fit. The inset (b) shows the neutron-gated Doppler-corrected γ -ray spectrum of ²⁹F in comparison to a simulated 100% direct γ decay to the known 1080 keV state in ²⁹F (orange line) and to pure background (dashed line), extracted from the reaction ${}^{29}F(p, 2p){}^{24}O$ in which no γ ray is present. The good agreement between the experimental spectrum and background proves that the observed neutron decay occurs to the ground state of ²⁹F. (c) Shell-model predicted spectroscopic strength C^2S of ³⁰F states produced by proton knockout from ³¹Ne with spin-parity assignment J^{π} . The states have been shifted by -600 keV to ease the comparison to the experimental spectrum (a). The gray curve depicts the summed energy spectrum in which calculated states are smeared by the experimental response.

Having identified the ³¹Ne $(p, 2p)^{29}$ F + *n* reaction channel, the two-body relative energy E_{fn} of the decaying ³⁰F system, shown in Fig. 1(a), is reconstructed based on the invariant mass using the four-momenta of fragment and

neutron of the two reaction products. The experimental data points shown are corrected for the energy-dependent neutron-detection efficiency and acceptance.

The experimental E_{fn} spectrum shows one clear peak. However, being an odd-odd nucleus, the level density is expected to be relatively large with, in particular, many negative-parity states as for ²⁸F (see discussion part). Thus, the relative-energy spectrum is likely to include unresolved resonances, the energies and widths of which cannot be constrained from the present statistics and energy resolution. To account for this, we fit the spectrum in a combination of a single resonance peak and a broad component including unresolved resonant contributions. The resonance is described using a single-level energy-dependent Breit-Wigner line shape following Refs. [34,37,38], while the broad unresolved contribution is modeled following Ref. [39] in the form of Eq. (2). The line shape, folded with the experimental response matrix, and the unresolved contributions are fitted simultaneously in a χ^2 minimization to the experimental data by varying the resonance energy and its width. The response matrix was obtained in a GEANT4 simulation and relates the true and reconstructed relative energy and shape, including detector-response effects. The relative-energy resolution is as low as ~0.10 MeV (1 σ) at $E_{fn} = 1$ MeV and ~0.03 MeV at 0.1 MeV, largely driven by the performance of the more granular NeuLAND demonstrator.

The best fit, shown by the gray curve in Fig. 1(a), has a reduced $\chi^2_{\rm red}$ of 0.97. It results in a resonance energy of $E^r_{fn} = 472 \pm 58(\text{stat}) \pm 33(\text{sys})$ keV. The systematic uncertainty is extracted from the maximum difference for two different fit scenarios, the one described above and the other assuming a single Breit-Wigner line shape, while being largely insensitive to the choice of ℓ (here $\ell = 1$). While the peak value is well described and stable under various fit conditions, the extracted resonance width of $\Gamma^r = 477^{+358}_{-177}$ (stat) keV is not, because of the weakly constrained unresolved contributions, in extreme cases it could be solely dominated by detector resolution or be a single resonance. Note that the quoted uncertainty has been extracted assuming a fixed contribution for the unresolved resonances. Assuming that no other resonance exists below this energy (see discussion below), a negative neutron separation energy of $S_n({}^{30}\text{F}) = -472 \pm 58(\text{stat}) \pm$ 33(sys) keV is deduced.

Discussion—The following discussion is based on the experimental observation confronted with shell-model calculations. The calculations have been performed in the full *sd-pf* valence space for neutrons and in the *sd* shell for protons while using an updated version of the SDPF-U-MIX effective interaction, named hereafter SDPF-U-MIX20 [19]. With respect to SDPF-U-MIX, monopole constraints have been incorporated in order to reproduce the $3/2^-$ and $7/2^-$ states along the N = 17 isotones in

²⁷Ne, ²⁹Mg, and ³¹Si, as well as to fix the Duflo-Zuker mass-formula master term [Eq. (2) of [40]] on the binding energies of P isotopes, including those beyond N = 20 when the $0f_{7/2}$ orbital is getting filled. The SDPF-U-MIX20 allows for a very good description of nuclear properties for a vast area of nuclei, ranging from *sd* nuclei to *pf* nuclei, including the "island of inversion" around ³²Mg and the properties of O and F at the neutron drip line.

Spectroscopy of ³⁰F: Only one resonance could be firmly established experimentally with a width of severalhundred keV in Fig. 1(a). However, our shell-model calculation predicts a large population of negative parity states in ³⁰F (full spectrum Fig. S3 in [34]) through the removal of a $0d_{5/2}$ or $1s_{1/2}$ proton from the intruder neutron $3/2^{-}$ ground state of ³¹Ne [23–25]. The summed theoretical energy spectrum shown in Fig. 1(c), in which each predicted state is scaled according to its spectroscopic strength C^2S and smeared by the experimental response, shows good agreement with the experimental one of Fig. 1(a) in terms of their shape, while being shifted by -600 keV. This a posteriori supports the use of a broad contribution in the experimental fit, which would mimic several unresolved resonances with small C^2S each. If a resonance with low C^2S value existed below the experimentally found one, such as the predicted 4⁻ state, this would lead to a smaller $|S_n|$ value by about 150 keV. Such an hypothetical shift in $|S_n|$ would further strengthen our conclusions discussed in the following.

Pairing and N = 20 gap: The systematics of S_n values as a function of neutron number N is shown for the phosphorus P, fluorine F, and oxygen O isotopes in Fig. 2. In the P chain, all the experimental values are taken from Ref. [21], which are well determined with less than 2-keV uncertainty. The odd-even staggering along the isotopic chain is due to the presence of shell gaps at N = 16(mostly seen in O chain, as discussed in Ref. [42]) and at N = 20, as well as pairing effects between these gaps. An N = 20 gap of 4.915(13) MeV can be estimated from the $S_n({}^{35}P_{20}) - S_n({}^{36}P_{21})$ difference.

In the F chain, the experimental S_n values shown in Fig. 2 are, except for ³⁰F, taken from the atomic mass evaluation [21], which makes use of the latest measurements of ^{27,28}F from Ref. [19]. The present value of $S_n(^{30}\text{F}) = -472$ keV is added to the figure. Even if not altering the following discussions, it is noted that the S_n value of ²⁶F could be shifted upward by about 200 keV as ²⁶F has a reported long-lived isomer state (see discussion in Ref. [43]). The amplitudes of S_n oscillations are similar to those in the O chain derived for ^{24–28}O from Refs. [22,44]. However, they are much weaker in the weakly bound or unbound F than in the P chain. This is at variance with the empirical variation of the pairing gap following $A^{-1/2}$ and with the prediction of an increased pairing gap at low density in infinite matter [45].



FIG. 2. Experimental and theoretical neutron separation energy S_n as a function of neutron number N for the fluorine F, Z = 9 (red circles), oxygen O, Z = 8 (magenta triangles), and phosphorus P, Z = 15 (blue squares), isotopes. Data points, including the new one at N = 21 for ³⁰F, are shown with their corresponding uncertainties (1 σ), often smaller than the size of the filled symbols. The theoretical results for P, F, and O, obtained from shell-model calculations using the SDPF-U-MIX20 interaction, are shown with the same symbols as data but with lighter color and linked by dashed lines instead of full lines. A compilation of S_n values with more even and odd nuclei showing the damping of oscillations and the progressive vanishing of the N = 20 shell closure toward the drip line can be found in [34] Fig. S4.

Noticeably, these oscillations remain constant in the F chain, even after passing N = 20. This is in stark contrast to the P and other chains at $Z \gtrsim 15$, in which a marked closed shell effect has been observed through a large drop in $S_n(N = 21)$ value. The absence of a sharp drop in S_n value after N = 20 in the F chain is a decisive proof that magicity is not restored close to the Z = 8, N = 20, 28 O nucleus. A compilation of S_n values toward the drip line for Z = 8-15 can be found in [34] Fig. S4.

There is extremely good agreement between our largescale shell-model calculations and experimental S_n values in the P chain. The agreement is also quite good for the F chain and for the known ^{24–28}O isotopes. However, the calculated S_n value of ³⁰F is –892 keV, which is 420 keV lower than the experimental one of –472 keV. Moreover, one observes that experimental oscillations are further damped in the F and O chains by about 20% as compared to theory for the most neutron-rich cases.

In the valley of stability ($Z \ge 14$), a large N = 20 gap of about 7 MeV is calculated using effective single-particle energies between the $0d_{3/2}$ and $0f_{7/2}$ orbitals and a smaller N = 28 gap of about 2 MeV separates the $0f_{7/2}$ and the $(1p_{3/2}, 1p_{1/2})$ orbitals (see ESPE in [34] Fig. S2). In the O and F chains, the N = 20 gap is only 2 MeV and the two 1p orbits become more bound than the $0f_{7/2}$ one. The pf shell inversion is also reflected by the neutron occupancy of the $0f_{7/2}$ and $1p_{3/2}$ shells of 0.2 and 0.8, respectively in ²⁹F, and 0.8 and 2.1, respectively in ³¹F. Low- ℓ weakly or unbound orbitals are expected to be rather sensitive to the proximity of the continuum [46,47] which may further reduce the N = 20 gap. Theory frameworks of Refs. [15,41] that incorporate continuum degrees of freedom reproduce well the constancy and damping of S_n oscillations in the F chain even after having passed N = 20 (cf. Fig. S5 of [34]), in particular the Gamow shell model calculation using the Furutani-Horiuchi-Tamagaki interaction [41].

Superfluidity: The close proximity of all neutron orbits and the fact that the proton Z = 8 core is likely preserved induce interesting properties for the collectivity (quadrupole, pairing) of these nuclei. According to our calculations, ²⁸O has 97% of pairs coupled to J = 0 (seniority 0), with 50% closed-shell configuration and 47% of pairs involved in *sd* to *fp* excitations, mostly between the $d_{3/2}$ and the $p_{3/2}$ orbitals. The ²⁹F nucleus is also dominated by pairs coupled to J = 0 (by 70%), with more than 60% of scatter from the *sd* to *pf* orbits.

Such a regime in which pairs of nucleons equivalently occupy nearby orbitals is usually defined as superfluid (see, e.g., Ch. 6 of Ref. [48]). A characteristic example of superfluidity is found in the tin isotopic chain where, between N = 50 and N = 82, (J = 0)-coupled neutron pairs scatter between all nearby orbitals, keeping the Z = 50 proton core mainly unaffected at low excitation energy. This has the consequence of observing almost constant pairing oscillations in the whole tin isotopic chain. The constancy of S_n oscillations in the F chain, experimentally established even above N = 20, and predicted to continue in ${}^{31}F_{22}$ with an S_n value of 924 keV, is a likely consequence of the mixing between orbitals and a further indication of the onset of this superfluid regime. The reduced amplitude of oscillations in the O and F chains, as compared to the P chain, for instance, can partially be explained by the mixed filling of the $d_{3/2}$ and $p_{3/2}$ orbitals. Indeed, the amplitude of the odd-even pairing oscillations are weaker in the $p_{3/2}$ orbital than in the $d_{3/2}$, as can be deduced from the observed amplitudes of pairing oscillations in the Ca isotopic chain with the sequential filling of the $d_{3/2}, f_{7/2}, p_{3/2}$, and $p_{1/2}$ orbitals [42]. A similar reduction of S_n oscillations has been found in the neutronrich B isotopes [20,49].

As for the nature of the superfluid phase in the (O,F) isotopic chains, the mixing between weakly bound orbits of different parities should favor the transition to a BEC regime with neutron pairs of much smaller size as compared to BCS according to Refs. [14,50–52]. This transition is planned to be explored on a theoretical ground using the relative coordinate of neutrons in shell-model calculations.

Future experimental works should focus on the determination of the relative distance or angle between neutrons using experimental techniques such as the ones described in Refs. [53,54].

Two-neutron halos: As discussed in Refs. [13,14,16,41] the presence of these low- ℓ orbitals, their high occupancy, and their relatively weak binding likely favors the development of two-neutron halo structures in ²⁹F and more importantly in ³¹F. This is corroborated by our shell-model calculations based on the large occupancy of the $p_{3/2}$ orbital by 0.8 and 2.1 neutrons for ²⁹F and ³¹F, respectively, and our predicted low S_{2n} values of 776 keV for ²⁹F, to be compared to the experimental value of 1130(540) keV [20,21], and 32 keV for ³¹F.

Summary-In this Letter, we report on the first study of the neutron-rich ³⁰F nucleus, produced by means of quasifree proton knockout reactions of a ³¹Ne beam on a liquid hydrogen target. The excitation energy spectrum of ³⁰F and its neutron separation energy S_n have been obtained using the invariant-mass method from the decay into $^{29}\text{F} + n$. Based on the deduced $S_n(^{30}\text{F})$ value of $-472 \pm$ $58(\text{stat}) \pm 33(\text{sys})$ keV, we find no sharp decrease in S_n after N = 20 but rather damped pairing oscillations of constant amplitude. The absence of a sharp drop is the most direct confirmation that the N = 20 shell gap is not restored in this region of the chart of nuclides close to ²⁸O. The constancy of oscillations, as well as their weaker amplitude as compared to the P isotones, are suggestive of a coupling to the continuum, as well as of the mixing between the nearby $0d_{3/2}$ and $1p_{3/2}$ orbitals. This mixing induces the establishment of a superfluid regime, which is further substantiated by shell model calculations in which ²⁸O and ²⁹F have strongly dominating configurations of neutron pairs coupled to J = 0, scattering by about half between the sd and fp shells. Searching for a transition to the superfluid BEC phase in the F chain and studying the two-neutron halo feature of ³¹F are imminent topics for the future.

Acknowledgments-We thank the accelerator staff of the RIKEN Nishina Center for their efforts in delivering the intense ⁴⁸Ca beam. This project was supported by Deutsche Forschungsgemeinschaft (DFG, German Research Foundation), Project-ID 279384907-SFB 1245, and the GSI-TU Darmstadt cooperation agreement. J.K. also acknowledges support from RIKEN as short-term International Program Associate and from Tokyo Institute of Technology under the Foreign Graduate Student Invitation Program. T. N. and Y. K. acknowledge support from JSPS KAKENHI Grants No. JP18H05404, No. JP21H04465, and No. JP24H00006. Y.K. also acknowledges partial support from JSPS KAKENHI Grant No. JP18K03672. N. L. A., F. D., J. G., F. M. M., and N. A. O. acknowledge partial support from the Franco-Japanese LIA-International Associated Laboratory for Nuclear Structure Problems as well as the French ANR-14-CE33-0022-02 EXPAND. I.G. was supported by the Helmholtz International Center for FAIR and Croatian Science Foundation under Projects No. 1257 and No. 7194. This work was also supported in part by the National Science Foundation, USA under Grant No. PHY-1102511. Z. D., Z. E., and D. S. were supported by National Research, Development and Innovation Fund of Hungary (NKFIH) Projects No. TKP2021-NKTA-42 and No. K147010, and I.K. by Project No. PD 124717. L.S. acknowledges support from the Institute for Basic Science under IBS-R031-D1. H.W. acknowledges the support by JSPS KAKENHI Grants No. JP21H04465 and No. JP18H05404.

- J. Erler, N. Birge, M. Kortelainen, W. Nazarewicz, E. Olsen, A. Perhac, and M. Stoitsov, The limits of the nuclear landscape, Nature (London) 486, 509 (2012).
- [2] S. R. Stroberg, J. D. Holt, A. Schwenk, and J. Simonis, *Ab initio* limits of atomic nuclei, Phys. Rev. Lett. **126**, 022501 (2021).
- [3] D. S. Ahn *et al.*, Location of the neutron dripline at fluorine and neon, Phys. Rev. Lett. **123**, 212501 (2019).
- [4] D. S. Ahn *et al.*, Discovery of ³⁹Na, Phys. Rev. Lett. **129**, 212502 (2022).
- [5] H. Hergert, A guided tour of *ab initio* nuclear many-body theory, Front. Phys. **8**, 379 (2020).
- [6] T. Otsuka, A. Gade, O. Sorlin, T. Suzuki, and Y. Utsuno, Evolution of shell structure in exotic nuclei, Rev. Mod. Phys. 92, 015002 (2020).
- [7] F. Nowacki, A. Obertelli, and A. Poves, The neutron-rich edge of the nuclear landscape: Experiment and theory, Prog. Part. Nucl. Phys. **120**, 103866 (2021).
- [8] P. Hansen and B. Jonson, The neutron halo of extremely neutron-rich nuclei, Europhys. Lett. 4, 409 (1987).
- [9] B. Gnoffo, S. Pirrone, G. Politi, G. Cardella, E. De Filippo, E. Geraci, C. Maiolino, N. S. Martorana, A. Pagano, E. V. Pagano, M. Papa, F. Risitano, F. Rizzo, P. Russotto, and M. Trimarchi, Clustering and molecular states in neutron rich nuclei, Front. Phys. **10**, 1061633 (2022).
- [10] M. Matsuo, Spatial structure of neutron Cooper pair in low density uniform matter, Phys. Rev. C 73, 044309 (2006).
- [11] K. Hagino, H. Sagawa, J. Carbonell, and P. Schuck, Coexistence of BCS- and BEC-like pair structures in halo nuclei, Phys. Rev. Lett. 99, 022506 (2007).
- [12] B. Y. Sun, H. Toki, and J. Meng, Relativistic description of BCS-BEC crossover in nuclear matter, Phys. Lett. B 683, 134 (2010).
- [13] S. Bagchi *et al.*, Two-neutron halo is unveiled in ²⁹F, Phys. Rev. Lett. **124**, 222504 (2020).
- [14] L. Fortunato, J. Casal, W. Horiuchi, J. Singh, and A. Vitturi, The ²⁹F nucleus as a lighthouse on the coast of the island of inversion, Commun. Phys. **3**, 132 (2020).
- [15] K. Fossez and J. Rotureau, Density matrix renormalization group description of the island of inversion isotopes ^{28–33}F, Phys. Rev. C 106, 034312 (2022).
- [16] G. Singh, J. Singh, J. Casal, and L. Fortunato, Exploring the halo character and dipole response in the dripline nucleus ³¹F, Phys. Rev. C **105**, 014328 (2022).

- [17] Y.-X. Luo, K. Fossez, Q. Liu, and J.-Y. Guo, Role of quadrupole deformation and continuum effects in the "island of inversion" nuclei ^{28,29,31}F, Phys. Rev. C **104**, 014307 (2021).
- [18] P. Doornenbal *et al.*, Low-Z shore of the "island of inversion" and the reduced neutron magicity toward ²⁸O, Phys. Rev. C **95**, 041301(R) (2017).
- [19] A. Revel *et al.* (SAMURAI21 Collaboration), Extending the southern shore of the island of inversion to ²⁸F, Phys. Rev. Lett. **124**, 152502 (2020).
- [20] L. Gaudefroy, W. Mittig, N. Orr, S. Varet, M. Chartier, P. Roussel-Chomaz, J. P. Ebran, B. Fernández-Domínguez, G. Frémont, P. Gangnant, A. Gillibert, S. Grévy, J. Libin, V. Maslov, S. Paschalis, B. Pietras, Y.-E. Penionzhkevich, C. Spitaels, and A. Villari, Direct mass measurements of ¹⁹B, ²²C, ²⁹F, ³¹Ne, ³⁴Na and other light exotic nuclei, Phys. Rev. Lett. **109**, 202503 (2012).
- [21] M. Wang, W. Huang, F. Kondev, G. Audi, and S. Naimi, The AME 2020 atomic mass evaluation (II). Tables, graphs and references, Chin. Phys. C 45, 030003 (2021).
- [22] Y. Kondo *et al.*, First observation of ²⁸O, Nature (London)
 620, 965 (2023).
- [23] T. Nakamura *et al.*, Halo structure of the island of inversion nucleus ³¹Ne, Phys. Rev. Lett. **103**, 262501 (2009).
- [24] M. Takechi *et al.*, Interaction cross sections for Ne isotopes towards the island of inversion and halo structures of ²⁹Ne and ³¹Ne, Phys. Lett. B **707**, 357 (2012).
- [25] T. Nakamura *et al.*, Deformation-driven *p*-wave halos at the drip line: ³¹Ne, Phys. Rev. Lett. **112**, 142501 (2014).
- [26] D. Chrisman *et al.*, Neutron-unbound states in ³¹Ne, Phys. Rev. C **104**, 034313 (2021).
- [27] T. Kubo, K. Kusaka, K. Yoshida, A. Yoshida, T. Ohnishi, M. Ohtake, Y. Yanagisawa, N. Fukuda, T. Haseyama, Y. Yano, N. Kakutani, T. Tsuchihashi, and K. Sato, Status and overview of superconducting radioactive isotope beam separator BigRIPS at RIKEN, IEEE Trans. Appl. Supercond. 17, 1069 (2007).
- [28] T. Kobayashi, N. Chiga, T. Isobe, Y. Kondo, T. Kubo, K. Kusaka, T. Motobayashi, T. Nakamura, J. Ohnishi, H. Okuno, H. Otsu, T. Sako, H. Sato, Y. Shimizu, K. Sekiguchi, K. Takahashi, R. Tanaka, and K. Yoneda, SAMURAI spectrometer for RI beam experiments, Nucl. Instrum. Methods Phys. Res., Sect. B **317**, 294 (2013).
- [29] A. Obertelli *et al.*, MINOS: A vertex tracker coupled to a thick liquid-hydrogen target for in-beam spectroscopy of exotic nuclei, Eur. Phys. J. A 50, 8 (2014).
- [30] S. Takeuchi, T. Motobayashi, Y. Togano, M. Matsushita, N. Aoi, K. Demichi, H. Hasegawa, and H. Murakami, DALI2: A NaI(Tl) detector array for measurements of γ rays from fast nuclei, Nucl. Instrum. Methods Phys. Res., Sect. A 763, 596 (2014).
- [31] K. Boretzky *et al.*, NeuLAND: The high-resolution neutron time-of-flight spectrometer for R³B at FAIR, Nucl. Instrum. Methods Phys. Res., Sect. A **1014**, 165701 (2021).
- [32] T. Nakamura and Y. Kondo, Large acceptance spectrometers for invariant mass spectroscopy of exotic nuclei and future developments, Nucl. Instrum. Methods Phys. Res., Sect. B 376, 156 (2016).
- [33] Y. Kondo, T. Tomai, and T. Nakamura, Recent progress and developments for experimental studies with the SAMURAI

spectrometer, Nucl. Instrum. Methods Phys. Res., Sect. B 463, 173 (2020).

- [34] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.133.082501, which includes Refs. [35,36] for Breit-Wigner lineshape, γ -ray spectrum, ³⁰F level scheme, ESPE, neutron separation energies, and calculations with continuum coupling.
- [35] Y. Luo, J. Okolowicz, M. Ploszajczak, and N. Michel, Shell model embedded in the continuum for binding systematics in neutron-rich isotopes of oxygen and fluor, arXiv:nucl-th/ 0211068.
- [36] B. Hu, Q. Wu, J. Li, Y. Ma, Z. Sun, N. Michel, and F. Xu, An *ab-initio* Gamow shell model approach with a core, Phys. Lett. B 802, 135206 (2020).
- [37] A. M. Lane and R. G. Thomas, *R*-matrix theory of nuclear reactions, Rev. Mod. Phys. **30**, 257 (1958).
- [38] M. Vandebrouck *et al.* (R3B Collaboration), Effective proton-neutron interaction near the drip line from unbound states in ^{25,26}F, Phys. Rev. C 96, 054305 (2017).
- [39] C. Caesar *et al.* (R3B Collaboration), Beyond the neutron drip line: The unbound oxygen isotopes ²⁵O and ²⁶O, Phys. Rev. C 88, 034313 (2013).
- [40] J. Mendoza-Temis, J. G. Hirsch, and A. P. Zuker, The anatomy of the simplest Duflo-Zuker mass formula, Nucl. Phys. A 843, 14 (2010).
- [41] N. Michel, J. G. Li, F. R. Xu, and W. Zuo, Two-neutron halo structure of ³¹F, Phys. Rev. C 101, 031301(R) (2020).
- [42] L. Lalanne *et al.*, N = 16 magicity revealed at the proton drip line through the study of ³⁵Ca, Phys. Rev. Lett. **131**, 092501 (2023).
- [43] A. Lepailleur *et al.*, Spectroscopy of ²⁶F to probe protonneutron forces close to the drip line, Phys. Rev. Lett. **110**, 082502 (2013).
- [44] Y. Kondo *et al.*, Nucleus ²⁶O: A barely unbound system beyond the drip line, Phys. Rev. Lett. **116**, 102503 (2016).
- [45] U. Lombardo and H.-J. Schultze, Superfluidity in neutron star matter, arXiv:astro-ph/0012209.
- [46] I. Hamamoto, S. V. Lukyanov, and X. Z. Zhang, Kinetic energy and spin-orbit splitting in nuclei near neutron drip line, Nucl. Phys. A 683, 255 (2001).
- [47] B. P. Kay, C. R. Hoffman, and A. O. Macchiavelli, Effect of weak binding on the apparent spin-orbit splitting in nuclei, Phys. Rev. Lett. 119, 182502 (2017).
- [48] P. Ring and P. Schuck, *The Nuclear Many-Body Problem* (Springer-Verlag, New York, 1980).
- [49] S. Leblond *et al.*, First observation of ²⁰B and ²¹B, Phys. Rev. Lett. **121**, 262502 (2018).
- [50] F. Catara, A. Insolia, E. Maglione, and A. Vitturi, Relation between pairing correlations and two-particle space correlations, Phys. Rev. C 29, 1091 (1984).
- [51] A. Obertelli and H. Sagawa, *Modern Nuclear Physics*, UNITEXT for Physics (Springer, Singapore, 2021), p. 423, 10.1007/978-981-16-2289-2.
- [52] Z. H. Yang *et al.*, Observation of the exotic 0^+_2 cluster state in ⁸He, Phys. Rev. Lett. **131**, 242501 (2023).
- [53] T. Nakamura *et al.*, Observation of strong low-lying *E*1 strength in the two-neutron halo nucleus ¹¹Li, Phys. Rev. Lett. **96**, 252502 (2006).
- [54] Y. Kubota *et al.*, Surface localization of the dineutron in ¹¹Li, Phys. Rev. Lett. **125**, 252501 (2020).