Control of the Radiative Heat Transfer in a Pair of Rotating Nanostructures

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The fluctuations of the electromagnetic field are at the origin of the near-field radiative heat transfer between nanostructures, as well as the Casimir forces and torques that they exert on each other. Here, working within the formalism of fluctuational electrodynamics, we investigate the simultaneous transfer of energy and angular momentum in a pair of rotating nanostructures. We demonstrate that, due to the rotation of the nanostructures, the radiative heat transfer between them can be increased, decreased, or even reversed with respect to the transfer that occurs in the absence of rotation, which is solely determined by the difference in the temperature of the nanostructures. This work unravels the unintuitive phenomena arising from the simultaneous transfer of energy and angular momentum in pairs of rotating nanostructures.

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Radiative heat transfer between material structures originates from the thermal fluctuations of the electromagnetic field [1]. When the distance between the structures is much smaller than the wavelength of the thermal radiation, the radiative heat transfer can greatly surpass the predictions of Planck's law due to the contribution of the near-field components of the electromagnetic field [2–7]. If the dimensions of the structures also fall within that range, the strong responses produced by their electromagnetic resonances provide a further enhancement of the radiative heat transfer [8–15].

Another important phenomenon originating from the vacuum and thermal fluctuations of the electromagnetic field is Casimir interactions [16–19]. These interactions produce forces and torques between neutral objects [20–27], which can play an important role in the mechanical behavior of nanostructures [28,29]. For instance, the Casimir force produces a friction for two parallel surfaces in relative motion as well as for an atom moving near a surface [30–32]. Analogously, the Casimir torque acting on a rotating nanostructure generates a friction that opposes the rotation and eventually stops it [33–37]. For systems containing multiple nanostructures, the Casimir torque enables the transfer of angular momentum between them [38–40]. Furthermore, these phenomena can even result in an analog to the Sagnac effect [41].

Radiative heat transfer and Casimir interactions are usually investigated separately. The former is typically studied for ensembles of motionless nanostructures, while, for the latter, it is common to assume that all of the nanostructures are at the same temperature. However, as we show in this Letter, the interplay between radiative heat transfer and Casimir interactions can give rise to very interesting phenomena.

In this Letter, we characterize the transfer of energy and angular momentum in a pair of rotating nanostructures with different temperatures and rotation frequencies. Thanks to the simultaneous study of both phenomena, we demonstrate that the rotation of the nanostructures can significantly modify the radiative heat transfer between them. In the absence of rotation, the energy transfer is determined by the difference in the temperature of the nanostructures, and is always directed from the hot nanostructure to the cold one [11, 12, 42]. However, when the nanostructures rotate, the radiative heat transfer can be enhanced, reduced, or even reversed, i.e., made to go from the cold nanostructure to the hot one, by adjusting their rotation frequencies. Our results, which are based on the fluctuational electrodynamics framework [43,44] and the dipolar approximation [45–49], provide the theoretical foundations to understand how the transfer of angular momentum modifies the transfer of energy in pairs of rotating nanostructures.

The system under consideration is depicted in Fig. 1. It consists of two axially symmetric nanostructures separated by a distance *l* along their symmetry axis, which we choose to be the *z* axis. The nanostructures have dimensions D_1 , D_2 and d_1 , d_2 along the directions perpendicular and parallel to the *z* axis, respectively. They rotate around the *z* axis with rotation frequencies Ω_1 and Ω_2 . The temperatures of the nanostructures, as defined in the frame at rest with each of them, are T_1 and T_2 while, for the environment, it is T_0 . We assume that the size of the nanostructures is significantly smaller than both their separation and the relevant wavelengths of the system, which are determined by the temperature of the nanostructures as well as their rotation and resonance

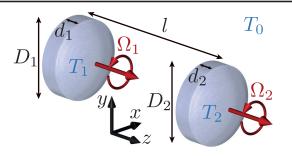


FIG. 1. The system under study consists of two axially symmetric nanostructures separated by a distance l along the z axis. The nanostructures have dimensions D_1 , d_1 and D_2 , d_2 , are at temperatures T_1 and T_2 , and rotate with frequencies Ω_1 and Ω_2 . The temperature of the environment is T_0 .

frequencies. These assumptions allow us to work within the dipolar approximation, in which the nanostructures are modeled as electric point dipoles.

We are interested in simultaneously studying the transfer of angular momentum and energy between the rotating nanostructures. To characterize these transfers, we calculate, respectively, the power radiated by the nanostructures and the electromagnetic torque acting on them. Within the dipolar limit, the torque acting on nanostructure 1 is given by $M_1 = \langle \mathbf{p}_1(t) \times \mathbf{E}_1(t) \rangle \cdot \hat{\mathbf{z}}$, while the power that it radiates is $P_1 = -\langle \mathbf{E}_1(t) \cdot \partial \mathbf{p}_1(t)/\partial t \rangle$. Here, $\mathbf{p}_1(t)$ and $\mathbf{E}_1(t)$ represent the self-consistent electric dipole and electric field in nanostructure 1 and the brackets indicate the average over fluctuations, which we perform using the fluctuation-dissipation theorem [33,50,51]. Following the procedure described in [52], we obtain the following expressions for the torque:

$$M_1 = -\int_{-\infty}^{\infty} d\omega [F^+ N_1^- - G^+ N_2^-]$$
(1)

and the power radiated:

$$P_1 = \int_{-\infty}^{\infty} d\omega \omega [F^+ N_1^- - G^+ N_2^- + F^z N_1^z - G^z N_2^z], \quad (2)$$

where $N_i^- = n(T_i, \omega - \Omega_i) - n(T_0, \omega)$ and $N_i^z = n(T_i, \omega)/2 - n(T_0, \omega)/2$, with $n(T, \omega) = [\exp(\hbar\omega/k_BT) - 1]^{-1}$. Furthermore, the functions F^{ν} and G^{ν} are defined as $F^{\nu} = (2\hbar/\pi)|h^{\nu}|^2 \text{Im}\{\chi_1^{\nu}\}\text{Im}\{g_0 + \alpha_2^{\nu}(g^{\nu})^2\}$ and $G^{\nu} = (2\hbar/\pi)|h^{\nu}g^{\nu}|^2 \text{Im}\{\chi_1^{\nu}\}\text{Im}\{\chi_2^{\nu}\}$, with $h^{\nu} = [1 - \alpha_1^{\nu}\alpha_2^{\nu}(g^{\nu})^2]^{-1}$, $\chi_i^{\nu} = \alpha_i^{\nu} - g_0|\alpha_i^{\nu}|^2$, $g_0 = 2ik^3/3$, $g^{\nu} = \exp(ikl)[(1 - \delta_{\nu z})k^2/l + (1 - 3\delta_{\nu z})(ik/l^2 - 1/l^3)]$, $k = \omega/c$, and $\delta_{\nu\mu}$ being the Kronecker delta. Importantly, we can obtain analogous expressions for nanostructure 2 by interchanging the indices $1 \leftrightarrow 2$ in Eqs. (1) and (2).

In these expressions, α_i^z represents the component of the polarizability of the nanostructure along the *z* axis, which is not affected by the rotation. On the other hand, α_i^{\pm} denotes the components of the effective polarizability seen from the

frame at rest, in the basis formed by the unit vectors $\hat{\mathbf{e}}^{\pm} = (\hat{\mathbf{x}} \pm i\hat{\mathbf{y}})/\sqrt{2}$. The calculation of these components is not trivial. If the intrinsic response of the nanostructure is assumed to remain unchanged by the rotation, and the Coriolis and centrifugal effects are neglected, the effective polarizability only accounts for the effect of the Doppler shift caused by the rotation [23,33–35,55–58]. However, it was later shown that the inclusion of these effects gives rise to corrections that can partially or completely cancel the effect of the Doppler shift and introduce other dependences with the rotation frequency [40,59–61].

Equations (1) and (2) allow us to calculate the transfer of angular momentum and energy between the rotating nanostructures by numerically computing the integrals over frequency. Nevertheless, they do not provide direct insight into the physical mechanisms behind these phenomena. Here, instead, we derive closed-form analytical expressions by considering the following approximations. First, we assume that the rotation frequencies Ω_1 and Ω_2 , as well as the thermal frequencies $\theta_1 = 2\pi k_B T_1/\hbar$ and $\theta_2 = 2\pi k_B T_2/\hbar$, are all much smaller than both c/l and the resonance frequencies of the nanostructures $\omega_{r,1}$ and $\omega_{r,2}$. Second, we assume that $D_1 \gg d_1$ and $D_2 \gg d_2$, which allows us to neglect the component of the polarizabilities along the z axis for both nanostructures. Moreover, as shown in [52], we describe α_i^{\pm} using a harmonic oscillator model and taking into account the Coriolis and centrifugal effects. With the approximations described above, the polarizability reduces to $\alpha_i^{\pm}(\omega) \approx a_i [1 + i(\omega \mp \Omega_i)\gamma_i/\omega_{r_i}^2]$, where γ_i is the nonradiative damping of the electromagnetic resonance, and a_i is a constant with units of polarizability. Finally, we neglect multiple scattering effects, i.e., $h^{\nu} \approx 1$. Upon applying all of these approximations, the torque acting on nanostructure 1 can be approximated by

$$\frac{M_1}{C} = -(\Omega_1 - \Omega_2)(\theta_1^2 + \theta_2^2) - 2(\Omega_1 - \Omega_2)^3, \quad (3)$$

and the power radiated by

$$\frac{P_1}{C} = \frac{\Pi_1}{C} + \frac{1}{2} (\theta_1^2 - \theta_2^2) (\Omega_1 - \Omega_2)^2 + (\Omega_1^2 - \Omega_2^2) \left[\frac{1}{2} (\theta_1^2 + \theta_2^2) + (\Omega_1 - \Omega_2)^2 \right].$$
(4)

Here, $\Pi_1 = C(\theta_1^4 - \theta_2^4)/10$ represents the power radiated by nanostructure 1 when neither of the nanostructures rotate, which has the same dependence with temperature as the Stefan-Boltzmann law. Furthermore, *C*, defined as

$$C = \frac{\hbar}{6\pi} \left(\frac{\gamma_1 \gamma_2}{\omega_{r,1}^2 \omega_{r,2}^2} \right) \left(\frac{a_1 a_2}{l^6} \right),$$

contains all of the information of the electromagnetic response of the nanostructures, and, in particular, of their

material properties. Again, analogous expressions for nanostructure 2, i.e., M_2 and P_2 , can be obtained by interchanging the indices $1 \leftrightarrow 2$.

The expressions above fully describe the transfer of angular momentum and energy between the two nanostructures. Examining them, we can readily verify that $M_1 + M_2 = 0$ and $P_1 + P_2 = 0$, which tells us that, under the approximations considered above, there is no transfer of angular momentum or energy between the nanostructures and the environment. For this reason, the two rotating nanostructures behave as a closed system. This is, indeed, expected, since the transfer to the environment occurs through far-field radiation, which, with the approximations detailed above, is negligible compared with the near-field interactions that determine the transfer between the nanostructures. Therefore, in the remainder of this work, we refer to P_1 as the power transferred between the nanostructures.

Equations (3) and (4) show that the torque and the power transferred depend on both the temperatures and the rotation frequencies of the two nanostructures. In particular, the sign of the torque is determined by the difference between the rotation frequencies of the nanostructures, and therefore vanishes when their rotation is synchronized. On the other hand, the temperature of the nanostructures only affects the magnitude of the torque, which remains finite even for $\theta_1 = \theta_2 = 0$, provided that $\Omega_1 \neq \Omega_2$.

The power transferred, however, shows a very different behavior: both its sign and magnitude depend on a nontrivial interplay between the rotation frequencies and the temperatures of the nanostructures. Interestingly, examining the last term of Eq. (4), we note that it is possible to obtain a nonzero P_1 even when the nanostructures have equal temperatures. In other words, the rotation of the nanostructures enables a transfer of energy, as if there were a temperature difference between them. To analyze this effect, we calculate the ratio between the temperatures $\xi = \theta_1/\theta_2$ that two nonrotating nanostructures need to have to produce the same power transferred as two rotating nanostructures with equal temperatures $\theta_1 = \theta_2$. This ratio, which is given by

$$\xi = \left\{ 1 + 10 \frac{\Omega_1^2 - \Omega_2^2}{\theta_2^2} \left[1 + \frac{(\Omega_1 - \Omega_2)^2}{\theta_2^2} \right] \right\}^{1/4}$$

is plotted in Fig. 2 as a function of both Ω_1 and Ω_2 . Examining these results, we observe that, for $|\Omega_1| > |\Omega_2|$, $\xi > 1$, while for, for $|\Omega_1| < |\Omega_2|$, the opposite is true. This means that, for nanostructures with equal temperatures, the power is always transferred from the nanostructure with the larger magnitude of rotation frequency to the nanostructure with the smaller one. Furthermore, the minimum and maximum values of ξ are achieved when the magnitude of the rotation frequency of one of the nanostructures is much smaller than the other. On the other hand, when

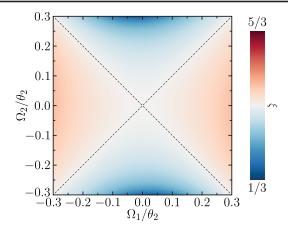


FIG. 2. Effective temperature ratio ξ for two nanostructures rotating with different frequencies. The dashed lines indicate the values of Ω_1 and Ω_2 for which the ratio is equal to one.

 $|\Omega_1| = |\Omega_2|$ (dashed lines), the temperature ratio is one and, therefore, the power transferred vanishes.

The results of Fig. 2 demonstrate that, for two nanostructures with equal temperatures, the rotation induces a transfer of energy and hence is effectively equivalent to a temperature difference. Therefore, if the nanostructures have different temperatures, we expect the rotation to modify the power transferred and even allow its direction to be changed. In order to explore this possibility, in Fig. 3, we plot P_1/Π_1 as a function of Ω_1 and Ω_2 for $\theta_1 = 1.5\theta_2$. We use black solid and dashed curves to indicate the frequencies for which P_1/Π_1 is equal to 0 and 1, respectively. These curves separate the results into three different regimes. In the first regime, $P_1/\Pi_1 > 1$, so the rotation serves to increase the power transferred between the nanostructures with respect to the nonrotating case. The enhancement is maximum when the nanostructures rotate in opposite directions but with the hotter nanostructure rotating faster than the colder one. The second regime is characterized by $0 < P_1/\Pi_1 < 1$, which means that the rotation reduces the power transferred. In this case, the contribution to P_1 of the terms in Eq. (4) that depend on the rotation frequencies counteract Π_1 , thus producing a decrease in the power transferred. When the combination of these terms surpasses Π_1 in magnitude, the power transferred changes its direction, going from the colder nanostructure to the hotter one. This corresponds to the third regime for which $P_1/\Pi_1 < 0$. Importantly, this effect is maximized when the nanostructures rotate in opposite directions with the colder nanostructure rotating faster than the hotter one. The results of Fig. 3 confirm that the transfer of angular momentum between the rotating nanostructures modifies the transfer of energy. Indeed, when $\Omega_1 = \Omega_2$, the transfer of angular momentum vanishes (since $M_1 = 0$) and, expectedly, $P_1 = \Pi_1$.

In order to get insight into the physical mechanisms that give rise to the different regimes illustrated in Fig. 3,

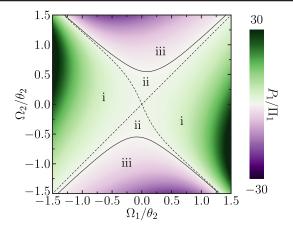


FIG. 3. Power transferred between two rotating nanostructures normalized to Π_1 for $\theta_1 = 1.5\theta_2$. The black solid and dashed curves signal $P_1/\Pi_1 = 0$ and $P_1/\Pi_1 = 1$, respectively, while the labels indicate the regimes in which $P_1/\Pi_1 > 1$ (i), $0 < P_1/\Pi_1 < 1$ (ii), and $P_1/\Pi_1 < 0$ (iii).

we analyze the change in the internal energy of the nanostructures. For nanostructure 1, this quantity is defined as $\dot{U}_1 = -P_1 - M_1\Omega_1$, where $-M_1\Omega_1$ represents the rate of decrease of its mechanical energy. Notice that we define the internal energy as all of the energy of the nanostructure that is not mechanical. Upon insertion of Eqs. (3) and (4), we obtain

$$\frac{\dot{U}_1}{C} = -\frac{\Pi_1}{C} + \theta_2^2 (\Omega_1 - \Omega_2)^2 + (\Omega_1 - \Omega_2)^4,$$

with a similar expression for nanostructure 2 obtained by interchanging the indices $1 \leftrightarrow 2$. While the first term of the equation corresponds to the power radiated in absence of rotation, the rest of the terms, which are always positive, only contribute when there is a difference in the rotation frequencies. We can also compute the change in the internal energy of the entire system, which is given by

$$\frac{\dot{U}_1 + \dot{U}_2}{C} = (\theta_1^2 + \theta_2^2)(\Omega_1 - \Omega_2)^2 + 2(\Omega_1 - \Omega_2)^4.$$

Interestingly, this quantity always increases, regardless of the temperatures of the nanostructures. Note that, since this is a closed system, this increase in the internal energy must come from a decrease in the mechanical energy of the system. The equations above provide us with information about the equilibrium conditions for the system. In particular, to simultaneously obtain $\dot{U}_1 = 0$ and $\dot{U}_2 = 0$, it is necessary that $\theta_1 = \theta_2$ and $\Omega_1 = \Omega_2$.

Figure 4 compares the value of the power transferred (black curve) with the rates of change of the mechanical (blue curves) and internal energy (red curves) of the nanostructures. We use solid and dashed curves for nanostructures 1 and 2, respectively. We assume $\Omega_1 = 0.5\Omega_2$

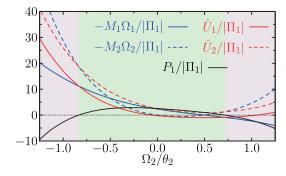


FIG. 4. Power transferred (black curve) and rates of change in mechanical energy (blue curves) and internal energy (red curves) for nanostructure 1 (solid curves) and 2 (dashed curves). All quantities are normalized to $|\Pi_1|$. We assume $\Omega_1 = 0.5\theta_2$ and $\theta_1 = 1.5\theta_2$. Regions of negative (positive) P_1 are indicated with a purple (green) background.

and $\theta_1 = 1.5\theta_2$ and plot all of the values as a function of Ω_2 . Unlike in Fig. 3, here, we normalize all of the quantities to $|\Pi_1|$ so their sign is not altered. We signal the regions in which the power transferred is reversed using a purple background, while the green background indicates that P_1 goes in the direction of Π_1 . As expected, the boundaries between these two regions are located at the values of Ω_2 for which the red and blue curves cross, since, at these points, the power transferred between the nanostructures vanishes. Furthermore, in the regions where the direction of the power transferred is reversed, the rate of decrease in mechanical energy of the colder nanostructure, $-M_2\Omega_2$, is larger than all of the other terms analyzed. This means that, for the colder nanostructure, the decrease in mechanical energy is larger than the increase in its internal energy. For the hotter nanostructure, on the other hand, we observe the exact opposite situation, that is, $\dot{U}_1 > -M_1\Omega_1$. This combination of behaviors is at the origin of the reversal of the direction of the power transferred. Indeed, the power transferred satisfies $2P_1 = U_2 \dot{U}_1 + M_2 \Omega_2 - M_1 \Omega_1$. Therefore, in order to reach $P_1 < 0$ for $\theta_1 > \theta_2$, it is necessary that $-M_2\Omega_2 + M_1\Omega_1 > U_2 - U_1$. This condition is clearly satisfied in the regions with a purple background, thus confirming that the change in the direction of the power transferred is associated with the imbalance between the decrease in the mechanical energy and the change in the internal energy of the nanostructures.

In summary, we have studied the simultaneous transfer of energy and angular momentum in a pair of rotating nanostructures. To that end, working within the framework of fluctuational electrodynamics and the dipolar approximation, we have derived analytical expressions for the torque and power transferred between the nanostructures. We have shown that, for equal temperatures but different rotation frequencies, there is a power transferred from the nanostructure that rotates faster to the one rotating at a slower frequency. When there is also a difference in the temperatures of the nanostructures, the power transferred displays a rich behavior arising from the nontrivial interplay between temperature and rotation frequency. In particular, we have shown that, depending on the rotation frequency of the nanostructures, the power transferred can be enhanced or reduced with respect to that of a nonrotating pair. Furthermore, it is also possible to reverse the direction of the transfer of energy, making it go from the colder to the hotter nanostructure. It is worth noting that our results are derived in the limit in which the thermal and rotation frequencies are much smaller than the resonances of the nanostructures. Therefore, the behaviors described here can be enhanced by exploiting the electromagnetic resonances of the system. Moreover, although we have considered a pair of nanostructures as a canonical example, our model can be readily applied to any material structure with a dipolar resonance as, for instance, a large molecule. Importantly, the range of temperatures for which the effects described in this work can take place is determined by the rotation frequencies of the nanostructures. This means that for temperatures of the order of 1 K, the rotation frequencies need to be ~100 GHz. These rotation frequencies are within experimental reach for molecules like fullerenes [62] and are one to two orders of magnitude beyond the rotation frequencies already achieved for nanostructures [63-65]. Our work provides fundamental understanding of how the transfer of angular momentum produced by the Casimir torque modifies the transfer of energy in rotating nanostructures. Therefore, the results of this work can be exploited to find new avenues to control the radiative heat transfer between nanoscale objects.

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