

Robust Quantum Hall Ferromagnetism near a Gate-Tuned $\nu = 1$ Landau Level CrossingMeng K. Ma,¹ Chengyu Wang,¹ Y. J. Chung,¹ L. N. Pfeiffer,¹ K. W. West,¹
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In a low-disorder two-dimensional electron system, when two Landau levels of opposite spin or pseudospin cross at the Fermi level, the dominance of the exchange energy can lead to a ferromagnetic, quantum Hall ground state whose gap is determined by the exchange energy and has skyrmions as its excitations. This is normally achieved via applying either hydrostatic pressure or uniaxial strain. We study here a very high-quality, low-density, two-dimensional hole system, confined to a 30-nm-wide (001) GaAs quantum well, in which the two lowest-energy Landau levels can be gate tuned to cross at and near filling factor $\nu = 1$. As we tune the field position of the crossing from one side of $\nu = 1$ to the other by changing the hole density, the energy gap for the quantum Hall state at $\nu = 1$ remains exceptionally large, and only shows a small dip near the crossing. The gap overall follows a \sqrt{B} dependence, expected for the exchange energy. Our data are consistent with a robust quantum Hall ferromagnet as the ground state.

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Quantum ferromagnetism of itinerant electrons has been a subject of interest for decades [1–3]. In its broadest context, when the electrons' exchange energy dominates over the Fermi (kinetic) and disorder energies, the electrons should align their spins and form a ferromagnetic ground state. However, this criterion is extremely difficult to achieve in metallic elements because of the very large Fermi energies [3]. In flat-band and dilute two-dimensional (2D) carrier systems, the criterion has been met very recently and ferromagnetic ground states have been reported [4–7], although it is important to keep in mind that disorder can play a very important role [8]. A ferromagnetic ground state has also been reported in a system of exotic, electron-magnetic-flux quasiparticles, namely, composite fermions [9], and a spontaneous valley polarization of itinerant electrons has been observed in a dilute 2D electron system where electrons normally occupy two, degenerate conduction-band valleys [10]; in the latter case, the electrons' valley degree of freedom plays the role of the spin degree of freedom.

Another platform for the emergence of quantum ferromagnetism is created when the 2D electron system is cooled to very low temperatures, and placed in a large perpendicular applied magnetic field (B). In this case, the electrons' kinetic energy is quenched as the electrons occupy the quantized Landau levels (LLs). In the simplest scenario, the main energy competing with the exchange energy is disorder and, in a sufficiently clean (low-disorder) electron system, the so-called quantum Hall (QH) ferromagnetism prevails. In particular, when two LLs of opposite spin polarity, or more generally pseudospin polarity, cross at the Fermi level, the 2D carriers form a

polarized, QH ground state with an energy gap separating it from its excitations [11–40]. The energy gap of such a QH ferromagnet is directly related to the Coulomb exchange energy, and the lowest-energy excitations can involve skyrmions, smooth spin textures, if the Zeeman energy is sufficiently small [13,16,29,36,41]. The pseudospin degree of freedom includes the real spin, conduction-band valley, layer, or electric subband, depending on the nature of the crossing LLs.

Here we focus on the ground state of a very-high-quality, dilute, 2D *hole* system (2DHS) confined to a (001) GaAs quantum well (QW) near LL filling factor $\nu = 1$ as the two lowest-energy LLs cross (Fig. 1). (In this Letter, we implicitly refer to LLs with smaller *magnitude* of energy, measured from the band edge, as having lower energy; in Fig. 1 and other figures, these LLs have the least negative energy values at any given B .) The crossing of the two lowest-energy LLs is unusual and challenging to access experimentally. It can be achieved in 2D electron systems in GaAs via tuning the g factor through zero by applying hydrostatic pressure [16], or in AIAs via tuning the valley splitting energy by applying uniaxial strain [29]. The 2DHSs in GaAs provide a particularly rich platform in this context because, thanks to the strong spin-orbit interaction, their LLs are highly nonlinear as a function of B [42] and can exhibit multiple crossings, even at $\nu = 1$. Moreover, the field positions of the crossings can be controlled by varying the QW width [43], or simply by changing the 2D hole density.

To place our study in a broader perspective, in Fig. 1 we show the results of our self-consistently calculated 2D hole energy (E) vs B LLs at $p = 5$, in units of 10^{10} cm^{-2} , which

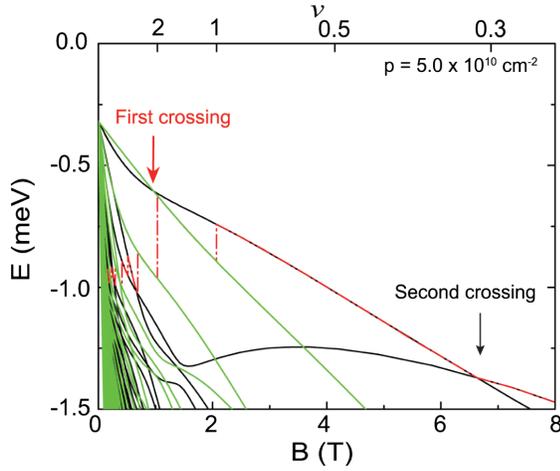


FIG. 1. Calculated energy (E) vs magnetic field (B) LL diagram for a 2DHS confined in a 30-nm-wide, (001) GaAs QW at a density of $5.0 \times 10^{10} \text{ cm}^{-2}$. The upper axis indicates the filling factor ν which is proportional to $1/B$. Black and green lines indicate LLs of opposite effective spin [44], and the red dash-dotted line traces the Fermi energy. The vertical arrows mark the positions of the two crossings of the two lowest-energy (in magnitude) LLs.

we use throughout this Letter. The calculations were performed using the multiband envelope function approximation based on the 8×8 Kane Hamiltonian [42]. They are essentially a Hartree calculation and do not include the exchange interaction. Since pure spin is not a good quantum number in a system with strong spin-orbit interaction, we have grouped the LLs in Fig. 1 into two pseudospin species, color coded using black and green [44]. The red dash-dotted line traces the position of the Fermi energy (E_F) as a function of B . The lowest two LLs have the very unusual characteristic that, depending on the parameters of the 2DHS, they can cross *twice* (Fig. 1). The

first crossing occurs between two LLs that have opposite pseudospin characters, while the second crossing involves a LL which emanates from an upper (excited) subband. The second crossing is remarkable on its own and entails very unusual evolutions of the ground state both at $\nu = 1$ [45,46] as well as at $\nu = 1/2$ where an even-denominator fractional QH liquid state [47], or an anisotropic, pinned Wigner solid state [48] can emerge. The details of the first crossing, which is the subject of our investigation here, are less known [49]. This is partly because the crossing typically occurs at small magnetic fields, implying that very dilute and yet low-disorder samples are needed for its study. Only very recently the presence of this crossing in a (001) GaAs 2DHS was demonstrated experimentally and, using optical techniques, it was shown that the 2DHS spins undergo a reversal as the LLs cross [40].

Figure 2 highlights in detail the expected evolution of the LLs and their crossings as a function of density. The calculations are shown for $p = 1.0, 2.0$, and 3.0 , and the color coding of the LLs is the same as in Fig. 1. In all three panels, the two LLs with opposite pseudospin cross at B slightly below 1 T (magenta up arrows). The black down arrows indicate the position of $\nu = 1$. For $p = 1.0$ [Fig. 2(a)], $\nu = 1$ occurs on the lower-field side of the crossing. At $\nu = 1$, E_F falls in an energy gap between two LLs and has a small but finite jump whose magnitude should give the energy gap for the $\nu = 1$ integer QH state (QHS). The situation for $p = 3.0$ [Fig. 2(c)] is qualitatively similar, except that here $\nu = 1$ occurs on the higher-field side of the LL crossing. At $p = 2.0$ [Fig. 2(b)], however, the crossing happens very close to $\nu = 1$; there is no jump of E_F , and one would expect the absence of a $\nu = 1$ QHS. The evolution presented in Fig. 2 then predicts that the $\nu = 1$ QHS should vanish and show a reentrant behavior as the density is tuned from a low to a high value.

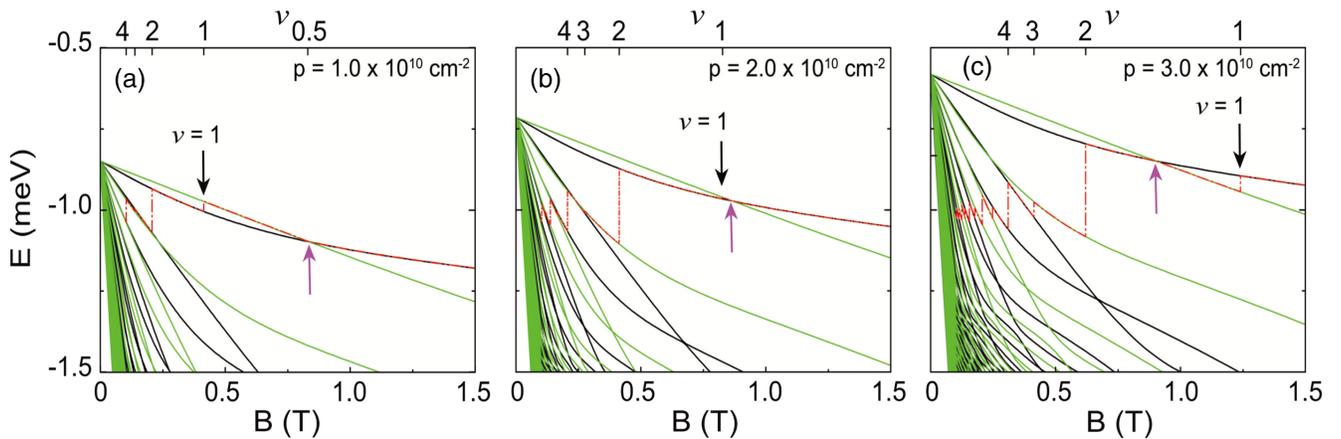


FIG. 2. Calculated LL diagrams for a 2DHS confined in a 30-nm-wide (001) GaAs QW at densities (a) 1.0 , (b) 2.0 , and (c) $3.0 \times 10^{10} \text{ cm}^{-2}$. The upper axes indicate the filling factor ν . As in Fig. 1, black and green lines indicate LLs of opposite effective spin [44], and the red dash-dotted line traces the Fermi energy. The downward arrows mark the positions of $\nu = 1$, and the upward arrows the positions of the first crossing of the two lowest-energy LLs.

As illustrated in the remainder of the Letter, this is very different from what we observe experimentally. Our magnetotransport measurements reveal that the LL crossing at $\nu = 1$ occurs at a much higher density of $p \simeq 4.6$, as signaled by a small dip in the energy gap ($^1\Delta$) of the $\nu = 1$ QHS. More important, in the entire density range, from $p \simeq 1.0$ to $\simeq 5.5$, the measured $^1\Delta$ is much larger than the single-particle effective Zeeman energies, and both its magnitude and field dependence ($\sim\sqrt{B}$) are consistent with what is expected for a QH ferromagnet with an exchange-enhanced energy gap.

The high-quality 2DHS studied here resides in a 30-nm-wide GaAs QW grown on a GaAs (100) substrate. The QW is flanked on each side by a 510-nm-thick $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$ barrier (spacer) layer followed by a C δ -doping layer. The structure is then buried under a 200-nm-thick $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$ layer, another C δ -doping layer, and a 28-nm-thick GaAs cap layer on top. The 2DHS has an as-grown density $p = 3.8$ and a low-temperature ($T = 0.3$ K) mobility $\mu = 1.3 \times 10^6$ cm^2/Vs . We performed our measurements on a 4 mm \times 4 mm van der Pauw geometry sample. Contacts were made by annealing InZn at 380 $^\circ\text{C}$ for 70 sec. To tune the 2D hole density while keeping the charge distribution symmetric, we placed the sample on melted In to make a back gate and deposited Ti/Au on the top surface as the front gate. The sample was cooled down in a cryogen-free dilution refrigerator with a base temperature of $\simeq 30$ mK, and also in a ^3He cryostat with a base temperature of $\simeq 0.30$ K. All transport measurements were performed using a low-frequency lock-in measurement technique at $\simeq 10$ Hz frequency with a $\simeq 50$ nA excitation current.

Figure 3 shows the temperature dependence of the longitudinal resistance R_{xx} vs B at $p = 3.8$ with both

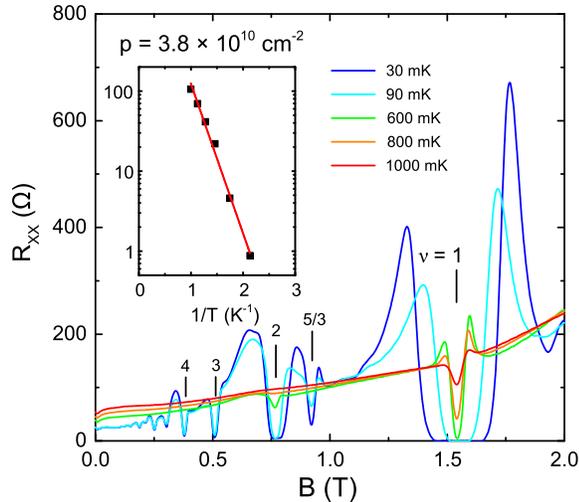


FIG. 3. Temperature dependence of the longitudinal resistance (R_{xx}) vs B at $p = 3.8 \times 10^{10}$ cm^{-2} . The vertical marks indicate the field positions for $\nu = 1, 2, 3, 4$, and $5/3$. The inset shows an Arrhenius plot of R_{xx} minimum at $\nu = 1$ vs $1/T$, and a linear fit (in red), yielding an energy gap of 8.6 K.

the front and back gates grounded. The vertical lines indicate the expected positions of several QHSs. The traces at the lowest temperatures show the presence of a well-developed *fractional* QHS at $\nu = 5/3$, as well as at $1/3, 2/5, 3/7, 2/3, 3/5, 4/7$, and even at $1/5$ at higher B [50]; also see Supplemental Material [43]. The observation of these fractional QHSs attests to the exceptional quality of this sample, at such low density. The inset in Fig. 3 shows an Arrhenius plot R_{xx} at $\nu = 1$ vs T from which we deduce the energy gap $^1\Delta$ for $\nu = 1$. In the Fig. 3 inset, the red line is a linear fit through the data points, and yields $^1\Delta \simeq 8.6$ K.

We repeated the activation energy measurements at $\nu = 1$ for 2D hole densities ranging from $\simeq 1.0$ to $\simeq 5.5$. This was achieved by gating the sample using both the front and the back gates while keeping the charge distribution symmetric. A summary of $^1\Delta$ as a function of p is shown in Fig. 4. Error bars for the measured energy gaps, based on the Arrhenius fits to the data points (see Fig. 3, inset, and also [43]), are also shown. The red open circles are the gaps determined from the calculated LLs as shown in Fig. 2, namely, the magnitude of the jump in E_F at $\nu = 1$. A LL crossing at $\nu = 1$ is experimentally observed at a density of $p \simeq 4.6$, evinced by a dip in $^1\Delta$. A clear discrepancy is seen in Fig. 4 between the predicted and measured positions of the crossing. This is not a surprise; in previous studies, similar LL calculations predict a *second* LL crossing also at a somewhat lower density compared to the experiments [47,51]. Besides the discrepancy in the predicted and measured positions of the crossing in Fig. 4, there is also a qualitative difference between the calculated and the experimentally measured gaps: The calculations predict that, starting from low densities, $^1\Delta$ should decrease as a function of increasing density, vanish when the crossing occurs at $\nu = 1$, and then increase again as the density is further increased. In sharp contrast, the experimentally measured $^1\Delta$ remain finite and are significantly larger than the calculations predict at all densities. The remarkable prominence of the $\nu = 1$ QHS is also evident in Fig. 3 traces: At higher temperatures, e.g., at 800 mK, the only minimum seen in R_{xx} is at $\nu = 1$.

We attribute the fact that the measured $^1\Delta$ is by far larger than the gap expected from the LL calculations to the presence of a QH ferromagnet at $\nu = 1$ with an exchange-enhanced energy gap [53]. In an ideal 2D carrier system, with zero layer thickness, no LL mixing, and no disorder, the energy gap for single spin flips in a QH ferromagnet is expected to be equal to the exchange energy $E_{\text{ex}} = \sqrt{\pi/2}e^2/4\pi\epsilon\epsilon_0 l_B$ where ϵ is the dielectric constant of the host material (13 for GaAs) and $l_B = \sqrt{e\hbar/B}$ is the magnetic length [13,54,55]. This value is reduced by a factor of 2 if the excitations are skyrmions [13]. Note that E_{ex} should vary as \sqrt{B} , and this is indeed what we observe in our experiments: the measured $^1\Delta$ overall follows a \sqrt{B} fit except in the vicinity of the crossing where it deviates from the \sqrt{B} fit (see Fig. 4). Quantitatively, for our sample, at $B = 2$ T, the expected, ideal E_{ex} is $\simeq 85$ K, much larger

than our measured ${}^1\Delta \simeq 8$ K near the LL crossing. However, this is reasonable and in line with previous measurements of ${}^1\Delta$ at LL crossings. For example, for 2D electrons in GaAs in the limit of zero g factor, ${}^1\Delta \simeq 12$ K was reported when $E_{\text{ex}} \simeq 213$ K [16], and for AlAs 2D electrons, ${}^1\Delta \simeq 6$ K was quoted when $E_{\text{ex}} \simeq 263$ K [29]. The much smaller measured energy gaps compared to E_{ex} have been attributed to the presence of skyrmions, finite electron layer thickness, LL mixing, and disorder, all of which are known to reduce the gap [16,56–58]. Considering these factors, the gap we measure, ${}^1\Delta \simeq 8$ K, is in fact surprisingly large, especially taking into account the significant amount of LL mixing we expect in our 2DHS because of its very low density and relatively large effective mass [59,60].

Next we discuss the role of the $\nu = 1$ LL crossing on ${}^1\Delta$ in our 2DHS. In previous measurements of a $\nu = 1$ LL crossing in GaAs and AlAs 2D electrons, a pronounced minimum in ${}^1\Delta$ was observed at the LL crossing [16,29]. The minimum, and the rapid enhancement of ${}^1\Delta$ away from the crossing, were attributed to the predominance of skyrmions at $\nu = 1$ at the crossing and the reduction in the skyrmions' size as $\nu = 1$ is tuned away from the crossing. In our data, we do observe a minimum in ${}^1\Delta$ at the crossing but it is not as pronounced as in the above cases. It is worth emphasizing that the experiments of Refs. [16,29] were performed at constant density and the LL crossing was induced by applying either hydrostatic pressure [16] or uniaxial strain [29]. In contrast, in our measurements we vary the density to cause the LL crossing at $\nu = 1$. This implies that, if E_{ex} is dominant, we would expect an increasing ${}^1\Delta$, reflective of the expected $E_{\text{ex}} \sim \sqrt{B}$ behavior, with a minimum, accounting for the vanishing effective Zeeman energy (and potential existence of skyrmions), superimposed on it. Our data in Fig. 4 clearly exhibit the \sqrt{B} dependence of the ${}^1\Delta$, consistent with the increase of E_{ex} with B [52].

In order to better present the behavior of ${}^1\Delta$ near the crossing, in the Fig. 4 inset, we show the deviation of the measured ${}^1\Delta$ from ${}^{\text{fit}}\Delta$ as a function of density (lower scale), or equivalently, B (upper scale). A sharp minimum is clearly seen near the measured crossing at $p \simeq 4.6$ ($B \simeq 1.9$ T). The blue and magenta solid lines show linear fits to the data points below and above the crossing, giving slopes of $\simeq -4.8$ K/T and $\simeq 3.7$ K/T, respectively. Note that the magenta line fitting is less reliable because of the relatively larger error bars in ${}^1\Delta$. Ideally, the ratios of these slopes to the theoretically calculated slopes in a single-particle picture should yield a reasonable estimate of the size of skyrmions near the crossing [16,29]. The slopes we deduce from Fig. 4 (inset) fits are indeed much larger than the slopes implied by the calculated LLs (red open circles in Fig. 4), suggesting large-size skyrmions, consistent with the conclusions reached in [40]. However, one should be cautious in determining a quantitative size for the

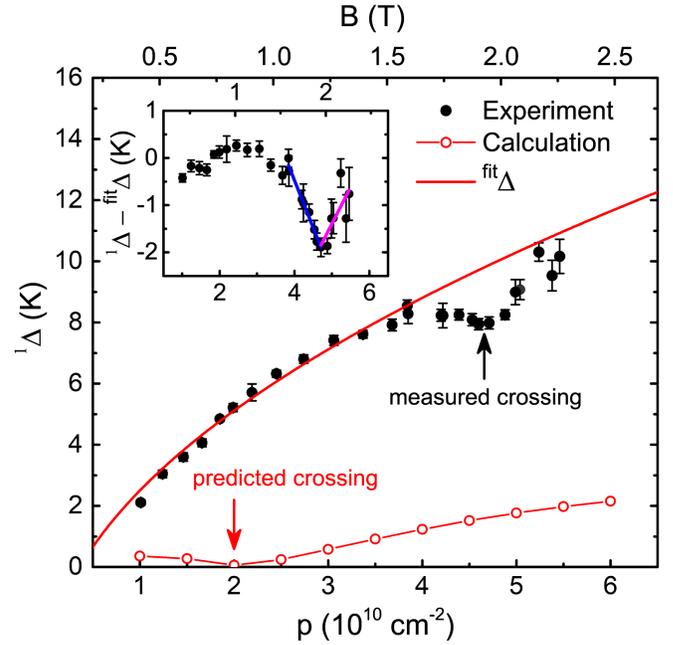


FIG. 4. Summary of the $\nu = 1$ gap (${}^1\Delta$) as a function of density (lower scale), or equivalently, B (upper scale). The black circles are the experimentally measured gaps, with error bars indicated. The red open circles represent the expected gaps from LL calculations which do not include exchange energy. Data points are connected by straight lines as guides to the eye. The black arrow indicates a dip in the measured gaps, manifesting a LL crossing at $p \simeq 4.6$. The red arrow indicates the expected crossing predicted by the LL calculations. A \sqrt{B} fit to the measured gaps (${}^{\text{fit}}\Delta$) is shown as a red curve [52]. Inset: deviation of the measured ${}^1\Delta$ from ${}^{\text{fit}}\Delta$ as a function of density (lower scale), or equivalently, B (upper scale). The blue and magenta solid lines show linear fits to the data points near the measured crossing.

skyrmions from our study, given the discrepancy between the observed and calculated positions of the LL crossing.

We emphasize that the fact that our measured ${}^1\Delta$ is much larger than the effective Zeeman energy expected from the LL calculations, and its \sqrt{B} dependence, are both strong indications that ${}^1\Delta$ is dominated by the exchange interaction and signals a robust QH ferromagnet. Our results should stimulate future many-body calculations that take the exchange energy of the 2D system into account and explain the experimental data quantitatively.

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- [52] The energy vs B fit shown in Fig. 4 (inset) as a red curve has the form: $9.8\sqrt{B} - 3.8$; the units for energy and B are K and T, respectively. The negative intercept, -3.8 K, can be interpreted as a measure of disorder, and it's comparable to the LL broadening expected in very high-quality GaAs 2DHSs. The B -dependent part of the fit can also be rewritten in terms of the Coulomb energy as $\sim 0.2e^2/4\pi\epsilon\epsilon_0 l_B$. Note that the coefficient (0.2) implies that the gap is a reasonably large fraction of the Coulomb (exchange) energy, despite the relatively large LL mixing parameter ($\simeq 14$ at 2 T), and finite layer thickness of our 2DHS ($w/l_B \simeq 1.7$ at 2 T); $w = 30$ nm is our QW width.
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