

Spectrally Sharp Near-Field Thermal Emission: Revealing Some Disagreements between a Casimir-Polder Sensor and Predictions from Far-Field Emittance

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Near-field thermal *emission* largely exceeds blackbody *radiation*, owing to spectrally sharp emission in surface polaritons. We turn the Casimir-Polder interaction between Cs($7P_{1/2}$) and a sapphire interface into a sensor sharply filtering, at 24.687 THz, the near-field sapphire emission at ~ 24.5 THz. The temperature evolution of the sapphire mode is demonstrated. The Cs sensor, sensitive to both dispersion and dissipation, suggests the polariton to be redshifted and sharper, as compared, up to 1100 K, to predictions from far-field sapphire emission, affected by birefringence and multiple resonances.

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The universality of blackbody radiation (BBR) [1] led to energy quantization for matter and photons, founding the quantum era. BBR applies in the far field (FF) only, with respect to a wavelength $\sim hc/k_B T$ (50 μm for 300 K). At shorter distances [2–5], the contribution of evanescent fields, whose spectral features are material-dependent, dramatically enhances thermal exchanges; similarly, the BBR limit can be beaten for small emitters [6,7]. This near-field (NF) regime opens fascinating applications [4–15], such as smart thermal infrared source (frequency, directivity, high-speed modulation) [16,17], coherent thermal emission controlled by surface engineering (gratings or metafabrication [18–22]), harvesting of thermal energy or refrigeration [23,24], thermal imaging [25–28], and thermal rectification [29–31]. Ultimately, for a “close contact” transfer at atomic scale, distinguishing “radiation” and “conduction” becomes questionable [32–35] because the evanescent field originates in thermally populated *surface polaritons* [36,37], i.e., hybrid particles coupling optical excitation and phonons originating in lattice excitation, hence involving a *phonon* transfer.

Spectral selectivity associated with the narrow-band NF thermal fluctuations [5], which affects both dissipative and dispersive effects, is essential for many applications. However, quantitative evaluations are few, often limited to very specific systems designed for nanothermal engineering [19,22]. Indeed, monitoring thermal exchanges between macroscopic bodies, or stabilizing a temperature difference, is challenging at nanometric distances [10,14]. NF scanning microscopy allows a local probing of the thermal field [25,26,38], but the nanoprobe itself perturbs the polariton spectrum [5,28,39].

The thermal electromagnetic fluctuations are constrained by boundary conditions imposed by surface shape and material properties, so that spatial variations of NF thermal exchanges depend primarily on surface modes, and Maxwell propagation. Hence, for sake of simplicity, we concentrate here on the *complex* surface response for an interface between a planar homogeneous hot material and vacuum, $S(\omega)$:

$$S(\omega) = [\varepsilon(\omega) - 1]/[\varepsilon(\omega) + 1], \quad (1)$$

with $\varepsilon(\omega)$ the macroscopic (relative) permittivity. As a major issue, further discussed, surface resonances occur for $\varepsilon(\omega) \rightarrow -1$, far away from bulk resonances [8,40–43].

NF thermal emission is now encompassed in fluctuating electrodynamics [44], which also covers Casimir *dispersion* forces [45,46] describing the macroscopic quantum attraction at short distances between two polarizable neutral bodies. Casimir interaction, originally described for $T = 0$, results from the boundary conditions for vacuum fluctuations. Precision Casimir experiments now test fundamental predictions (standard model or hypothetical non-Newtonian gravity [47–49]), but demand $T \neq 0$ corrections and a realistic material description [50–52]. The analogous “Casimir-Polder” (CP) interaction [53,54] between a neutral surface and a distant atom, benefiting from the intrinsic accuracy of atomic physics, has received various investigations in the very short distance regime—i.e. dipole-dipole van der Waals (vW) interaction. Among achievements, resonant couplings with surface modes [41,55,56], and temperature dependence, were notably demonstrated [57,58].

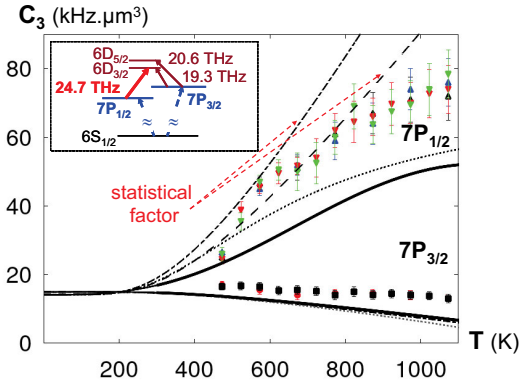


FIG. 1. Experimental evaluations of $C_3(T)$ for Cs($7P$) derived from FM-SR spectroscopy on the $6S_{1/2} \rightarrow \{7P_{1/2}, 7P_{3/2}\}$ doublet (see inset and relevant dipole couplings), and predictions. For the $6S_{1/2} \rightarrow 7P_{1/2}$ transition, the 4 hyperfine components are plotted separately (black triangles: $4 \rightarrow 4$, blue triangles: $4 \rightarrow 3$; red down triangles: $3 \rightarrow 3$, green down triangles: $3 \rightarrow 4$); for the $6S_{1/2} \rightarrow 7P_{3/2}$ transition, black and red squares are, respectively, for the $3 \rightarrow \{2, 3, 4\}$ and $4 \rightarrow \{3, 4, 5\}$ manifolds; Cs reservoir temperature is 180 °C. The dashed and dashed-dotted lines are predictions based upon sapphire permittivity at ~ 300 K (respectively, [60] and [61]), the dotted ones consider a T -dependent permittivity [62]; the thick ones use our sapphire measurements.

Here, we analyze the narrow NF emission of sapphire (Al_2O_3), a technologically important material, up to $T \sim 1100$ K, by comparing two radically different methods: (i) Through a quasi-coincidence [41,55] between the sapphire surface emission and the Cs $7P_{1/2} \rightarrow 6D_{3/2}$ transition ($\omega_{\text{at}}/2\pi = 24.687$ THz, i.e., ~ 12.15 μm or ~ 823 cm^{-1} [41,55,56,59]—see inset of Fig. 1), the CP interaction on Cs($7P_{1/2}$) at short distance (~ 100 nm) narrowly filters the polariton thermal emission at $\omega_p/2\pi \sim 24.5$ THz (~ 1200 K) [41,56]. (ii) Alternately, we evaluate surface polariton properties, i.e., $S(\omega)$ from Eq. (1), with $\epsilon(\omega)$ extrapolated from the broadband FF thermal emission.

In the short distance vW limit, the CP interaction varies as $-C_3 \cdot z^{-3}$ (z : atom-surface distance [41,43,57–59]). The interaction, dominated by infrared transition couplings (see Supplemental Material [63]), strongly varies when the thermal emission of the surface polariton (at ω_p) nearly coincides with an *absorption* transition (at ω_{at} —dipole strength D_{at}) [57,58,63], following

$$C_3(T) - C_3(T=0) = -2D_{\text{at}}^2 \Re[S(\omega_{\text{at}})] \cdot [\exp(\hbar\omega_{\text{at}}/k_B T) - 1]^{-1} + o(T). \quad (2)$$

In Eq. (2), the dominant right-hand-side term depends on the thermal Bose-Einstein factor, and on the surface resonant response (*real*, i.e., dispersion) filtered at ω_{at} ; the $o(T)$ term, residual for $k_B T \geq \hbar\omega_{\text{at}}$, includes the

nonresonant dipole couplings, and a D_{at}^2 contribution remaining insensitive to the surface resonance.

To measure C_3 , frequency-modulated selective reflection spectroscopy (FM-SR) at a vapor interface is a robust method, probing a typical depth $\sim \lambda_{\text{opt}}/2\pi$ [55,56,58,59,87,88]. The measurement results from an optimized fitting of the experimental spectrum, on the basis of a single-parameter family of dimensionless FM-SR spectra [63]. We perform FM-SR on the second resonance doublet of Cs $6S_{1/2} \rightarrow \{7P_{1/2}, 7P_{3/2}\}$ (respectively, $\lambda_{\text{opt}} = 459$ nm, $\lambda_{\text{opt}} = 456$ nm) [59]. As a spectroscopic method, FM-SR yields a differential coefficient $\Delta C_3 = [(C_3(|7P\rangle) - C_3(|6S_{1/2}\rangle))]$, here dominated by $C_3(|7P\rangle)$, i.e., $C_3(|7P_{1/2}\rangle)$ or $C_3(|7P_{3/2}\rangle)$ [59]. Cs($7P_{3/2}$) is primarily investigated for comparison purposes, as only coupled to the remote wing of the sapphire polariton—through $7P_{3/2} \rightarrow \{6D_{3/2}, 6D_{5/2}\}$ transitions, respectively, at 19.259 and 20.544 THz, see inset of Fig. 1 and [63].

Figure 1 synthesizes our $C_3(|7P\rangle, T)$ measurements. For Cs($7P_{1/2}$), $C_3(T)$ nearly triples from 500 to 1100 K, while it gently decreases for Cs($7P_{3/2}$). This growth (owing to $\Re[S(\omega_{\text{at}})] < 0$) evidences the *resonant* coupling between Cs($7P_{1/2}$) and sapphire thermal emission. It slows down at high- T : this signs a temperature modification of the surface resonance, i.e., a T dependence for $\Re[S(\omega_{\text{at}}, T)]$; otherwise, $C_3(T)$ should follow the statistical factor of Eq. (2), governing the dashed and dashed-dotted lines (Fig. 1) derived with Eq. (1) for a constant sapphire permittivity—as measured at ambient temperature only [60,61] (see also [89]). Figure 1 also shows predictions (dotted and thick lines) with a T -dependent sapphire permittivity ([43,62,90] and discussion in [63]): as a trend, the agreement with our NF atomic sensor determinations for $C_3(T)$ is better, but remains relative, even for the thick line derived from our own measurements on sapphire windows from the very same origin than the one of the Cs vapor cell (identically superpolished and annealed, see Refs. [58,63]). Ironically, when considering this careful evaluation of $S(\omega_{\text{at}}, T)$ —detailed below—the agreement is slightly worse than for predictions (dotted line) considering a permittivity $\epsilon(\omega, T)$ [62,63] evaluated from measurements limited to the midinfrared transparency region, on sapphire samples of an unknown origin, and modeled with an additional extrinsic resonance.

From FF thermal emission, that we have recorded with a state-of-the-art spectrometer [91], the complex-valued $\epsilon(\omega, T)$, yielding $S(\omega, T)$, is extracted by fitting [43,63] a modified Lorentz dielectric function model including Gaussian multiphonon contributions *via* self-energy functions (wave number-dependent dampings). Sapphire birefringence adds a touch of complexity: the window at Cs vapor interface is c_{\perp} (cut perpendicular to the c axis) to ensure the cylindrical symmetry of CP interaction, yielding an effective permittivity $\epsilon_{\text{eff}} = (\epsilon_o \cdot \epsilon_e)^{1/2}$ [41,92] (ϵ_o and ϵ_e ,

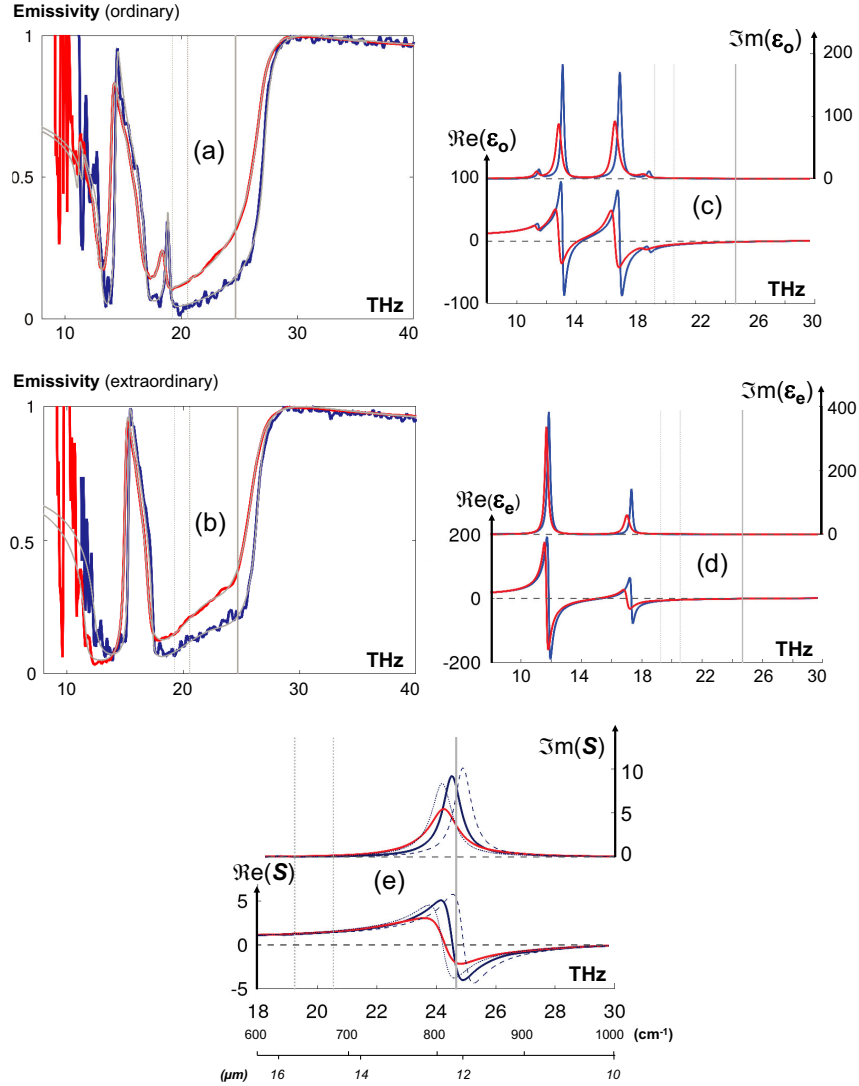


FIG. 2. Sapphire *spectral* response at ~ 500 (blue), and ~ 1000 K (red)—for exact temperatures and more details, see Ref. [63]. Experimental emissivity spectrum (reliable above 12 THz, see Ref. [63]), and analytical fittings (black): (a) c_{\perp} sapphire window, yielding ϵ_o . (b) c_{\parallel} sapphire window and parallel polarization, yielding ϵ_e . Relative permittivity $\epsilon(\omega)$ extrapolated from analytical fits of emissivity: (c) $\epsilon_o(\omega)$; (d) $\epsilon_e(\omega)$. (e) Complex surface response $S(\omega)$ calculated for $\epsilon_{\text{eff}}(\omega) = (\epsilon_o \cdot \epsilon_e)^{1/2}$ (full line), along with ~ 500 K responses $S_o(\omega)$ and $S_e(\omega)$ [from $\epsilon_o(\omega)$ and $\epsilon_e(\omega)$] (respectively, dashed and dotted line). Note the additional horizontal scale in cm^{-1} , and μm , provided for convenience. The vertical markers show the dominant couplings: full line for $\text{Cs}(7P_{1/2})$, dotted lines for $\text{Cs}(7P_{3/2})$.

respectively, the ordinary and extraordinary axes permittivity). The number of intrinsic modes is imposed by crystallography, depending on orientation (4 for ordinary, 2 for extraordinary [41,43,60]). Figure 2 exemplifies the measured and calculated emissivity sapphire spectra [Figs. 2(a)–2(b)] for $T \sim 500$ and $T \sim 1000$ K (more temperatures in [63]). No salient singularities on emissivity [Figs. 2(a)–2(b)] help to locate resonances for $\epsilon(\omega)$ [Figs. 2(c)–2(d)], or $S(\omega)$ [Fig. 2(e)].

Along with thermal enhancement of CP dispersion forces involving *virtual* atom-surface exchanges, surface thermal emission should induce *real* resonant energy

absorption $7P_{1/2} \rightarrow 6D_{3/2}$, with the same z^{-3} spatial dependence [40,57,93]. The reverse $6D_{3/2} \rightarrow 7P_{1/2}$ transfer, analyzed as a Förster-like *quenching* of atomic excitation induced by an absorbing surface mode, had been demonstrated [94], nevertheless without quantitative measurements. We have unsuccessfully attempted to detect directly, as in [94], this $\text{Cs}(7P_{1/2})$ absorption of thermal energy, through an induced $\text{Cs}(6D_{3/2})$ population. Rather, we have extended the use of *linear* FM-SR, from the evaluation of the *dispersive* part of the surface interaction, to quantitative information on the *dissipative* exchanges, checking the relative amplitude of the doublet components

$6S_{1/2} \rightarrow 7P_{1/2}, 7P_{3/2}$. No NF thermal energy transfer is expected for Cs($7P_{3/2}$), while thermal transfer shortens the Cs($7P_{1/2}$) lifetime, specifically implying a spatially-dependent optical width, from γ_∞ in free-space to $\gamma(z) = \gamma_\infty + \Delta\Gamma(T) \cdot z^{-3}$, with

$$\Delta\Gamma(T) = 4 D_{\text{at}}^2 \cdot \Im m[S(\omega_{\text{at}})] \cdot [\exp(\hbar\omega_{\text{at}}/k_B T) - 1]^{-1}. \quad (3)$$

This lifetime shortening of Cs($7P_{1/2}$), governed by $\Im m[S(\omega_{\text{at}})]$, follows the same statistical factor as Eq. (2) [63], and the same z^{-3} dependence. The additional spatial dependence $\gamma(z)$ mostly reduces amplitude of FM-SR spectra, complexifying moderately the line shape family with an additional parameter (see Ref. [63]). Inserting our estimates [Fig. 2(e) and [63]] into Eq. (3) yields $\Delta\Gamma(T = 1000 \text{ K}) \sim 40 \text{ kHz } \mu\text{m}^3$: the amplitude of the $6S_{1/2}-7P_{1/2}$ FM-SR signal should become, at high- T , about twice smaller than for the unaffected $6S_{1/2}-7P_{3/2}$ transition (see Fig. 3). Indeed, close to ω_{at} , $\Re e[S(\omega, T)]$ and $\Im m[S(\omega, T)]$ evolve nearly parallel above $\sim 500 \text{ K}$, yielding $\Im m([S(\omega_{\text{at}}, T)]/\Re e[S(\omega_{\text{at}}, T)]) \sim 1-2$ [63]. Actually, the experimental amplitude ratio (Fig. 3) agrees with $T = 0$ predictions, once standard geometrical ratios for fine and hyperfine components [56,59,95] are included. In view of our measurements accuracy, this implies $\Im m[S(\omega_{\text{at}})]/\Re e[S(\omega_{\text{at}})] \leq 0.1-0.2$.

The discrepancies between our NF measurements and predictions from FF emissivity fitting cannot be explained by uncertainties affecting temperature measurements, atom dipole couplings, or the $C_3(T)$ evaluation from FM-SR spectra (see Ref. [63]). Rather, relatively to expectations from Fig. 2(e), we suspect the polariton resonance to be sharper and red-shifted, because, close to a surface resonance, $S(\omega)$ is merely a complex Lorentzian [96], with $\Im m S(\omega)$ and $\Re e S(\omega)$ associated respectively to absorption

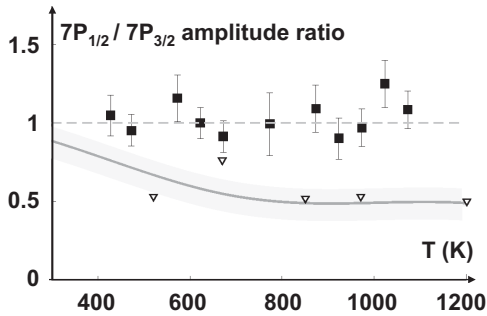


FIG. 3. Temperature dependence of the FM-SR amplitude ratio [$6S_{1/2} \rightarrow 7P_{1/2}$ over $6S_{1/2} \rightarrow 7P_{3/2}$]; amplitudes are normalized to $C_3 = 0$, and to the geometrical factors (fine and hyperfine manifolds [59]). The discrete triangles are predictions evaluated from our $S(\omega, T)$ [Fig. 2(e) and [63]], the thick line is evaluated for $S(\omega, T)$ derived from [62]. The light gray area around the thick line accounts for amplitude ratio dependence with the optical width (central part: $\gamma_\infty = 20 \text{ MHz}$).

and dispersion. Hence, $\Im m[S(\omega_{\text{at}})]/|\Re e S(\omega_{\text{at}})| \ll 1$ implies that ω_{at} falls away from the anomalous dispersion region, with the peak amplitude for $S(\omega)$ largely exceeding $\Re e[S(\omega_{\text{at}})]$; $\Re e[S(\omega_{\text{at}})] < 0$ confirms that ω_{at} lies in the blue wing of the surface resonance. This hypothetical conclusion appears not incompatible with previous observations benefiting of the same Cs/sapphire coincidence at lower temperatures [63]. A complementary test for sapphire could be offered with Rb($7P_{3/2}$), through the dual resonant couplings $7P_{3/2} \rightarrow \{6D_{3/2}, 6D_{5/2}\}$, respectively, at 24.494 and 24.561 THz [56].

Finally, for Cs($7P_{3/2}$), $C_3(T)$ appears slightly above predictions (Fig. 1), here insensitive to the specific modeling of sapphire polariton. This contrasts with the very good agreement found previously for Cs($7D_{3/2}$) [58,63], on the same cell, for a very comparable situation. However, the main T -dependent coupling was at 27.7 THz, in the opposite (blue) wing of the polariton, away from the multiple resonances of sapphire polariton. Uncertainties on $S(\omega, T)$ could be more severe for the red wing of ω_p , where $\epsilon_o(\omega)$ and $\epsilon_e(\omega)$ differ considerably because of birefringence [see Figs. 2(c)–2(d), major resonances respectively at ~ 13.5 and ~ 17 THz, vs ~ 12 THz]. In particular, the major ϵ_e resonance falls partly outside the effective measurement range ($\sim 12-60$ THz, see Ref. [63]), i.e., $\epsilon_e(\omega)$ is extrapolated, rather than resulting from a genuine fitting. Additionally, the ϵ_e resonance appears narrower than the two main resonances for ϵ_o [Fig. 2(d)], and this width impacts the remote wing of ϵ_{eff} , up to ω_{at} .

To summarize, we demonstrate strong magnification of the CP interaction for Cs($7P_{1/2}$) through the resonant coupling to the NF thermally emitted surface polariton. The observed $C_3(T)$, not amenable to Bose-Einstein statistics, evidences a temperature evolution of surface resonance. The FM-SR linearity allows comparing the very different behaviors of the Cs($7P$) doublet components: it reveals unique to provide simultaneously information related to dispersive and dissipative contributions of the surface emission. Predictions classically derived from the fitting of FF thermal emission at high- T for $\Im m[S(\omega_{\text{at}})]$ disagree with FM-SR measurements, so that we suspect the actual surface resonance to be sharper than expected and slightly redshifted. This discrepancy also appears with alternate descriptions of bulk sapphire properties: extrapolation of FF emission to the surface resonance is fragile, and here, birefringence and sapphire multiple resonances bring extra difficulties.

Our results tackle the issue, of a general interest, of accuracy when evaluating surface mode resonances and NF spectral emission. Aside from the large shift between surface and bulk resonances, extrapolating $\epsilon(\omega, T)$ from broadband FF emissivity (or reflectance) [43,60,63] is intrinsically delicate as the complex-valued permittivity has to be derived from a real-valued spectral measurement. This is permitted by the Kramers-Kronig relationship but

requires in the principle to know the entire spectrum. Classically, on a limited spectral range (5–25 μm in our case), a “guessed” analytical shape is optimized for permittivity, leading to a variety of sets of fitting parameters. The resulting ambiguity induces only negligible effects for $\epsilon(\omega)$ and $S(\omega)$ in our modeling [63]. However, all models imply hard-to-test assumptions to describe the very remote wings of $\epsilon(\omega)$ resonance, essential for evaluating $S(\omega_p)$. This would make valuable a direct measurement of the complex refractive index, in the range of the expected surface resonance. Ellipsometry is appropriate for this purpose, but remains underdeveloped in the infrared range and at high- T . The few corresponding measurements rely mostly on “spectroscopic ellipsometry,” based upon an *a priori* description of the permittivity (see, e.g., [61,97]).

Even if we have restricted ourselves to the extreme NF regime, and to thermal exchanges where one of the “materials” (Cs) is a narrow filter ideally known, uncertainties issues for surface resonances remain extremely relevant for longer distances, or for nanostructured interfaces—including exchanges between two-dimensional layered materials [98]. Indeed, unexpected surface responses were often observed [25], evoking complex mechanisms, including non local response [99], strain [60], hot electrons within colder phonon vibrations [100], local glass structure instead of a crystalline one [101], along with chemical residuals [102,103]. Here, the consistency of fitting FM-SR spectra with a z^{-3} potential is confirmed, in a regime dominated by the surface thermal emission: this makes very credible that Cs atoms effectively interact with a neutral surface; oppositely, when deriving $\epsilon(\omega)$ from reflectance measurement, ideal “bulk” homogeneity and local planarity are implicit, ignoring issues of atomistic surface reorganization [104] or low-dimensionality [105].

Evaluating accurately NF thermal emission, including surface resonances, should benefit to various prospects: (i) In Casimir research, oversimplified models describing material properties (e.g., Drude vs plasma [106]) lead to known discrepancies: literature and tabulated data (e.g., [107]) should be scrutinized critically. For CP interaction, NF material properties will govern the fine temperature tuning, turning vW attraction into repulsion, see, e.g., [43]. (ii) Converting thermal surface emission into a quantized excitation (here, the unobserved $7P_{1/2} \rightarrow 6D_{3/2}$ absorption) would open exciting possibilities [108,109], among which selective thermal NF population of molecular vibration modes (e.g. SiC surface modes at 28.5 THz coincide with NH_3 or SF_6 vibrations): this “surface thermal pumping” would ultimately generate specific (non “Boltzmann”) internal energy distributions. (iii) Birefringence, which notably affects sapphire, but SiC too, is shown here to induce dramatic changes of thermal infrared emission bands with orientation [110].

Engineering NF thermal conductivity, isolation, or rectification by orientating microbodies from the same material [10], appears exciting: presently, predicting the orientation dependence of surface resonances remains challenging [111].

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