

# Resonant Control of Elastic Collisions between $^{23}\text{Na}^{40}\text{K}$ Molecules and $^{40}\text{K}$ Atoms

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We have demonstrated the resonant control of the elastic scattering cross sections in the vicinity of Feshbach resonances between  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms by studying the thermalization between them. The elastic scattering cross sections vary by more than 2 orders of magnitude close to the resonance, and can be well described by an asymmetric Fano profile. The parameters that characterize the magnetically tunable  $s$ -wave scattering length are determined from the elastic scattering cross sections. The observation of resonantly controlled elastic scattering cross sections opens up the possibility to study strongly interacting atom-molecule mixtures and improve our understanding of the complex atom-molecule Feshbach resonances.

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Feshbach resonances are of great importance to the study of ultracold gases [1]. They occur when the energy of a bound state of a collisional system coincides with that of a scattering state. Magnetic fields can be used to tune the collisional system in and out of resonances if the bound state and the scattering state have different magnetic moments. The magnetically tunable atomic Feshbach resonances have been used as a powerful tool to study strongly interacting quantum gases [2–4], Efimov resonances [5], and the association of diatomic molecules [6,7]. Resonant control of the  $s$ -wave scattering length is essential to these applications [8–11].

Feshbach resonances involving ultracold molecules are remarkably complex [12]. For the heavy alkali-metal diatomic molecules formed from ultracold atomic gases [13–21], many rovibrational states of the molecules may contribute to resonant states, and thus it is expected that scattering resonances play crucial roles in ultracold collisions involving molecules. However, the large number of collision channels, the uncertainties of the potential energy surface, and the complexity of the three-body or four-body dynamics make the coupled-channel calculations very difficult. Such theoretical studies are now becoming increasingly possible due to recent advances in numerical simulations of ultracold molecular dynamics [22–29]. Currently, ultracold collisions involving molecules are usually studied by analyzing the density of short-range chaotic resonant states using the statistical method [30,31]. The universal loss rate coefficient is one of the main predictions, which is usually compared with the experiments [15–18,21,32–35]. However, for atom-molecule collisions, the estimated mean spacing between neighboring states is actually much larger

than the temperature of the ultracold gases [23,36,37] and thus the analysis based on the density of states and the thermal averaging over many resonances is in principle not applicable. A recent experiment in  $^{40}\text{K}^{87}\text{Rb} + ^{87}\text{Rb}$  collisions has reported a lifetime of the complex that is about 5 orders larger than the predictions based on the density of states [38].

Recently, magnetically tunable atom-molecule Feshbach resonances have been observed in inelastic collisions between singlet ground-state  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms [39,40], and reactive collisions between triplet ground-state  $^{23}\text{Na}^6\text{Li}$  molecules and  $^{23}\text{Na}$  atoms [41]. A detailed analysis of the resonance pattern in collisions of  $^{23}\text{Na}^{40}\text{K}$  with  $^{40}\text{K}$  suggests that the resonant states associated with these resonances may be the long-range bound states [40], but not the short-range chaotic bound states that are usually considered. The observation of well-isolated individual atom-molecule Feshbach resonances opens up the possibility of controlling the interactions in atom-molecule gases. For molecular collisions with inelastic or reactive losses, the  $s$ -wave scattering length in the vicinity of Feshbach resonances may be described by a simple formula [42],

$$a(B) = a_{\text{BG}} \left( 1 - \frac{\Delta}{B - B_0 - i\gamma/2} \right), \quad (1)$$

where  $a_{\text{BG}}$  denotes the background scattering length,  $B_0$  represents the resonance position,  $\Delta$  represents the resonance width, and  $\gamma$  is a total decay term including the natural linewidth of the bound state and the width due to the coupling between the bound and scattering states.

So far, only the resonantly enhanced losses of the molecules can be studied near the Feshbach resonances. This largely limits the application of the atom-molecule Feshbach resonance, since many important applications of Feshbach resonances require the control of the  $s$ -wave scattering length or equivalently, the elastic collision cross sections  $\sigma_{\text{el}} = 4\pi|a|^2$ . Because of the large inelastic loss rate coefficients, it is unclear whether tunable elastic collisions can be observed. Although in the collisions between  $^{23}\text{Na}^{6}\text{Li}$  and  $^{23}\text{Na}$ , a model based on the Fabry-Perot interferometer is used to extract the scattering length from the enhanced loss rate coefficients [41], direct observation of magnetically controlled elastic collisions or the scattering length remains elusive.

In this Letter, we report on the study of resonant control of elastic collisions in the vicinity of a Feshbach resonance between  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms. The  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms are both prepared in the maximally spin stretched state. We study the thermalization between  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms, from which the elastic scattering cross sections can be obtained. We find that the elastic scattering cross sections vary by more than 2 orders of magnitude close to the resonance. The elastic scattering cross sections can be well described by an asymmetric Fano profile, which is a hallmark of Feshbach resonance. The four parameters that characterize a Feshbach resonance are directly obtained from the elastic scattering cross sections. The demonstration of resonantly controlling the  $s$ -wave scattering length paves the way towards studying strongly interacting atom-molecule mixtures and improves the understanding of the complex atom-molecule collisions.

Our experiment starts with an ultracold mixture of  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms. The experimental procedures for preparing the ultracold mixture have been introduced in previous works [43,44]. Briefly, we load laser-cooled  $^{23}\text{Na}$  and  $^{40}\text{K}$  atoms into a cloverleaf magnetic trap to perform evaporative cooling. The atomic mixtures are then loaded into a large-volume three-beam optical dipole trap for further evaporative cooling. At the end of optical evaporative cooling, we create an atomic mixture containing about  $3.0 \times 10^5$   $^{23}\text{Na}$  atoms and  $2.3 \times 10^5$   $^{40}\text{K}$  atoms. The trap frequencies for  $^{40}\text{K}$  atoms are  $(\omega_x, \omega_y, \omega_z) = 2\pi \times (238, 71, 24)$  Hz. The atomic Feshbach resonance between the  $|f, m_f\rangle_{\text{Na}} = |1, 1\rangle$  state and the  $|f, m_f\rangle_{\text{K}} = |9/2, -9/2\rangle$  state at about 78.3 G is used to form  $^{23}\text{Na}^{40}\text{K}$  Feshbach molecules. We ramp the magnetic field from 80 G to 77.6 G to create about  $2.8 \times 10^4$   $^{23}\text{Na}^{40}\text{K}$  Feshbach molecules. The  $^{23}\text{Na}^{40}\text{K}$  Feshbach molecules are then transferred to the rovibrational ground state by stimulated Raman adiabatic passage (STIRAP). We prepare the  $^{23}\text{Na}^{40}\text{K}$  molecules in the maximally polarized hyperfine level  $|v, N, m_{i_{\text{Na}}}, m_{i_{\text{K}}}\rangle = |0, 0, -3/2, -4\rangle$  of the rovibrational ground state, where  $v$  and  $N$  represent the vibrational and rotational quantum

numbers, and  $m_{i_{\text{Na}}}$  and  $m_{i_{\text{K}}}$  denote the nuclear spin projections of  $^{23}\text{Na}$  and  $^{40}\text{K}$ , respectively. We use the hyperfine level of the excited state  $F_1 \approx 3/2$ ,  $m_{F_1} \approx -3/2$ , and  $m_K \approx -3$  as the intermediate state for the STIRAP [45,46]. The  $\sigma^-$  polarized pump laser and the  $\sigma^+$  polarized Stokes laser propagate along the direction of the magnetic field. The efficiency of a round-trip STIRAP is about 50%. After removing the remaining  $^{23}\text{Na}$  atoms by resonant light pulses, we prepare an ultracold mixture of  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms.

We study the elastic collisions between  $^{23}\text{Na}^{40}\text{K}$  molecules in the  $|0, 0, -3/2, -4\rangle$  state and  $^{40}\text{K}$  atoms in the  $|9/2, -9/2\rangle$  state in the vicinity of an atom-molecule Feshbach resonance located at about 48 G. After the ultracold atom-molecule mixture is prepared, we ramp the magnetic field to a target value in 3 ms. We then apply a 50- $\mu\text{s}$  weak resonant light pulse to heat the  $^{40}\text{K}$  atoms. After the heating pulse, the temperatures of the  $^{40}\text{K}$  atoms and the  $^{23}\text{Na}^{40}\text{K}$  molecules are about 500 nK and 300 nK, respectively. The heating light pulse also reduces the atom numbers by a factor of about 2. The  $^{23}\text{Na}^{40}\text{K}$  molecules and the  $^{40}\text{K}$  atoms are held at the target magnetic field for a short time. The uncertainty of the magnetic field is about 200 mG. We then remove the  $^{40}\text{K}$  atoms by a strong resonant light pulse and ramp the magnetic field back to 77.6 G. The  $^{23}\text{Na}^{40}\text{K}$  molecules are transferred back to the Feshbach state and are detected by absorption imaging along the  $z$  direction.

During the hold time at the target magnetic field, the temperature of the  $^{23}\text{Na}^{40}\text{K}$  molecules will increase due to elastic collisions with the  $^{40}\text{K}$  atoms. We have checked that the heating of the molecules is dominantly caused by the elastic collisions with the hot atoms. If the atoms are not heated, no notable heating of the molecules can be observed. Since the number of  $^{40}\text{K}$  atoms is about one order of magnitude larger than that of the molecules, we may assume that the temperature of the  $^{40}\text{K}$  atoms is constant and the temperature of the  $^{23}\text{Na}^{40}\text{K}$  molecules changes according to  $T(t) = T_f - (T_f - T_i)e^{-\Gamma_{\text{th}}t}$ , where  $T_i$  and  $T_f$  represent the initial and final temperatures, respectively, and  $\Gamma_{\text{th}}$  is the thermalization rate. The thermalization rate can be extracted from the time evolution of the molecule cloud sizes. For a Maxwell-Boltzmann distribution, the column density distributions obtained from the absorption image can be fit to two-dimensional Gaussian functions  $\propto e^{-x^2/(2\sigma_x^2) - y^2/(2\sigma_y^2)}$ , where the cloud sizes along the  $x$  and  $y$  directions can be described by  $\sigma_{x,y}^2(t) = [k_B T(t)/m_{\text{NaK}}](\tau_{\text{TOF}}^2 + 1/\omega_{x,y}^2)$ , with  $\tau_{\text{TOF}}$  being the time of flight.

The squares of the molecule cloud sizes  $\sigma_{x,y}^2$  extracted from the absorption images are shown in Fig. 1 as a function of the hold time for several target magnetic fields. The increases of the cloud sizes along both the  $x$  and  $y$  directions versus the hold time reflect the thermalization

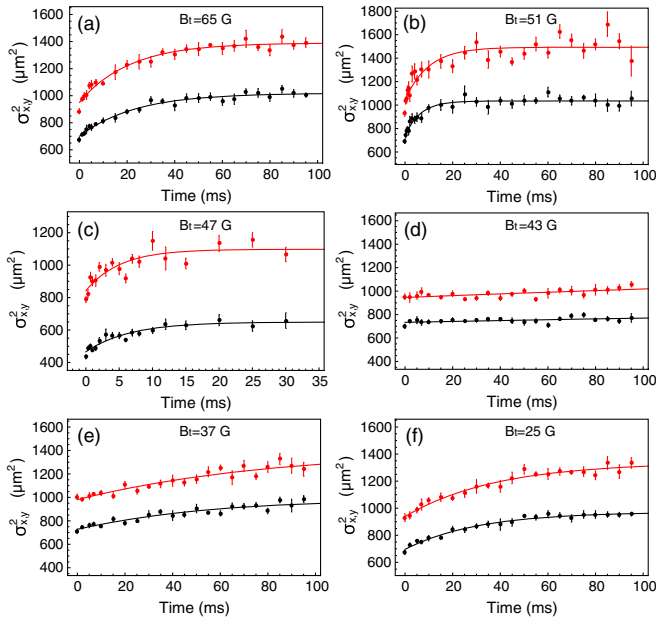


FIG. 1. The thermalization of the  $^{23}\text{Na}^{40}\text{K}$  molecules following the heating of the  $^{40}\text{K}$  atoms. The squares of the molecular cloud sizes  $\sigma_x^2$  (red) and  $\sigma_y^2$  (black) are plotted as a function of the hold time at various target magnetic fields. The molecular cloud sizes are extracted from the absorption images taken after a time of flight of 3–4 ms. The increases of cloud sizes are due to the elastic collisions between the  $^{23}\text{Na}^{40}\text{K}$  molecules and the  $^{40}\text{K}$  atoms. The solid lines are the fits of the data points to exponential functions  $\sigma_{x,y}^2 = A_{x,y}e^{-\Gamma_{x,y}t} + B_{x,y}$  where the parameters  $A$ ,  $B$ , and  $\Gamma$  are the fitting parameters. For the magnetic fields close to 43 G at which the thermalization is very weak, the parameters  $B$  are fixed. The mean thermalization rate  $\Gamma_{\text{th}} = (\Gamma_x + \Gamma_y)/2$  is used to calculate the elastic scattering cross section. Error bars represent the standard error of the mean.

due to elastic collisions. It can be clearly seen that the thermalization rate changes with the magnetic fields. The thermalization is very fast at 47 G, which indicates that the elastic collisions are resonantly enhanced. However, at 43 G the thermalization is largely suppressed. This indicates that the elastic scattering cross section has a minimum at about 43 G. Note that at 48 G, it is difficult to determine the thermalization rate due to the strong inelastic losses. We fit the molecule cloud sizes using an exponential function  $\sigma_{x,y}^2 = A_{x,y}e^{-\Gamma_{x,y}t} + B_{x,y}$  where the parameters  $A$ ,  $B$ , and  $\Gamma$  are the fitting parameters. For the magnetic fields close to 43 G, the thermalization is very weak, and thus we set the parameter  $B$  to the mean value of the fit results obtained at other magnetic fields to obtain a stable fit.

We determine the elastic scattering cross section from the measured thermalization rate using the formula [47–49]  $\Gamma_{\text{th}} = n_{\text{ov}}\sigma_{\text{el}}v_{\text{rel}}/(3/\xi)$ , where  $n_{\text{ov}} = (N_{\text{NaK}} + N_{\text{K}}) \times \{(2\pi k_B T_{\text{K}}/m_{\text{K}}\bar{\omega}_{\text{K}}^2)[1 + (m_{\text{K}}T_{\text{NaK}}/m_{\text{NaK}}T_{\text{K}}\gamma_t^2)]\}^{-3/2}$  is the overlap density with  $\gamma_t = 0.79$  being the ratio between the trap frequencies for  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$  atoms,

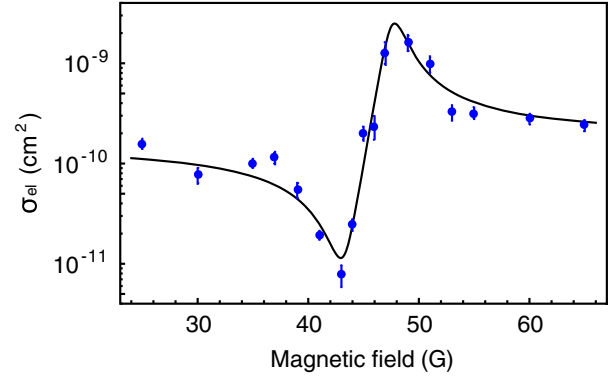


FIG. 2. The elastic scattering cross sections, calculated from the thermalization rate, are plotted as a function of the magnetic fields. The solid line is the fit using the formula  $\sigma_{\text{el}} = 4\pi(\alpha^2 + \beta^2)$ , where the scattering length  $a = \alpha - i\beta$  is given by Eq. (1). The parameters obtained from the fit are  $a_{\text{BG}} = -692(36)a_0$ ,  $\Delta = -4.3(4)$  G,  $B_0 = 47.5(3)$  G, and  $\gamma = 2.4(4)$  G. Error bars represent the standard error.

$v_{\text{rel}} = \sqrt{(8k_B/\pi)(T_{\text{K}}/m_{\text{K}} + T_{\text{NaK}}/m_{\text{NaK}})}$  is the relative mean velocity, and the parameter  $\xi = 4m_{\text{NaK}}m_{\text{K}}/(m_{\text{NaK}} + m_{\text{K}})^2$  represents the mass effect. The elastic scattering cross sections determined in this way are shown in Fig. 2 as a function of the magnetic fields, where the mean value  $\Gamma_{\text{th}} = (\Gamma_x + \Gamma_y)/2$  is used in the calculation.

The elastic scattering cross sections can be changed by more than 2 orders of magnitude via varying the magnetic field. The elastic scattering cross section shows a clear asymmetric Fano line shape [1,50], which is a hallmark of Feshbach resonance. The minimum of the elastic scattering cross section is caused by the Fano interference between the background scattering amplitude in the open channel and the resonant scattering amplitude originating from the bound state in the closed channel. It represents the quantum control of the elastic atom-molecule collisions via quantum interference.

We use Eq. (1) to describe the  $s$ -wave scattering length. In this case, the  $s$ -wave elastic scattering cross section may be described by  $\sigma_{\text{el}} = 4\pi(\alpha^2 + \beta^2)$ , where the complex scattering length  $a = \alpha - i\beta$  with  $\alpha$  and  $\beta$  real numbers. When using this simple analytic model, we have neglected the momentum-dependent factor  $f(k) = 1/(1 + k^2|a|^2 + 2k\beta)$  [42,51], which will be important very close to the resonance position. This is justified since the data used in the fit are not very close to the resonance position, and thus the momentum-dependent factor may be neglected. We fit the measured elastic scattering cross sections using this analytic formula, where  $a_{\text{BG}}$ ,  $\Delta$ ,  $B_0$ , and  $\gamma$  are the fitting parameters.

The fit can only give the absolute value of the background scattering length, but not its sign. The sign of the background scattering length can be determined as follows. Since the minimum of the scattering cross section is below the resonance position, there are two possibilities. If the

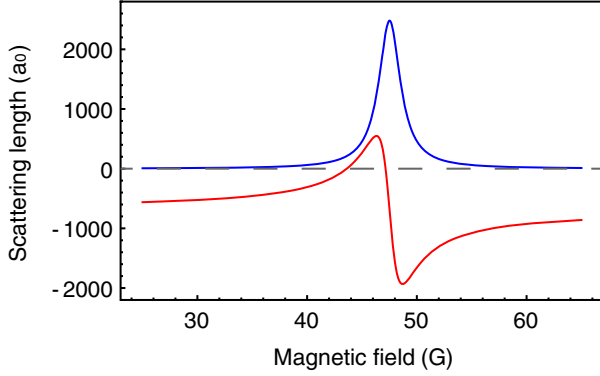


FIG. 3. The real (red) and imaginary (blue) parts of the scattering length are plotted as a function of the magnetic field. The scattering length is plotted according to Eq. (1), with the parameters determined from the elastic scattering cross sections.

bound state is on the low field side of the resonance, the background scattering length is negative. On the contrary, the background scattering length is positive. Following the arguments in Ref. [40], since both the molecules and atoms are in the maximally polarized state, the triatomic bound states accounting for this resonance must have a nonzero total spin-free rotational angular momentum  $J \geq 1$ , and the bound state must approach the scattering state from the low field side of the resonance. Therefore, the background scattering length is negative. We obtain  $a_{BG} = -692(36)a_0$ ,  $\Delta = -4.3(4)$  G,  $B_0 = 47.5(3)$  G, and  $\gamma = 2.4(4)$  G. The magnetically tunable scattering length is thus determined. The real and imaginary parts of the scattering length are plotted in Fig. 3.

The strong coupling between the bound state and the scattering state causes avoided crossing, and thus the resonance position is different from the intersection between the bare bound state and the scattering state. The intersection between the bare states may be determined using the formula [52]  $B_c = B_0 - \Delta r_{BG}(1 - r_{BG})/[1 + (1 - r_{BG})^2]$ , where  $r_{BG} = a_{BG}/\bar{a}$  with  $\bar{a} = 74a_0$  the mean scattering length. We obtain  $B_c = 43.7$  G, which is about 4 G lower than the resonance position. This value is very close to the narrow resonances at about 43.4 G in the collision channels  $|0, 0, -1/2, -4\rangle + |9/2, -9/2\rangle$  and  $|0, 0, 1/2, -4\rangle + |9/2, -9/2\rangle$  [40]. This indicates that the bare bound states for these resonances may bunch together, even if the projections of the total angular momentum are different. Therefore, the determination of the bare bound state for broad resonances is important to understand the resonance pattern. The resonance pattern may be used to estimate the magnetic moment between the bound state and the scattering state.

It is interesting to compare the elastic collisions with the inelastic collisions. To this end, we measure the loss rate coefficients of the  $^{23}\text{Na}^{40}\text{K}$  molecules in the atom-molecule mixtures. After ramping the magnetic field to a target value, we monitor the time evolution of the  $^{23}\text{Na}^{40}\text{K}$  molecules.

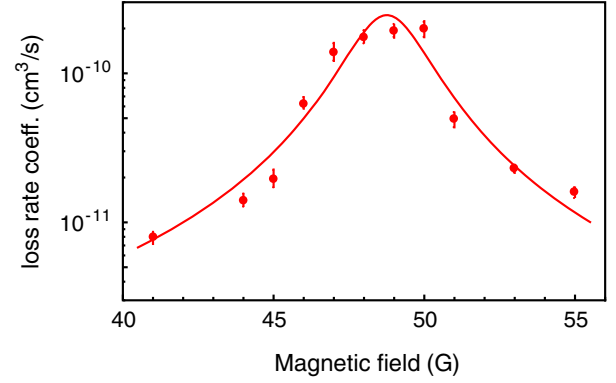


FIG. 4. The loss rate coefficients obtained by measuring the losses of the  $^{23}\text{Na}^{40}\text{K}$  molecules in the atom-molecule mixture. The solid line is a Lorentzian fit to the data. Error bars represent the standard error.

Assuming the loss of the  $^{23}\text{Na}^{40}\text{K}$  molecules is caused by two-body inelastic collisions with the  $^{40}\text{K}$  atoms, the loss rate coefficients are given by the ratio between the measured decay rate and the density of  $^{40}\text{K}$  atoms overlapped with  $^{23}\text{Na}^{40}\text{K}$  molecules atoms. The measured loss rate coefficients are shown in Fig. 4. According to Eq. (1), if we assume  $a_{BG}$  is real, the loss rate coefficient is proportional to  $\beta$  which is described by a Lorentz function [53]. A Lorentz fit of the data points gives the resonance position  $B_0^{\text{in}} = 48.8(3)$  G and the FWHM width  $\gamma^{\text{in}} = 2.8(5)$  G. These values are very close to the values determined from the elastic collision cross sections. The peak value of the loss rate coefficient is larger than the universal loss rate coefficients  $1.3 \times 10^{-10} \text{ cm}^3/\text{s}$  by a factor of about 2.

The maximum loss rate coefficient may also be calculated from the formula  $2h\beta f(k)/\mu$  with  $\mu$  the reduced mass, using the parameters determined from the elastic scattering cross sections. Integrating over a Maxwell distribution, we obtain a maximum loss rate coefficient of about  $1.5 \times 10^{-9} \text{ cm}^3/\text{s}$ . This value is larger than the measured peak value by a factor of about 6. Several reasons may cause this discrepancy. One reason is the uncertainty of the density calibration, which is difficult to determine accurately. Another reason is that for the loss measurement, the  $^{40}\text{K}$  atoms are in the moderate degenerate regime with a temperature of about  $0.6 T_F$ . However, for simplicity, we have used the Maxwell distribution to calculate the loss rate coefficients. Future work is needed to understand whether there are other important mechanisms. Besides, given the measured elastic scattering cross sections and the inelastic loss rate coefficients, we may estimate the good-to-bad collision ratio using the ratio between  $\sigma_{\text{el}} v_{\text{rel}}$  and the loss rate coefficients. The obtained good-to-bad collision ratio is about 10-30 at the magnetic fields between 49 G and 55 G.

In summary, we have demonstrated the resonant control of elastic collisions between  $^{23}\text{Na}^{40}\text{K}$  molecules and  $^{40}\text{K}$



atoms. The observation of the magnetic tunable elastic scattering cross sections will help to improve our understanding of the complex atom-molecule Feshbach resonances. In previous theoretical works, different theoretical models are developed to calculate the loss rate coefficients [30,31,36,37,51] and compare them with experiments [15–18,21,32–35]. The tunable elastic scattering cross sections near the Feshbach resonances thus provide an important benchmark for future theoretical studies of atom-molecule collisions. The elastic scattering cross sections may also be useful in determining the short-range parameters required in the multichannel quantum-defect model for anisotropic interactions [54].

The direct observation of the elastic scattering cross sections or the scattering length opens up the possibility of studying strongly interacting atom-molecule mixtures. Recently, ultracold mixtures of molecules and atoms have been proposed to study a new type of impurity problem, i.e., angulon [55–58], which is a counterpart of the polaron. The atom-molecule Feshbach resonances may be useful since it can provide the strong interaction that is necessary in studying the impurity problem in ultracold gases [59–62]. Besides studying strongly interacting mixtures, the universal binding energies of the triatomic bound states close to the resonance may be determined from the scattering length, which can be compared with the binding energies obtained from the radio-frequency association spectroscopy [43].

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