Measurement of Coherent Elastic Neutrino-Nucleus Scattering from Reactor Antineutrinos

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The 96.4 day exposure of a 3 kg ultralow noise germanium detector to the high flux of antineutrinos from a power nuclear reactor is described. A very strong preference ($p < 1.2 \times 10^{-3}$) for the presence of a coherent elastic neutrino-nucleus scattering (CE ν NS) component in the data is found, when compared to a background-only model. No such effect is visible in 25 days of operation during reactor outages. The best-fit CE ν NS signal is in good agreement with expectations based on a recent characterization of germanium response to sub-keV nuclear recoils. Deviations of order 60% from the standard model CE ν NS prediction can be excluded using present data. Standing uncertainties in models of germanium quenching factor, neutrino energy spectrum, and background are examined.

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We have recently reported [1] on the deployment of a *p*-type point contact (PPC) germanium detector [2] in close proximity to the core of the Dresden-II boiling water reactor (BWR). The device, dubbed NCC-1701, combines presently unique characteristics of large mass (2.924 kg) and low energy threshold (0.2 keV_{ee}) within a compact shield, enabling a search for subtle sub-keV signals expected from coherent elastic neutrino-nucleus scattering (CE ν NS) [3,4]. Details on detector, shielding, fieldprogrammable gate array-based data-acquisition system (DAQ), background characterization, calibrations, and data treatment are provided in Ref. [1]. The main objective of this installation was to study the practicality of reactor monitoring using a small-footprint PPC assembly in the aggressive environment (radiation, temperature, electromagnetic and radio-frequency interference, acoustic noise, vibration) a few meters from a commercial reactor core [1]. The neutrino detector miniaturization afforded by a large CE_vNS cross section permits us to envision such technological applications, in the near future [5]. Reactor sources can significantly expand the potential of $CE\nu NS$ to probe physics beyond the standard model (SM) [6].

The new dataset highlighted in this Letter spans the period between 1/22/2021 (month/day/year) and 5/8/2021, during which the reactor was operated at its full nominal power of 2.96 GW_{th} (Rx-ON). Interruptions on days 515–516, 535–537, and 546–552 (referenced to detector installation on 10/19/2019) were due to data storage overflows during a time of limited access to the site, resulting in a 96.4 day effective exposure. The start of this new run followed the installation of a spot cooler [7] able to reduce the temperature inside the detector shield while external temperatures approached 35 °C. This led to a significant decrease in detector cryocooler power and spurious DAQ triggers produced by its mechanical vibrations when operated in extreme conditions. An extended technical drop in reactor power determined the end of this run.

An additional 2.5-cm-thick layer of borated polyethylene was placed on the bottom side of the shield assembly on 6/13/2020. That surface featured only a minimal thickness of hydrogenated material, facilitating neutron ingress. As predicted by simulations using dedicated environmental background measurements as input [1], this straightforward upgrade resulted in a further drop by a factor of 2 in the low-energy spectrum, presently dominated by the elastic scattering of epithermal neutrons [1]. The peak at 1.297 keV_{ee} from L-shell electron capture (EC) in 71 Ge following neutron capture in ⁷⁰Ge was also reduced by a factor of 4 with respect to its previous activity [1], once a new secular equilibrium between 71Ge production and decay $(T_{1/2} = 11.4d)$ was reached. The 20 day Rx-ON run reported on in Ref. [1] immediately followed a first installation of neutron moderator, i.e., was preequilibrium and hence subject to an elevated ⁷¹Ge decay rate from preceding activation.

New information obtained from the reactor operator allowed us to establish a precise distance between PPC crystal and the center point of the BWR core. This had been

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estimated in Ref. [1] at 8 m based on initially available data. The improved figure is a center-to-center distance of 10.39 m, with active fuel elements located 7.48 to 13.31 m from the PPC. The axial and radial power profiles of the fuel assembly, specific to this period of exposure, were used to simulate the effect of an extended antineutrino source (3.66 m tall, 4.57 m diameter) in such close proximity to a comparatively pointlike target. This produces a negligible 0.8% reduction in the antineutrino flux expected from a point-equivalent source at 10.39 m. Our best-effort estimate of this flux is then $4.8 \times 10^{13} \overline{\nu_e}/\text{cm}^2$ s with a ~2% uncertainty based on the dispersion seen in other assessments [8–11]. Time-dependent changes of O(0.1)% to this flux during the fuel cycle [8] are neglected here.

A third *in situ* characterization of detector response to low-energy signals was performed on 1/22/2021, using a programmable electronic pulser to mimic the fast rise time of preamplifier signals from interactions in the bulk of the PPC crystal [1,12]. This confirmed the stability of signal acceptance (SA) over extended periods of time [13]. The uncertainty associated to SA from the cumulative of these pulser calibrations varies from 8.6% to 1.3% across the sub-keV region of interest (ROI) for a CE ν NS search [13]. This is combined with the statistical uncertainty of events passing data cuts, to generate error bars in the reconstructed (i.e., corrected for SA) spectra of Fig. 1.

The choice of stringent data cuts made in Ref. [1] was maintained in the present analysis, with the exception of a small increase to an edge-finding condition ($\varepsilon > \varepsilon_{\min}$, Fig. 2 in Ref. [1]). This conservative measure was preemptively adopted to ensure an absence of correlation between the accepted event rate near detector threshold, where the CE_vNS signal is expected to accumulate, and time-varying systematics discussed next. For consistency, the data previously acquired during 25 days of reactor outages [1] were reanalyzed with this modification. Resulting changes to this Rx-OFF spectrum (Fig. 1) are minimal and dominated by a small drop in overall normalization, traceable to an incorrectly calculated dead-time fraction in Ref. [1]. Both spectra in Fig. 1 account for dead time (16.5%) from spurious veto coincidences and PPC preamplifier saturation.

Special attention was paid to testing for contamination (unrejected electronic or microphonic noise, slow rise-time surface events [12]) in the spectral region next to the 0.2 keV_{ee} analysis threshold, as this might lead to an excess able to mimic a CE ν NS signal. Figure 2 displays the temporal evolution during Rx-ON of environmental parameters able to cause such backgrounds, together with daily rates of low-energy (0.2–0.3 keV_{ee}) events rejected by quality cuts [1], those passing all cuts, and for signals contributing to the *L*-shell EC peak. Four statistical estimators (Blomqvist β , Goodman-Kruskal γ , Kendal τ , Spearman rank) were used to explore monotonic—but not necessarily linear—correlations between these non-normal



FIG. 1. Energy spectra of PPC bulk events during Rx-ON and Rx-OFF periods. The CE ν NS expectation (red line) uses the MHVE antineutrino spectrum and Fe-filter quenching factor (see text). A dashed red line illustrates the impact of quenching on CE ν NS. Black dotted lines signal the ⁷¹Ge *M*-shell EC contribution, derived from *L*-shell EC at 1.29 keV_{ee}. This process is noticeable in Rx-OFF data, taken prior to the addition of neutron moderator (i.e., following intense ⁷¹Ge activation).

datasets. The implementation of these tests used here [26] generates a *p*-value statistic, with p < 0.05 signaling that the hypothesis of independence between datasets is unlikely. As expected from considerations expressed above, temperature, cryocooler power, and trigger rate exhibit a strong correlation $(10^{-23} evident$ by simple inspection of Fig. 2. The rate of low-energy events rejected by quality cuts clearly correlates to these environmental parameters $(4 \times 10^{-11} . Low$ energy events passing all cuts are, on the other hand, independent of environmental factors (0.13 ,including electronic noise, and as such exhibit the expected Gaussianity around their mean. They are also independent of rejected events (0.38 . The rate of L-shellEC events is independent of trigger rate (0.41 ,illustrating the stability of DAQ throughput during this run. The electronic noise intrinsic to the detector is independent from all other environmental factors (0.09 ,indicating a good stability of PPC leakage current in present temperature conditions [1]. This type of correlation analysis is of crucial importance prior to a $CE\nu NS$ search using PPCs, in view of the dominance of microphonic noise in the ROI [27].

A possible contamination with surface events in the spectra of Fig. 1 was quantified by studying the rise-time distributions of Rx-ON signals passing all cuts, prior to the



FIG. 2. From top to bottom (panels 1–4 are daily averages, 5–7 daily rates): (1) PPC electronic noise, measured using pretrigger preamplifier traces, (2) temperature inside the shield, (3) cryo-cooler power, (4) DAQ trigger rate, (5) events rejected by a last-applied quality cut against microphonics, (6) events passing all cuts, (7) events under the *L*-shell EC peak. Error bars are statistical and therefore larger for partial data-acquisition days (see text). Side panels show data dispersion (histogram) and the Gaussian expected from their mean.

application of a stringent condition selecting fast bulk events [1]. Unconstrained, characteristic log-normal distributions [1,28,29] were used for fitting slow and fast components. Fits were performed as a function of energy, over 50-eV-wide regions. Following the rise-time cut, the contamination derived from these fits is a negligible 1.5%, with no tendency to increase near threshold.

As a final safeguard, traces from a large fraction (25%) of events below 0.275 keV_{ee} passing all cuts were randomly selected for visual inspection (Fig. 3). No candidates suspect of failing rejection of surface events or any other anomalies were found. This last precaution, made possible

FIG. 3. Preamplifier trace for a typical radiation-induced lowenergy pulse passing all cuts, showing characteristic rise and decay times. The latter is intentionally elongated [1] via a 1 μ F dcblocking capacitor. Red lines show the wavelet-denoised trace. Wavelet parameters are separately optimized for edge-finding (left-hand panel; see Ref. [1]) and rise-time (r.t.) analysis (righthand panel). A blue line shows a tanh fit to the rising edge [32]. A strict condition (r.t. < 660 ns; see Ref. [1]) selects PPC bulk events with negligible surface event contamination (see text).

by a custom FPGA-based DAQ [1], is also important: commercial DAQ systems unable to digitize and store individual preamplifier traces [27,30,31] are not indicated for a CE ν NS search, as they do not allow the user to reject surface events or temporally isolated microphonics, both prone to near-threshold accumulation.

Figure 1 displays the CE ν NS signal predicted by the SM for the present Rx-ON exposure. Two antineutrino energy spectra were considered for this calculation. The first ("Kopeikin" in what follows), previously used in Ref. [1], is described in Ref. [33]. The second ("MHVE") adopts an approach suggested in Ref. [34], where spectral information above a neutrino energy of 2 MeV is taken from Refs. [35,36], and Ref. [37] is used below this energy. We find good agreement between our signal predictions and those by others [5,38,39], but note small differences of order 20% among these. Similarly for the spectral choices just described. The need for a standardized reactor source description has been recently emphasized [40].

The CE ν NS signal-to-background ratio achieved at threshold is ~1/4, the same as during the first observation of this process, prior to the subtraction of environmental backgrounds feasible at a pulsed spallation neutrino source [4,41]. For a steady-state reactor source this is not a possibility. Instead, a spectral model able to describe sub-keV backgrounds must be adopted to investigate a CE ν NS signal presence. Large, predictable spectral changes following sequential additions of very modest amounts of neutron moderator (a factor of 3 reduction in sub-keV rate in Ref. [1], a factor of 2 here) point to the elastic scattering of epithermal neutrons as the presently dominant source. The spectral shape model used to describe this component (a free exponential plus a free constant term [1]) is simple, as expected for a ROI just $\sim 1 \text{ keV}$ wide. It is also versatile, accommodating simulated variations in epithermal spectral hardness, cross-section libraries, quenching factor (QF) (including deviations from the Lindhard model [42,43]), veto threshold, and progressive addition of moderator [1,13].

The quenching factor describes the observed reduction in ionization yield produced by a nuclear recoil when compared to an electron recoil of the same energy (Fig. 1; see Ref. [43]). The CONUS experiment has recently imposed bounds on germanium QF models applicable to CEvNS [30]. Those still allowed generate a negligible $CE\nu NS$ contribution to the NCC-1701 Rx-ON spectrum above ~0.45 keV_{ee}. Applying the epithermal background model to the spectra of Fig. 1 above this energy generates an excellent fit to both Rx-ON and Rx-OFF data. However, extrapolation of the best fit down to threshold points to a significant low-energy excess in both cases. Electron capture from the M shell in ⁷¹Ge can contribute to this excess via the effect of detector energy resolution on its expected 0.158 keV_{ee} deposition [Fig. 1; see Ref. [1]). The ratio of M-shell to L-shell EC in germanium has been experimentally determined at 0.16 ± 0.03 [44], in good agreement with a theoretical expectation of 0.17 [45]. Using this ratio and extending the fitting region to encompass L-shell EC generates a robust prediction for the *M*-shell contribution (Fig. 1; see Ref. [13]). An increasing SA uncertainty above 1.5 keV_{ee} [13] defines a fitting window extending from threshold to this energy. A Gaussian L-shell EC peak with free amplitude, centroid, and width, including a subsidiary contribution from L_2 capture [13,46,47], completes the background model.

A Markov chain Monte Carlo ensemble sampler [48,49] was employed to fit the null hypothesis H_0 (background model only) and several alternative hypotheses H_1 (background plus CE ν NS signal, with a dependence on choice of QF and neutrino spectrum) to Rx-ON and Rx-OFF spectra, treating both datasets identically. The preference for one hypothesis over the other is obtained via their Bayes factor (B_{10} , "ratio of evidences"), computed by evaluating their respective integrals over parameter likelihood and assuming the same prior probability for both [50]. This approach to hypothesis testing allows us to compare non-nested models with the same number of degrees of freedom [13], as is done below, and to rank the premises used to define H_1 .

In a first step the CE ν NS signal in H_1 was approximated as an exponential $A_{0.2}e^{-(E-0.2)/\xi}$, where $A_{0.2}$ is its amplitude at threshold, *E* is energy in keV_{ee}, and ξ a decay constant. This parametrization is introduced solely to investigate which QF models are best supported by the data. The quality of this approximation is adequate, but varies across QF models. Introducing a prior to account for CONUS constraints on the QF [13], the best-fit values of $A_{0.2}$ and ξ for the Rx-ON spectrum are in good agreement with

FIG. 4. Favored values for CE ν NS parameters $A_{0.2}$ and ξ for Rx-ON (red) and Rx-OFF (blue) data. Dotted (dashed) lines indicate the 1σ (2σ) contour extracted from Markov chain Monte Carlo corner plots [13]. A cross marks the best-fit Rx-ON parameter values. For Rx-OFF this is $A_{0.2} = 3.6^{+6.2}_{-2.7}$, with ill-defined ξ . Other symbols denote CE ν NS predictions for combinations of neutrino spectra (gray for MHVE, black for Kopeikin) and QF (circles for indicated constant values, triangles for Lindhard with $\kappa = 0.157$ [13], diamonds for YBe, and squares for Fef).

expectations based on a recent QF characterization using sub-keV nuclear recoils (Fig. 4; see Ref. [43]). The QF models favored are not in tension with present CONUS data [13]. These are denoted by "YBe" for a model based on photoneutron source measurements and "Fef" for one derived using iron-filtered monochromatic neutrons [13,43]. As expected, the best-fit $A_{0.2}$ for Rx-OFF is compatible with zero (Fig. 4). Figure 5 illustrates the good agreement of the background model with both Rx-ON and Rx-OFF data (reduced χ^2 of 0.90 and 0.87, respectively), and the presence of a CE ν NS-compatible excess for Rx-ON only.

The preference for H_1 over H_0 (i.e., rejection of H_0 in favor of H_1) was quantified for six combinations of QF and neutrino spectrum (triangles, diamonds, and squares in Fig. 4), without free parameters or approximations in the CE ν NS component. For Rx-ON, Fef yields a B_{10} equal to 34.0 (MHVE) and 34.8 (Kopeikin). This corresponds to a "very strong" preference for the presence of CE ν NS according to the classic tabulation by Jeffreys [51]. For the YBe QF this becomes $B_{10} = 13.2$ (MHVE) or 11.2 (Kopeikin), i.e., "strong" evidence for H_1 . For Lindhard the values are 4.0 and 3.1, respectively ("moderate" Bayesian evidence). All B_{10} values for Rx-OFF support H_0 instead ($B_{10} \ll 1$), ranging from "moderately" (Lindhard) to "extremely" (Fef).

FIG. 5. Residual difference between the spectra of Fig. 1 and the best-fit background components (epithermal neutron, M-, L_1 -, and L_2 -shell EC) in the alternative hypothesis H_1 when using an exponential approximation for the CE ν NS signal (see text). A solid (dotted) line shows the calculated CE ν NS signal prediction for MHVE-Fef (MHVE-Lindhard) in the SM. The insets expand the residual above 0.7 keV_{ee}.

As a final test, a free amplitude was allowed to multiply the SM differential rate calculated for the favored MHVE-Fef (Kopeikin-Fef) interpretations, during H_1 fits. Its returned best-fit value is $0.97^{+0.31}_{-0.27}$ (1.17^{+0.42}). Deviations from the SM introducing new physics involve CEvNS spectral distortions more complex than a mere change in signal rate [6]. However, based on this simple assessment, the present dataset [13] should allow us to exclude deviations of order 60% with ~95% confidence, as long as the new QF models in Ref. [43] are embraced. This bestfit amplitude is nevertheless $3.2^{+0.14}_{-0.15}$ for MHVE-Lindhard, as can be ascertained from Fig. 5. If Lindhard is accepted as an accurate description of the sub-keV germanium QF, this might be interpreted as evidence for new physics [38] or, alternatively, for the incompleteness of the background model employed. Comparisons over the 0.45-1.5 keV_{ee} spectral region of the present H_0 against alternatives involving more complex background spectral shapes (exponential plus linear, double exponential, etc.) moderately but consistently favor the current H_0 description under a Bayes factor test. Further work in understanding sub-keV quenching factors and their underlying physical mechanisms is needed for $CE\nu NS$ to meet its full potential in the search for physics beyond the SM [38,43,52].

Constrained by the caveats that present uncertainties in quenching factor [53,54], background model, and antineutrino spectrum introduce, this dataset provides a very strong preference for an interpretation that includes the standard model CE ν NS signal, present during periods of reactor operation only. Experimentation with NCC-1701 at the Dresden-II BWR has provided an invaluable operating experience: with additional shielding upgrades that preserve compactness and the resolution of a technical issue affecting the neutron veto [1], Rx-ON backgrounds can be made comparable to Rx-OFF even in closest possible proximity to a reactor core (simulations show that full veto performance alone would reduce the Rx-ON background by a further factor of 2). Based on previous experience at sites profiting from a shallow overburden [55,56], a planned relocation of NCC-1701 to a "tendon gallery" surrounding a reactor containment dome should generate a signal-to-background ratio at threshold of $\gtrsim 20$. This will facilitate a precision measurement of $CE\nu NS$ and PPC utilization as a reactor-monitoring tool. An exciting future of applications in fundamental science and technology awaits for $CE\nu NS$ detectors.

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