

Coherent Spin-Phonon Scattering in Facilitated Rydberg Lattices

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We investigate the dynamics of a one-dimensional spin system with facilitation constraint that can be studied using Rydberg atoms in arrays of optical tweezer traps. The elementary degrees of freedom of the system are domains of Rydberg excitations that expand ballistically through the lattice. Because of mechanical forces, Rydberg excited atoms are coupled to vibrations within their traps. At zero temperature and large trap depth, it is known that virtually excited lattice vibrations only renormalize the timescale of the ballistic propagation. However, when vibrational excitations are initially present—i.e., when the external motion of the atoms is prepared in an excited Fock state, coherent state or thermal state—resonant scattering between spin domain walls and phonons takes place. This coherent and deterministic process, which is free from disorder, leads to a reduction of the power-law exponent characterizing the expansion of spin domains. Furthermore, the spin domain dynamics is sensitive to the coherence properties of the atoms' vibrational state, such as the relative phase of coherently superimposed Fock states. Even for a translationally invariant initial state the latter manifests macroscopically in a phase-sensitive asymmetric expansion.

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Introduction.—One of the central topics in quantum many-body physics relates to the study of transport properties of excitations, correlations, or energy, which allows us to categorize models into different classes [1,2]. For example, chaotic systems generically feature diffusive transport [3–7], while disorder may induce subdiffusive dynamics or even localization [8–11]. On the contrary, ballistic transport and diffusive dynamics are typically featured in free and interacting integrable systems [12–20], since they are characterized by an extensive number of local conserved charges [21]. An intermediate behavior between diffusive and ballistic dynamics has been observed, also experimentally [22–26], in a class of integrable models with certain additional symmetries [27–32], which appear to lie in the Kardar-Parisi-Zhang universality class [33].

Recently, transport properties have also been studied in quantum systems subject to kinetic constraints [34–40]. These are generally characterized by slow dynamics and reduced transport due to the scarce connectivity between different many-body states [41–44]. Physical manifestations of such models can be efficiently implemented in Rydberg quantum simulators, in which trapped atoms, excited to high-lying electronic states, feature strong state-dependent dipolar interactions [45–48]. Thanks to their versatility, these experimental platforms have led to several breakthroughs in the fields of quantum simulation and quantum computation [49–57]. Concomitant to the

strong electrostatic interactions are mechanical forces, that couple the internal atomic degrees of freedom to the external motional ones [58,59]. On the one hand, these forces can—when uncontrolled—be sources of undesired incoherent effects, such as dissipation and heating [60–62]. On the other hand, coherent spin-phonon couplings allow us to engineer long-range multibody interactions [63], to implement cooling protocols [64], to explore polaron physics [65–69], and to realize artificial molecular systems [70,71]. The impact of coherent lattice vibrations on the nonequilibrium dynamics of kinetically constrained quantum systems is currently unexplored. However, with the recent advancements in the domain of Rydberg quantum simulation platforms, such studies will be soon within reach [72].

In this work we explore the dynamics of elementary degrees of freedom (spin domains) in a chain of Rydberg atoms subject to the facilitation (anti-blockade) constraint. We show that the interaction with lattice vibrations manifests in an alteration of the power-law exponent characterizing the expansion of spin domains. At zero temperature, the exponent does not depend on the spin-phonon coupling strength, provided that it is sufficiently weak, as scattering is off resonant. However, when vibrational excitations are initially present, resonant scattering between phonons and spin domains leads to a quantitative decrease of the exponent. Coherent spin-phonon interactions thus may

inhibit excitation transport, thereby providing a connection to disorder-free settings that display localization phenomena [73,74]. Finally, we show that the spin domain expansion dynamics is sensitive to the phase of the vibrational states, which causes an asymmetric expansion even in a translationally invariant system [75,76].

Model.—We consider a one-dimensional chain of N atoms, each one loaded in an optical tweezer trap and whose electronic structure is modeled as a two-level system [see Fig. 1(a)]. The state $|\downarrow\rangle$ denotes the ground state, while $|\uparrow\rangle$ represents the Rydberg (excited) state. The traps, which are separated by a nearest neighbor distance a_0 , have a trap frequency ω . The atoms are driven by a laser with Rabi frequency Ω and detuning Δ , which couples the ground state to the Rydberg state. Two atoms in the Rydberg state, placed at sites j and k , interact via a distance dependent potential of the form $V(\mathbf{r}_j, \mathbf{r}_k) = C_\gamma |\mathbf{r}_j - \mathbf{r}_k|^{-\gamma}$. Here γ is the characteristic power law exponent (dipole-dipole interaction: $\gamma = 3$, van der Waals interaction: $\gamma = 6$). The Hamiltonian of the system is then given by ($\hbar = 1$)

$$H = \sum_{j=1}^N \left(\Omega \sigma_j^x + \Delta n_j + \sum_{k < j} V(\mathbf{r}_j, \mathbf{r}_k) n_j n_k + \omega a_j^\dagger a_j \right),$$

where $\sigma^x = |\uparrow\rangle\langle\downarrow| + |\downarrow\rangle\langle\uparrow|$ is the spin flip operator and $n = |\uparrow\rangle\langle\uparrow|$ projects onto the Rydberg state. Writing the position fluctuations in the traps in terms of the bosonic operators as $\delta x_j = (a_j^\dagger + a_j)/\sqrt{2m\omega}$ and neglecting the interactions beyond the nearest-neighbor ones (assumed to be small compared to Ω , see Supplemental Material [77]), yields the simplified Hamiltonian [67,68]

$$H = \sum_{j=1}^N \left\{ \Omega \sigma_j^x + \Delta n_j + \omega a_j^\dagger a_j + \left[V_{\text{NN}}^{(0)} - \kappa (a_j^\dagger + a_j - a_{j+1}^\dagger - a_{j+1}) \right] n_j n_{j+1} \right\}, \quad (1)$$

where periodic boundary conditions are adopted. Here $V_{\text{NN}}^{(0)}$ is the interaction between two excited nearest-neighbor atoms when they are located at the center of the respective traps and $\kappa = \gamma C_\gamma / (a_0^{\gamma+1} \sqrt{2m\omega})$ is the spin-phonon coupling constant, which is proportional to the gradient of the interaction potential evaluated at the lattice spacing a_0 [see Fig. 1(a)]. Such spin-phonon coupling accounts for the mechanical forces arising from the interaction between neighboring Rydberg excitations. These forces displace the atoms from the center of the respective traps only when they are in the Rydberg state, thereby coupling the internal (spin) degrees of freedom to the external (motional) ones.

Facilitated dynamics.—We consider the situation in which the dynamics of the Rydberg chain is subject to the facilitation (antiblockade) constraint [84–90]. This is obtained when the otherwise detuned laser is put on resonance by the single-atom energy shift induced by

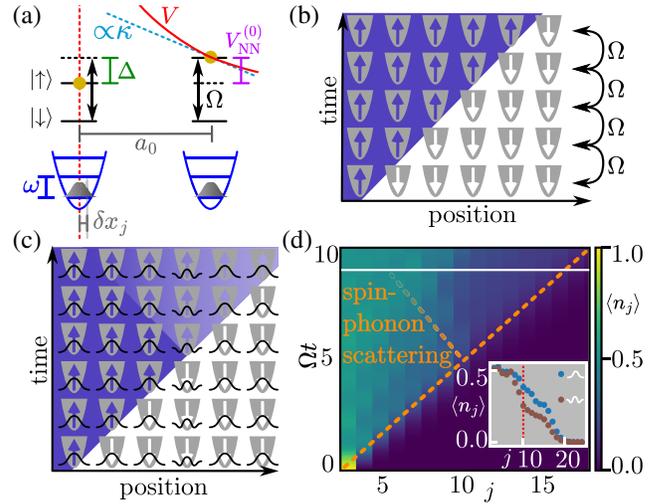


FIG. 1. Spin-phonon scattering in a Rydberg chain. (a) Atoms are treated as (fictitious) spins where the spin-down state is the ground state and the spin-up state is the Rydberg state. A laser with Rabi frequency Ω and detuning Δ excites the atoms to the Rydberg state under the facilitation condition $\Delta + V_{\text{NN}}^{(0)} = 0$, i.e., the detuning is chosen such that it cancels the nearest neighbor interaction $V_{\text{NN}}^{(0)}$. Atoms are trapped in a state-independent harmonic potential with frequency ω and δx_j is the deviation of the j th atom from the center of the respective trap. Spin and motional degrees of freedom are coupled, with spin-phonon coupling constant κ which is proportional to the gradient of the potential V evaluated at the lattice spacing a_0 . (b) Ballistic expansion of a spin domain (blue) in the absence of spin-phonon coupling: an excited Rydberg atom facilitates the excitation of the neighboring one at a rate proportional to Ω . (c) Spin-phonon scattering: the vibrational state of each atom is prepared in the ground state (Gaussian profile), except for one atom which is initialized in a higher-lying Fock state. When the domain wall reaches this site, it scatters off the phonon excitation. (d) Numerical simulation of the spin-phonon scattering, where the atom at site $j = 10$ is initialized in the Fock state $|2\rangle$ and all others in Fock state $|0\rangle$. Scattering (backreflection) of the domain wall reduces the Rydberg density $\langle n_j \rangle$ beyond $j = 10$ (orange dashed line). This is clearly seen in the inset which shows the Rydberg density $\langle n_j \rangle$ at time $\Omega t = 9$ (white line in main plot) with the phonon excitation at site $j = 10$ in Fock state $|2\rangle$ (brown points) and without it (blue points).

the Rydberg interaction, i.e., $\Delta + V_{\text{NN}}^{(0)} = 0$. Under this condition, ground state atoms that are next to an already excited atom get resonantly coupled to the Rydberg state. The further assumption that both the next-nearest-neighbor interaction and the Rabi frequency are much smaller than the detuning, $V(\mathbf{r}_j^0, \mathbf{r}_{j+2}^0) \ll |\Delta|$ and $\Omega \ll |\Delta|$, leads to a constrained dynamics that conserves the number of domain walls delimiting domains of consecutive Rydberg excitations. This drastically reduces the connectivity between the many-body states, and the Hilbert space is decomposed into disconnected sectors, labeled by the number of domain walls [91].

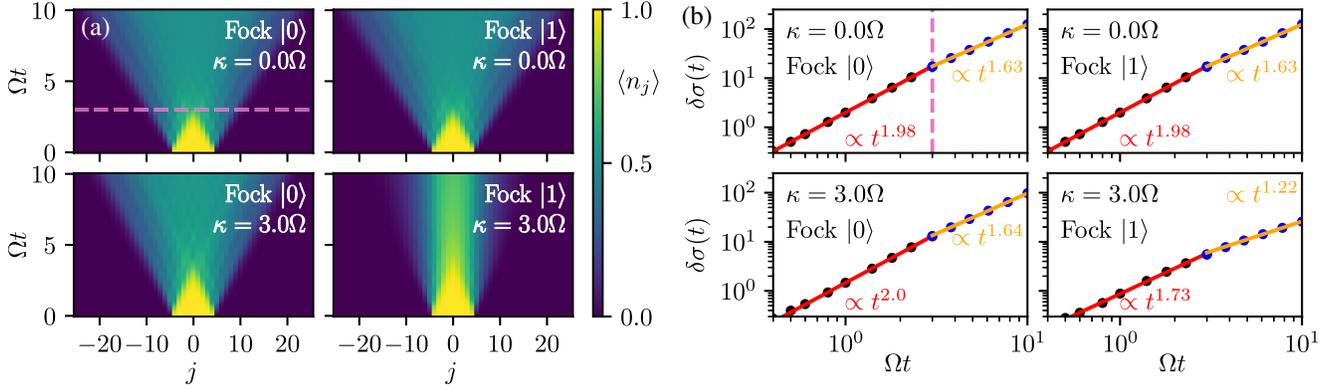


FIG. 2. Expansion of spin domain in the absence and presence of phonons. (a) Rydberg density $\langle n_j \rangle$ for a spin domain initialized with $r_0 = 9$ Rydberg excitations and centered at $j = 0$. In the absence of spin-phonon coupling ($\kappa = 0$), the domain expands approximately ballistically, independently on whether the atoms are initially prepared in their vibrational ground state, $|0\rangle$ (left column), or first Fock state $|1\rangle$ (right column). When the spin-phonon coupling is switched on (we consider $\kappa = 3.0\Omega$), ballistic expansion persists in the left column, while a drastic change is visible on the right. The reason is that when atoms are prepared in their vibrational ground state only virtual transitions to higher-lying phonon states take place, which merely renormalizes the ballistic propagation speed. In the presence of initial phonon excitations, however, coherent spin-phonon scattering takes place, which alters the expansion dynamics dramatically. (b) The corresponding Rydberg density variance difference $\delta\sigma(t)$, Eq. (3). The power-law exponent changes at $\Omega t \approx 3$, where the initial spin domain has dissolved [see violet dashed line in the top left panel]. A clear change of exponent is observed in the bottom right panel ($\kappa = 3.0\Omega$, initial vibrational state of all atoms $|1\rangle$). Data are obtained via TEBD simulations of the dynamics under Hamiltonian (1) for $\omega = 8\Omega$, $\Delta = 500\Omega$. The maximum number of phonons per site is truncated to 7.

Here, we focus on the single domain sector, i.e., the sector with two domain walls, and initially prepare a spin domain with r_0 consecutive Rydberg excitations. To evaluate its dynamics, we perform numerical simulations of Hamiltonian (1) utilizing the time-evolving block decimation algorithm (TEBD) [78,92–97]. In the absence of spin-phonon coupling, i.e., $\kappa = 0$, the two domain walls propagate freely along the lattice as free fermions [98]. This results in a ballistic expansion of the spin domain whose size increases linearly in time, as sketched in Fig. 1(b). To quantitatively assess this expansion, we evaluate the dynamics of the Rydberg density variance σ , defined as

$$\sigma(t) = \sum_{j=1}^N j^2 \frac{\langle n_j(t) \rangle}{\mathcal{N}(t)} - \left(\sum_{j=1}^N j \frac{\langle n_j(t) \rangle}{\mathcal{N}(t)} \right)^2, \quad (2)$$

where $\langle \dots \rangle$ denotes the quantum expectation value and $\mathcal{N}(t) = \sum_{k=1}^N \langle n_k(t) \rangle$ is the total Rydberg density. The density variance (2), which can be measured experimentally [99], quantifies the spreading dynamics of the spin domain. It is connected to the mean square displacement used in Refs. [100–102] and to the width of the density propagator studied in Ref. [103] for a disordered fermionic model. The density variance is expected to increase over time as

$$\delta\sigma(t) = \sigma(t) - \sigma(0) \sim t^\beta, \quad (3)$$

where $\sigma(0) = (r_0^2 - 1)/12$ is the density variance of the spin domain at $t = 0$. When $\kappa = 0$, i.e., in the absence of

spin-phonon coupling, we expect $\beta = 2$ (free fermions). This is indeed the case, as shown in the first two panels of Figs. 2(a) and 2(b) where we plot the time evolution of the Rydberg density and $\delta\sigma(t)$, respectively. We note a crossover time that separates two regions characterized by two different exponents. The short-time behavior provides $\beta \approx 1.98$ reproducing our expectation, while for larger times the exponent decreases to $\beta \approx 1.63$. This behavior is a consequence of the conservation of the number of domain walls: throughout the facilitation dynamics, the domain walls cannot coalesce and therefore are subject to a hard-core repulsive potential [88]. This translates into the interruption of the ballistic expansion when the two domain walls are about to collide, which happens at $\Omega t \approx 3$. Note that this effect is exclusively due to the finite size of the initial spin domain [77].

In the presence of spin-phonon coupling, $\kappa \neq 0$, we find that the expansion of the spin domain strongly depends on the initial state of the phonons. In particular, when the atoms are initially prepared in their vibrational ground state $\otimes_{j=1}^N |0\rangle$, the initial ballistic expansion is maintained and the effect of the spin-phonon coupling is limited to a renormalization of the expansion velocity [67,68]. On the contrary, when the atoms are initially prepared in the first Fock state $\otimes_{j=1}^N |1\rangle$, the expansion of the domain changes dramatically and the exponent of the Rydberg density variance drops to $\beta \approx 1.73$ and $\beta \approx 1.22$ before and after the crossover time (see Fig. 2).

Effective model for the spin-phonon scattering.—The reason for the alteration of excitation transport in the

presence of initial phonon excitations is resonant spin-phonon scattering [see Figs. 1(c)–1(d)], for which we will construct an effective model. Since the facilitation dynamics conserves the number of domain walls, the single spin domain can expand or shrink, but it is not allowed to split into two domains or disappear. The state of such a spin domain can therefore be characterized with only two coordinates, namely, its center-of-mass (c.m.) position and its relative coordinate (or the number of excitations it contains). The introduction of these two coordinates is particularly advantageous because it allows us to reduce the complex many-body dynamics to a simpler two-body dynamics. As outlined in the Supplemental Material [77], we formulate Hamiltonian (1) in terms of these two coordinates. By further decomposing the c.m. coordinate and the boson operator a_j into Fourier modes, respectively labeled by q and A_p , and after applying various unitary transformations, one gets the Hamiltonian $H = \sum_{q=1}^N |q\rangle \langle q| \otimes H_q$, with

$$H_q = 2J_q(\{N_p\}) \sum_{k=1}^{N-1} \cos\left(\frac{k\pi}{N}\right) |k\rangle \langle k| + \omega \sum_p N_p + \kappa \sum_{k,k',p} f_{k,k',p} |k\rangle \langle k'| \otimes (A_p + A_p^\dagger), \quad (4)$$

where $J_q(\{N_p\}) = 2\Omega \cos[(\pi/N)(q + \sum_p pN_p)]$ and $N_p = A_p^\dagger A_p$. The first term provides a set of quasiparticle excitations labeled by their quasimomentum k , whose dispersion relation is connected to the expansion speed of the spin domain. Their interaction with the phonons is encoded in the third term, where $f_{k,k',p}$ are the spin-phonon coupling matrix elements that are derived in the Supplemental Material [77]. This spin-phonon coupling term is responsible for the change in the expansion of the spin domain shown in Fig. 2. For $\kappa = 0$ the free dynamics of the quasiparticles results in the visible light cone emanating from the boundaries of the initial domain. In contrast, even for moderate values of κ/ω , the presence of phonon excitations in the initial state drastically changes the dynamics of the domain. In order to analytically explore this regime, we note that the spin-phonon coupling term is the only one that does not conserve the total number of phonon excitations $N_{\text{phon}} = \sum_p \langle N_p \rangle$. Therefore, when $|\kappa| \ll \omega$, the subspaces with different N_{phon} are only weakly coupled, making N_{phon} an approximately good quantum number. In this regime, we can derive an effective Hamiltonian that describes the facilitation dynamics in a given phonon subspace. This is formally accomplished by applying a Schrieffer-Wolff transformation [104] to Hamiltonian (4) so that we obtain an effective Hamiltonian, $H_{\text{eff}}^{(q)}$, valid in each of the phonon subspaces, given by [77]

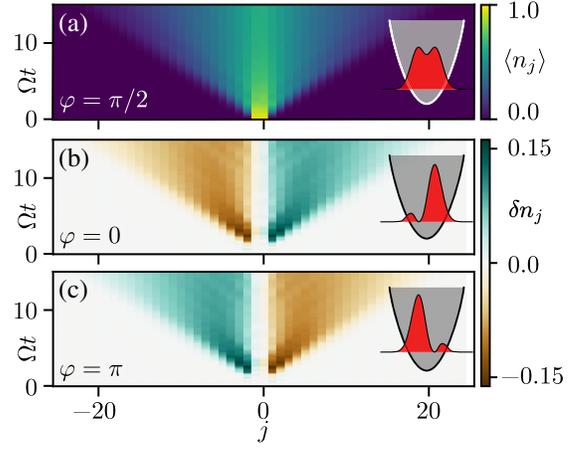


FIG. 3. Phase sensitivity of spin-phonon scattering. (a) Expansion of the spin domain from the initial state with $r_0 = 2$ Rydberg excitations. All the atoms are initially prepared in the vibrational state $|\varphi = \pi/2\rangle$, giving rise to the position distribution in the trap shown in the right. The value of the Rydberg density $\langle n_j \rangle$ remains symmetric around the c.m. of the spin domain at all times. (b), (c) Asymmetric domain expansion when the vibrational state of the atoms is initially prepared in $|\varphi = 0\rangle$ and $|\varphi = \pi\rangle$, respectively. The asymmetry, quantified by $\delta n_j = \langle n_j \rangle - \langle n_{-j-1} \rangle$, is due to the fact that the initial state is not symmetric under the operation $k \rightarrow N - k$ and $a_k \rightarrow -a_{N-k}$, which is, instead, a symmetry of the Hamiltonian. The simulations are carried out with $\omega = 8$, $\Delta = 200$, $\kappa = 4 \Omega$ and the maximum number of phonons per site is truncated to 3.

$$H_{\text{eff}}^{(q)} = 2J_q(\{N_p\}) \sum_{k=1}^{N-1} \cos\left(\frac{k\pi}{N}\right) |k\rangle \langle k| + \omega \sum_p N_p - \kappa^2 \sum_{k,k'} F_{k,k'}(\{A_p\}) |k\rangle \langle k'| + \mathcal{O}(\kappa^3). \quad (5)$$

This equation shows that the phonons mediate an effective interaction between quasiparticles, with matrix elements $F_{k,k'}(\{A_p\})$. These contain terms like $A_m^\dagger A_n$, which have nonzero matrix elements only if $N_{\text{phon}} > 0$ [77]. Therefore, when phonon excitations are already present in the initial state, these terms mediate additional interactions between quasiparticles that would not be present if the atoms were initialized in their vibrational ground state [68]. This is consistent with the numerical results, shown in the bottom panels of Fig. 2, that attribute the inhibition of the ballistic spin domain expansion to the presence of vibrational excitations in the initial state.

Phase sensitivity of spin-phonon scattering.—In the following we show that the coherence of spin-phonon scattering can be observed macroscopically. To this end we consider the situation in which the vibrational state of all the atoms is initially prepared in a coherent superposition of Fock states $|0\rangle$ and $|1\rangle$, as $|\varphi\rangle = 1/\sqrt{2}(|0\rangle + e^{i\varphi}|1\rangle)$, which is specified by the phase $\varphi \in [0, 2\pi)$. Despite being initialized in a translationally invariant state, the spin

domain expands generically in an asymmetric fashion around its initial position. This is seen in Fig. 3. The asymmetry is controlled by the phase: for $\varphi = \pi/2$ the spin domain expands symmetrically, for $\varphi = 0$ ($\varphi = \pi$) the two domain walls propagate differently, with the right (left) front showing a larger Rydberg density. The emergence of this asymmetric expansion is a consequence of the fact that the initial state is not invariant under the operation $k \rightarrow N - k$ and $a_k \rightarrow -a_{N-k}$, which is, however, a symmetry of the Hamiltonian.

Summary and outlook.—We investigated the role of spin-phonon interaction on the nonequilibrium dynamics of Rydberg excitations in a chain of trapped atoms subject to the antiblockade constraint. While aspects of our study are certainly idealized compared to the experimental state-of-the-art, e.g., we assume state-independent trapping, we could identify coherent spin-phonon scattering as a mechanism that qualitatively alters the propagation of elementary excitations. In the future, it would be interesting to consider the impact of these processes in a many-body setting, by lifting the restriction to the single spin domain sector. Here one could ask whether the resulting complex spin-boson system supports the formation of localized many-body states in a disorder-free setting. Exploring this regime, which due to the huge Hilbert space size is challenging to treat on classical computers, could be an interesting use case for the next generation of quantum simulators.

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- [1] B. Bertini, F. Heidrich-Meisner, C. Karrasch, T. Prosen, R. Steinigeweg, and M. Žnidarič, Finite-temperature transport in one-dimensional quantum lattice models, *Rev. Mod. Phys.* **93**, 025003 (2021).
 - [2] C.-C. Chien, S. Peotta, and M. Di Ventra, Quantum transport in ultracold atoms, *Nat. Phys.* **11**, 998 (2015).
 - [3] C. Karrasch, J. E. Moore, and F. Heidrich-Meisner, Real-time and real-space spin and energy dynamics in one-dimensional spin- $\frac{1}{2}$ systems induced by local quantum

- quenches at finite temperatures, *Phys. Rev. B* **89**, 075139 (2014).
- [4] J. Lux, J. Müller, A. Mitra, and A. Rosch, Hydrodynamic long-time tails after a quantum quench, *Phys. Rev. A* **89**, 053608 (2014).
- [5] Y. Gu, X.-L. Qi, and D. Stanford, Local criticality, diffusion and chaos in generalized Sachdev-Ye-Kitaev models, *J. High Energy Phys.* **05** (2017) 125.
- [6] M. Blake, R. A. Davison, and S. Sachdev, Thermal diffusivity and chaos in metals without quasiparticles, *Phys. Rev. D* **96**, 106008 (2017).
- [7] A. J. Friedman, S. Gopalakrishnan, and R. Vasseur, Diffusive hydrodynamics from integrability breaking, *Phys. Rev. B* **101**, 180302(R) (2020).
- [8] D. Basko, I. Aleiner, and B. Altshuler, Metal-insulator transition in a weakly interacting many-electron system with localized single-particle states, *Ann. Phys. (N.Y.)* **321**, 1126 (2006).
- [9] Y. Bar Lev, G. Cohen, and D. R. Reichman, Absence of diffusion in an interacting system of spinless fermions on a one-dimensional disordered lattice, *Phys. Rev. Lett.* **114**, 100601 (2015).
- [10] J. Z. Imbrie, On many-body localization for quantum spin chains, *J. Stat. Phys.* **163**, 998 (2016).
- [11] M. Žnidarič, A. Scardicchio, and V. K. Varma, Diffusive and subdiffusive spin transport in the ergodic phase of a many-body localizable system, *Phys. Rev. Lett.* **117**, 040601 (2016).
- [12] J. Sirker, R. G. Pereira, and I. Affleck, Diffusion and ballistic transport in one-dimensional quantum systems, *Phys. Rev. Lett.* **103**, 216602 (2009).
- [13] M. Žnidarič, Spin transport in a one-dimensional anisotropic Heisenberg model, *Phys. Rev. Lett.* **106**, 220601 (2011).
- [14] E. Ilievski and J. De Nardis, Ballistic transport in the one-dimensional Hubbard model: The hydrodynamic approach, *Phys. Rev. B* **96**, 081118(R) (2017).
- [15] M. Medenjak, C. Karrasch, and T. c. v. Prosen, Lower bounding diffusion constant by the curvature of drude weight, *Phys. Rev. Lett.* **119**, 080602 (2017).
- [16] J. De Nardis, D. Bernard, and B. Doyon, Hydrodynamic diffusion in integrable systems, *Phys. Rev. Lett.* **121**, 160603 (2018).
- [17] S. Gopalakrishnan, D. A. Huse, V. Khemani, and R. Vasseur, Hydrodynamics of operator spreading and quasi-particle diffusion in interacting integrable systems, *Phys. Rev. B* **98**, 220303(R) (2018).
- [18] P. N. Jepsen, J. Amato-Grill, I. Dimitrova, W. W. Ho, E. Demler, and W. Ketterle, Spin transport in a tunable Heisenberg model realized with ultracold atoms, *Nature (London)* **588**, 403 (2020).
- [19] M. Dupont and J. E. Moore, Universal spin dynamics in infinite-temperature one-dimensional quantum magnets, *Phys. Rev. B* **101**, 121106(R) (2020).
- [20] A. Bastianello, A. D. Luca, and R. Vasseur, Hydrodynamics of weak integrability breaking, *J. Stat. Mech.* (2021) 114003.
- [21] D. A. Abanin, E. Altman, I. Bloch, and M. Serbyn, Colloquium: Many-body localization, thermalization, and entanglement, *Rev. Mod. Phys.* **91**, 021001 (2019).

- [22] S. Hild, T. Fukuhara, P. Schauß, J. Zeiher, M. Knap, E. Demler, I. Bloch, and C. Gross, Far-from-equilibrium spin transport in Heisenberg quantum magnets, *Phys. Rev. Lett.* **113**, 147205 (2014).
- [23] A. Scheie, N. E. Sherman, M. Dupont, S. E. Nagler, M. B. Stone, G. E. Granroth, J. E. Moore, and D. A. Tennant, Detection of Kardar–Parisi–Zhang hydrodynamics in a quantum Heisenberg spin-1/2 chain, *Nat. Phys.* **17**, 726 (2021).
- [24] D. Wei, A. Rubio-Abadal, B. Ye, F. Machado, J. Kemp, K. Srakaew, S. Hollerith, J. Rui, S. Gopalakrishnan, N. Y. Yao, I. Bloch, and J. Zeiher, Quantum gas microscopy of Kardar–Parisi–Zhang superdiffusion, *Science* **376**, 716 (2022).
- [25] M. K. Joshi, F. Kranzl, A. Schuckert, I. Lovas, C. Maier, R. Blatt, M. Knap, and C. F. Roos, Observing emergent hydrodynamics in a long-range quantum magnet, *Science* **376**, 720 (2022).
- [26] J. F. Wienand, S. Karch, A. Impertro, C. Schweizer, E. McCulloch, R. Vasseur, S. Gopalakrishnan, M. Aidelsburger, and I. Bloch, Emergence of fluctuating hydrodynamics in chaotic quantum systems, [arXiv:2306.11457](https://arxiv.org/abs/2306.11457).
- [27] M. Ljubotina, M. Žnidarič, and T. Prosen, Spin diffusion from an inhomogeneous quench in an integrable system, *Nat. Commun.* **8**, 16117 (2017).
- [28] E. Ilievski, J. De Nardis, M. Medenjak, and T. c. v. Prosen, Superdiffusion in one-dimensional quantum lattice models, *Phys. Rev. Lett.* **121**, 230602 (2018).
- [29] J. De Nardis, M. Medenjak, C. Karrasch, and E. Ilievski, Anomalous spin diffusion in one-dimensional antiferromagnets, *Phys. Rev. Lett.* **123**, 186601 (2019).
- [30] S. Gopalakrishnan and R. Vasseur, Kinetic theory of spin diffusion and superdiffusion in XXZ spin chains, *Phys. Rev. Lett.* **122**, 127202 (2019).
- [31] M. Ljubotina, M. Žnidarič, and T. c. v. Prosen, Kardar–Parisi–Zhang physics in the quantum Heisenberg magnet, *Phys. Rev. Lett.* **122**, 210602 (2019).
- [32] V. B. Bulchandani, Kardar–Parisi–Zhang universality from soft gauge modes, *Phys. Rev. B* **101**, 041411(R) (2020).
- [33] M. Kardar, G. Parisi, and Y.-C. Zhang, Dynamic scaling of growing interfaces, *Phys. Rev. Lett.* **56**, 889 (1986).
- [34] Z. Lan, M. van Horssen, S. Powell, and J. P. Garrahan, Quantum slow relaxation and metastability due to dynamical constraints, *Phys. Rev. Lett.* **121**, 040603 (2018).
- [35] N. Pancotti, G. Giudice, J. I. Cirac, J. P. Garrahan, and M. C. Bañuls, Quantum east model: Localization, non-thermal eigenstates, and slow dynamics, *Phys. Rev. X* **10**, 021051 (2020).
- [36] Z.-C. Yang, Distinction between transport and Rényi entropy growth in kinetically constrained models, *Phys. Rev. B* **106**, L220303 (2022).
- [37] J. Feldmeier, W. Witzczak-Krempa, and M. Knap, Emergent tracer dynamics in constrained quantum systems, *Phys. Rev. B* **106**, 094303 (2022).
- [38] M. Ljubotina, J.-Y. Desaulès, M. Serbyn, and Z. Papić, Superdiffusive energy transport in kinetically constrained models, *Phys. Rev. X* **13**, 011033 (2023).
- [39] C. Chen, Y. Chen, and X. Wang, Superdiffusive to ballistic transports in nonintegrable Rydberg chains, [arXiv:2304.05553](https://arxiv.org/abs/2304.05553).
- [40] C. Wang and Z.-C. Yang, Freezing transition in the particle-conserving East model, *Phys. Rev. B* **108**, 144308 (2023).
- [41] J. P. Garrahan, Aspects of non-equilibrium in classical and quantum systems: Slow relaxation and glasses, dynamical large deviations, quantum non-ergodicity, and open quantum dynamics, *Physica (Amsterdam)* **504A**, 130 (2018).
- [42] A. Gromov, A. Lucas, and R. M. Nandkishore, Fracton hydrodynamics, *Phys. Rev. Res.* **2**, 033124 (2020).
- [43] H. Singh, B. A. Ware, R. Vasseur, and A. J. Friedman, Subdiffusion and many-body quantum chaos with kinetic constraints, *Phys. Rev. Lett.* **127**, 230602 (2021).
- [44] J. Richter and A. Pal, Anomalous hydrodynamics in a class of scarred frustration-free Hamiltonians, *Phys. Rev. Res.* **4**, L012003 (2022).
- [45] M. Saffman, T. G. Walker, and K. Molmer, Quantum information with Rydberg atoms, *Rev. Mod. Phys.* **82**, 2313 (2010).
- [46] C. S. Adams, J. D. Pritchard, and J. P. Shaffer, Rydberg atom quantum technologies, *J. Phys. B* **53**, 012002 (2019).
- [47] A. Browaeys and T. Lahaye, Many-body physics with individually controlled Rydberg atoms, *Nat. Phys.* **16**, 132 (2020).
- [48] X. Wu, X. Liang, Y. Tian, F. Yang, C. Chen, Y.-C. Liu, M. K. Tey, and L. You, A concise review of Rydberg atom based quantum computation and quantum simulation, *Chin. Phys. B* **30**, 020305 (2021).
- [49] D. Jaksch, J. I. Cirac, P. Zoller, S. L. Rolston, R. Côté, and M. D. Lukin, Fast quantum gates for neutral atoms, *Phys. Rev. Lett.* **85**, 2208 (2000).
- [50] I. Bloch, J. Dalibard, and S. Nascimbène, Quantum simulations with ultracold quantum gases, *Nat. Phys.* **8**, 267 (2012).
- [51] Y. Wang, A. Kumar, T.-Y. Wu, and D. S. Weiss, Single-qubit gates based on targeted phase shifts in a 3D neutral atom array, *Science* **352**, 1562 (2016).
- [52] R. Han, H. K. Ng, and B.-G. Englert, Implementing a neutral-atom controlled-phase gate with a single Rydberg pulse, *Europhys. Lett.* **113**, 40001 (2016).
- [53] S.-L. Su, E. Liang, S. Zhang, J.-J. Wen, L.-L. Sun, Z. Jin, and A.-D. Zhu, One-step implementation of the Rydberg–Rydberg-interaction gate, *Phys. Rev. A* **93**, 012306 (2016).
- [54] D. Petrosyan, F. Motzoi, M. Saffman, and K. Mølmer, High-fidelity Rydberg quantum gate via a two-atom dark state, *Phys. Rev. A* **96**, 042306 (2017).
- [55] A. M. Kaufman and K.-K. Ni, Quantum science with optical tweezer arrays of ultracold atoms and molecules, *Nat. Phys.* **17**, 1324 (2021).
- [56] S. R. Cohen and J. D. Thompson, Quantum computing with circular Rydberg atoms, *PRX Quantum* **2**, 030322 (2021).
- [57] A. Pagano, S. Weber, D. Jaschke, T. Pfau, F. Meinert, S. Montangero, and H. P. Büchler, Error budgeting for a controlled-phase gate with strontium-88 Rydberg atoms, *Phys. Rev. Res.* **4**, 033019 (2022).
- [58] P. Méhaignerie, C. Sayrin, J.-M. Raimond, M. Brune, and G. Roux, Spin-motion coupling in a circular-Rydberg-state

- quantum simulator: Case of two atoms, *Phys. Rev. A* **107**, 063106 (2023).
- [59] W.-X. Li, J.-L. Wu, S.-L. Su, and J. Qian, High-tolerance antiblockade SWAP gates using optimal pulse drivings, *Phys. Rev. A* **109**, 012608 (2024).
- [60] R. Faoro, C. Simonelli, M. Archimi, G. Masella, M. M. Valado, E. Arimondo, R. Mannella, D. Ciampini, and O. Morsch, van der Waals explosion of cold Rydberg clusters, *Phys. Rev. A* **93**, 030701(R) (2016).
- [61] F. Robicheaux, T. M. Graham, and M. Saffman, Photon-recoil and laser-focusing limits to Rydberg gate fidelity, *Phys. Rev. A* **103**, 022424 (2021).
- [62] Z. Zhang, M. Yuan, B. Sundar, and K. R. A. Hazzard, Motional decoherence in ultracold Rydberg atom quantum simulators of spin models, [arXiv:2201.08463](https://arxiv.org/abs/2201.08463).
- [63] F. M. Gambetta, W. Li, F. Schmidt-Kaler, and I. Lesanovsky, Engineering nonbinary Rydberg interactions via phonons in an optical lattice, *Phys. Rev. Lett.* **124**, 043402 (2020).
- [64] R. Belyansky, J. T. Young, P. Bienias, Z. Eldredge, A. M. Kaufman, P. Zoller, and A. V. Gorshkov, Nondestructive cooling of an atomic quantum register via state-insensitive Rydberg interactions, *Phys. Rev. Lett.* **123**, 213603 (2019).
- [65] F. Camargo, R. Schmidt, J. D. Whalen, R. Ding, G. Woehl, S. Yoshida, J. Burgdörfer, F. B. Dunning, H. R. Sadeghpour, E. Demler, and T. C. Killian, Creation of Rydberg polarons in a Bose gas, *Phys. Rev. Lett.* **120**, 083401 (2018).
- [66] M. Płodzień, T. Sowiński, and S. Kokkelmans, Simulating polaron biophysics with Rydberg atoms, *Sci. Rep.* **8**, 9247 (2018).
- [67] P. P. Mazza, R. Schmidt, and I. Lesanovsky, Vibrational dressing in kinetically constrained Rydberg spin systems, *Phys. Rev. Lett.* **125**, 033602 (2020).
- [68] M. Magoni, P. P. Mazza, and I. Lesanovsky, Phonon dressing of a facilitated one-dimensional Rydberg lattice gas, *SciPost Phys. Core* **5**, 041 (2022).
- [69] A. Kosior, S. Kokkelmans, M. Lewenstein, J. Zakrzewski, and M. Płodzień, Phonon-assisted coherent transport of excitations in Rydberg-dressed atom arrays, *Phys. Rev. A* **108**, 043308 (2023).
- [70] F. M. Gambetta, C. Zhang, M. Hennrich, I. Lesanovsky, and W. Li, Exploring the many-body dynamics near a conical intersection with trapped Rydberg ions, *Phys. Rev. Lett.* **126**, 233404 (2021).
- [71] M. Magoni, R. Joshi, and I. Lesanovsky, Molecular dynamics in Rydberg tweezer arrays: Spin-phonon entanglement and Jahn-Teller effect, *Phys. Rev. Lett.* **131**, 093002 (2023).
- [72] M. Morgado and S. Whitlock, Quantum simulation and computing with Rydberg-interacting qubits, *AVS Quantum Sci.* **3**, 023501 (2021).
- [73] M. Schiulaz, A. Silva, and M. Müller, Dynamics in many-body localized quantum systems without disorder, *Phys. Rev. B* **91**, 184202 (2015).
- [74] A. Smith, J. Knolle, D. L. Kovrizhin, and R. Moessner, Disorder-free localization, *Phys. Rev. Lett.* **118**, 266601 (2017).
- [75] R. J. Valencia-Tortora, N. Pancotti, M. Fleischhauer, H. Bernien, and J. Marino, A Rydberg platform for non-ergodic chiral quantum dynamics, [arXiv:2309.12392](https://arxiv.org/abs/2309.12392).
- [76] P. Kitson, T. Haug, A. La Magna, O. Morsch, and L. Amico, Rydberg atomtronic devices, [arXiv:2310.18242](https://arxiv.org/abs/2310.18242).
- [77] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.132.133401> for details on the derivations of the main text and experimental considerations, which includes Refs. [61,68,78–83].
- [78] J. R. Johansson, P. D. Nation, and F. Nori, QuTiP: An open-source Python framework for the dynamics of open quantum systems, *Comput. Phys. Commun.* **183**, 1760 (2012).
- [79] T. D. Lee, F. E. Low, and D. Pines, The motion of slow electrons in a polar crystal, *Phys. Rev.* **90**, 297 (1953).
- [80] M. Abramowitz and I. A. Stegun, *Handbook of Mathematical Functions with Formulas, Graphs, and Mathematical Tables* (National Bureau of Standards Applied Mathematics Series 55, U.S. Government Printing Office, Washington, DC, 1970).
- [81] Y. Jiao, X. Han, Z. Yang, J. Li, G. Raithel, J. Zhao, and S. Jia, Spectroscopy of cesium Rydberg atoms in strong radio-frequency fields, *Phys. Rev. A* **94**, 023832 (2016).
- [82] S. Zhang, F. Robicheaux, and M. Saffman, Magic-wavelength optical traps for Rydberg atoms, *Phys. Rev. A* **84**, 043408 (2011).
- [83] I. I. Beterov, I. I. Ryabtsev, D. B. Tretyakov, and V. M. Entin, Quasiclassical calculations of blackbody-radiation-induced depopulation rates and effective lifetimes of Rydberg nS , nP , and nD alkali-metal atoms with $n \leq 80$, *Phys. Rev. A* **79**, 052504 (2009).
- [84] C. Ates, T. Pohl, T. Pattard, and J. M. Rost, Antiblockade in Rydberg excitation of an ultracold lattice gas, *Phys. Rev. Lett.* **98**, 023002 (2007).
- [85] T. Amthor, C. Giese, C. S. Hofmann, and M. Weidemüller, Evidence of antiblockade in an ultracold Rydberg gas, *Phys. Rev. Lett.* **104**, 013001 (2010).
- [86] M. Mattioli, A. W. Glätzle, and W. Lechner, From classical to quantum non-equilibrium dynamics of Rydberg excitations in optical lattices, *New J. Phys.* **17**, 113039 (2015).
- [87] S.-L. Su, Y. Gao, E. Liang, and S. Zhang, Fast Rydberg antiblockade regime and its applications in quantum logic gates, *Phys. Rev. A* **95**, 022319 (2017).
- [88] M. Magoni, P. P. Mazza, and I. Lesanovsky, Emergent Bloch oscillations in a kinetically constrained Rydberg spin lattice, *Phys. Rev. Lett.* **126**, 103002 (2021).
- [89] L. Festa, N. Lorenz, L.-M. Steinert, Z. Chen, P. Osterholz, R. Eberhard, and C. Gross, Blackbody-radiation-induced facilitated excitation of Rydberg atoms in optical tweezers, *Phys. Rev. A* **105**, 013109 (2022).
- [90] F. Liu, Z.-C. Yang, P. Bienias, T. Iadecola, and A. V. Gorshkov, Localization and criticality in antiblockaded two-dimensional Rydberg atom arrays, *Phys. Rev. Lett.* **128**, 013603 (2022).
- [91] M. Marcuzzi, J. Minar, D. Barredo, S. de Léséleuc, H. Labuhn, T. Lahaye, A. Browaeys, E. Levi, and I. Lesanovsky, Facilitation dynamics and localization phenomena in Rydberg lattice gases with position disorder, *Phys. Rev. Lett.* **118**, 063606 (2017).

- [92] G. Vidal, Classical simulation of infinite-size quantum lattice systems in one spatial dimension, *Phys. Rev. Lett.* **98**, 070201 (2007).
- [93] R. Orús, A practical introduction to tensor networks: Matrix product states and projected entangled pair states, *Ann. Phys. (N.Y.)* **349**, 117 (2014).
- [94] J. Gray, QUIMB: A PYTHON package for quantum information and many-body calculations, *J. Open Source Software* **3**, 819 (2018).
- [95] S. Paeckel, T. Köhler, A. Swoboda, S. R. Manmana, U. Schollwöck, and C. Hubig, Time-evolution methods for matrix-product states, *Ann. Phys. (N.Y.)* **411**, 167998 (2019).
- [96] J. I. Cirac, D. Pérez-García, N. Schuch, and F. Verstraete, Matrix product states and projected entangled pair states: Concepts, symmetries, theorems, *Rev. Mod. Phys.* **93**, 045003 (2021).
- [97] C. Nill, The MPS code is available under the GPLv3 at [10.5281/zenodo.10495896](https://zenodo.org/record/10495896) (2024).
- [98] M. Ostmann, M. Marcuzzi, J. Minar, and I. Lesanovsky, Synthetic lattices, flat bands and localization in Rydberg quantum simulators, *Quantum Sci. Technol.* **4**, 02LT01 (2019).
- [99] S. Ebadi, T. T. Wang, H. Levine, A. Keesling, G. Semeghini, A. Omran, D. Bluvstein, R. Samajdar, H. Pichler, W. W. Ho, S. Choi, S. Sachdev, M. Greiner, V. Vuletić, and M. D. Lukin, Quantum phases of matter on a 256-atom programmable quantum simulator, *Nature (London)* **595**, 227 (2021).
- [100] R. Steinigeweg, F. Jin, D. Schmidtke, H. De Raedt, K. Michielsen, and J. Gemmer, Real-time broadening of nonequilibrium density profiles and the role of the specific initial-state realization, *Phys. Rev. B* **95**, 035155 (2017).
- [101] T. L. M. Lezama and Y. B. Lev, Logarithmic, noise-induced dynamics in the Anderson insulator, *SciPost Phys.* **12**, 174 (2022).
- [102] P. Sierant, T. Chanda, M. Lewenstein, and J. Zakrzewski, Slow dynamics of a mobile impurity interacting with an Anderson insulator, *Phys. Rev. B* **107**, 144201 (2023).
- [103] S. Bera, G. De Tomasi, F. Weiner, and F. Evers, Density propagator for many-body localization: Finite-size effects, transient subdiffusion, and exponential decay, *Phys. Rev. Lett.* **118**, 196801 (2017).
- [104] J. R. Schrieffer and P. A. Wolff, Relation between the Anderson and Kondo Hamiltonians, *Phys. Rev.* **149**, 491 (1966).