

## Manipulation of Giant Multipole Resonances via Vortex $\gamma$ Photons

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Traditional photonuclear reactions primarily excite giant dipole resonances, making the measurement of isovector giant resonances with higher multipolarities a great challenge. In this Letter, the manipulation of collective excitations of different multipole transitions in even-even nuclei via vortex  $\gamma$  photons is investigated. We develop the calculation method for photonuclear cross sections induced by the vortex  $\gamma$  photon beam using the fully self-consistent random-phase approximation plus particle-vibration coupling (RPA + PVC) model based on Skyrme density functional. We find that the electromagnetic transitions with multipolarity  $J < |m_\gamma|$  are forbidden for vortex  $\gamma$  photons due to the angular momentum conservation, with  $m_\gamma$  being the projection of total angular momentum of  $\gamma$  photon on its propagation direction. For instance, this allows for probing the isovector giant quadrupole resonance without interference from dipole transitions using vortex  $\gamma$  photons with  $m_\gamma = 2$ . Furthermore, the electromagnetic transition with  $J = |m_\gamma| + 1$  vanishes at a specific polar angle. Therefore, the giant resonances with specific multipolarity can be extracted via vortex  $\gamma$  photons. Moreover, the vortex properties of  $\gamma$  photons can be meticulously diagnosed by measuring the nuclear photon-absorption cross section. Our method opens new avenues for photonuclear excitations, generation of coherent  $\gamma$  photon laser and precise detection of vortex particles, and consequently, has significant impact on nuclear physics, nuclear astrophysics and strong laser physics.

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The collective excitation modes of quantum many-body systems are pervasive in a diversity of physics subdisciplines [1], such as condensed matter physics [2,3], atomic physics [4–6], nuclear physics [7–10], and particle physics [11,12]. In atomic nuclei, the giant resonances (GRs) appear to be a global feature of nuclei arising from the collective motion of the nucleons within the nucleus [7]. GRs not only play a fundamental role in nuclear structure research, but also serve as a means of constraining the nuclear equation of state [13], which is crucial for understanding a host of astrophysical phenomena [14–17], such as supernova explosions [17] and the structure of neutron stars [14,16].

GRs have been found to exist in the energy range of approximately 10–30 MeV, and their modes are characterized by the quantum numbers related to multipolarity, spin, and isospin [7]. The isovector giant dipole resonance, in which neutrons oscillate against protons [7], was first discovered in 1937 via photonuclear reaction [18,19]. While photons can provide transition strengths in a

model-independent way, owing to the well-known excitation mechanism of electromagnetic force, they generate primarily the giant dipole resonance (GDR) [20]. The giant quadrupole resonance (GQR), in which the nucleons undergo quadrupole deformation [21], was the next fundamental mode discovered in the 1970s [22–25]. It has been systematically studied over the nuclear chart using inelastic scattering of charged particles [26]; however, these probes, such as alpha particles, protons, and  $^3\text{He}$ , mainly induce isoscalar excitations [26]. The study of the isovector giant quadrupole resonance (IVGQR) has always been a challenge due to the lack of a highly selective experimental probe. Detailed studies on IVGQR are invaluable for nuclear structure and nuclear astrophysics, for instance, to constrain the nuclear effective mass, the isovector channel of the nuclear effective interaction, the density dependence of the nuclear symmetry energy [13,27,28], etc. At present, the main experimental studies are based on electron scattering, which displays a large spread in the reported parameters (e.g., transition strengths and

resonance widths [21,29]) due to the difficulty in disentanglement of different GR modes [7]. In photonuclear reactions, IVGQR is only a minor component and extracted by observing the electric dipole ( $E1$ )-electric quadrupole ( $E2$ ) interference term using the intense, nearly monoenergetic,  $\sim 100\%$  linearly polarized  $\gamma$ -ray beams [29,30]. These difficulties in detecting IVGQR are attributed to the preference of  $E1$  excitations over higher multiplicities by several orders of magnitudes from photon excitations. Nevertheless, the introduction of nonzero orbital angular momenta (OAM) to photons could potentially alter the selection rule and enable the unique extraction of higher multipole excitations. This would completely broaden the conventional understanding of photonuclear reactions and unlock new horizons in nuclear physics [31,32].

Vortex photons, described by wave functions with helical phases and carrying intrinsic OAM along the propagation direction [33,34], have given rise to new phenomena in various fields of physics, such as optical physics [35,36], astrophysics [37,38], and atomic physics [39,40]. Currently, vortex photons spanning from visible to x-ray regimes have been generated experimentally through optical mode conversion techniques, high harmonic generation, or coherent radiation in helical undulators and laser facilities [41–46]. With the rapid developments of ultraintense, ultrashort laser techniques [47,48], the generation of vortex  $\gamma$  photons is extensively proposed theoretically, where most of the studies consider Compton scattering to attain high energy and OAM [32,49–61]. Studies of atomic excitation using vortex photons [39,40,62–72] have shown that absorption of photons with nonzero OAM by atoms can excite multipole transitions that are otherwise suppressed for plane wave photons, due to modifications of the atomic transition selection rules on the beam axis. In nuclear physics, cross sections of deuteron photodisintegration by vortex photons [73] via  ${}^3S_1 \rightarrow {}^1S_0$  magnetic dipole ( $M1$ ) transition have been compared with those by plane wave photons. Nonetheless, the excitations of higher multipole transitions in nuclei via vortex photons are still an open question.

In this Letter, we investigate the collective excitations of different multipole transitions in even-even nuclei ( $J_i = 0$ ) via vortex  $\gamma$  photons. We develop the calculation method for photonuclear cross sections induced by the vortex  $\gamma$  photon beam using the fully self-consistent RPA + PVC model based on Skyrme density functional [74–77]. According to the interaction scenario illustrated in Fig. 1, the electromagnetic transitions are unrestricted for plane wave  $\gamma$  photons since the selection rule of plane wave is  $|J_i - J_f| \leq J \leq J_i + J_f$ ,  $M_f - M_i = \Lambda$ . However, for vortex  $\gamma$  photons, when the nucleus is positioned on the beam axis, the selection rule is modified to  $M_f - M_i = m_\gamma$  due to the conservation laws of angular momentum, with  $m_\gamma$  being the projection of the total angular momentum (TAM) of  $\gamma$  photon on its propagation direction. Therefore, the electromagnetic transitions with multipolarity  $J < |m_\gamma|$

are forbidden (indicated as the forbidden transitions). Because of the dependence on polar angle  $\theta_k$ , the electromagnetic transition with  $J = |m_\gamma| + 1$  could vanish at a specific polar angle, thus transitions almost entirely come from  $J = |m_\gamma|$  case (indicated as the quasipure transitions). Manipulating GRs with different multiplicities via vortex  $\gamma$  photons with different  $m_\gamma$  enables investigating isovector giant resonances of higher multiplicities without interference from other transitions, which broadens the research scope of photonuclear reaction compared with plane wave  $\gamma$  photons, and provides valuable insights into the nuclear structure and nuclear astrophysics [17,20,28]. Additionally, the forbidden and quasipure transitions excited by vortex  $\gamma$  photons might construct a three-level system for coherent zeptosecond  $\gamma$  photon laser [78–80].

Meanwhile, exploring the vortex properties of single  $\gamma$  photon is a fascinating area of research [32,41]. Vortex photons, ranging from visible to x-ray frequencies, have been successfully detected through interference with a reference beam [42–46]. However, detecting the vortex  $\gamma$  photons remains a challenge. We find that the vortex properties of  $\gamma$  photons can be determined accurately by measuring the nuclear photon-absorption cross section.

In the RPA + PVC model, the coupling of single-nucleon states to low-lying phonons (1 particle-1 hole-1 phonon configurations) is taken into account. While the RPA model provides a good description of GRs' energies, the PVC effect is crucial for describing the damping width of GRs [81]. Using the strength function  $S_{\mu J}$  (electric,  $\mu = E$ ; magnetic,  $\mu = M$ ) obtained by RPA + PVC model, we can derive the nuclear photon-absorption cross section  $\sigma^{(pl)}$  of a plane wave  $\gamma$  photon beam interacting with nucleus [see Eq. (8) in Supplemental Material (SM) [82]].

Different vortex modes exhibit similar characteristics in the vicinity of beam axis and different asymptotic behavior in the region far away from the beam axis (see Sec. III of SM [82]). Take the Bessel mode for example, the nuclear photon-absorption cross section  $\sigma^{(tw)}$  of a vortex  $\gamma$  photon beam, interacting with nucleus, differs from the case of plane wave due to the vortex state's vector potential  $\mathbf{A}_{\chi m_\gamma k_z \Lambda}^{(tw)}$  [34,82] and its ensuing change in the flux density and transition amplitude. The vortex state can be characterized by a definite transverse momentum  $\chi = |\mathbf{k}_\perp|$ , longitudinal momentum  $k_z$ ,  $m_\gamma$ , and helicity  $\Lambda$ . In momentum space, the vortex state can be interpreted as a coherent superposition of plane waves, arranged on a cone defined by the polar angle  $\theta_k = \arctan(\chi/k_z)$ . In general, vortex  $\gamma$  photon is the superposition of spin eigenstates, thus one can get  $m_s = 0, \pm\Lambda$  and  $m_l = m_\gamma, m_\gamma \mp \Lambda$ . When  $\theta_k \rightarrow 0$ , the vortex  $\gamma$  photon is approaching the limit of plane wave  $\gamma$  photon, and is almost in the spin eigenstate, thus one has  $m_s \simeq \Lambda$  and  $m_l \simeq m_\gamma - \Lambda$ . To normalize the nuclear photon-absorption cross sections of vortex  $\gamma$  photon to the plane wave case, we assume that the average flux density of

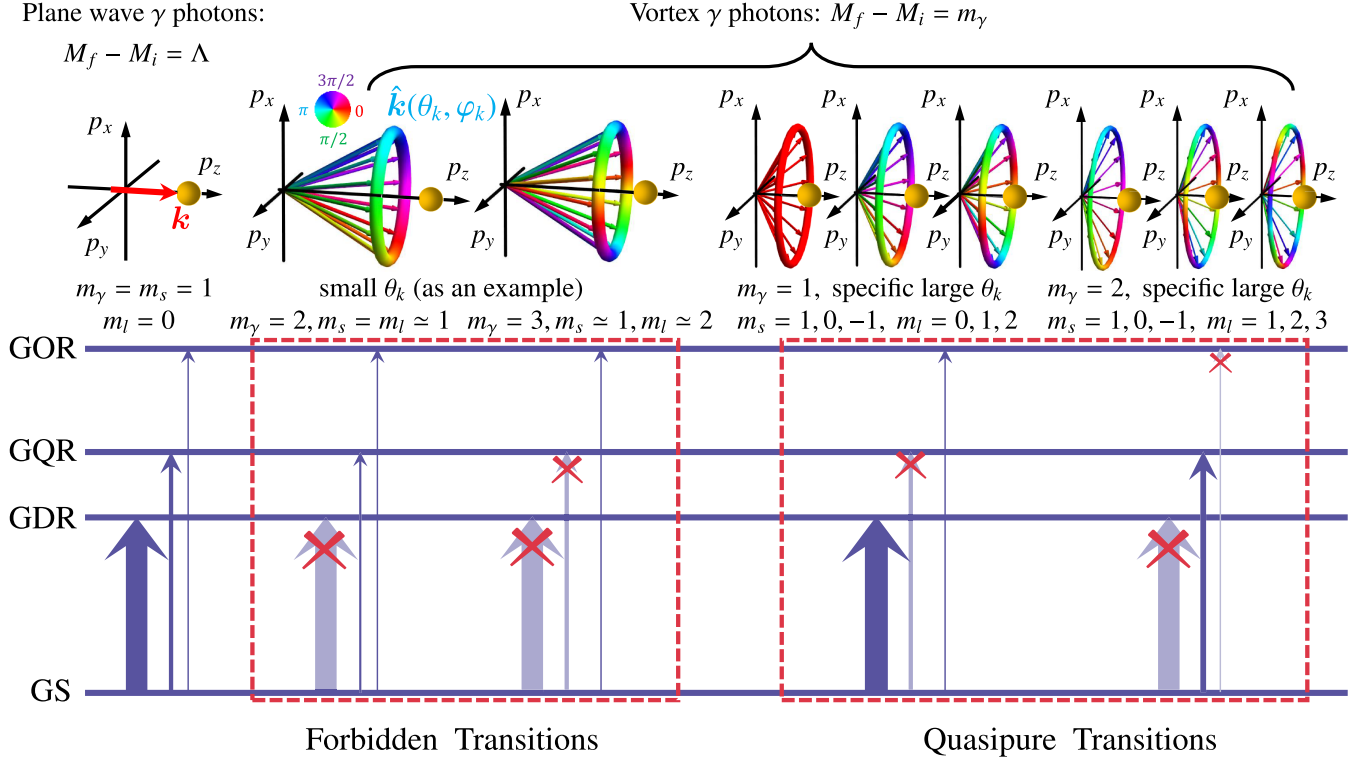


FIG. 1. Scenario of nuclear responses for even-even nuclei excited either by plane wave or vortex  $\gamma$  photons on the beam axis. In the momentum space, the vortex state consists of multiple plane waves with conically distributed  $\mathbf{k}$  vectors characterized by the polar angle  $\theta_k$  and the azimuth angle  $\varphi_k$ . The mutual phases (color coded) of the plane waves in the spectrum increase by  $2\pi m_l$  around the circle, where  $m_l$  ( $m_s$ ) is the projection of the OAM (spin) of  $\gamma$  photon on its propagation direction with  $m_l = m_\gamma - m_s$  and the helicity  $\Lambda = 1$ .  $M_i$  ( $M_f$ ) is the projection of the total angular momentum on the  $\gamma$  photon's propagation direction for the initial (final) state of the nucleus. The arrows linking the ground state (GS) to GDR, GQR, and giant octupole resonance (GOR) symbolize electromagnetic transitions with multiplicities  $J = 1, 2, 3$ , respectively. The “Forbidden Transitions” represent that electromagnetic transitions with  $J < |m_\gamma|$  are forbidden (for all  $\theta_k$ ), and the “Quasipure Transitions” indicate electromagnetic transitions predominantly contributed by  $J = |m_\gamma|$  (for specific  $\theta_k$ ).

vortex  $\gamma$  photons along its propagation direction is equivalent to that of plane wave multiplied by  $\cos \theta_k$  [70,83]. We introduce a quantity  $r^{(tw)}$ , which represents the ratio of vortex and plane wave cross section for nuclear excitation, i.e.,  $r^{(tw)} = \sigma^{(tw)} / \sigma^{(pl)}$ ,

$$r^{(tw)} = \frac{\sum_{M_i M_f} J_{m_\gamma + M_i - M_f}^2(\chi b) |\sum_{M'_i M'_f} d_{M_i M'_i}^{J_i}(\theta_k) d_{M_f M'_f}^{J_f}(\theta_k) M_{M'_i M'_f}^{(pl)}|^2}{\cos \theta_k \sum_{M'_i M'_f} |M_{M'_i M'_f}^{(pl)}|^2}. \quad (1)$$

The ratio  $r^{(tw)}$  exhibits two supplementary features being dependent upon the vortex properties of the incoming  $\gamma$  photons (i.e.,  $m_\gamma$  and  $\theta_k$ ). One is the Bessel function  $J_{m_\gamma + M_i - M_f}(\chi b)$  (with the impact parameter  $b$ ) that stems from the transverse structure of vortex  $\gamma$  photons with a Bessel mode. The other is the Wigner  $d$  function  $d_{M_f M'_f}^{J_f}(\theta_k)$  [ $d_{M_i M'_i}^{J_i}(\theta_k)$ ], which arises from the transformation of the projection of the nuclear TAM from the propagation axis of vortex  $\gamma$  photon to the orientation of

its plane wave component  $\mathbf{k}$ , in order to express the transition amplitude in terms of the plane wave case  $M_{M'_i M'_f}^{(pl)}$  (with the selection rule  $M'_f - M'_i = \Lambda$ ). With the property of Bessel function [84], the selection rule is modified as  $M_f - M_i = m_\gamma$  on the beam axis, which indicates that the full projection of the TAM of  $\gamma$  photon along its propagation direction can be transferred to the nuclear degrees of freedom. This results in the forbidden transitions in Fig. 1. For even-even nuclei, the TAM and its projection are  $J_i = M_i = M'_i = 0$ . Because of the selection rules for vortex and plane wave  $\gamma$  photons mentioned above, the ratio  $r^{(tw)}$  on the beam axis ( $b = 0$ ) becomes

$$r^{(tw)} = |d_{m_\gamma \Lambda}^{J_f}(\theta_k)|^2 / \cos \theta_k. \quad (2)$$

For specific  $\theta_k$  with  $d_{m_\gamma \Lambda}^{J_f}(\theta_k) = 0$ , the ratio  $r^{(tw)}$  vanishes, which results in the quasipure transitions in Fig. 1. In this Letter, we focus on the interaction between vortex  $\gamma$  photon beam and a single nucleus, which results in the  $b$

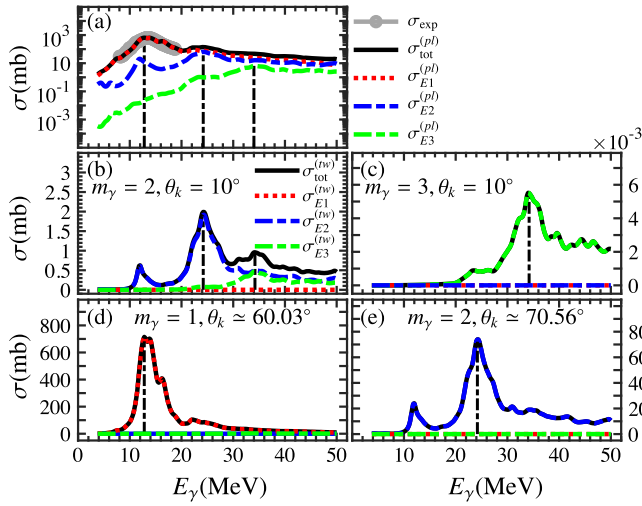


FIG. 2. (a) The experimental [85] and theoretical photon-absorption cross sections of  $^{208}\text{Pb}$  for plane wave  $\gamma$  photons. (b)–(e) The theoretical photon-absorption cross sections of  $^{208}\text{Pb}$  on the beam axis for vortex  $\gamma$  photons with various  $m_\gamma$  and  $\theta_k$ , respectively. Here,  $\Lambda = 1$ ,  $\sigma_{\text{tot}}^{(pl)} = \sigma_{E1}^{(pl)} + \sigma_{E2}^{(pl)} + \sigma_{E3}^{(pl)}$ , and  $\sigma_{\text{tot}}^{(tw)} = \sigma_{E1}^{(tw)} + \sigma_{E2}^{(tw)} + \sigma_{E3}^{(tw)}$ .

dependence of  $r^{(tw)}$ , and the realistic feasibility about this reaction is discussed later. The effects of macroscopic and mesoscopic target are discussed in Sec. IV of SM [82].

Vortex effects on the nucleus are the same for electric and magnetic transitions since the ratio  $r^{(tw)}$  is parity independent and angular momentum dependent. For convenience, we perform calculations of the electric transitions ( $E1$ ,  $E2$ , and  $E3$ ) in nucleus  $^{208}\text{Pb}$  using both plane wave  $\gamma$  photons and vortex  $\gamma$  photons with Bessel mode, and the nuclear photon-absorption cross sections are shown in Fig. 2. We choose  $^{208}\text{Pb}$  due to the availability of experimental data [85], the large photon-absorption cross section, and ongoing challenges in IVGQR [29,30]. The excitation of other even-even nuclei by vortex  $\gamma$  photons is similar, albeit with changes in the characteristic photon-absorption cross sections. For plane wave  $\gamma$  photons [Fig. 2(a)], we find that the theoretical results are in good agreement with the experiment. It is also found that the  $E1$ ,  $E2$ , and  $E3$  photon-absorption cross sections of plane wave exhibit characteristic peaks. Below photon energy 20 MeV, the total cross section  $\sigma_{\text{tot}}^{(pl)}$  is dominated by the  $E1$  cross section  $\sigma_{E1}^{(pl)}$ . While the photon energy  $E_\gamma$  exceeds 20 MeV, the contribution from  $\sigma_{E1}^{(pl)}$  is a bit larger than that of  $\sigma_{E2}^{(pl)}$ . For  $\sigma_{E3}^{(pl)}$ , its contribution is always negligible. Thus, studying  $E2$  and  $E3$  cross sections using plane wave  $\gamma$  photons is challenging.

However, when the nucleus is positioned on the beam axis ( $b = 0$ ), the contribution of  $E2$  cross section can be distinguished by vortex  $\gamma$  photon with  $m_\gamma = 2$  due to the forbiddance of  $E1$  transition and the dominance of  $E2$

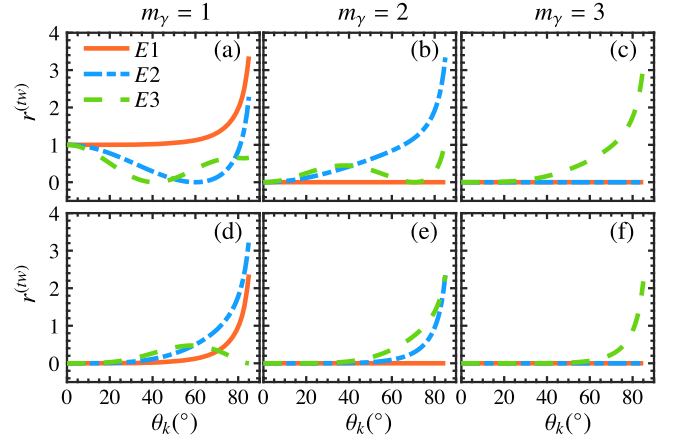


FIG. 3. The ratio of  $E1$ ,  $E2$ , and  $E3$  transitions ( $r_{E1}^{(tw)}$ ,  $r_{E2}^{(tw)}$ , and  $r_{E3}^{(tw)}$ ) vs the polar angle  $\theta_k$  on the beam axis. (a)–(c):  $\Lambda = 1$  with  $m_\gamma = 1$ ,  $m_\gamma = 2$ ,  $m_\gamma = 3$ , respectively. (d)–(f) are similar but for  $\Lambda = -1$ .

transition, as shown in Fig. 2(b) ( $\theta_k = 10^\circ$  as an example) and corresponding to the forbidden  $E1$  transition in Fig. 1. Similarly, the contribution of  $E3$  cross section can be distinguished by vortex  $\gamma$  photon with  $m_\gamma = 3$ , as shown in Fig. 2(c) corresponding to the forbidden  $E1$  and  $E2$  transitions in Fig. 1. As a result, we can find that vortex  $\gamma$  photons with  $m_\gamma = 1$ ,  $m_\gamma = 2$ , and  $m_\gamma = 3$  are with the different peak energies of the photon-absorption cross section corresponding to the peak energies of  $E1$ ,  $E2$ , and  $E3$  transitions of plane wave, respectively [Figs. 2(b)–(d)]. Thus, the projection of TAM  $m_\gamma$  of vortex  $\gamma$  photons can be determined by the measurement of the peak energy. Furthermore, the transitions with  $J = |m_\gamma| + 1$  could vanish at specific  $\theta_k$  (see Fig. 3), so we take these angles to plot the corresponding cross sections in Figs. 2(d) and (e), where vortex  $\gamma$  photons with  $m_\gamma = 1$  and  $m_\gamma = 2$  can result in the occurrence of the quasipure  $E1$  and  $E2$  transitions, respectively, with a cross section comparable to that of the plane wave. In principle, the quasipure  $E3$  transition can also be induced by vortex  $\gamma$  photon with  $m_\gamma = 3$ , and specific  $\theta_k$  (Fig. 4 in SM [82]).

In order to understand the occurrence of the quasipure transition, the ratios  $r_{E1}^{(tw)}$ ,  $r_{E2}^{(tw)}$ , and  $r_{E3}^{(tw)}$  on the beam axis ( $b = 0$ ) as a function of  $\theta_k$  [see Eq. (2)] are shown in Fig. 3. In Fig. 3(a),  $E2$  transition is forbidden for vortex  $\gamma$  photon with  $m_\gamma = 1$  at  $\theta_k \approx 60.03^\circ$  [ $d_{11}^2(\theta_k) = 0$ ], resulting in a quasipure  $E1$  cross section and  $r_{E1}^{(tw)} = 1.13$ , which corresponds to Fig. 2(d). Similarly, in Fig. 3(b),  $E3$  transition is forbidden for a vortex  $\gamma$  photon with  $m_\gamma = 2$  at  $\theta_k \approx 70.56^\circ$  [ $d_{21}^3(\theta_k) = 0$ ], resulting in a quasipure  $E2$  cross section and  $r_{E2}^{(tw)} = 1.19$ , which corresponds to Fig. 2(e). We can see that in Figs. 3(b),(c),(e),(f), transitions with  $J < |m_\gamma|$  are always forbidden independent of  $\theta_k$  and  $\Lambda$  due to the angular momentum selection rule. Besides,  $r^{(tw)}$  becomes



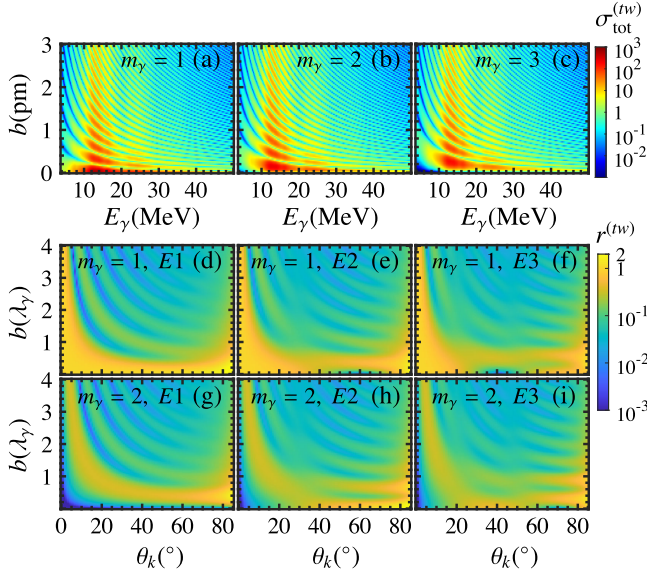


FIG. 4. (a)–(c): Distributions of total vortex photon-absorption cross section  $\sigma_{\text{tot}}^{(tw)}$  (mb) in the plane of the impact parameter  $b$  and the energy  $E_\gamma$  with the polar angle  $\theta_k = 10^\circ$  and  $m_\gamma = 1$ ,  $m_\gamma = 2$  and  $m_\gamma = 3$ , respectively. (d)–(i): Distributions of the ratio  $r^{(tw)}$  in the plane of the impact parameter  $b$  and the polar angle  $\theta_k$  at the energy  $E_\gamma = E_{\gamma,1}$  with its corresponding photon wavelength  $\lambda_\gamma$ , where  $m_\gamma = 1$  for panels (d)–(f) and  $m_\gamma = 2$  for panels (g)–(i). Here,  $E_{\gamma,1}$  is the peak energy of the  $E1$  transition for the plane wave case [see Fig. 2(a)].

extremely large at the large polar angle (near  $90^\circ$ ), which is due to  $\cos\theta$  dependence of the corresponding effective flux density of vortex  $\gamma$  photon along its propagation direction. Furthermore, the polar angle  $\theta_k$  of vortex  $\gamma$  photon can be determined by the measurement of  $r^{(tw)}$ , and the vortex topological charge  $m_l$  can be further inferred as  $m_l = m_\gamma$ ,  $m_\gamma \pm \Lambda$  with probabilities  $|d_{0\Lambda}^1(\theta_k)|^2$ ,  $|d_{\mp 1,\Lambda}^1(\theta_k)|^2$ , respectively.

In the region far away from the beam axis (the impact parameter  $b \neq 0$ ), the photon energy  $E_\gamma$  dependence of  $\sigma_{\text{tot}}^{(tw)}$  and the polar angle  $\theta_k$  dependence of  $r^{(tw)}$  are shown in Fig. 4. There is no specific selection rule since the system has no axial symmetry, thus there are no forbidden transitions. Moreover, the  $1^-$  (GDR),  $2^+$  (GQR), and  $3^-$  (GOR) states come from the superposition of  $M_f = 0, \pm 1$ ,  $M_f = 0, \pm 1, \pm 2$ , and  $M_f = 0, \pm 1, \pm 2, \pm 3$ , respectively. In contrast, for vortex  $\gamma$  photon at  $b = 0$ ,  $M_f = m_\gamma$ , and for plane wave  $\gamma$  photon,  $M_f = \Lambda$ . At the small polar angle  $\theta_k$ ,  $\sigma_{E1}^{(tw)}$ ,  $\sigma_{E2}^{(tw)}$ , and  $\sigma_{E3}^{(tw)}$  are dominated by  $M_f = \Lambda$ , which returns to the selection rule of plane wave. With increasing  $\theta_k$ , the contributions from  $M_f \neq \Lambda$  increase (Figs. 5–7 in SM [82]). From the peak position in Figs. 4(a)–(c) as well as Fig. 8 in SM [82], one can see the cross section from  $E1$  is dominated, just as the plane wave case. The vortex photon-absorption cross section  $\sigma^{(tw)} \propto J_z^{(tw)}$  [Eq. (17) in

SM [82]] due to the dominated  $E1$  transition, thus the dependence of cross section on impact parameter  $b$  and  $m_\gamma$  in Fig. 4 follows the behavior of Bessel function  $J_{m_\gamma - m_s}(\chi\rho)$  in  $J_z^{(tw)}$ . We also find that, as the impact parameter  $b$  increases,  $r^{(tw)}$  decreases. For typical interatomic distances in crystals (0.1 nm),  $r^{(tw)}$  is  $\simeq 10^{-4}$  for vortex state with Bessel mode and  $\simeq 0$  with Bessel-Gauss mode (details in Fig. 9 of SM [82]), which means that the absorption of the vortex beam by other nuclei being offset ( $\gtrsim 0.1$  nm) from the vortex beam axis can be neglected. Furthermore, the superposition of vortex  $\gamma$  photons with different  $m_\gamma$  could make the vortex photon-absorption cross sections azimuth-dependent (Figs. 10 and 11 in SM [82]).

In order to selectively observe the quasipure GR transitions of different multiplicities, the target nuclei should be located near the beam axis, and there are two possible options: one involves interacting the vortex beam with a single, trapped ion [40,62], while the other involves interaction with a solid target, such as a single crystal. The former offers the advantage of easier manipulation of the alignment and offset of the vortex beam with respect to the nucleus, but it has the disadvantage of low probability, necessitating the time accumulation and highly brilliant vortex  $\gamma$  beams, which are promising based on the interaction of ultraintense lasers with material [86] and are discussed in Refs. [53,54,56,57,60,87]. The latter offers the advantage of a relatively large reaction rate, but it presents the difficulty of achieving synchronous alignment of the vortex beam axis with the nuclei.

In conclusion, we demonstrate the ability of vortex  $\gamma$  photons to manipulate the population of giant multipole resonance, enabling the occurrence of the forbidden and quasipure transitions and ensuing the extraction of isovector giant resonances with specific multipolarity. Moreover, measuring nuclear photon-absorption cross sections can meticulously diagnose the vortex  $\gamma$  photons. Our findings may have significant implications for the studies of nuclear physics, nuclear astrophysics, and strong laser physics. For instance, our method would open a completely new avenue for experimental nuclear spectroscopy that makes previously unexplored nuclear high-energy states measurable in an exclusive way, provide new opportunities for constraining nuclear equation of state, enable highly accurate detection for the properties of vortex particles, unlock new possibilities for designing coherent  $\gamma$  photon laser, etc.

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