

## Crystallizing Kagome Artificial Spin Ice

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(Received 17 January 2022; revised 16 March 2022; accepted 11 July 2022; published 29 July 2022)

Artificial spin ices are engineered arrays of dipolarly coupled nanobar magnets. They enable direct investigations of fascinating collective phenomena from their diverse microstates. However, experimental access to ground states in the geometrically frustrated systems has proven difficult, limiting studies and applications of novel properties and functionalities from the low energy states. Here, we introduce a convenient approach to control the competing dipolar interactions between the neighboring nanomagnets, allowing us to tailor the vertex degeneracy of the ground states. We achieve this by tuning the length of selected nanobar magnets in the spin ice lattice. We demonstrate the effectiveness of our method by realizing multiple low energy microstates in a kagome artificial spin ice, particularly the hardly accessible long range ordered ground state—the spin crystal state. Our strategy can be directly applied to other artificial spin systems to achieve exotic phases and explore new emergent collective behaviors.

DOI: 10.1103/PhysRevLett.129.057202

Artificial spin ices (ASIs) are exemplar material-by-design systems with intriguing physical phenomena such as geometrical frustration [1–6], monopolelike excitations [7–10], Coulomb phase [10,11], and phase transitions [12–14]. They lead to novel functionalities with great potential for applications, such as low-power data storage [15], encryption devices [16], and advanced computations [17–19]. As one of the simplest ASI structures, the kagome ASI has attracted extensive attention [2,7–9,12,13,20–29], because it is highly frustrated and contains a rich phase diagram. Theoretical investigations suggest four thermal phases with reducing temperatures [13,21,28,30]: a high temperature paramagnetic state (PM phase); a spin liquid with correlated spins satisfying the kagome ice rule (“two in–one out” or “two out–one in”) but with neither charge nor spin ordering (SL1 phase); a long-range ordered charge crystal in a disordered spin liquid state (SL2 phase); as well as a spin crystal state in which the spins have long-range ordering (LRO phase) as the lowest temperature state. These thermal phases were used to understand the temperature dependent magnetotransport results in honeycomb structures of nanowire networks (which is sometimes also called kagome ASI, because the moments of the nanowires

satisfy the kagome ice rule), where the LRO spin crystal state may contribute to the topological Hall signals at the lowest temperatures [30]. However, previous investigations have shown that direct experimental access of the spin crystal states of a kagome ASI is challenging [12,31]. With the exception of the magnetic writing approach [31], no LRO spin crystal state has been unambiguously visualized in a kagome ASI consisting of fully disconnected nanobar magnets, hindering investigations of emergent phenomena and phase transitions from its low energy manifolds.

The collective properties of ASIs are directly associated with their lattice geometries, and are intimately governed by the competing dipolar interactions between their constituent elements, i.e., the single-domain nanobar magnets [16,32–34]. The difficulty of obtaining the LRO state of a kagome ASI originates from the extensive degeneracy of the ground state, resulting from the high frustration of the tri-leg vertices. The ground state of a kagome ASI exhibits neither charge nor spin order when only nearest-neighbor interactions are considered [21,35]. Further-neighbor interactions induce charge and/or spin ordering [13,21,28]. However, these longer-distance interactions are much weaker than that from the nearest neighbor. As a result,

the properties of artificial spin ices are mostly dominated by the nearest-neighbor interactions. Recently, utilizing the micromagnetic nature of connected vertices in the honeycomb structure of nanowire networks, the LRO spin crystal phase of kagome ices was realized for the first time, in which notches were introduced to reduce the vertex degeneracy [36]. More recently, asymmetric bridges were introduced to break the sixfold symmetry of kagome ASI's vertices, leading to a direct real-space imaging of the phase transitions [37]. However, these strategies are not applicable to kagome ASIs consisting of disconnected nanobar magnets. In this Letter, we develop a new method to tailor the vertex degeneracy and the ground states of a kagome ASI of disconnected magnetic nanobars, and we directly present the phase transition from the SL1 liquid to LRO crystal state. Unlike the recently realized connected kagome ASI structure [36,37], in which the coupling is dominated by short range exchange interaction, our disconnected ASIs maintain their long range dipolar interaction, therefore, allowing us to directly evaluate the critical role of the nearest and/or next nearest neighbor interactions, which is crucial for understanding the phase transitions between the various low energy manifolds of ASIs.

In square ASIs, the six vertex configurations satisfying the spin ice-rule are divided into two types according to energy [1,2,10,11,14,17,18,22,24,29,38–44]. The lowest energy configuration is twofold degenerate, leading to the formation of a long-range ordered ground state [1,38–41]. The low degeneracy of 2 in a square ASI is induced by the nonequal interactions between the nanobar magnets at each vertex. Following this notion, we developed a method to achieve the LRO spin ice state of a regular kagome ice by inducing nonequal interactions between the three nanobar magnets at a vertex, which reduces the ground state degeneracy of a kagome vertex from 6 to 2. As shown in Fig. 1(a), we increase the length of one of the three nanobar magnets ( $\alpha$ ) in each vertex, while maintaining the length of the other two magnets ( $\beta$ ) and the lattice constant (see Fig. S1 of Supplemental Material for the detailed arrangement of  $\alpha$  and  $\beta$  magnets in the lattice [45]). This breaks the threefold rotation symmetry of the vertex. The interactions between the three nanobar magnets at each vertex are no longer equivalent. As shown in Fig. 1(b), the original sixfold degenerate vertices are divided into two groups of Type *K-I* and *K-II* configurations with different energies. We denote the interaction energy of the frustrated magnet pair between two  $\beta$  nanomagnets in Type *K-I* vertices as  $J_1$ , while that between  $\alpha$  and  $\beta$  nanomagnets in Type *K-II* vertices as  $J_2$  [Fig. 1(b)]. Since each vertex satisfying the kagome ice rule contains only one frustrated magnet pair,  $J_1$  and  $J_2$  also represent the energies of the Type *K-I* and *K-II* vertices, respectively. Because the end points of the lengthened  $\alpha$  nanomagnet are closer to the vertex center,  $J_1$  is lower than  $J_2$ , resulting in the twofold degenerate Type *K-I* vertices to be the ground

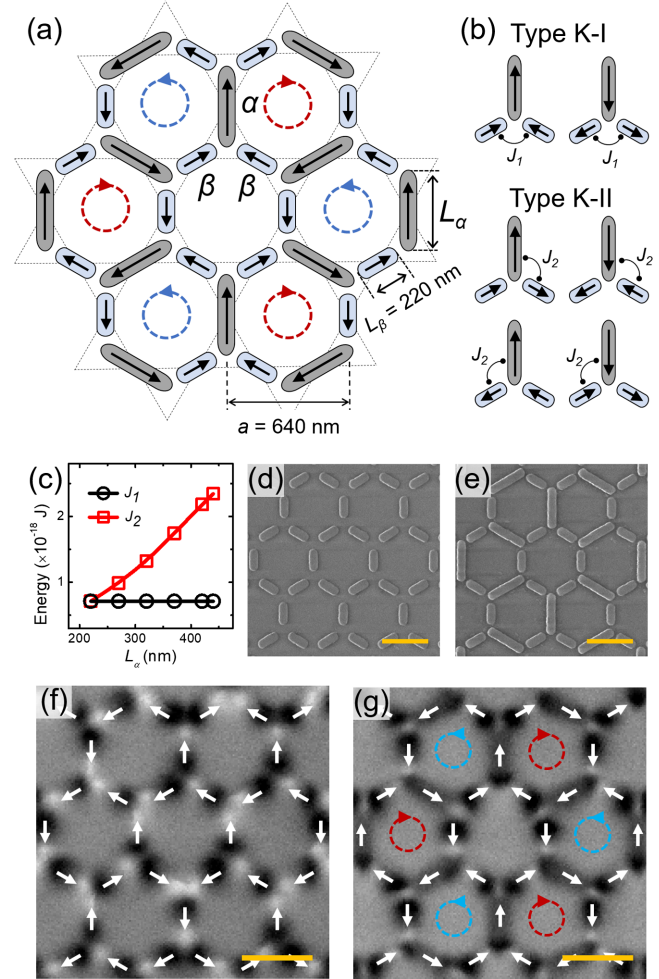


FIG. 1. Tunable kagome artificial spin ice. (a) Design of tunable kagome artificial spin ice with extended length  $L_\alpha$  of  $\alpha$  magnets and fixed length  $L_\beta$  of  $\beta$  nanomagnets. (b) Six low energy vertex configurations satisfying the kagome ice rule are separated into two groups based on energies.  $J_1$  and  $J_2$  are the coupling strengths of frustrated magnet pairs. (c) Evolution of the vertex energies as a function of  $L_\alpha$ . (d) and (e) SEM images of kagome artificial spin ices with  $L_\alpha = 220$  nm (d) and  $L_\alpha = 420$  nm (e), respectively. Scale bar, 500 nm. (f) and (g) MFM images corresponding to (d) and (e), respectively. Arrows indicate spin configurations. Scale bar, 500 nm.

state configuration. As shown in Fig. 1(a), when all the vertices are satisfied to be in the Type *K-I* ground state configuration, a LRO spin crystal emerges. We can further tailor the energy difference between Type *K-I* and *K-II* vertices by varying the length ( $L_\alpha$ ) of the  $\alpha$  nanomagnet. Figure 1(c) presents the vertex energy evolution of Type *K-I* and *K-II* vertices as a function of  $L_\alpha$ , calculated from micromagnetic simulation using MuMax3 [46]. It shows that  $J_2$  increases with  $L_\alpha$  while  $J_1$  remains constant. Thus, the energy difference  $J_2 - J_1$  between Type *K-I* and *K-II* vertices increases with  $L_\alpha$ . Therefore, varying the length of the  $\alpha$  nanomagnets allows us to regulate the effective

temperature, similar to the effect of tuning the vertex notch in the connected honeycomb structures [36]. This enables us to tailor the phases in a fully disconnected kagome ASI.

To experimentally validate this approach, we fabricated kagome ASIs with Permalloy nanomagnets and with a series of  $L_\alpha$  values (220 nm, 270 nm, 320 nm, 370 nm, 420 nm, and 440 nm) for the  $\alpha$  nanomagnets (see SEM images in Fig. S2 of Supplemental Material [45]). The length ( $L_\beta$ ) of the  $\beta$  magnets is fixed at 220 nm, and the lattice constant is  $a = 640$  nm for all samples [Fig. 1(a)]. The width and thickness of all the nanomagnets are 80 and 15 nm, respectively. Details of the sample fabrication process and parameters can be found in Supplemental Material [45]. A demagnetization procedure (see Supplemental Material [45]) lasting 72 h was performed to obtain the low-energy states [11,47]. Figures 1(d) and 1(e) show the SEM images of the samples with  $L_\alpha = 220$  nm and 420 nm, respectively. The corresponding magnetic force microscopy (MFM) images are displayed in Figs. 1(f) and 1(g), respectively, which allow us to determine the magnetic moment (or spin) configurations [see arrows in Figs. 1(f) and 1(g)]. The results show that all the vertices in all measured samples satisfy the kagome ice rule (two in–one out or two out–one in). This indicates our demagnetization procedure successfully brought the samples into the low energy ice rule manifold. The conventional kagome ASI with  $L_\alpha = L_\beta$  [Fig. 1(d)] exhibits disordered spin and charge configurations [Fig. 1(f)], consistent with the frozen spin liquid SL1 state. In contrast, the modified kagome ASI with  $L_\alpha > L_\beta$  [Fig. 1(e)] exhibits

perfect spin and charge ordering [Fig. 1(g)], leading to a successful realization of the LRO spin crystal ground state.

The transition from SL1 phase to LRO spin crystal phase is demonstrated by the MFM images of samples with increasing  $L_\alpha$  values in Figs. 2(a)–2(f). The corresponding maps of vertex distributions in Figs. 2(g)–2(l) shows that domains of crystallization become larger with  $L_\alpha$ . For the sample with  $L_\alpha = 220$  nm (the conventional kagome ASI), the Type *K*-I and *K*-II vertices are degenerate, leading to a disordered magnetic state with vertex populations of 33.75% and 66.25% for Type *K*-I and *K*-II vertices, respectively. This is consistent with the configurational (or random) populations of 1/3 and 2/3 for Type *K*-I and *K*-II vertices, as expected for a spin liquid, and proves that our demagnetization procedure effectively brought the system into an effective thermal equilibrium state. When  $L_\alpha > 220$  nm, the Type *K*-II vertices become an excited state. With increasing  $L_\alpha$ , the energy difference between Type *K*-I and Type *K*-II vertices increases [Fig. 1(c)] and thus the population of Type *K*-I vertices gradually increases. As shown in Figs. 2(g)–2(l), ordered domains of Type *K*-I vertices emerge and grow with increasing  $L_\alpha$ . For the sample with large  $L_\alpha$ , such as 440 nm [Fig. 2(l)], 93% of the vertices are in the Type *K*-I ground state, and domain walls composed of excited Type *K*-II vertices (red) are clearly visible. These results match nicely with our Monte Carlo simulations (Figs. S3 and S4 of Supplemental Material [45]) conducted using a thermal annealing protocol and considering only nearest-neighbor interactions (see Supplemental Material [45]). This suggests that the

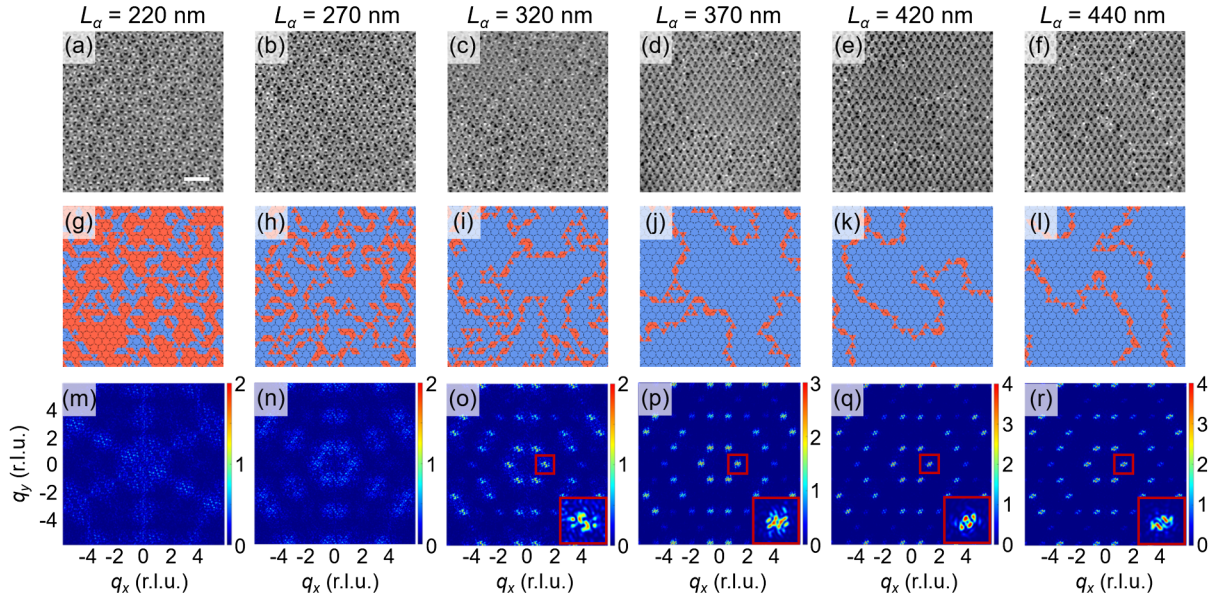


FIG. 2. Transition from liquid to crystal. (a)–(f) MFM images for samples with various  $L_\alpha$  values, respectively. Scale bar, 2  $\mu\text{m}$ . (g)–(l) spin configurations and vertex distributions extracted from (a)–(f). Type *K*-I and *K*-II vertices are shown in blue and red, respectively. (m)–(r) corresponding maps of magnetic structure factors calculated respectively from the spin configurations in (g)–(l). Insets of (o)–(r) show expanded views of the split Bragg peaks. r.l.u.: reciprocal lattice unit.



transition from SL1 phase to LRO spin crystal state is dominated by the nearest-neighbor interactions.

We can further elucidate the phase transition from liquid to crystal using magnetic structure factors [11,47]. Maps of the magnetic spin structure factor are shown in Figs. 2(m)–2(r). For the conventional kagome ASI ( $L_\alpha = 220$  nm), the magnetic spin structure factor map shows structured diffusive pattern [Fig. 2(m)], consistent with previous results of SL1 phase [13,36]. With gradually increasing  $L_\alpha$ , we can clearly observe the emergence and enhancement of Bragg peaks [Figs. 2(o)–2(r)]. These Bragg peaks show split-peak structures whose number reduces with increasing  $L_\alpha$ , as shown in the insets of Figs. 2(o)–2(r). These split Bragg peaks originate from scattering between domains, as demonstrated by the structure factor maps of the artificial domain configurations in Fig. S5 of Supplemental Material [45]. The number of domains decreases when they merge, resulting in a reduced number of split Bragg peaks. This suggests that the texture of Bragg peaks could be used as a qualitative parameter to investigate ordering and domain formation in ASIs, e.g., we could estimate the relative sizes of domains from the number of split Bragg peaks.

Previous investigations of conventional kagome ASIs revealed local ordering of magnetic charges [22–24]. Figures 3(a)–3(f) are maps of magnetic charge configurations corresponding to the spin and/or vertex configurations in Figs. 2(g)–2(l). We can see that the charge domains of the twofold degenerate phases (green and yellow) grow with increasing  $L_\alpha$ . When comparing the charge distributions to the vertex or spin distributions, we can see that their profiles match very well with each other for the samples with large  $L_\alpha$  values [Figs. 2(i)–2(l) and 3(c)–3(f)], i.e., the charge ordering is embedded in the spin ordering for spin crystal state. However, the charge and vertex distributions deviate as the number of Type K-II vertices increases [Figs. 2(g) and 3(a)]. A similar behavior is observed when we compare the magnetic spin structure factor maps with

the magnetic charge structure factor maps. For large  $L_\alpha$ , both spin [Figs. 2(o)–2(r)] and charge [Figs. 3(i)–3(l)] structure factor maps exhibit clear Bragg peaks with the same peak splitting [insets of Figs. 2(o)–2(r) and Figs. 3(i)–3(l)]. However, for small  $L_\alpha$  values, e.g., for the conventional kagome ASI with  $L_\alpha = L_\beta = 220$  nm, the spin structure factor map is structured but diffusive [Figs. 2(m) and 2(n)], while in contrast, the charge structure factor maps display clear Bragg peaks, although they are broad [Figs. 3(g) and 3(h)]. This indicates the emergence of charge ordering in the spin liquid state. As mentioned earlier, charge ordering should not appear when there are only nearest-neighbor interactions and the sixfold symmetry is not broken [21,35]. Our Monte Carlo simulations with only nearest-neighbor interactions show that there are no Bragg peaks in the magnetic charge structure factor map for conventional kagome ASI (Fig. S6g of Supplemental Material [45]). This suggests that further-neighbor interactions beyond nearest neighbor play a role in the liquid state. On the other hand, the consistency between experiment [Figs. 3(i)–3(l)] and simulation [Figs. S6(i)–S6(l)] of Supplemental Material [45] for samples with large  $L_\alpha$  unambiguously suggests the LRO spin crystal phase can be established with only nearest-neighbor interactions.

We have shown that the local interactions of an ASI have significant impact on their collective behavior and ultimately affect the properties of the entire system. The length of selective nanobar magnets can be used as a convenient knob to tune the local coupling strength, which enables us to access various low-energy manifolds and phase transitions in a fully disconnected ASI. We proved that although the next-nearest neighbor interaction plays a notable role through the magnetic charge structure factor maps, the crystallization of the kagome ice structure with reduced vertex degeneracies is dominated only by the nearest neighbor interaction. This method could be used to manipulate the frustration in ASIs for attaining even

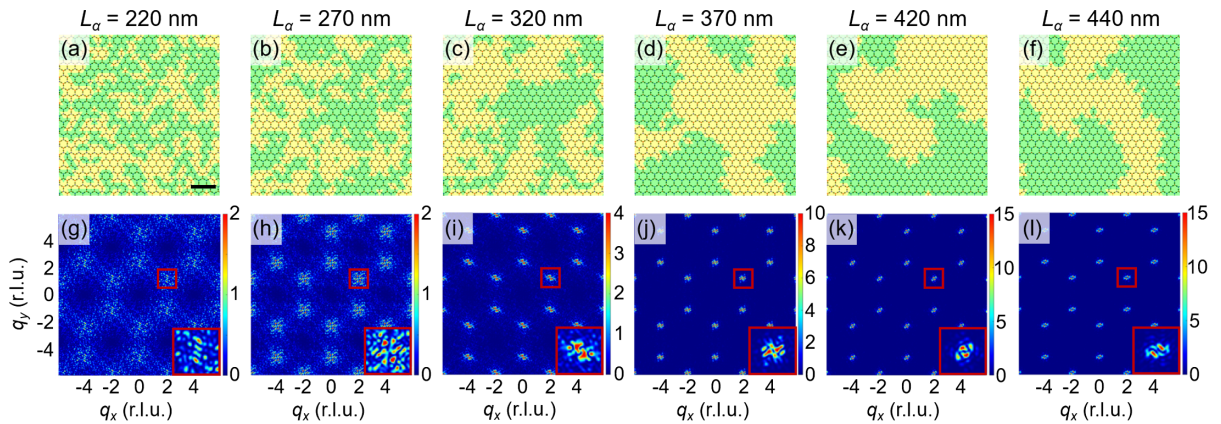


FIG. 3. Magnetic charge ordering. (a)–(f) magnetic charge distributions corresponding to MFM images in Figs. 2(a)–2(f), respectively. Green and yellow denote two phases of magnetic charge ordering. Scale bar,  $2 \mu\text{m}$ . (g)–(l) maps of magnetic charge structure factors associated with (a)–(f). Insets show expanded views of the split Bragg peaks. r.l.u.: reciprocal lattice unit.

more exotic ground state phases (see Figs. S7 of Supplemental Material [45]). It would also allow us to realize new magnetic configurations that are hard to access with magnetization method, e.g., to design novel ASIs with composite ground states in which different low energy states coexist in the same sample, as illustrated by the hybrid ground state of both liquid and crystal in Fig. S8 of Supplemental Material [45]. This would allow us to investigate phase transitions between these new types of low energy states. Furthermore, kinetics becomes topologically protected in the SL2 phase and in the LRO state [48], and our structural modifications can be employed to fine-tune different kinetic regimes in thermal realizations or under field inversions. In addition, this method is also applicable to other types of artificial spin ices, leading to new opportunities to explore more exotic collective phenomena, such as novel phases and phase transitions. It could also be combined with the other structure modification strategies, such as lattice transformation [49,50], to design new ASIs with controllable degeneracies. This method, maintaining the dipolar coupling between disconnected nanomagnets, could result in different spin dynamic properties and magnonic applications [51,52] than those in connected systems [36,37]. Moreover, our approach avoids complex analysis of the micromagnetic structures such as the domains and domain-walls in the vertices of connected systems, and thus offers a simpler kagome model which can connect with a variety of systems outside of magnetism, such as metal organic frameworks [53] and mechanical metamaterials [54,55]. Last but not least, the observed Bragg peaks' splitting induced by spin scattering between domains could lead to an alternative way to investigate domain-domain wall formation in ASIs.

This work is supported by the National Key R&D Program of China (2018YFA0209002 and 2021YFA0718802), the National Natural Science Foundation of China (61771235, 61971464, 61727805, 11961141002, 62101243), Jiangsu Excellent Young Scholar program (BK20200008), the Innovation Program for Quantum Science and Technology (2021ZD0303400) and Jiangsu Shuangchuang program. Part of the project design (Z. L. X.) and manuscript writing (Z. L. X. and W. K. K.) are supported by the U.S. Department of Energy, Office of Science, Basic Energy Sciences, Materials Sciences and Engineering. Z. L. X. also acknowledges support from the National Science Foundation under Grant No. DMR-1901843 for his efforts on data analysis. Y. D. acknowledges support from the Major Scientific Research Project of Zhejiang Lab (2019MB0AD01), the Center initiated Research Project of Zhejiang Lab (2021MBOAL01), and the Major Project of Natural Science Foundation of Zhejiang Province (LD22F050002). The work of C. N. was carried out under the auspices of the U.S.

DoE through the Los Alamos National Laboratory, operated by Triad National Security, LLC (Contract No. 229892333218NCA000001) and founded by a grant from the DOE-LDRD office.

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