


## NMR Surface Relaxivity in a Time-Dependent Porous System

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We demonstrate an unexpected decay-recovery behavior in the time-dependent  $^1\text{H}$  NMR relaxation times of water confined within a hydrating porous material. Our observations are rationalized by considering the combined effects of decreasing material pore size and evolving interfacial chemistry, which facilitate a transition between surface-limited and diffusion-limited relaxation regimes. Such behavior necessitates the realization of temporally evolving surface relaxivity, highlighting potential caveats in the classical interpretation of NMR relaxation data obtained from complex porous systems.

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While functional porous materials underpin a vast array of processes of importance to the energy, environment, chemical, and construction sectors, characterization of key structural and interfacial properties within such systems is severely hampered by their optically opaque nature. Nuclear magnetic resonance (NMR) relaxation measurements (also termed nuclear spin relaxation measurements) provide a versatile and nondestructive approach with which to probe the dynamics of spin-bearing fluids within porous materials [1,2], and have been applied widely to the study of both equilibrium fluid properties (informing pore size distributions [3,4], adsorption phenomena [5,6] and diffusive exchange processes [7,8]) and to obtain time-resolved insight into evolving material structures (such as cements [9–13]). In this Letter we expand upon the established interpretation of NMR relaxation data when probing such time-resolved material properties, elucidating the uniquely coupled sensitivity of such measurements to the temporal evolution of both pore structure characteristics and surface chemistry properties simultaneously.

For fluid-saturated porous media, expressions for the dependence of observed  $^1\text{H}$  (proton) longitudinal ( $T_1$ ) and transverse ( $T_2$ ) NMR relaxation behavior on pore structure and interfacial chemistry are well known, taking the general form [14]

$$\frac{1}{T_i} \approx \frac{1}{T_{i,\text{bulk}}} + \left( \frac{d}{2\alpha\rho_i} + \frac{d^2}{8\alpha D} \right)^{-1}, \quad (1)$$

wherein  $i \in \{1, 2\}$ , and where additional terms may be required to fully account for observed  $T_2$  relaxation rates in the presence of magnetic susceptibility contrast across the solid-fluid interface [15,16]; such effects are mitigated in this work by performing our measurements at low magnetic field [17]. Here,  $T_i$  are the observed (measured) time constants and  $T_{i,\text{bulk}}$  represent the time constants for the unrestricted bulk fluid. Terms within parentheses then

describe the extent to which pore structure and interfacial chemistry perturb the observed relaxation characteristics:  $d$  is the pore diameter,  $\alpha$  is a dimensionless shape parameter (taking values of 1, 2, or 3 for planar, slit, or cylindrical pores, respectively), and  $D$  is the self-diffusion coefficient of the confined fluid. The terms  $\rho_i$  are the (spatially averaged) surface relaxivities of the solid-fluid interface, which may be modeled as  $\rho_i = \lambda/T_{i,\text{surf}}$  [18], where  $T_{i,\text{surf}}$  are the relaxation time constants within an adsorbed surface layer of thickness  $\lambda$ . Such terms describe enhanced rates of relaxation which occur at solid-fluid interfaces both due to a reduction in molecular mobility within the adsorbed surface layer [19] and through dipolar proton-electron interactions between adsorbate-bound  $^1\text{H}$  and paramagnetic species on the pore surface [14]. Established limiting cases for such relaxation dynamics exist. In the limit  $D/d \ll \rho_i$  for instance, surface relaxation rates are significantly more rapid than the rates of diffusive transport across the pores, with Eq. (1) reducing to

$$\frac{1}{T_i} \approx \frac{1}{T_{i,\text{bulk}}} + \frac{8\alpha D}{d^2}. \quad (2)$$

Conversely, in the limit  $D/d \gg \rho_i$ , diffusion across the pore is sufficiently more rapid than the rates of enhanced surface relaxation at the pore surface, with Eq. (1) reducing to

$$\frac{1}{T_i} \approx \frac{1}{T_{i,\text{bulk}}} + \frac{2\alpha\rho_i}{d}. \quad (3)$$

Such limits are referred to according to the overall rate controlling process; Eq. (2) therefore describes diffusion-limited relaxation, while Eq. (3) describes surface-limited relaxation. Here, we discuss data which for the first time permit clear identification of a temporal transition between

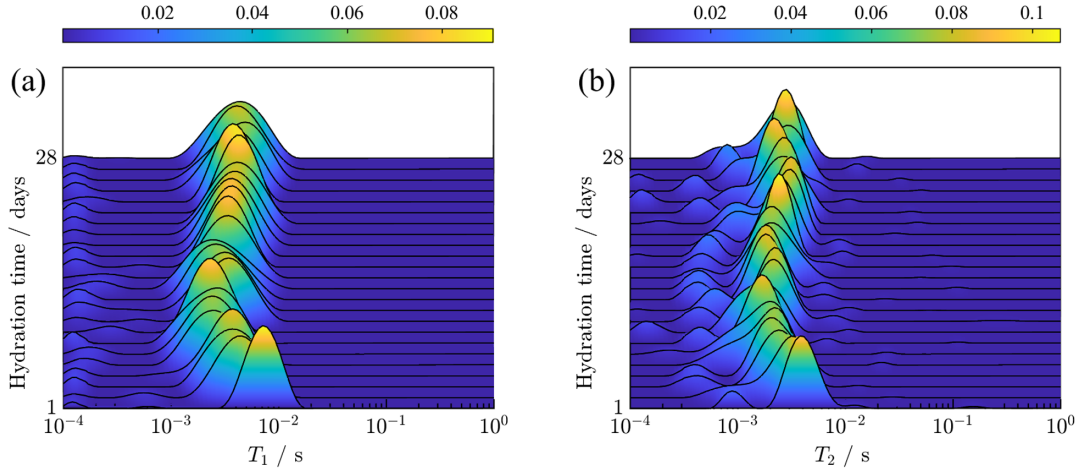


FIG. 1. Example (a)  $T_1$  and (b)  $T_2$  relaxation distributions for the hydrating material investigated in this study. Relaxation data were acquired over the first 28 days of material hydration. Color bars define the probability density of each relaxation distribution.

these limiting regimes within an evolving three-dimensional porous microstructure.

Figure 1 shows  $^1\text{H}$   $T_1$  and  $T_2$  distributions obtained at low magnetic field ( $B_0 = 0.05$  T;  $\nu_0(^1\text{H}) = 2$  MHz) for tap water within the hydrating engineering material cemented paste backfill (CPB) [20–22]. This porous material comprised a mixture of spherical fly ash particles, minerals tailings, ordinary Portland cement, and water (see Supplemental Material [23] for extended details of materials preparation), with the solids containing 7.9 wt%, 3.2 wt%, and 2.6 wt%  $\text{Fe}_2\text{O}_3$ , respectively, as measured by inductively coupled plasma optical emission spectroscopy, wherein paramagnetic  $\text{Fe}^{3+}$  ions provide the dominant source of relaxation sinks for adsorbed water at the pore surface. NMR measurements were performed under ambient conditions using inversion recovery [29] and CPMG (Carr-Purcell Meiboom-Gill) NMR pulse sequences [30,31], respectively, with the resulting data inverted to produce probability density distributions of observed  $T_1$  and  $T_2$  times via Tikhonov regularization [32–34] (see Supplemental Material [23] for extended NMR methods). Acquired  $T_1$  distributions [Fig. 1(a)] show a large primary peak, typical of systems in which sufficiently slow  $T_1$  relaxation characteristics allow extensive diffusive mixing between water confined within different pore sizes [35]. Acquired  $T_2$  distributions [Fig. 2(a)], which are naturally more sensitive to local pore geometry than  $T_1$  due to shorter relaxation times, reveal multiple relaxation environments, indicative of water confined within a hierarchically porous cement structure. Such distributions are consistent with established models of cement hydration [36], with the assignment of these relaxation peaks to specific hydrating pore structures detailed elsewhere [37,38].

In this Letter we consider only the modal relaxation times from each inverted distribution, termed  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$ , respectively, which are dominated by the most populous pore structures within the hydrating material

under study (capillary pores in traditional cement chemistry notation [39]). In recent work investigating the hydration behavior of a similar material in the absence of fly ash particles, a clear monoexponential relationship was observed between these modal time constants and hydration time  $t_h$ , which defines the experimental period across which the material is allowed to evolve. This relationship took the form  $\langle T_i \rangle_{\text{sl}} = a_i \exp(-b_i t_h) + c_i$  [37], where  $b_i$  are the observed material hydration rates,  $a_i$  provides a scaling factor, and  $c_i$  are offset parameters necessary to account for nonzero pore sizes at long  $t_h$ ; the subscript “sl” indicates that surface-limited relaxation is assumed within this system [38]. Fitting  $\langle T_i \rangle_{\text{sl}}$  against  $t_h$  then enables the extraction and comparison of material hydration rates  $b_i$ , facilitating quantitative contrast between different material formulations, preparation procedures, and hydration conditions.

Figures 2(a) and 2(b) detail the temporal evolution of our acquired  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$  data across 28 days of hydration. Rather than the expected monoexponential decay behavior, however, a clear decay-recovery process (subscript “dr”) is observed for each data set which may be modeled as

$$\langle T_i \rangle_{\text{dr}} = a'_i \exp(-b'_i t_h) - a_i \exp(-b_i t_h) + c_i. \quad (4)$$

We rationalize this biexponential behavior through consideration of a transition between the diffusion- and surface-limited relaxation processes described in Eqs. (2) and (3). In our chosen material the use of fly ash introduces a high  $\text{Fe}_2\text{O}_3$  content (7.9 wt% as measured by inductively coupled plasma optical emission spectroscopy), providing a significantly increased paramagnetic  $\text{Fe}^{3+}$  concentration ( $[\text{Fe}^{3+}]$ ) compared to that present in previous relaxation investigations of similar hydrating materials [37,38]. Surface relaxivity values  $\rho_i = \lambda/T_{i,\text{surf}}$  are sensitive to  $[\text{Fe}^{3+}]$  via the established expressions [10,14]

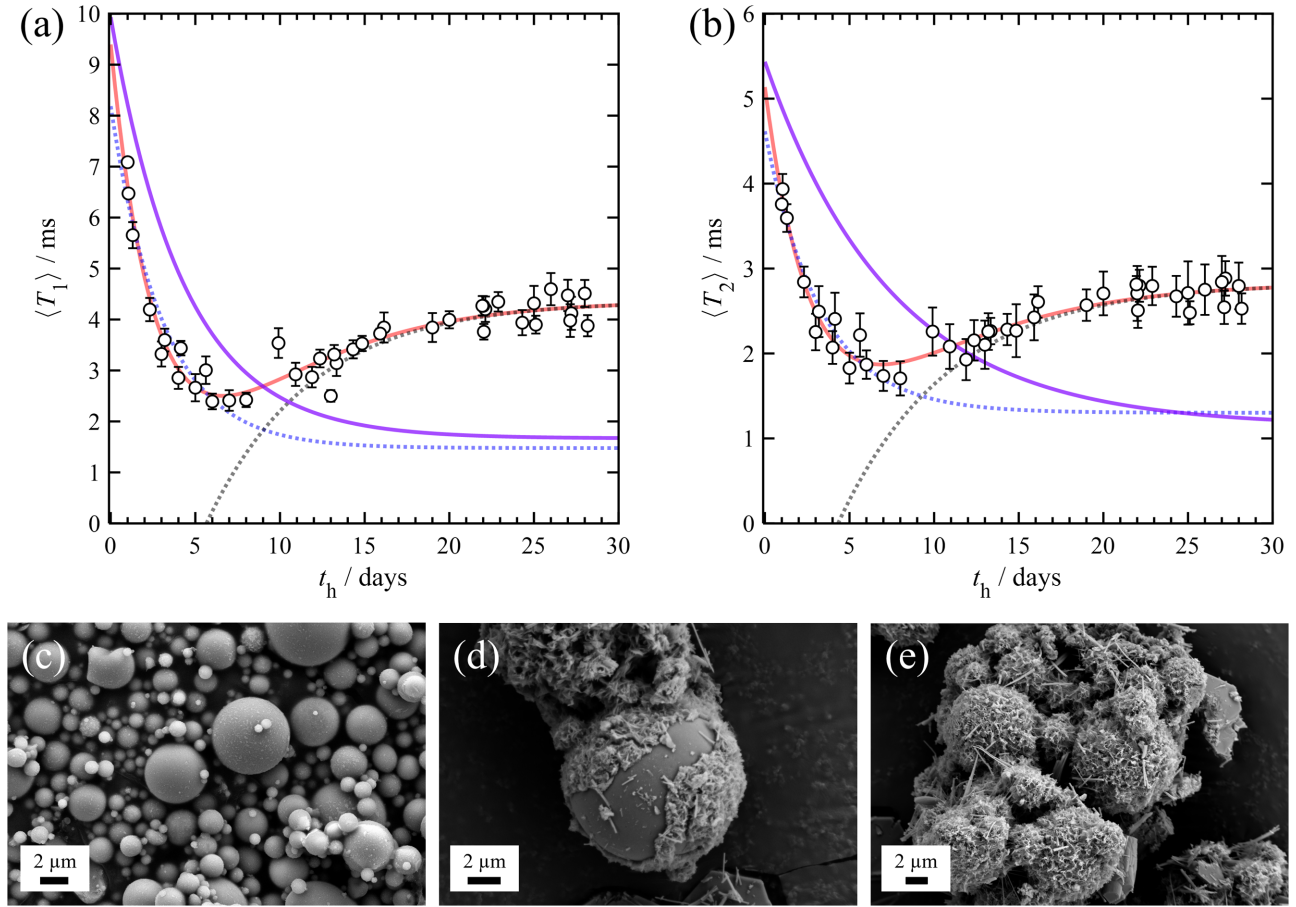


FIG. 2. (a)  $\langle T_1 \rangle$  and (b)  $\langle T_2 \rangle$   $^1\text{H}$  NMR relaxation evolution of water confined within the hydrating CPB material investigated here over 28 days. Error bars indicate  $\pm 1$  standard deviation ( $n = 3$ ), while data points without error bars were acquired only once. Red curves indicate a fit to Eq. (4) with  $b'_i = 2b_i$ . Blue curves show monoexponential fits to data at  $t_h < 10$  d, while gray curves represent the deconvoluted recovery components of Eq. (4), respectively. Purple curves show fitted monoexponential decay data obtained from similar hydrating systems in the absence of highly paramagnetic fly ash [37], demonstrating reduced decay rates relative to our data at short  $t_h$ . Bottom panels illustrate SEM images of fly ash particles; (c) shows fly ash particles in the absence of any cement hydration products ( $t_h = 0$ ); while (d) and (e) evidence surface C-S-H adlayer formation following 7 and 14 days of hydration, respectively.

$$\frac{1}{T_{1,\text{surf}}} = \beta [3J(\omega_I) + 7(\omega_S)],$$

$$\frac{1}{T_{2,\text{surf}}} = \frac{\beta}{2} [8J(0) + 3J(\omega_I) + 13(\omega_S)], \quad (5)$$

where the spectral density functions  $J(\omega_x) = \tau_m \ln[1 + \omega_x^2 \tau_m^2 / (\tau_m^2 + \omega_x^2 \tau_s^2)]$  (with  $x \in \{I, S\}$ ) capture the relationship between surface  $^1\text{H}$  relaxation rates and the dynamics of adsorbed water molecules at the internal pore surfaces of the hydrating material [14]. Here, the correlation times  $\tau_m$  and  $\tau_s$  are the translational correlation time of water molecules between paramagnetic relaxation sinks, and the surface residence time before desorption, respectively, while the frequencies  $\omega_I$  and  $\omega_S$  are obtained via  $\omega_x = \gamma_x B_0$ , where  $\gamma_I$  and  $\gamma_S$  are the proton and electron gyromagnetic ratios, respectively [40]. Importantly, the prefactor is given by  $\beta \propto \sigma \delta^{-4} \gamma_I^2 \gamma_S^2 \hbar^2 S(S+1)$ , where  $\sigma$

is the density of paramagnetic surface species of spin  $S$  at the pore surface (and hence assumed directly dependent on  $[\text{Fe}^{3+}]$  for our system;  $S = 5/2$  for  $\text{Fe}^{3+}$ );  $\delta$  is the distance of closest approach between adsorbate molecule and surface spins, while  $\hbar$  is the reduced Plank constant [10].

Godefroy *et al.* demonstrated a dependence between  $[\text{Fe}^{3+}]$  and limiting relaxation regime for a series of model porous structures comprising silicon carbide grains [14,41], evidencing a clear transition between diffusion-limited and surface-limited relaxation upon material cleaning to reduce  $[\text{Fe}^{3+}]$ . In the present work we conjecture that the temporal evolution of our hydrating porous material serves to facilitate this transition. Specifically, the dissolution-precipitation reactions responsible for cement hydration processes lead to the deposition of calcium silicate hydrate (C-S-H in cement chemistry notation) adlayers at the material pore surface [42], which is expected to both decrease the capillary pore size and limit access to the



highly paramagnetic fly ash particles upon increasing hydration time. We support this interpretation in Fig. 2 via scanning electron microscope (SEM) imaging of a sample of our hydrating material, which clearly demonstrates the time-dependent deposition of C-S-H across fly ash particle surfaces during the hydration period investigated. At short  $t_h$  we therefore interpret our observed relaxation behavior as dominated by interactions with high  $[\text{Fe}^{3+}]$  fly ash particles [Fig. 2(c)]; following Eq. (5) these interactions facilitate large  $\rho_i$  values, causing pore water to undergo diffusion-limited  $^1\text{H}$  relaxation (subscript “dl”) according to Eq. (2). A result of the above interpretation is that a square dependence on pore size is expected during pore structure evolution at short  $t_h$ , of the form  $T_i \propto d^2$ . Given the established monoexponential decay relationship between  $\langle T_i \rangle_{\text{sl}}$  and  $t_h$  in the absence of fly ash cobinder [of the form  $\langle T_i \rangle_{\text{sl}} \sim d \sim \exp(-b_i t_h)$  [37]], an initial decay of the form  $\langle T_i \rangle_{\text{dl}} \sim d^2 \sim \exp(-2b_i t_h)$  is then expected from our present data; this rapid decay processes is accounted for by the primed components of our biexponential model expression in Eq. (4). As a simple visual comparison, blue dotted decay curves within Figs. 2(a) and 2(b) show a scaled monoexponential fit to our  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$  data at  $t_h < 10$  d [with decay rates constrained to equal those obtained from our full fit to Eq. (4) described below], while fitted relaxation data obtained from a comparable hydrating material in the absence of highly paramagnetic fly ash are shown in purple (data obtained from Ref. [37]; further details are provided in Supplemental Material [23]). Enhanced relaxation time decay rates are clearly evident in the presence of fly ash (blue dotted curves), providing support for the expectation of comparably large  $\rho_i$  values, and hence for the interpretation of diffusion-limited relaxation at short  $t_h$ . Note that given these two hydrating materials are likely characterized by different pore structures and surface relaxivities, quantitative comparisons between the relaxation time values exhibited by these two systems are not possible, and we make no attempt to ascribe a physical interpretation to the convergence of these curves at short  $t_h$ , which can only be coincidental.

Following nucleation at the solid-liquid interface, C-S-H deposits continue to grow across the available pore surfaces according to established mechanisms of cementitious hydration [36]. The evolution of such adlayers is demonstrated for the present system in Figs. 2(d) and 2(e), which reveal the difference in adlayer growth following  $t_h = 7$  d and  $t_h = 14$  d, respectively. As C-S-H adlayers cover the internal surfaces of the hydrating pore network, dipolar interactions between the high concentration of fly ash-bound  $\text{Fe}^{3+}$  and  $^1\text{H}$  spins associated with confined pore water will be reduced, decreasing the spatially averaged surface relaxivity  $\rho_i$  of the capillary pore structures; such continued adlayer growth is therefore fundamental in initiating the proposed transition between diffusion- and surface-limited relaxation. An associated transition time

may be estimated and will be associated with the shortest measured  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$  times, which in the present work occur at  $t_h \approx 7$  d. While the continuous temporal growth and deposition of surface adlayers serves to reduce the material pore sizes over time, this process continues to be convoluted with the above reduction in  $\rho_i$ . Such pore size changes do not lead to a continuous reduction in  $\langle T_i \rangle_{\text{dr}}$  as would occur within systems exhibiting classical surface-limited relaxation wherein  $\rho_i$  values are assumed time independent ( $d\rho_i/dt_h \approx 0$ ). Rather, we interpret the observed *increase* in  $\langle T_i \rangle_{\text{dr}}$  with increasing  $t_h$  as a direct consequence of the coupling between pore structure evolution and decreasing  $\rho_i$ ; this  $\langle T_i \rangle$  recovery process is deconvoluted in gray within Figs. 2(a) and 2(b) and is accounted for by the second exponential term of Eq. (4).

A consequence of the above discussion is that we may now directly interpret  $b_i$  within Eq. (4) as material hydration rates, which are equated with the rate of changing surface relaxivity under surface-limited conditions. Appropriate fitting of our data to this expression with the constraint  $b'_i = 2b_i$  was performed [red curves in Figs. 2(a) and 2(b)], yielding hydration rates  $b_1 = 0.16 \pm 0.02 \text{ d}^{-1}$  and  $b_2 = 0.15 \pm 0.02 \text{ d}^{-1}$ . Remarkably, these values are in excellent agreement with previously observed CPB hydration rates of  $0.08\text{--}0.2 \text{ d}^{-1}$  obtained in the absence of fly ash [37]. This result provides both confidence in the above data interpretation and suggests that the assumption of  $d\rho_i/dt_h \approx 0$  in the absence of fly ash is reasonable. We note for completeness that while  $b_1 \approx b_2$  here, such equivalence is not necessarily expected given the differing sensitivities of  $\langle T_1 \rangle$  and  $\langle T_2 \rangle$  to the fine structure of hierarchical pore networks within hydrating cementlike materials (demonstrated in Fig. 1).

In summary, this work has demonstrated the measurement of nuclear spin relaxation phenomena within a dynamic and temporally evolving three-dimensional porous structure exhibiting changes to both pore size and pore surface chemistry. Our observations provide clear evidence that the  $^1\text{H}$  NMR relaxation characteristics of water confined within such systems can exhibit sensitivity to both phenomena simultaneously, and that our measured relaxation data are susceptible to the resulting temporal changes in pore structure surface relaxivity. We anticipate the consideration of such time dependent surface relaxation phenomena will be critical in avoiding the erroneous interpretation of time-resolved relaxation data obtain from complex porous materials, especially when considering systems containing potentially high concentrations of paramagnetic species, or in reactive (catalytic) systems, where, e.g., the coking of polar pore surfaces is expected through the formation of reaction byproducts.

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