Intrinsic Nonlinear Hall Detection of the Néel Vector for Two-Dimensional **Antiferromagnetic Spintronics**

Jizhang Wang¹, Hui Zeng,² Wenhui Duan¹,^{2,3,4,5} and Huaqing Huang¹,^{5,6,*} ¹School of Physics, Peking University, Beijing 100871, China

²State Key Laboratory of Low-Dimensional Quantum Physics, Department of Physics, Tsinghua University,

Beijing 100084, China

³Institute for Advanced Study, Tsinghua University, Beijing 100084, China

⁴Frontier Science Center for Quantum Information, Beijing 100084, China

⁵Collaborative Innovation Center of Quantum Matter, Beijing 100871, China

⁶Center for High Energy Physics, Peking University, Beijing 100871, China

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The respective unique merit of antiferromagnets and two-dimensional (2D) materials in spintronic applications inspires us to exploit 2D antiferromagnetic spintronics. However, the detection of the Néel vector in 2D antiferromagnets remains a great challenge because the measured signals usually decrease significantly in the 2D limit. Here we propose that the Néel vector of 2D antiferromagnets can be efficiently detected by the intrinsic nonlinear Hall (INH) effect which exhibits unexpected significant signals. As a specific example, we show that the INH conductivity of the monolayer manganese chalcogenides MnX (X = S, Se, Te) can reach the order of $nm \cdot mA/V^2$, which is orders of magnitude larger than experimental values of paradigmatic antiferromagnetic spintronic materials. The INH effect can be accurately controlled by shifting the chemical potential around the band edge, which is experimentally feasible via electric gating or charge doping. Moreover, we explicitly demonstrate its 2π -periodic dependence on the Néel vector orientation based on an effective $k \cdot p$ model. Our findings enable flexible design schemes and promising material platforms for spintronic memory device applications based on 2D antiferromagnets.

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Introduction.-The desire to reduce the size and power consumption of spintronic devices stimulated the emergence of a new field referred to as two-dimensional (2D) spintronics [1–6]. Two-dimensional materials with atomic thickness have attracted extraordinary interest in spintronics because they not only provide a promising opportunity to push the relevant devices to the 2D limit, but also enable the hopeful exploration of new spintronic phenomena due to their unusual spin-dependent properties, such as the spin-valley coupling of transition metal dichalcogenides [7] and the spin-momentum locking of quantum spin Hall insulators [8]. However, almost all the existing 2D materials proposed for spintronics are nonmagnetic or ferromagnetic [9] (e.g., CrI₃ [10] and CrGeTe₃ [11]). In this Letter, we extend the 2D spintronics to antiferromagnets and show that the Néel vector, which serves as a state variable for 2D antiferromagnetic spintronics, can be detected by the nonlinear Hall measurement.

Antiferromagnets composed of antiferromagnetically coupled magnetic elements are attractive for spintronics because of their faster dynamics, zero stray fields, and insensitivity to magnetic perturbations [12-14]. The robust high-speed manipulation of the Néel vector [15,16], such as ultrafast 90° switching by current-induced spin-orbit torque [17-22] and reproducible 180° reversal by flipping the polarity of the writing current [23,24], have been demonstrated in recent experiments. However, the failure of Néel vector detections via conventional magnetic techniques due to the absence of net magnetization poses a major challenge for practical applications of antiferromagnetic spintronics [12]. Several optical and microscopic methods, such as the spin-polarized scanning tunneling microscopy [25], the x-ray magnetic linear dichroism microscopy [26], the femtosecond pump-probe magneto-optical experiment [27], the spatially resolved second-harmonic generation [28,29], and the diamond nitrogen-vacancy scanning probe magnetometry [30] work for accurate detection of the Néel vector. The anisotropic magnetoresistance (AMR) effect is useful for experimental detection of a 90° rotation but is invariant upon a 180° reversal of the Néel vector, and its small magnitude limits the readout speed and the possible miniaturization [31]. Recently, the reversed Néel vector states have been electrically distinguished by a secondorder magnetoresistance effect [24,32,33], but have been limited in bulk materials. Since the readout speed and size scalability are usually proportional to the magnitude of the response signal which could significantly diminish in the ultimate atomic limit [13,34], it is, therefore, natural to raise the question: how to efficiently detect the Néel vector with a significantly large readout signal for 2D antiferromagnetic spintronics?



FIG. 1. Atomic and band structure of MnS. (a),(b) The top and side view of monolayer MnS with $N \| \hat{x}$ and $N \| \hat{y}$. Red arrows indicate magnetic moments. (c) The band structure of MnS with $N \| \hat{x}$. The insert shows the Brillouin zone. (d) The enlarged plot of bands in small-gap regions.

In this Letter, we predict that the Néel vector of 2D antiferromagnets can be efficiently read out using the intrinsic nonlinear Hall (INH) effect which exhibits a significant signal that can be detected by experimental means. Taking 2D manganese chalcogenide MnX (X = S, Se, Te) as an example, we show that the INH conductivity of the MnS monolayer can reach the order of $nm \cdot mA/V^2$, which is orders of magnitude larger than the experimentally measured values of typical antiferromagnets CuMnAs [24,32] and Mn₂Au [33]. The INH effect can be controlled by shifting the chemical potential via electric gating or charge doping. We further develop an effective $k \cdot p$ model to explain its dependence on the Néel vector direction with a 2π periodicity. Together with the efficient write-in approach based on current-induced spin-orbit torques, our findings constitute promising design schemes and material platforms for 2D antiferromagnetic spintronics.

Atomic and band structures.—Owing to similar crystal structures of 2D MnX, which have been successfully synthesized in experiments [35], we take MnS as an example hereafter and defer the rest to the Supplemental Material [36]. As shown in Fig. 1(a), MnS crystallizes in an AA-stacked bilayer honeycomb lattice, where Mn (and X) atoms on the top and bottom layers (Mn_1 and Mn_2) occupy opposite sublattices. The lattice structure belongs to the space group of $P\bar{3}m1$ (No. 164, D_{3d}^3). Our first-principles calculations [36] show that the magnetic moments are 4.36 μ_B per Mn and are antiferromagnetically ordered, which are consistent with previous studies [47]. The Néel vector N, defined as the difference of the magnetic moments between Mn₁ and Mn₂ in the unit cell, shows significant in-plane anisotropy with the magnetocrystalline anisotropy energy being 0.4 meV/unit cell. For N lying in different in-plane directions, there is little energy difference (see Fig. S5 in the Supplemental Material [36]), indicating that it is possible to electrically manipulate N by current pulses via spin-orbit torques [19,24,48,49]. Importantly, for any arbitrary direction of N denoted by the polar angle θ with respect to the x axis, the spatial and time-reversal symmetry combination (\mathcal{PT}) is preserved.

Figure 1(c) shows the band structure for 2D MnS with $N||\hat{x}$. Because of the \mathcal{PT} symmetry, every band is doubly degenerate. It is noted that some nearly degenerate points (NDPs) lie at Γ at the valence band maximum and along the Γ -M line around $E \approx -0.8$ eV. Since the valence bands are dominated by the S-p orbitals, the weak spin-orbit coupling (SOC) of S only induces slight band splitting at the NDPs [see Fig. 1(d)] compared with MnSe and MnTe [36], which plays a crucial role for the INH effect, as we will discuss later.

INH effect in MnS.-In general, the nonlinear Hall conductivity tensor is defined as the quadratic current response **J** to electric field **E**: $J^{\alpha} = \sum_{\beta \neq \alpha, \gamma} \sigma^{\alpha \beta \gamma} E^{\beta} E^{\gamma}$, where α , β , γ are Cartesian indices. The nonlinear Hall conductivity can be separated into time-reversal-even (T-even) and T-odd parts, but only the latter can be utilized to detect the Néel vector reversal. In 2D antiferromagnets respecting the \mathcal{PT} symmetry, the \mathcal{T} -even Berry curvature dipole (BCD) contribution σ_{BCD} is strictly forbidden [50,51]. In contrast, the T-odd INH conductivity $\sigma_{\rm INH}$ which is allowed becomes an ideal quantity for the Néel vector detection, and is therefore our main concern. Despite the possible presence of extrinsic mechanisms [36], recent experiments show the dominance of σ_{INH} over other contributions [37,38]. The INH conductivity can be expressed in terms of band quantities as [52,53]

$$\sigma_{\rm INH}^{\alpha\beta\gamma} = \int_{\rm BZ} \frac{\mathrm{d}\boldsymbol{k}}{(2\pi)^d} \Lambda^{\alpha\beta\gamma}(\boldsymbol{k}) = \int_{\rm BZ} \frac{\mathrm{d}\boldsymbol{k}}{(2\pi)^d} \sum_n \lambda_n^{\alpha\beta\gamma} \frac{\partial f(\boldsymbol{\epsilon}_n;\boldsymbol{\mu})}{\partial \boldsymbol{\epsilon}_n},$$
(1)

$$\lambda_n^{\alpha\beta\gamma} = v_n^{\alpha} G_{\beta\gamma}^n(\boldsymbol{k}) - v_n^{\beta} G_{\alpha\gamma}^n(\boldsymbol{k}), \qquad (2)$$

$$G^{n}_{\alpha\beta}(\boldsymbol{k}) = 2e^{3} \operatorname{Re} \sum_{m \neq n} \frac{A^{nm}_{\alpha}(\boldsymbol{k}) A^{mn}_{\beta}(\boldsymbol{k})}{\epsilon_{n}(\boldsymbol{k}) - \epsilon_{m}(\boldsymbol{k})}, \qquad (3)$$



FIG. 2. The INH conductivity of MnS. (a) $\sigma_{\text{INH}}^{yxx}$ for $N \| \hat{x}$ and (b) $\sigma_{\text{INH}}^{xyy}$ for $N \| \hat{y}$ as a function of the chemical potential μ . (c),(d) $\sigma_{\text{INH}}^{yyy}$ and $\sigma_{\text{INH}}^{yxx}$ at (c) $\mu = -8$ meV and (d) -795 meV when N rotates in the x-y plane.

where $G^n_{\alpha\beta}(\mathbf{k})$ is the Berry-connection polarizability (BCP) and $\Lambda^{\alpha\beta}(\mathbf{k}) [\lambda_n^{\alpha\beta}(\mathbf{k})]$ is the (band-resolved) BCP dipole. $A^{nm} = \langle u_n | i \nabla_k u_m \rangle$ is the Berry connection with $|u_n\rangle$ the periodic part of the *n*th Bloch state, ϵ_n is the energy of the *n*th Bloch state, \mathbf{v} is the band velocity, $f(\epsilon_n; \mu)$ is the Fermi-Dirac distribution for energy ϵ_n at the chemical potential μ , and *d* is the dimension of the system.

We first analyze the symmetry constraint on σ_{INH} . Taking $N \| \hat{x}$ as an example, the magnetic configuration belongs to the 2'/m magnetic space group. The allowed components are $\sigma_{\text{INH}}^{xzx} = -\sigma_{\text{INH}}^{zxx}$, $\sigma_{\text{INH}}^{yzy} = -\sigma_{\text{INH}}^{zyy}$, $\sigma_{\text{INH}}^{xyx} = -\sigma_{\text{INH}}^{yxx}$, and $\sigma_{\text{INH}}^{yzz} = -\sigma_{\text{INH}}^{zyz}$, while the rest vanishes [36]. Given that the Hall bar for transport measurements of 2D materials is usually set up within the plane, we focus on the in-plane component $\sigma_{\text{INH}}^{yxx}$ ($\sigma_{\text{INH}}^{xyy}$) with N along the x (y) direction for describing the INH effect in 2D MnS. Figures 2(a) and 2(b) show the calculated σ_{INH} as a function of μ . For a down-shift of μ upon hole doping, σ_{INH}^{yxx} and σ_{INH}^{xyy} exhibit significant peaks with opposite signs at $\mu = -8$ and -19 meV near the band edge, and at -795, and -821 meV which are close to the NDPs along the Γ -M line. This signifies that the dominant contributions of σ_{INH} are from these small-gap regions. Remarkably, when N is along the x(y) direction, the peaks of $\sigma_{\text{INH}}^{yxx}$ ($\sigma_{\text{INH}}^{xyy}$) are on the order of nm \cdot mA/V².

It is worth noting that despite the atomically ultrathin 2D nature, the significant value of σ_{INH} in MnS is 2 orders of magnitude larger than the values reported in antiferromagnetic CuMnAs [24,32] and Mn₂Au [33] (~10⁻² nm · mA/V²), which are prototype materials of antiferromagnetic memory devices. The peak value of σ_{INH} in MnS is even comparable to the large σ_{BCD} in \mathcal{T} -invariant few-layer WTe₂ [54,55]. In practice, the

carrier doping for 2D materials ($\sim 10^{13}$ cm⁻²) can be conveniently controlled by electric gating [51,56–59], electron-beam irradiation [60,61], or remote modulation [62,63]. We, therefore, expect that it is experimentally feasible to measure our predicted INH effect in MnS.

Next, we show that σ_{INH} depends sensitively on the direction of *N*. As shown in Figs. 2(c) and 2(d), both $\sigma_{\text{INH}}^{xyy}$ and $\sigma_{\text{INH}}^{yxx}$ exhibit a 2π periodicity when *N* rotates in the plane, which satisfies the *T*-odd constraint that $\sigma_{\text{INH}}(\theta) = -\sigma_{\text{INH}}(\theta + \pi)$. The angular dependence of σ_{INH} is approximately described by cosine or sine trigonometric functions. Therefore, the reorientation of *N* can be fully detected by measuring the INH effect, which is a unique merit over the conventional AMR-based approach that cannot distinguish a 180° reversal. In particular, the sign of $\sigma_{\text{INH}}^{yxx}$ ($\sigma_{\text{INH}}^{xyy}$) can be used to distinguish *N* reversal in the $\pm x$ direction ($\theta = 0$ or π) [in $\pm y$ direction ($\theta = \pi/2$ or $3\pi/2$)]. Therefore, the INH effect can serve as a powerful tool for detecting *N*.

To gain underlying insight into the behavior of $\sigma_{\text{INH}}^{yxx}$, we analyze the band-resolved BCP dipole $\lambda_n^{yxx}(k)$, which exhibits the contribution to $\sigma_{\text{INH}}^{yxx}$ from each band. Similar to other band geometric quantities such as the Berry curvature, $\lambda_n^{yxx}(k)$ encodes the interband coherence. Figure 3(a) shows the energy difference between the top two valence bands, where one NDP at Γ and six along Γ -*M* lines can be observed. In addition, the small-gap region forms a snowflakelike shape centered at Γ . These NDPs give rise to small denominators for the BCP in Eq. (3) and hence a large contribution to λ_n^{yxx} for the top two valance bands, as shown in Fig. 3(b).

Owing to the derivative of the Fermi-Dirac function $\partial f/\partial \epsilon \approx \delta(\epsilon - \mu)$ in Eq. (1), $\sigma_{\rm INH}$ is a Fermi-surface property. Therefore, only NDPs close to μ make significant contributions to $\sigma_{\rm INH}$. To examine the *k*-resolved contribution for different $\sigma_{\rm INH}$ peaks, we plot the distribution of the BCP dipole $\Lambda^{yxx}(k)$ for different peaks of $\sigma_{\rm INH}^{yxx}$, as shown in Figs. 3(c) and 3(d). The calculated Λ^{yxx} at $\mu = -19$ meV mainly distributes around Γ , while the dominant contribution to Λ^{yxx} at $\mu = -795$ meV comes from the small-gap region including the rest NDPs. This indicates that a large $\sigma_{\rm INH}$ can be achieved by tuning μ toward such regions.

As shown in Figs. 3(c)–3(e), despite complicated sign changes of Λ^{yxx} , it is actually an even function with respect to Γ -*M* due to the additional constraint from crystalline symmetries \mathcal{M}_x for $N \| \hat{x}$. On the contrary, Λ^{xyy} is dictated to be an odd function with respect to \mathcal{M}_x [see Fig. 3(e)], which leads to the disappearance of $\sigma_{\text{INH}}^{xyy}$ at $\theta = 0$ (and π) [see Fig. 2(d)]. Similarly, for $N \| \hat{y}, \Lambda^{xyy}$ becomes an even function with respect to Γ -*K*, but the preserved symmetry C_{2x} demands that Λ^{yxx} be an odd function (see Fig. S9 in the Supplemental Material [36]). Although the distribution of $\Lambda^{\alpha\beta\gamma}$ seems unaltered when *N* rotates from \hat{x} to \hat{y} , our detailed analysis indicates that it delicately changes to



FIG. 3. (a) Energy difference between top two valence bands in the Brillouin zone. (b) The band-resolved BCP dipole λ_n^{yxx} for the top two valence bands (n = 19 and 21) for $N \parallel \hat{x}$. The distribution around two NDPs are enlarged. (c)–(e) *k*-resolved distribution of (c) Λ^{yxx} at $\mu = -19$ meV, (d) Λ^{yxx} at -795 meV, and (e) Λ^{xyy} at -795 meV for $N \parallel \hat{x}$. The insert in (c) shows the enlarged plot of Λ^{yxx} around Γ at -19 meV. The vertical green dashed lines in (b)–(e) indicate the mirror symmetry \mathcal{M}_x perpendicular to the *x* axis.

satisfy different symmetry constraints, which results in distinct σ_{INH} after integrating over the whole Brillouin zone.

Effective $k \cdot p$ *model.*—To better understand the Néel vector orientation dependence of σ_{INH} in MnS, we construct an effective $k \cdot p$ model to describe the top two valence bands around Γ . To do so, we first establish an effective model with D_{3d} symmetry and then consider the antiferromagnetism by introducing opposite Zeeman exchange fields for two sublattices. We start from the antibonding and bonding states of S-p orbitals on two sublattices, $|\eta = \pm, p_{\alpha}, s\rangle =$ $(1/\sqrt{2})(|S_1, p_{\alpha}, s\rangle \pm |S_2, p_{\alpha}, s\rangle)$, where α indicates $p_x \pm$ ip_{v} orbitals and $s = \uparrow \downarrow$ for spin. We label the sublattice, orbital, and spin degree of freedom with Pauli matrices λ , τ , and σ , respectively. The symmetry operations of the D_{3d} group are represented as $C_{3z} = \lambda_0 \otimes \exp(-i2\pi\tau_z/3) \otimes$ $\exp\left(-i\pi\sigma_z/3\right), \ \mathcal{M}_y = \lambda_0 \otimes -\tau_x \otimes -i\sigma_x, \ \mathcal{P} = \lambda_z \otimes -\tau_0 \otimes \sigma_0,$ $\mathcal{T} = \lambda_0 \otimes -\tau_x \otimes -i\sigma_y K$, where K is the complex conjugate operator. In this representation, the full eight-band Hamiltonian reads as

$$H = \begin{pmatrix} H_{+} & T_{x} - iT_{y} \\ T_{x} + iT_{y} & H_{-} \end{pmatrix} + J\lambda_{x}\tau_{0}(\boldsymbol{n}\cdot\boldsymbol{\sigma}), \quad (4)$$

where H_{\pm} are the antibonding and bonding subspace Hamiltonian, T_y couples two sublattices, and T_x is the coupling of orbitals within one sublattice (see the Supplemental Material [36]). The last term represents the Zeeman exchange field where J is the coupling strength and $\mathbf{n} = (n_x, n_y, n_z)$ represents the Néel vector orientation. To describe the top two valence bands, we then downfold the Hamiltonian to the antibonding subspace based on the Löwding perturbation method [64,65], which yields

$$\begin{split} H_{\text{eff}} &= H_{D_{3d}} + H_{n,\parallel} + H_{n,\perp}, \\ H_{D_{3d}} &= C_0 + C_1 k^2 + (C_2 + C_3 k^2) \tau_z \sigma_z + C_4 k_-^2 \tau_x \sigma_0 \\ &\quad + C_5 k_+^2 \tau_z \sigma_y, \\ H_{n,\parallel} &= A_1 (k_y n_x - k_x n_y) + A_2 (k_y n_x - k_x n_y) \tau_z \sigma_z \\ &\quad + A_3 [(k_y n_x + k_x n_y) \tau_x + (k_y n_y - k_x n_x) \tau_y] \sigma_0, \\ H_{n,\perp} &= A_4 (k_y \tau_z \sigma_x - k_x \tau_z \sigma_y) n_z + A_5 (k_y \tau_y - k_x \tau_x) \sigma_0 n_z, \end{split}$$
(5)

where $k_{\pm} = k_x \pm ik_y$, $k^2 = k_x^2 + k_y^2$. C_i are materialdependent parameters, among which C_2 and C_3 represent the SOC-induced band splitting. A_i are related to antiferromagnetism.

As illustrations, let us consider the case of $N \| \hat{x} \|$ [i.e., n = (1, 0, 0)]. Keeping up to the lowest order of k, we arrive at

$$H_{\text{eff}}^{(100)}(k) = C_0 + A_1 k_y + (C_2 + A_2 k_y) \tau_z \sigma_z + A_3 (k_y \tau_x - k_x \tau_y).$$
(6)

This is a tilted massive Dirac model where C_2 is the SOC-induced mass controlling the gap and A_1 represents the antiferromagnetic-induced tile of the Dirac cone. The energy spectrum is given by $E = C_0 + A_1 k_y \pm \sqrt{(C_2 + A_2 k_y)^2 + A_3^2 (k_x^2 + k_y^2)}$. In this model, the non-vanishing component is $\sigma_{\text{INH}}^{yxx} = -\sigma_{\text{INH}}^{xyx}$ which exhibits two peaks with opposite signs when μ approaches the small-gap region, consistent with Fig. 2(a). Because the quadratic



FIG. 4. (a) The 90° *N* switching is controlled by two orthogonal writing currents. (b) The 180° *N* reversal is controlled by flipping the polarity of the writing current. The write current (red arrows) and the corresponding preferred Néel vector orientations (red double arrows) are labeled "0" and "1." The readout is performed by injecting a probing current I^{ω} and measuring the nonlinear transverse voltage $V^{2\omega}$.

terms of k, which would bend over the upper valence band significantly, are neglected in the above model [Eq. (6)], the quantitative discrepancy would be eliminated once these terms are included (see Figs. S1–S2 in the Supplemental Material [36]).

Interestingly, when *N* rotates in the *x*-*y* plane with a polar angle θ with respect to the *x* axis, it is convenient to obtain the effective model by a coordinate transformation. Consequently, the σ_{INH} transform as

$$\sigma_{\text{INH}}^{yxx}(\theta) = \cos(\theta)\sigma_{\text{INH}}^{yxx}(0), \tag{7}$$

$$\sigma_{\text{INH}}^{xyy}(\theta) = -\sin(\theta)\sigma_{\text{INH}}^{yxx}(0), \qquad (8)$$

which is consistent with the θ -dependent behavior of σ_{INH} in Fig. 2(c). Similarly, for σ_{INH} at $\mu \approx -800$ meV, we construct an effective model with three pairs of overtilted massive Dirac cones [66,67] that are related by symmetry, and the angular dependence of σ_{INH} is attributed to the *N*-dependent tilts that are not canceled within Dirac cone pairs [36]. Thus, the effective $k \cdot p$ model qualitatively explains the large σ_{INH} at small-gap regions and its special angular dependence in MnS. These INH features are expected in 2D \mathcal{PT} -symmetric antiferromagnets with similar band structures.

Discussion and summary.—In usual Hall measurements with a planar geometry of the setup, the applied electric field may be along a general direction instead of aligning with the crystal axes. When one applies an in-plane electric field $\mathbf{E} = E(\cos \phi, \sin \phi, 0)$ where ϕ is the polar angle with respect to the x axis, the measured in-plane INH current (along the perpendicular direction) is

$$J_{\rm INH} = \sigma_{\rm INH}^{\rm in-plane}(\theta, \phi) E^2, \qquad (9)$$

where the angle-dependent INH conductivity is

$$\sigma_{\text{INH}}^{\text{in-plane}}(\theta,\phi) = \cos(\theta-\phi)\sigma_{\text{INH}}^{yxx}(0).$$
(10)

The INH conductivity is maximized (minimized) when E and N are parallel (antiparallel), but vanishes when they are perpendicular.

The above functionality motivates us to propose a 2D antiferromagnetic memory device based on the standard Hall-bar setup. As shown in Fig. 4, reversible orthogonal switching or 180° reversal of N, which represents two memory states, can be controlled by applying the writing current along two orthogonal directions [17-19,68,69] or flipping its polarity [23,24]. In both schemes, the INH detection of N can be performed by injecting a probing current I^{ω} with frequency ω and measuring the transverse voltage with double frequency $V^{2\omega}$, which has been implemented in previous nonlinear Hall measurements [51,54,70–75]. However, the two states in Fig. 4(a) [4(b)] are represented by zero and finite signals (two opposite signals). In addition, second harmonic Hall signals due to the slight derivation of N perturbed by the currentinduced torques could be detectable by external magnetic field scans [76-78].

In summary, we have predicted the INH detection of N in 2D antiferromagnets MnX, which provides a promising material platform and efficient electric readout approach for 2D antiferromagnetic spintronics. Combined with the high-speed write-in scheme using picosecond current pulses, it is possible to achieve ultrafast and multilevel memory device applications based on 2D antiferromagnets. For example, six-level triaxial memories with N parallel or antiparallel to MnS axes can be constructed since the INH effect enables one to distinguish these states and their reversed images. In addition, the vast number of 2D antiferromagnetic semiconductors, such as MnPS₃ [29,79–81], TaCoTe₂ [82], Fe₂TeO₆ and SrFe₂S₂O [83], bilayer Fe₃GeTe₂ [84], and CrCl₃ [85], hold great promise for future research.

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J. W. and H. Z. contributed equally to this work.

^{*}Corresponding author.

huaqing.huang@pku.edu.cn

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