First Exploration of Monopole-Driven Shell Evolution above the $N = 126$ Shell Closure: New Millisecond Isomers in ²¹³Tl and ²¹⁵Tl

T. T. Yeung Φ , ^{1,2} A. I. Morales Φ , ^{[3,*](#page-0-0)} J. Wu Φ , ^{4,5,[†](#page-0-1)} M. Liu Φ ,⁶ C. Yuan Φ ,⁶ S. Nishimura,² V. H. Phong,^{2,7} N. Fukuda,² J. L. Tain,³ T. Davinson,⁸ K. P. Rykaczewski,⁹ R. Yokoyama,^{10,11} T. Isobe,² M. Niikura^{no, 1,2} Zs. Podolyák,¹² G. Alcalá,³ A. Algora,^{3,13} J. M. Allmond^o,⁹ J. Agramunt,³ C. Appleton,⁸ H. Baba,² R. Caballero-Folch,¹⁴ F. Calvino,¹⁵ M. P. Carpenter, ¹⁶ I. Dillmann (1, 1, 17 A. Estrade, ¹⁸ T. Gao, ¹⁹ C. J. Griffin, ¹⁴ R. K. Grzywacz, ^{10,9} O. Hall, ⁸ Y. Hirayama, ²⁰ B. M. Hue Φ , 27 E. Ideguchi, 21 G. G. Kiss Φ , 13,2 K. Kokubun, 1 F. G. Kondev, 16 R. Mizuno, 1 M. Mukai, 22 N. Nepal, 18 M. N. Nurhafiza,²³ S. Ohta,¹¹ S. E. A. Orrigo[®],³ M. Pallàs,¹⁵ J. Park,²⁴ B. C. Rasco®,⁹ D. Rodríguez-García®,³ H. Sakurai,^{2,1} L. Sexton,^{8,14} Y. Shimizu,² H. Suzuki,² A. Vitéz-Sveiczer,^{13,25} H. Takeda,² A. Tarifeno-Saldivia,^{15,3} A. Tolosa-Delgado,²⁶ J. A. Victoria,³ Y. X. Watanabe,²⁰ and J. M. Yap¹⁹ ¹Department of Physics, The University of Tokyo, 7-3-1 Hongo, Bunkyo, Tokyo 113-0033, Japan $\frac{2\text{BIEEN}}{2\text{BIEEN}}$ Nighing Center 2.1 Hinggang Wake, Saitang 251,0108, Japan R IKEN Nishina Center, 2-1 Hirosawa, Wako, Saitama 351-0198, Japan 3 Instituto de Física Corpuscular, CSIC-Universitat de València, E-46071 València, Spain ⁴National Nuclear Data Center, Brookhaven National Laboratory, Upton, New York 11973, USA ⁵Facility for Rare Isotope Beams, Michigan State University, East Lansing, Michigan 48824, USA ⁶Sino-French Institute of Nuclear Engineering and Technology, Sun Yat-Sen University, Zhuhai, Guangdong 519082, China
⁷ Easylty of Physics, University of Science, Victory National ['] Faculty of Physics, University of Science, Vietnam National University, Hanoi 120062, Vietnam
⁸Sebool of Physics and Astronomy, University of Ediphyseb, EH0, 3ED Ediphyseb, United Kinodo ⁸School of Physics and Astronomy, University of Edinburgh, EH9 3FD Edinburgh, United Kingdom
⁹Physics Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831-6368, USA ¹⁰Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA
¹¹Center for Nuclear Study, the University of Tokyo, 2-1 Hirosawa, Wako Saitama 351-0198, Japan
¹²Department of Physics, ¹³HUN-REN Institute for Nuclear Research, Bem tér 18/c, Debrecen H4032, Hungary
¹⁴TRIUMF, Vancouver, British Columbia, V6T 2A3, Canada
¹⁵Universitat Politecnica de Catalunya, E-08028 Barcelona, Spain
¹⁶Physics Div ¹⁹Department of Physics, The University of Hong Kong, Pokfulam, Hong Kong, China ²⁰Wako Nuclear Science Center (WNSC), Institute of Particle and Nuclear Studies (IPNS), High Energy Accelerator Research Organization (KEK), Wako, Saitama 351-0198, Japan
²¹ Research Center for Nuclear Physics (RCNP), Osaka University, 10-1 Mihogaoka, Ibaraki, Osaka 567-0047, Japan
²² Department of Physic ⁵University of Debrecen, PhD school of Physics, H-4026, Debrecen, Hungary
²⁶Department of Physics, University of Jyvaskylä, 40014 Jyväskylä, Finland 27 Institute of Physics, Vietnam Academy of Science and Technology, Hanoi 10000, Vietnam (Received 12 January 2024; revised 5 March 2024; accepted 24 April 2024; published 13 August 2024) Isomer spectroscopy of heavy neutron-rich nuclei beyond the $N = 126$ closed shell has been performed for the first time at the Radioactive Isotope Beam Factory of the RIKEN Nishina Center. New millisecond isomers have been identified at low excitation energies, $985.3(19)$ keV in ²¹³Tl and 874(5) keV in ²¹⁵Tl. The measured half-lives of 1.34(5) ms in ²¹³Tl and 3.0(3) ms in ²¹⁵Tl suggest spins and parities 11/2[−] with the single proton-hole configuration $\pi h_{11/2}$ as leading component. They are populated via E1 transitions by the decay of higher-lying isomeric states with proposed spin and parity $17/2^+$, interpreted as arising from a single $\pi s_{1/2}$ proton hole coupled to the 8⁺ seniority isomer in the ^{A+1}Pb cores. The lowering of the 11/2[−] states is ascribed to an increase of the $\pi h_{11/2}$ proton effective single-particle energy as the second $\nu g_{9/2}$ orbital is filled by neutrons, owing to a significant reduction of the proton-neutron monopole interaction

[^{*}](#page-0-2) Contact author: Ana.Morales@ific.uv.es [†](#page-0-2) Contact author: jwu2@bnl.gov

between the $\pi h_{11/2}$ and $\nu g_{9/2}$ orbitals. The new ms isomers provide the first experimental observation of shell evolution in the almost unexplored $N > 126$ nuclear region below doubly magic ²⁰⁸Pb.

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The study of nuclei far from the valley of stability, socalled exotic or rare nuclei, is crucial to understand the evolution of the shell-model orbitals at extreme numbers of protons (Z) and neutrons (N) [\[1](#page-5-0)–[6\]](#page-5-1). The resulting structural properties in rare nuclei [\[7](#page-5-2)–[12](#page-5-3)] are determinant to advance our knowledge of the reaction and decay rates in key astrophysical events [[13](#page-5-4)–[15](#page-6-0)], in particular, the nucleosynthesis processes producing elements heavier than iron [\[16](#page-6-1)[,17\]](#page-6-2). In this regard, systematic studies of nuclear states described by single-particle excitations provide invaluable insight on the evolution of shell structure near closed shells. This is a key aspect to better predict structural phenomena in yet unexplored nucleosynthetic nuclei [[10](#page-5-5),[18](#page-6-3)].

Hitherto, the heaviest spherical closed shells known are $Z = 82$ and $N = 126$, constituting doubly magic $\frac{208}{82}P_{0.126}^{\text{O}}$. To what extent the heaviest shell gaps hold away from ²⁰⁸Pb and what their impact is on the timescales and final abundances of the rapid neutron-capture (r) process [\[19\]](#page-6-4) still remains a conundrum. The weak interaction rates in this region are particularly crucial since they regulate the nucleosynthesis of the actinides via the abundance stockpiles at the third r-process waiting point $[16,19-25]$ $[16,19-25]$ $[16,19-25]$ $[16,19-25]$. They strongly depend on the ordering and energies of single proton and neutron orbitals near the Fermi surface, the most relevant of which have large total angular momentum i (see Fig. 2 of Ref. [\[26\]](#page-6-6), p. 1529). In many theoretical frame-works [\[27](#page-6-7)–[29](#page-6-8)], the β decay of $N \sim 126$ nuclei is dominated by high-energy parity-changing first-forbidden (ff) transitions that prevail over the allowed Gamow-Teller (GT) decays (ν 0h_{9/2} $\rightarrow \pi$ 0h_{11/2}) and (ν 0i_{11/2} $\rightarrow \pi$ 0i_{13/2}), resulting in substantially enhanced rates. Since the contributions of ff and GT transitions are affected by changing singleparticle energies (SPEs), shell evolution around ²⁰⁸Pb, specially of the high-j orbitals driving GT strength, becomes of general interest in both nuclear structure and nuclear astrophysics.

In the present Letter, we report on the development of spin isomerism in the single proton-hole $\pi 0h_{11/2}$ states of 213 Tl₁₃₂ and 215 Tl₁₃₄, with six and eight neutron particles above $N = 126$. These are the first millisecond isomers reported in the $N > 126$ region below ²⁰⁸Pb, and might prelude the development of astromers that impact on the final elemental abundances of heavy nuclei in the r process [\[30\]](#page-6-9). The new $J^{\pi} = (11/2^{-})$ levels have energies about 300 keV lower than the ones predicted by shell-model calculations [\[31\]](#page-6-10). The energy decrease is ascribed to an upward trend of the π 0 $h_{11/2}$ proton effective SPE (ESPE) as the $\nu 1g_{9/2}$ shell is filled by neutrons. This effect is driven by the monopole interaction, which is the lowest order component of the residual nucleon–nucleon interaction [\[26\]](#page-6-6). The results thus provide the first experimental observation of shell evolution in a high-j orbital beyond ²⁰⁸Pb, a key structural feature to help improving the global nuclear models used in *r*-process simulations [\[29](#page-6-8)[,32,](#page-6-11)[33](#page-6-12)]. These, at present, show strong discrepancies towards the $N = 126$ waiting point and beyond, and need stringent constraints to provide higher-quality calculated β -decay inputs getting far away from stability.

Spectroscopic studies of heavy $N > 126$ nuclei have been carried out for the first time at the RIBF facility, RIKEN Nishina Center. The cyclotron acceleration complex delivered a stable ^{238}U beam at an energy of 345 MeV/nucleon. The beam intensity was the highest reached so far in a fragmentation facility, 70 pnA. The most exotic $N > 126$ nuclei in the isotopic chains of $_{77}$ Ir to $_{84}$ Po were produced in fragmentation reactions of ²³⁸U colliding to a Be target 5-mm thick.

Separation and identification of heavy nuclei are known to be a challenge in fragmentation facilities [[34](#page-6-13)]. At RIKEN, unambiguous information on the mass-to-charge ratio A/Q was obtained using thin degraders at the dispersive focal planes of the BigRIPS spectrometer [[35](#page-6-14)]. Identification in atomic number Z was achieved using a novel telescope array consisting of four tilted Si detectors which provided accurate energy losses for the transmitted heavy fragments. The Si telescope was placed at the exit of the ZeroDegree spectrometer [[36](#page-6-15)].

A total of about 4000 ions of ²¹³Tl and 1000 ions of ²¹⁵Tl were implanted in the active stopper WAS3ABi [\[37\]](#page-6-16). It consisted of a compact stack of four 1-mm thick Double-Sided Si Strip Detectors (DSSSD), each with 32×32 pixels. The implantation setup was completed by BRIKEN [\[38,](#page-6-17)[39\]](#page-6-18), a hybrid detection array consisting of 140 ³He proportional counters and two segmented clover-type HPGe detectors. Because of severe damage of one of the two HPGe detectors in the experiment, only one of them was used for analysis, providing an absolute γ-ray efficiency of ∼1% at 1408 keV. More details of the setup are provided in Ref. [[39](#page-6-18)].

Implanted nuclei, β particles, and conversion electrons— henceforth called Meitner-Ellis electrons or MEEs [[40](#page-6-19)] were discriminated by the energy deposited in WAS3ABi. The active stopper also recorded the time, DSSSD and (X, Y) strip position for each of these events. The energy and time of γ rays were registered by the HPGe clover detector. This information was recorded on an event basis by independent data acquisition systems in order to reconstruct off-line the radioactive decay(s) of the implanted residues using correlations in position and time [\[39](#page-6-18)[,41,](#page-6-20)[42](#page-6-21)].

FIG. 1. (a) and (b) MEE energy spectra of ²¹³Tl and ²¹⁵Tl, respectively. (c) and (d) Singles isomeric γ spectra of ²¹³Tl and ²¹⁵Tl, respectively (black). For comparison, the background spectra of correlations between ions and preceding γ rays are also shown (red). (e) and (f) γ-ray spectra in prompt-time coincidence with the MEEs at the left of the blue dotted lines in panels (a) and (b), respectively. (g) and (h) Spectra of γ rays preceding the decay of the MEEs at the left of the blue dotted lines in panels (a) and (b), respectively. Inset panels in (a)–(d) show time distributions of MEEs and preceding γ rays [marked in italics in panels (c) and (d)]. Unbinned maximum likelihood fits to an exponential function plus a constant background are indicated in yellow.

Isomeric states were investigated in a broad dynamic time range exploiting two procedures. The first consists in building the time differences between implanted ions and subsequent γ rays [[41](#page-6-20)–[44](#page-6-22)]. The shortest time differences are limited by the prompt flash produced by the implantation [[43](#page-6-23)], of approximately 200 ns. The second procedure exploits the production of MEEs in the internal decay of the isomer. In such cases, additional conditions on the discrete MEEs energies and (X, Y) strip distance between implanted ions and MEEs are applied. The shortest time difference for ion—MEE correlations is fixed off-line to 500 μs to avoid the dead time caused by the electronic processing of implantation events.

Figures [1\(a\)](#page-2-0) and [1\(b\)](#page-2-0) show energy spectra of MEEs correlated with ions of 213 Tl and 215 Tl. The spatial correlations are restricted to the same DSSSD and pixel of implantation in WAS3ABi. Maximum ion–MEE time differences of up to 40 ms are applied. Figures [1\(c\)](#page-2-0) and $1(d)$ show γ rays detected up to 6 ms after implantations of 213 Tl and 215 Tl, respectively. For the two nuclei, we find three γ rays in 2-μs prompt-time delayed coincidence with the MEE peaks, see Figs. [1\(e\)](#page-2-0) and [1\(f\)](#page-2-0). The γ transitions at 379.3(8) keV in ²¹³Tl and 598.3(10) keV in ²¹⁵Tl are found to decay up to 5 ms before the MEE [see Figs. $1(g)$ and [1\(h\)](#page-2-0)]. The time distributions of the MEEs and the preceding $γ$ rays, shown in the inset panels of Figs. 1(a)–[1\(d\)](#page-2-0), reveal the existence of two isomeric states in each nucleus. Unbinned maximum likelihood fits including probability density functions of the isomer exponential decay and a constant background related to random correlations return half-lives of $t_{1/2}=1.34(5)$ ms and $t_{1/2}=4.3(4)$ µs for ²¹³Tl, and $t_{1/2}=3.0(3)$ ms and $t_{1/2}$ < 210 ns for ²¹⁵Tl. The present half-life of the 379.3(8)-keV γ peak agrees within 1 standard deviation with the reported value of $t_{1/2}$ = $4.1(5)$ μs [\[45\]](#page-6-24), thus benchmarking the identification and correlation procedures used at RIBF.

In Fig. [2,](#page-2-1) the isomeric level schemes of ²¹³Tl and ²¹⁵Tl are compared to shell-model calculations (henceforth called

FIG. 2. Isomeric decay schemes of ²¹³Tl and ²¹⁵Tl compared with shell-model calculations SM1 [\[31\]](#page-6-10). $11/2^-$ states and E3 transitions are indicated in blue, while isomeric half-lives are shown in red. Arrow widths are proportional to transition intensities.

FIG. 3. (a) Experimental levels of odd-mass Tl isotopes with $N \ge 126$ (filled squares) compared to shell-model calculations (lines). States with leading single proton-hole configurations are shown in purple colors, while levels arising from proton-core couplings are marked in blue tones. (b) Same as (a) for the even-A Pb isotones. (c) Measured $B(E2; 17/2^+ \rightarrow 13/2^+)$ values for Tl (filled squares) compared to shell-model calculations. For ²¹³Tl ($N = 132$), the range of $B(E2)$ strengths for a transition of 20–80 keV is drawn. For ²¹⁵Tl ($N = 134$), the arrow indicates the lower limit obtained from the isomeric lifetime measured in this Letter. Experimental $B(E2; 8^+ \rightarrow 6^+)$ strengths for the Pb isotones (empty squares) are also shown. (d) Same as (c) for $B(E3; 11/2^- \rightarrow 5/2^+)$ strengths. In all panels, SM1 calculations are indicated in dashed lines, SM2 in solid lines, and SM3 in dotted lines. Experimental data for $207-211$ Tl and ²¹⁰–²¹⁶Pb are taken from Refs. [\[44,](#page-6-22)[45,](#page-6-24)[52,](#page-6-31)[53](#page-6-32),[55](#page-6-34)].

SM1) using the code KSHELL [[46](#page-6-25)]. The valence space consists of the proton orbitals $0g_{7/2}$, $1d_{5/2}$, $1d_{3/2}$, $2s_{1/2}$, $0h_{11/2}$ below $Z = 82$ and the neutron orbitals $0i_{11/2}$, $1g_{9/2}$, $1g_{7/2}$, $2d_{5/2}$, $2d_{3/2}$, $3s_{1/2}$, $0j_{15/2}$ above $N = 126$. The twobody matrix elements are based on the Kuo-Herling [\[47,](#page-6-26)[48\]](#page-6-27) and $VMU + LS$ [[49](#page-6-28)[,50\]](#page-6-29) interactions as described in Refs. [[31](#page-6-10)[,51\]](#page-6-30). The single neutron and proton hole energies are taken from the experimental spectra of ²⁰⁹Pb and ²⁰⁷Tl, respectively. The transition probabilities are calculated using empirical effective charges of $e_v = 0.8$ for neutrons and $e_{\pi} = 1.8$ for protons [[31](#page-6-10)]. For the most exotic ²¹⁵Tl, we allow at most two neutrons exciting from the $\nu 1g_{9/2}$, $\nu 0i_{11/2}$, and $\nu 0j_{15/2}$ orbitals to the $\nu 1g_{7/2}$, $\nu 2d_{5/2}$, ν 2d_{3/2}, and ν 3s_{1/2} ones. No excitations across the ²⁰⁸Pb core are considered.

The experimental excitation spectra of the two nuclei are proposed based on the spectroscopic information of Fig. [1](#page-2-0), γ-ray intensity balance, and comparison with SM1 calculations. They reveal alike structures, with a $(17/2^+)$ isomeric state decaying through the $(13/2^+) \rightarrow (11/2^-) \rightarrow$ $(5/2^+) \rightarrow (3/2^+) \rightarrow (1/2^+)$ cascade. In the lighter ²⁰⁹Tl, the analogous $(17/2^+)$ long-lived level was previously attributed to the coupling of a $\pi s_{1/2}$ proton hole with the seniority $v = 2$, (8^+) isomer in ²¹⁰Pb [[52](#page-6-31),[53](#page-6-32)]. Similarly, the leading component of the $(17/2^+)$ states in ²¹³Tl and ²¹⁵Tl corresponds to the $\pi s_{1/2}^{-1} \otimes \nu(g_{9/2})_{8^+}^n$ configuration. The isomeric nature of the newly observed states, hence, provides experimental evidence of good preservation of seniority in proton-hole-core coupled states well beyond ²⁰⁸Pb.

Looking at Fig. [2](#page-2-1), the $(17/2^+)$ levels decay via lowenergy E2 transitions to the $(13/2^+)$ states, with predominant configuration $\pi s_{1/2}^{-1} \otimes \nu(g_{9/2})_{6^+}^n$. The absence of K α x rays in Figs. 1(c)–[1\(d\)](#page-2-0) indicates that the energies of the $17/2^+ \rightarrow 13/2^+$ transitions in ²¹³Tl and ²¹⁵Tl are more likely below the binding energy of the Tl K electron, 85.5 keV. In ²⁰⁹Tl, the $(13/2^+)$ state decays to the $(9/2^+)$ level, with main $\pi s_{1/2}^{-1} \otimes \nu(g_{9/2})_{4^+}^2$ configuration, by a stretched $E2$ transition [\[52](#page-6-31)[,53\]](#page-6-32). For the more exotic ²¹³Tl and ²¹⁵Tl, the $(13/2⁺)$ state no longer follows the seniority sequence but populates the $J^{\pi} = (11/2^{-})$ level, mainly described by an unpaired proton hole in the $\pi h_{11/2}$ orbital, via an E1 decay. The $(11/2⁻)$ state, which becomes isomeric, populates the yrast $(5/2^+)$ level arising from the $\pi s_{1/2}^{-1} \otimes \nu(g_{9/2})_{2^+}^n$ coupling. The calculated conversion coefficients [\[54\]](#page-6-33) of the corresponding E3 transitions at 243.4(15) keV in ²¹³Tl [$\alpha_{th} = 1.48(2)$] and 135(5) keV in ²¹⁵Tl [$\alpha_{th} = 28(7)$] explain the pronounced Meitner-Ellis peaks in Figs. [1\(a\)](#page-2-0) and [1\(b\).](#page-2-0) The decay finally feeds the $J^{\pi} = (3/2^+)$ level, mainly described by a proton $\pi d_{3/2}^{-1}$ hole excitation, and the $J^{\pi} = (1/2^+)$ ground state, with leading configuration $\pi s_{1/2}^{-1}$.

The excited states of odd-A Tl nuclei with two to eight neutrons above $N = 126$, reported in this Letter and previous works [\[53,](#page-6-32)[55\]](#page-6-34), are shown by colored solid squares in Fig. [3\(a\)](#page-3-0). The unexpected fall of the $(11/2⁻)$ state from 1369 keV in ²⁰⁹Tl to 985 keV in ²¹³Tl and 874 keV in ²¹⁵Tl provides the first stringent proof of shell evolution in the $Z < 82$, $N > 126$ quadrant beyond ²⁰⁸Pb. The SM1 calculations, shown as a dashed magenta line, predict comparable excitation energies along the $\nu 1g_{9/2}$ orbital, failing to reproduce the lowering of the π 0 $h_{11/2}$ proton-hole state in exotic Tl isotopes at increasing N.

To argue the crucial role of the monopole interaction in reproducing the downward trend of the $J^{\pi} = (11/2^{-})$ states, we first consider a constant shift of 300 keV in the $\pi 0h_{11/2}$ orbital SPE used in calculation SM1. The resulting $11/2^-$ energy in ²¹³Tl agrees with experiment, but the calculation fails for $207,209$ Tl, predicting energies ∼300 keV lower. Yet one should note the ESPE is given by the addition of SPE and $n \cdot V_m$, where *n* is the particle occupancy and V_m is the monopole interaction. While the

TABLE I. Experimental excitation energies (in keV) of the $11/2₁⁻$ states in odd-mass Tl isotopes compared to the shellmodel calculations SM1 [[31](#page-6-10)] and SM2, which use reduced $(\nu 1g_{9/2}, \pi 0h_{11/2})$ matrix elements. New experimental information is indicated in bold. Previous data are taken from Refs. [\[55,](#page-6-34)[56](#page-6-41)].

Nucleus	207 T1	209 Tl	211T1	213T1	215T1
$E_{11/2}^{exp}$	1348.18(16)	1369(10)	\cdots	985.3(19)	874(5)
$E_{11/2}^{SM1}$	1349	1331	1306	1273	1251
$E_{11/2}^{SM2}$	1349	1230	1103	961	802

spherical doubly magic SPE is constant, the ESPE changes as a function of *n* owing to V_m . In the Tl isotopes, the reduction of $J^{\pi} = (11/2^-)$ excitation energies occurs as neutrons are added to the $\nu 1g_{9/2}$ orbital. Hence, a weakening of the proton-neutron monopole interaction between the π 0 $h_{11/2}$ and ν 1 $g_{9/2}$ orbitals is more likely driving the observed lowering. To test the aforesaid hypothesis, we reduce the corresponding monopole matrix elements in SM1 by 60%. This quantity is chosen to reproduce the energy of the $J^{\pi} = (11/2^-)$ level in ²¹³Tl. We apply the truncation used in SM1 for 215 Tl to calculate excitation energies and electromagnetic properties in all Tl nuclei. The theoretical results using the modified effective Hamiltonian and truncated model space are labeled as SM2 in Table [I](#page-4-0) and shown in solid lines in Fig. [3.](#page-3-0) The new SM2 calculations do not only reproduce well the energy decrease of the $(11/2^-)$ levels, but the whole low energy spectra of $^{209-215}$ Tl and $^{210-216}$ Pb, as evinced in Figs. [3\(a\)](#page-3-0) and [3\(b\).](#page-3-0) Further, the lowering of the $(11/2⁻)$ states by the monopole effect can be interpreted in the Nilsson meanfield model by a small increase in deformation which drives an approach of the $\pi 2s_{1/2}$ [400] and $\pi 0h_{11/2}$ [505] orbitals.

Because of the particle-core mechanism [\[57,](#page-6-35)[58\]](#page-6-36), the energies of the $(5/2^+)$ and $(13/2^+)$ states in odd-A Tl nuclei are similar to those of the seniority (2^+) and (6^+) levels in the ^{A+1}Pb isotones, see Figs. [3\(a\)](#page-3-0) and [3\(b\).](#page-3-0) The same situation is expected for the $B(E2, 17/2^+ \rightarrow 13/2^+)$ values, which should presumably follow the parabolic seniority behavior reported for the $(8^+) \rightarrow (6^+)$ transitions in Pb [[44](#page-6-22)]. Figure [3\(c\)](#page-3-0) shows by filled squares the experimental $B(E2)$ strengths for Tl nuclei, where the reported $t_{1/2}=0.58(8)$ -μs γ ray at 144 keV in ²¹¹Tl [[45](#page-6-24)] is considered to deexcite the $(17/2⁺)$ isomer. The analogous $B(E2)$ values in the ^{A+1}Pb cores are also indicated by empty squares. The Tl nuclei show a breaking of symmetry around the middle of the $\nu 1g_{9/2}$ orbital, a behavior predicted for both Tl and Pb isotopes by SM2 (solid lines). This is in line with previous calculations using the Kuo-Herling and other realistic two-body interactions [[44](#page-6-22)]. The dissimilarity between the experimental transition strengths of ²¹¹Tl and ²¹²Pb ($N = 130$) is also significant, of about 1

order of magnitude. With our new data, we can further test the underlying residual interaction to understand the observed distortion from seniority in the Tl isotopes. To this aim, we have performed more realistic shell-model calculations in a larger model space (henceforth called SM3), including the five proton orbits below $Z = 82$ and the π 0 $h_{9/2}$, π 1 $f_{7/2}$, and π 0 $i_{13/2}$ orbitals above, and the $\nu 1g_{9/2}$, $\nu 0i_{11/2}$, and $\nu 0j_{15/2}$ orbitals above $N = 126$. The calculations include one proton excitation across the $Z =$ 82 shell gap, allowing for the $\Delta j = 2$ proton-core excitation $\pi s_{1/2}^{-1}(h_{11/2}^{-1}f_{7/2}) \otimes (\nu g_{9/2}^{n})$ in the Tl isotopes. This results in a general enhancement of the quadrupole collectivity, evinced by the dotted lines in Fig. [3\(c\).](#page-3-0) With SM3, the agreement between measured and calculated $B(E2)$ strengths improves significantly for the Tl isotopes. However, the experimental trend followed by the Pb nuclei is not reproduced, supporting the importance of neutron excitations across the $N = 126$ shell gap in $Z = 82$ nuclei [\[44\]](#page-6-22).

The $B(E3; 11/2^- \rightarrow 5/2^+)$ strengths derived in the present work for 213 Tl and 215 Tl are shown by filled squares in Fig. [3\(d\).](#page-3-0) Comparison with calculations SM2 (solid line) and SM3 (dashed line) reveals discrepancies of about 1 order of magnitude between experiment and theory. According to SM2, the E3 transitions are mediated by admixtures of $\pi d_{5/2}^{-1}$ with the dominant $\pi s_{1/2}^{-1} \otimes 2^+$ configuration in the $J^{\pi} = 5/2_1^+$ states, resulting in sizable single-particle $\pi h_{11/2} \rightarrow \pi d_{5/2}$ E3 strength. These admixtures, which amount to 5% in ²¹³Tl and 8% in ²¹⁵Tl, explain the increasing trend of the calculated $B(E3)$, but not the excess of the experimental values. The missing strength might come from admixtures of the $\pi h_{11/2}^{-1}$ excitation with the $\pi d_{5/2}^{-1} \otimes 3^-$ octupole coupling in the $11/2^-_1$ states. The 3[−] collective octupole phonon in ²⁰⁸Pb [[59](#page-6-37)] has been previously found to enhance the E3 rates between singleparticle-like levels in neighboring nuclei [[60](#page-6-38)–[62\]](#page-6-39). The $B(E3)$ values reported here, in between the shell-model estimates and $B(E3) = 33.8(6)$ W.u. for the 3⁻ phonon [\[63\]](#page-6-40), support this assumption.

The SM3 calculations, which allow for one proton-core excitation to the π 0 $h_{9/2}$, π 1 $f_{7/2}$, and π 0 $i_{13/2}$ orbitals above $Z = 82$, predict slightly enhanced $B(E3)$ strengths than SM2. Though far from supplying a full treatment of the particle-octupole coupling effect in a shell-model framework, SM3 provides indications of what can be expected in a thorough computation of excitations across the shell gaps. Together with the $B(E2)$ results discussed before, our Letter evinces the importance of breaking the ²⁰⁸Pb core to understand the electromagnetic properties of $Z < 82$, $N > 126$ nuclei.

In summary, first spectroscopy of the rarest $N > 126$ Tl nuclei has been performed at RIKEN in a pioneering experiment. Excited isomeric structures with $J^{\pi} =$ $(17/2^+)$ and $(11/2^-)$ were populated in ²¹³Tl and ²¹⁵Tl, providing spectral information not accessible in any other nuclear facility. The development of spin isomerism in the single proton-hole $\pi 0h_{11/2}$ states has been observed for the first time and attributed to a significant reduction of the monopole $(\nu 1g_{9/2}, \pi 0h_{11/2})$ matrix elements, strongly supporting the crucial role of the monopole interaction [\[64\]](#page-6-42) in shifting the $\pi 0h_{11/2}$ ESPE below ²⁰⁸Pb. The observed phenomenon resembles the reduction of the proton $\pi 0f_{7/2} - \pi 0f_{5/2}$ spin-orbit splitting by effect of the strong monopole interaction near 78 78 78 Ni [8], which is boosted by the filling of the first $\nu \theta g_{9/2}$ neutron shell [[11,](#page-5-7)[65](#page-6-43),[66](#page-6-44)]. In parallel, the conservation of seniority has been proven through the excitation energy and $B(E2)$ of the $(17/2^+)$ isomers, which are interpreted as the coupling of a $\pi s_{1/2}$ proton hole to the (8^+) seniority isomers in the ^{A+1}Pb isotones. Such a study becomes unique in that no other isotopic chain provides a testing ground to investigate the impact of the particle-core mechanism [\[57\]](#page-6-35) on the $B(E2)$ seniority cancellation rule across a complete *j* orbital. The new results represent a first step to understanding how the high-*j* orbitals evolve away from doubly magic ^{208}Pb , of special importance to model the β decay towards the actinides in the r process and pave the way to search for astromers beyond $N = 126$, which can potentially influence the final abundance distribution of the heaviest elements.

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