Possible Eliashberg-Type Superconductivity Enhancement Effects in a Two-Band Superconductor MgB₂ Driven by Narrow-Band THz Pulses

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(Received 16 May 2023; revised 1 August 2023; accepted 19 September 2023; published 1 November 2023)

We study THz-driven condensate dynamics in epitaxial thin films of MgB₂, a prototype two-band superconductor (SC) with weak interband coupling. The temperature and excitation density dependent dynamics follow the behavior predicted by the phenomenological bottleneck model for the single-gap SC, implying adiabatic coupling between the two condensates on the ps timescale. The amplitude of the THz-driven suppression of condensate density reveals an unexpected decrease in pair-breaking efficiency with increasing temperature—unlike in the case of optical excitation. The reduced pair-breaking efficiency of narrow-band THz pulses, displaying minimum near $\approx 0.7 T_c$, is attributed to THz-driven, long-lived, nonthermal quasiparticle distribution, resulting in Eliashberg-type enhancement of superconductivity, competing with pair breaking.

DOI: 10.1103/PhysRevLett.131.186903

Light-induced manipulation of symmetry-broken ground states like superconductors, density waves, or magnetic materials has been at the forefront of modern solid-state physics research for over a decade. While excitation with femtosecond optical pulses at photon energies much larger than energies of gaps or relevant bosonic excitations normally results in a light-induced suppression of the order parameter, excitation of selected lattice vibrations, or resonant electronic transitions may result in metastable states that cannot be reached by quasithermal pathways. Examples of such include modulation of optical gap in CH₃NH₃PbI₃ by THz driving of optical phonons [1], possible light-induced superconductivity at temperatures above the superconducting critical temperature [2-4], switching to a hidden state in 1T-TaS₂ [5], generation of spin-density-wave order at high temperatures in BaFe₂As₂ [6], or inducing ferroelectricity in $SrTiO_3$ [7].

While most of these approaches are based on nonadiabatic effects, light-induced enhancement of superconductivity (SC) in conventional BCS superconductors was first demonstrated in the 1960s [8–11]. The fascinating enhancement of critical temperature, critical current, and the superconducting gap was observed in clean type-I superconductors under continuous illumination with electromagnetic radiation at subgap frequencies [8,9]. While subgap excitation does not lead to condensate depletion and thus conserves the number of quasiparticles (QPs), it may result in a nonthermal QP distribution via excitation of thermally excited QPs away from the gap edge. As the low-lying QPs are much more effective in inhibiting pairing correlations than high-energy QPs, the nonthermal QP distribution results in the enhancement of SC, as demonstrated by Eliashberg by solving the self-consistent BCS gap equation under such nonequilibrium [12–14]. Refinements of the Eliashberg model, considering that the QP recombination rate is increasing with increasing QP energy, suggested that even an overall reduction of QP density can be realized [15,16].

As such effects rely on a nonthermal QP distribution, experimental studies with continuous microwave illumination were largely limited to materials with large electron mean free paths, and the resulting enhancements of the gap, critical current, and critical temperature were of the order of 1% [10,11]. However, even in NbN, a prototype dirty-limit SC, signatures of gap enhancement were observed on a 50 ps timescale, when photoexciting with narrow-band THz pulses [17]. To investigate such transient phenomena further, MgB₂, a prototype two-band BCS superconductor with the highest critical temperature ($T_c \approx 40$ K) among metallic phonon-mediated BCS superconductors (at ambient pressure) presents an interesting alternative. MgB₂ is characterized by two distinct types of electronic bands crossing the Fermi energy, E_f , the quasi-two-dimensional holelike σ bands, and the three-dimensional π bands [18,19]. As demonstrated by tunneling [20,21], photoemission [22], and Raman spectroscopy [23], the superconducting state is characterized by two distinct isotropic gaps with $\Delta_{\pi} \approx 2 \text{ meV}$ and $\Delta_{\sigma} \approx 7 \text{ meV}$ [20–24] in the π and σ bands, respectively. The presence of a single T_c with two well-distinguished gaps suggests a weak, yet not negligible, interband coupling [18,19]. The low intraband scattering rates [25,26] and the relatively large value of Δ_{σ} make MgB₂ an ideal test system to study SC enhancement effects driven by narrow-band THz pulses.

In this Letter, we present systematic studies of condensate dynamics in clean epitaxial MgB₂ thin films [25,27], following excitation with narrow-band THz pulses, with frequencies between $2\Delta_{\pi}/h$ and $2\Delta_{\sigma}/h$. By studying the temperature (*T*) and absorbed energy density (*A*) dependence of the THz-driven gap suppression and recovery dynamics, and comparing the results with those obtained by near-infrared (NIR) pumping at 1.55 eV, we provide evidence of long-lived Eliashberg SC enhancement effects in MgB₂. These increase with increasing *T*, reflecting an increase in the density of thermally excited QPs, until reaching the temperature where also $2\Delta_{\sigma}(T)$ drops below the THz photon energy.

Time-resolved studies of the dynamics following excitation with THz pulses were performed at the free electron laser (FEL) facility in Helmholtz-Zentrum Dresden-Rossendorf, providing intense picosecond narrow-band (bandwidth $\Delta \nu_{\text{FEL}} \approx 30 \text{ GHz}$) THz pulses with tunable frequency ν_{FEL} at a repetition rate of 13 MHz [28,29]. We investigated high-quality epitaxial (001) single-crystalline MgB₂ thin films grown on MgO (111) substrate by hybrid physical-chemical vapor deposition [27]. Films, with thicknesses of 15 and 30 nm on $5 \times 5 \text{ mm}^2$ substrates were characterized by x-ray diffraction and charge transport measurements [25]. Experiments were carried out in a single-color pump-probe configuration using $\nu_{\text{FEL}} = 1.5$, 2.1 and 2.7 THz, where $2\Delta_{\pi} < h\nu_{\text{FEL}} < 2\Delta_{\sigma}$. For reference, we performed complementary studies of dynamics driven by 50 fs NIR pulses. The high repetition rate of the FEL results in continuous heating of the sample, which is taken into account (all the quoted temperatures below take continuous heating into account [29]). As critical temperatures of samples investigated in different beam times varied between \approx 32 K (15 nm film) and \approx 36 K (30 nm film) we present the T-dependent data as a function of reduced temperature T/T_c . We focus on data with $\nu_{\rm FEL} = 2.7$ THz, providing the highest dynamic range and signal-to-noise ratio.

Figure 1 presents selected traces of the induced suppression and recovery of superconductivity, recorded at different ν_{FEL} . As elaborated in the Supplemental Material [29], these traces present the evolution of the *effective* superconducting gap Δ as a function of time delay t_d . More precisely, we plot $[\delta \Delta(t_d)/\Delta(T)]$, where $\delta \Delta(t_d) \equiv$ $\Delta(t_d) - \Delta(T)$, and $\Delta(T)$ is the equilibrium value of the



FIG. 1. Evolution of the THz-driven suppression of the effective gap, normalized to the absorbed energy density $\{\delta\Delta(t_d)/[\Delta(T) \cdot A]\}$ recorded at the cryostat temperature T = 4.2 K with (a) 1.5 THz, (b) 2.1 THz, and (c) 2.7 THz pulses. The experimental data points are represented by solid symbols (absorbed energy densities, A are in mJ/cm³) while dashed lines represent the fits to the data using Eq. (1). The shaded regions represent the cross-correlations of THz pulses. The normalized gap suppression amplitudes are of the same order of magnitude for all three ν_{FEL} . While the relative errors in calculated A for each ν_{FEL} are negligible, the absolute values of A are correct within a factor of 2 due to the large reflectivity of MgB₂ and the FEL mode quality. (d) Approximate T dependence of gaps $2\Delta_{\pi}$ and $2\Delta_{\sigma}$ compared to $h\nu_{\text{FEL}} = 2.7$ THz (dashed horizontal line).

effective gap at the sample temperature *T*. $\delta\Delta(t_d)$ is extracted from the recorded dynamics of the film transmission $\delta \text{Tr}(t_d)$ and equilibrium Tr(T), assuming the so-called T^* model [36,37]. This model, applied to describe the time evolution of the SC state in NbN [17], assumes that in nonequilibrium QPs, the condensate(s) and the high frequency ($\hbar\omega > 2\Delta$) bosonic excitations [in this case high-frequency acoustic phonons (HFP)] are characterized by an elevated effective temperature T^* . The low energy ($\hbar\omega < 2\Delta$) acoustic phonons thereby remain at the base temperature.

The effective gap description, where $\Delta(t) \propto \Delta_{\sigma}(t) \propto \Delta_{\pi}(t)$, is supported by the long timescales of the dynamics and the fact that the absorbed energy density required to suppress SC, A_{sup} , matches the total condensation energy E_c of MgB₂ [29]. Since $E_c = \frac{1}{2}N_{\pi}(0)\Delta_{\pi}^2 + \frac{1}{2}N_{\sigma}(0)\Delta_{\sigma}^2$ and the normal state densities of states in the π and σ bands $N_{\pi,\sigma}(0)$ are comparable [18,19], \approx 90% of E_c stems from pairing in the σ band. Thus, $A_{sup} \approx E_c$ implies that the two gaps Δ_{π} , Δ_{σ} follow the same dynamics (beyond the resolution limit of \approx 20 ps) despite the fact that for excitation with $h\nu_{FEL} < 2\Delta_{\sigma}$ only pairs in the π band can directly be broken. The underlying fast thermalization between the two condensates likely proceeds through their coupling via the Leggett mode [23,39]. Since excitation with $h\nu_{\text{FEL}} > 2\Delta_{\pi}$ does result in Cooper pair breaking, with $\delta\Delta$ proportional to *A*, dividing the relative gap suppression by *A*, and analyzing $[\delta\Delta(t_d)/\Delta(T)A]$ (in % per (mJ/cm³)), allows us to emphasize the nonlinear behavior of the THz-driven gap dynamics. Panels (a)–(c) of Fig. 1 show $[\delta\Delta(t_d)/\Delta(T)A]$, recorded at T = 4.2 K for different *A* and $\nu_{\text{FEL}} = 1.5$ THz (a), 2.1 THz (b), and 2.7 THz (c). The induced reduction of Δ is followed by the recovery of SC order on the timescale between \approx 50 ps and several 100 ps, depending on *T* and *A*. We fit the traces using a model considering that pair breaking and recovery are exponential processes [40]

$$\frac{\delta\Delta(t_d)}{\Delta(T)A} = H(t_d, \tau_{\rm rec}, \sigma) \times \left(Ce^{-\frac{t_d}{\tau_{\rm rec}}} + B\right). \tag{1}$$

Here $\tau_{\rm rec}$ is the SC state recovery time, *C* is the amplitude of the normalized gap suppression, and *B* accounts for the residual gap suppression at large time delays (bolometric response). The rise time of the recorded transient σ is accounted for by a Heaviside function convoluted with the Gaussian with pulse-width σ , $H(t_d, \tau_{\rm rec}, \sigma)$ [40]. Here, σ can be larger than the temporal resolution limit of $\sqrt{2}\tau_{\rm FEL}$, where $\tau_{\rm FEL}$ is the duration of the THz pulse.

Several observations can be made by inspecting the traces in Figs. 1(a)–1(c): (i) τ_{rec} is similar for different ν_{FEL} and depends on *T* and *A*; (ii) the rise time σ depends on ν_{FEL} , being nearly resolution limited at $\nu_{\text{FEL}} = 1.5$ THz while increasing for $\nu_{\text{FEL}} \ge 2.1$ THz [29]; (iii) over a large range of excitation densities (≈ 2 orders of magnitude) the gap suppression amplitude displays a nonlinear dependence on *A*.

 $\tau_{\rm rec}$ and σ display similar temperature and excitation density dependence as in the case of NIR excitation [29,41]. Further, their dependences follow the same trend as in a single-gap BCS superconductor NbN [17], accounted for by the phenomenological boson bottleneck model [11,42]. In this model the delayed suppression of the condensate reflects the pair breaking by bosonic excitations, while its recovery is governed by the decay of HFP population [11,42]. In experiments with narrow-band THz excitation, such a delayed pair breaking has not been resolved before [43,44]. Since this process is clearly resolved only for $\nu_{\rm FEL} \gtrsim 2.1$ THz (see Supplemental Material [29]), we speculate the process originates from pair breaking by HFP ($\hbar \omega > 2\Delta_{\pi}$) that can be created at higher $\nu_{\rm FEL}$ since $\nu_{\rm FEL} \gtrsim 2.1$ THz $\gtrsim 4\Delta_{\pi}/h$ [29].

We focus on T and A dependence of the gap suppression amplitude $[\delta \Delta_{\max}/\Delta(T)]$ presented in Fig. 2. The first observation is a weakly sublinear dependence of $[\delta \Delta_{\max}/\Delta(T)]$ on A over the entire T range. This is consistent with the phonon bottleneck model [11,38,42,45]. Here, following the initial thermalization between condensate(s), QPs and HFPs to a common temperature T^* , part of the absorbed energy is transferred to the HFP subsystem. At low T and A the fraction of energy in the



FIG. 2. (a) The amplitude of photoinduced gap suppression for $\nu_{\text{FEL}} = 2.7$ THz as a function of *T* for several *A* (in mJ/cm³). (b) All collected data presented in the contour plot versus *A* and *T*. Starlike marks represent the data points, areas that could not be accessed in the experiment are masked with gray. Note the logarithmic vertical scales.

HFP subsystem is negligible [11,45]. However, this fraction gradually increases with increasing T^* , since $\Delta(T^*)$ reduces and—correspondingly—the specific heat of HFP increases [46].

The second, more remarkable observation, is that $[\delta \Delta_{\text{max}} / \Delta(T)A]$ decreases with increasing *T* at constant *A*, with pair-breaking efficiency displaying a pronounced minimum near $T/T_c = 0.7$. At face value, this result implies that at $T/T_c \approx 0.7$ the same absorbed energy density results in nearly twice smaller number of broken Cooper pairs as at the lowest temperatures.

The question arises if the observed decrease in pairbreaking efficiency and its minimum near 0.7 T_c can be accounted for by an increase in the fraction of energy required to heat up HFPs to T^* ? To test this hypothesis, we performed simulations of $[\delta \Delta_{\max} / \Delta(T)](T, A)$ using the phenomenological bottleneck model, which is applicable for weak to moderate excitation densities and for temperatures not too close to T_c [11,42,45]. Assuming a quasiequilibrium between the OPs and HFPs is reached, their concentrations are determined by the detailed balance equation $Rn_{T^*}^2 = \beta N_{T^*}$, where n_{T^*} and N_{T^*} are the QP and HFP concentrations corresponding to a common T^* . The microscopic constants R and β are the bare OP recombination rate and the pair-breaking rate by HFP absorption, respectively. Assuming that densities of photoexcited QPs/HFPs are substantially larger than their thermal densities, this boils down to the energy conservation law $A = n_{T^*}\Delta(T) +$ $2\Delta(T)N_{T^*} = n_{T^*}\Delta(T) + 2\Delta(T)n_{T^*}^2(R/\beta)$, with $\Delta(T)$ being the effective gap.

To compare with experiments, we consider that $\delta\Delta$ is proportional to the density of photoexcited QPs, $n_{\text{PE}} \approx n_{T^*}$ and use Δ_{π} as a characteristic gap energy. We further assume $\beta^{-1} \approx 30 \text{ ps}$ ($\beta^{-1} \approx 15 \text{ ps}$ for NIR



FIG. 3. Simulation of photoinduced gap suppression normalized to A using the phenomenological phonon-bottleneck model. The vertical scales are logarithmic. The value of QP recombination rate R [in (unit cell volume)/ps] is varied over 2 orders of magnitude. Simulations reveal the weakly sublinear A dependence, consistent with experiments. A decrease in pair-breaking efficiency with T (at constant A, exhibiting a minimum near $(T/T_c) \approx 0.7$ as seen in Fig. 2 is, however, not reproduced.

excitation [41]), and vary *R* over a large range around $R \approx 100$ (unit cell volume)/ps extracted from NIR excitation experiments [41]. The results of simulations are presented in Fig. 3. While, similar to experimental results, $(n_{\rm PE}/A)$ displays a weak sublinear dependence on *A* over the entire *T* range, no decrease or minimum in $n_{\rm PE}$ with increasing *T* is observed. Instead, $n_{\rm PE}$ smoothly increases with *T* over the entire range of *A* for all values of *R*.

We performed complementary optical pump-THz probe (OPTP) experiments, where MgB₂ films were excited with 50 fs NIR pulses at 800 nm. As opposed to THz excitation, NIR photons excite electrons from far below to far above the Fermi energy. In this case, SC is suppressed dominantly via pair breaking by HFPs created during the relaxation of hot OPs [11]. As the hot carrier relaxation requires a cascade of scattering events, the resulting QP distribution should be much closer to thermal than in the case of narrow-band THz excitation. The data obtained in the OPTP experiment were processed using the same approach as the data obtained with narrow-band THz excitation [29]. The extracted $[\delta \Delta_{\text{max}} / \Delta(T)](A, T)$ for the case of NIR excitation is shown in Fig. 4. Unlike in the case of THz pumping (Fig. 2), NIR excitation results in a monotonic increase of $[\delta \Delta_{\max} / \Delta(T) A]$ with increasing T, much like simulated (Fig. 3).

The comparison of gap dynamics in MgB₂ driven by the THz and NIR pulses, demonstrates a substantial reduction in the pair-breaking efficiency with increasing *T* under narrow-band THz excitation, with a pronounced minimum near $\approx 0.7 T_c$. The unexpected reduction in the pair-breaking efficiency with *T* suggests the existence of a process that is competing with THz-driven pair breaking, becoming stronger as *T* increases. This observation is consistent with early studies of microwave enhancement of SC, attributed



FIG. 4. (a) The amplitude of gap suppression in case of excitation with NIR pulses as a function of T at different A (in mJ/cm³). (b) All data, normalized to A, presented in a contour plot. The vertical scales are logarithmic. Starlike markers represent the data points; areas that are not accessible are masked with gray.

to excitation of thermal QPs away from the gap edge. This scenario also accounts for the observation of a minimum in pair-breaking efficiency near $\approx 0.7 T_c$. Namely, at low-*T* where $h\nu_{\text{FEL}} < 2\Delta_{\sigma}$ no direct pair breaking in the σ band is possible. Near 0.75 T_c , $h\nu_{\text{FEL}} \approx 2\Delta_{\sigma}$ [Fig. 1(d)], opening an additional pair-breaking channel and thereby increasing the pair-breaking efficiency for $h\nu_{\text{FEL}} \ge 2\Delta_{\sigma}$.

Our results suggest Eliashberg-type superconductivity enhancement effects are competing with pair breaking in THz-driven MgB₂, implying a highly nonthermal QP distribution on the timescale of at least a few tens of picoseconds. The questions arise, which processes limit the QP thermalization (in the strict sense of QPs reaching the Fermi-Dirac distribution) and what is the difference between optical and THz excitation? As opposed to THz drive, optical excitation creates QPs with energies in the eV range. On the fs timescale these hot QPs first relax via e-e collisions. When QP energies are reduced down to $\sqrt{\Omega_D E_f}$, Ω_D being the Debye energy, e-ph relaxation starts to dominate [47], resulting in a high concentration of phonons on the (sub-)ps timescale [47,48]. The cascade of scattering events and the multitude of scattering channels, including anharmonic decay of high energy optical phonons [48], is the basis for nearly thermal QP distribution following optical excitation. In the case of THz excitation, thermalization of QPs with energies in the 10 meV range is governed by the e-ph scattering, and can easily take as long as 100 ps at low T [47,49]. Moreover, due to the coherence factors, the e-ph scattering rate is substantially lower than the QP recombination rate [50], the latter not leading to QP thermalization.

In the early studies with continuous microwave irradiation [8-11] the SC enhancement effects of the order of 1% were observed. Here, using intense THz pulses, the observed reduction in the pair-breaking efficiency is as high as a factor of ≈ 2 at $T \approx 0.7 T_c$. Based on the magnitude of the effect, one may expect that in the absence of pair breaking, i.e., for $h\nu_{\text{FEL}} < 2\Delta_{\pi}$, a gap increase of up to a factor of ≈ 2 could be realized at temperatures where the density of thermally excited QPs becomes substantial.

To summarize, the systematic study of SC state dynamics in the two-band BCS superconductor MgB₂ reveals a pronounced coupling between the π - and σ -band condensates, where the two adiabatically follow each other on a picosecond timescale. At low T, we demonstrate that the pair-breaking dynamics depends on T, A, and $h\nu_{\text{FEL}}$ [29]. While we cannot exclude that the behavior is linked to the coupling between the two condensates, the dependence on $h\nu_{\rm FFL}$ [29] suggests it is related to the delayed pair breaking by phonons with $\hbar \omega > 2\Delta_{\pi}$ generated when $h\nu_{\text{FEL}} > 4\Delta_{\pi}$. Most importantly, tracking the excitation and T dependence of the THz-driven gap reduction, we observe a dramatic decrease in the pair-breaking efficiency with increasing T, resulting in a pronounced minimum near 0.7 T_c . The lack of such behavior under photoexcitation with NIR pulses suggests that narrow-band THz excitation results in a highly nonthermal OP distribution on the 100 ps timescale, resulting in Eliashberg-type superconductivity enhancement effects.

This work was funded by the German Research Foundation, Grant No. TRR 173-268565370 (project A05) and TRR 288-422213477 (project B08). T. D. acknowledges support from the Alexander von Humboldt Foundation.

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- H. Kim, J. Hunger, E. Cánovas, M. Karakus, Z. Mics, M. Grechko, D. Turchinovich, S. H. Parekh, and M. Bonn, Nat. Commun. 8, 687 (2017).
- [2] M. Mitrano, A. Cantaluppi, D. Nicoletti, S. Kaiser, A. Perucchi, S. Lupi, P. Di Pietro, D. Pontiroli, M. Riccò, S. R. Clark *et al.*, Nature (London) **530**, 461 (2016).
- [3] K. Isoyama, N. Yoshikawa, K. Katsumi, J. Wong, N. Shikama, Y. Sakishita, F. Nabeshima, A. Maeda, and R. Shimano, Commun. Phys. 4, 160 (2021).
- [4] A. Cavalleri, Contemp. Phys. 59, 31 (2018).
- [5] L. Stojchevska, I. Vaskivskyi, T. Mertelj, P. Kusar, D. Svetin, S. Brazovskii, and D. Mihailovic, Science 344, 177 (2014).
- [6] K. W. Kim, A. Pashkin, H. Schäfer, M. Beyer, M. Porer, T. Wolf, C. Bernhard, J. Demsar, R. Huber, and A. Leitenstorfer, Nat. Mater. 11, 497 (2012).
- [7] T. Nova, A. Disa, M. Fechner, and A. Cavalleri, Science 364, 1075 (2019).
- [8] A. Wyatt, V. Dmitriev, W. Moore, and F. Sheard, Phys. Rev. Lett. 16, 1166 (1966).
- [9] A. Dayem and J. Wiegand, Phys. Rev. 155, 419 (1967).
- [10] M. Tinkham, Introduction to Superconductivity, 2nd ed., (Dover Publications, Inc., Mineola, New York, 2004).
- [11] J. Demsar, J. Low Temp. Phys. 201, 676 (2020).

- [12] G. Eliashberg, ZhETF Pis. Red. 11, 186 (1970) [JETP Lett.
 11, 114 (1970)], http://jetpletters.ru/ps/1716/article_26086
 .shtml.
- [13] B. Ivlev, S. Lisitsyn, and G. Eliashberg, J. Low Temp. Phys. 10, 449 (1973).
- [14] J. B. Curtis, Z. M. Raines, A. A. Allocca, M. Hafezi, and V. M. Galitski, Phys. Rev. Lett. **122**, 167002 (2019).
- [15] J.-J. Chang and D. Scalapino, Phys. Rev. B 15, 2651 (1977).
- [16] U. Eckern, A. Schmid, M. Schmutz, and G. Schön, J. Low Temp. Phys. 36, 643 (1979).
- [17] M. Beck, M. Klammer, S. Lang, P. Leiderer, V. V. Kabanov, G. Gol'Tsman, and J. Demsar, Phys. Rev. Lett. 107, 177007 (2011).
- [18] A. Y. Liu, I. I. Mazin, and J. Kortus, Phys. Rev. Lett. 87, 087005 (2001).
- [19] X. Xi, Rep. Prog. Phys. 71, 116501 (2008).
- [20] P. Szabó, P. Samuely, J. Kačmarčík, T. Klein, J. Marcus, D. Fruchart, S. Miraglia, C. Marcenat, and A. G. M. Jansen, Phys. Rev. Lett. 87, 137005 (2001).
- [21] M. Iavarone, G. Karapetrov, A. Koshelev, W. Kwok, G. Crabtree, D. Hinks, W. Kang, E.-M. Choi, H. J. Kim, H.-J. Kim *et al.*, Phys. Rev. Lett. **89**, 187002 (2002).
- [22] S. Souma, Y. Machida, T. Sato, T. Takahashi, H. Matsui, S.-C. Wang, H. Ding, A. Kaminski, J. Campuzano, S. Sasaki *et al.*, Nature (London) **423**, 65 (2003).
- [23] G. Blumberg, A. Mialitsin, B. S. Dennis, M. V. Klein, N. D. Zhigadlo, and J. Karpinski, Phys. Rev. Lett. 99, 227002 (2007).
- [24] H. Kim, K. Cho, M. A. Tanatar, V. Taufour, S. K. Kim, S. L. Bud'ko, P. C. Canfield, V. G. Kogan, and R. Prozorov, Symmetry 11, 1012 (2019).
- [25] S. Kovalev, T. Dong, L.-Y. Shi, C. Reinhoffer, T.-Q. Xu, H.-Z. Wang, Y. Wang, Z.-Z. Gan, S. Germanskiy, J.-C. Deinert *et al.*, Phys. Rev. B **104**, L140505 (2021).
- [26] J. Fiore, M. Udina, M. Marciani, G. Seibold, and L. Benfatto, Phys. Rev. B 106, 094515 (2022).
- [27] C. Zhang, Y. Wang, D. Wang, Y. Zhang, Z.-H. Liu, Q.-R. Feng, and Z.-Z. Gan, J. Appl. Phys. **114**, 023903 (2013).
- [28] M. Helm, S. Winnerl, A. Pashkin, J. Klopf, J.-C. Deinert, S. Kovalev, P. Evtushenko, U. Lehnert, R. Xiang, A. Arnold *et al.*, Eur. Phys. J. Plus **138**, 158 (2023).
- [29] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.131.186903, which includes Refs. [30–35], for experimental setup description, data processing methods and procedures.
- [30] J. Chen, X. Xu, J. Zhou, and B. Li, Rev. Mod. Phys. 94, 025002 (2022).
- [31] P. Peumans, A. Yakimov, and S. R. Forrest, J. Appl. Phys. 93, 3693 (2003).
- [32] Y. R. Koh, J. Shi, B. Wang, R. Hu, H. Ahmad, S. Kerdsongpanya, E. Milosevic, W. A. Doolittle, D. Gall, Z. Tian *et al.*, Phys. Rev. B **102**, 205304 (2020).
- [33] G. Blumberg, A. Mialitsin, B. Dennis, N. Zhigadlo, and J. Karpinski, Physica C (Amsterdam) 456, 75 (2007).
- [34] W. Li, Y. Li, R. Chen, R. Zeng, M. Zhu, H. Jin, and S. Dou, J. Phys. Condens. Matter 20, 255235 (2008).
- [35] G. A. Slack, Phys. Rev. 126, 427 (1962).
- [36] W. Parker, Phys. Rev. B 12, 3667 (1975).
- [37] We consider a generalized version of the T^* model, i.e, the Rothwarf-Taylor model [38], applicable also for nonthermal

QP/high-frequency-phonon distributions. Experimentally, since the superconductivity-induced changes in the THz transmission of a SC film are governed by the inductive response of the condensate [17], the THz transmission presents a direct probe of the condensate density.

- [38] A. Rothwarf and B. Taylor, Phys. Rev. Lett. 19, 27 (1967).
- [39] F. Giorgianni, T. Cea, C. Vicario, C. P. Hauri, W. K. Withanage, X. Xi, and L. Benfatto, Nat. Phys. 15, 341 (2019).
- [40] M. Eichberger, H. Schäfer, M. Krumova, M. Beyer, J. Demsar, H. Berger, G. Moriena, G. Sciaini, and R. Miller, Nature (London) 468, 799 (2010).
- [41] J. Demsar, R. D. Averitt, A. J. Taylor, V. V. Kabanov, W. N. Kang, H. J. Kim, E. M. Choi, and S. I. Lee, Phys. Rev. Lett. 91, 267002 (2003).
- [42] V. V. Kabanov, J. Demsar, and D. Mihailovic, Phys. Rev. Lett. 95, 147002 (2005).
- [43] M. Beck, I. Rousseau, M. Klammer, P. Leiderer, M. Mittendorff, S. Winnerl, M. Helm, G. N. Gol'tsman, and J. Demsar, Phys. Rev. Lett. **110**, 267003 (2013).

- [44] M. Beck, M. Klammer, I. Rousseau, M. Obergfell, P. Leiderer, M. Helm, V. V. Kabanov, I. Diamant, A. Rabinowicz, Y. Dagan, and J. Demsar, Phys. Rev. B 95, 085106 (2017).
- [45] A. R. Pokharel, S. Y. Agustsson, V. V. Kabanov, F. Iga, T. Takabatake, H. Okamura, and J. Demsar, Phys. Rev. B 103, 115134 (2021).
- [46] V. V. Kabanov, J. Demsar, B. Podobnik, and D. Mihailovic, Phys. Rev. B 59, 1497 (1999).
- [47] V. V. Baranov and V. V. Kabanov, Phys. Rev. B 89, 125102 (2014).
- [48] D. Novko, F. Caruso, C. Draxl, and E. Cappelluti, Phys. Rev. Lett. **124**, 077001 (2020).
- [49] J. Demsar and T. Dekorsy, *Optical Techniques for Solid-State Materials Characterization*, edited by R. P. Prasankumar and A. J. Taylor (Francis & Taylor, New York, 2011), pp. 291–328.
- [50] S. B. Kaplan, C. Chi, D. Langenberg, J.-J. Chang, S. Jafarey, and D. Scalapino, Phys. Rev. B 14, 4854 (1976).