## **Radium Ion Optical Clock**

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We report the first operation of a Ra<sup>+</sup> optical clock, a promising high-performance clock candidate. The clock uses a single trapped <sup>226</sup>Ra<sup>+</sup> ion and operates on the  $7s^2S_{1/2} \rightarrow 6d^2D_{5/2}$  electric quadrupole transition. By self-referencing three pairs of symmetric Zeeman transitions, we demonstrate a frequency instability of  $1.1 \times 10^{-13}/\sqrt{\tau}$ , where  $\tau$  is the averaging time in seconds. The total systematic uncertainty is evaluated to be  $\Delta \nu/\nu = 9 \times 10^{-16}$ . Using the clock, we realize the first measurement of the ratio of the  $D_{5/2}$  state to the  $S_{1/2}$  state Landé g-factors:  $g_D/g_S = 0.598 \, 805 \, 3(11)$ . A Ra<sup>+</sup> optical clock could improve limits on the time variation of the fine structure constant,  $\dot{\alpha}/\alpha$ , in an optical frequency comparison. The ion also has several features that make it a suitable system for a transportable optical clock.

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Optical clocks, based on narrow-linewidth atomic transitions, are the most precise instruments ever realized [1]. The performance of several optical clocks, using different atoms, have now surpassed that of the primary cesium frequency standard [2-5], which marks a significant advance toward a proposed redefinition of the second [6]. Optical clocks also have the potential to uncover new physics beyond the standard model at the highprecision, low-energy frontier, including searches for ultralight scalar dark matter [7], the time variation of fundamental constants [8,9], and violations of Einstein's equivalence principle [10]. In an effort to improve clock performance, atomic systems that are less sensitive to limiting systematic uncertainties such as Lu<sup>+</sup> [11] and  $Ba^{4+}$  [12] have been proposed. For both advancing clock performance and for their enhanced sensitivity to potential sources of new physics, systems including highly charged ions [13] and a radioactive thorium nuclear clock [14,15] are being pursued.

The radium ion is well suited to realizing a highperformance optical clock [16]. The  $7s^2S_{1/2} \rightarrow 6d^2D_{5/2}$ electric quadrupole clock transition ( $\lambda = 728$  nm,  $\tau \approx 300$  ms,  $\Gamma/2\pi = 0.5$  Hz) in Ra<sup>+</sup> has a small, negative differential static scalar polarizability (DSSP)  $\Delta \alpha_0 =$ -22.2(1.7) a.u. [17]. This leads to both a small frequency shift due to the blackbody radiation (BBR) environment and allows for clock operation at a trap drive frequency (6.2 MHz) such that the micromotion-induced scalar Stark shift and the second-order Doppler shift cancel [18,19]. Along with the expected clock performance, the radium ion has the largest positive enhancement to the time variation of the fine structure constant,  $\kappa_{Ra} = 2.8$ , of any demonstrated clock [20]. The current constraint on  $\dot{\alpha}/\alpha$  is derived from a frequency comparison between an optical clock based on the Yb<sup>+</sup> (E2) transition ( $\tau \approx 50$  ms) and a second clock based on the Yb<sup>+</sup> (E3) transition [9]. Considering sensitivities of demonstrated clocks, the Yb<sup>+</sup> (E2) transition has the second largest positive enhancement to the time variation of the fine structure constant,  $\kappa_{E2} = 1$ , and the Yb<sup>+</sup> (E3) transition has largest negative enhancement,  $\kappa_{E3} = -6$ . This makes the radium ion an appealing system to compare against other clocks to improve constraints on  $\dot{\alpha}/\alpha$ .

In this Letter, we demonstrate the first operation of a radium optical clock by stabilizing a narrow-linewidth laser at 728 nm to the  $7s^2S_{1/2} \rightarrow 6d^2D_{5/2}$  transition of a single  $^{226}$ Ra<sup>+</sup> ion (I = 0). The 728 nm laser is an external cavity diode laser stabilized to an ultralow expansion glass cavity. We present an evaluation of the key systematic shifts and uncertainties as well as a self-referenced measurement of the clock frequency instability. From measurements made during the clock operation, we report the first measurement of the ratio of the  $D_{5/2}$  state to the  $S_{1/2}$  state Landé *g*-factors.

The relevant Ra<sup>+</sup> level structure, laser configuration, and quantization field used in this Letter are shown in Fig. 1. A single radium-226 ion is loaded by laser ablation of an  $\sim 10 \ \mu \text{Ci} \text{ RaCl}_2$  target located 15 mm from the center of a linear Paul trap with characteristic dimensions  $r_0 = 3$  and  $z_0 = 7.5$  mm, see [21]. The radio frequency (rf) trap drive is operated at  $\Omega_{\rm rf}/2\pi = 993$  kHz, and for a single radium ion the axial secular frequency is  $\omega_z/2\pi = 78.5$  kHz and the radial secular frequencies are  $\omega_r/2\pi = 141$  and 156 kHz. Acousto-optic modulators (AOMs) control the frequency and amplitude of all beams during clock operation. Clock state readout is performed by collecting 468 nm photons scattered by the Ra<sup>+</sup> ion onto a photomultiplier tube [22]. As there is no magnetic field shielding around the vacuum apparatus, each clock interrogation cycle is synchronized to the laboratory 60 Hz power line to minimize Zeeman shifts due to magnetic field fluctuations.

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FIG. 1. (a) The Ra<sup>+</sup> level structure for clock operation. (b) Orientation of the lasers and the magnetic field used in this Letter. The 728 nm clock beam (red) is at 45° with respect to the magnetic field to drive all ten possible Zeeman transitions between the  $S_{1/2}$  and  $D_{5/2}$  states.

Linearly polarized 728 nm light is used to drive the  $|S_{1/2}, m = \pm 1/2\rangle \rightarrow |D_{5/2}, m = \pm 1/2\rangle$  (C1),  $|S_{1/2}, m = \pm 1/2\rangle \rightarrow |D_{5/2}, m = \pm 3/2\rangle$  (C2), and  $|S_{1/2}, m = \pm 1/2\rangle \rightarrow |D_{5/2}, m = \pm 5/2\rangle$  (C3) symmetric Zeeman transitions to operate the clock in a self-comparison mode [23]. By measuring symmetric Zeeman components that comprise all sublevels of the  $D_{5/2}$  state (|m| = 1/2, 3/2, 5/2), the linear Zeeman shift and the electric quadrupole shift are both canceled [23,24].

Each clock interrogation cycle begins with an initial state detection (0.5 ms) to determine correct initialization of the population into the  $S_{1/2}$  or  $D_{3/2}$  laser cooling states. Following the initial state detection, the ion is Doppler cooled (5 ms) and the population is optically pumped to the appropriate  $|S_{1/2}, m = \pm 1/2\rangle$  state (2 ms). We then coherently interrogate the clock transition (3 ms) on either the blue- or red-detuned half width at half maximum (HWHM), after which a state detection pulse is applied. In addition to probing the HWHM of the Zeeman transitions to determine the transition center frequency, we also interrogate the peak maximum, as well as six detunings around the peak. For every 20 interrogation cycles of the HWHM and peak maximum, we interrogate the six detunings around the peak to ensure that symmetric Zeeman transitions are probed with equal excitation probabilities and that all transitions remain locked, see Fig. 2 inset. To reset the system, we clean out population remaining in the  $D_{5/2}$  state by driving the  $D_{5/2} \rightarrow P_{3/2}$ dipole transition (200  $\mu$ s) where decays populate the  $S_{1/2}$ and  $D_{3/2}$  states.

After each interrogation cycle, the frequencies of the six Zeeman transitions are updated with individual lock servos to stabilize the clock laser's frequency to the  $7s^2S_{1/2} \rightarrow 6d^2D_{5/2}$  atomic resonance. The error signal for an interrogation cycle is given by  $E = (n_b - n_r)/n$ , where  $n_b$  and  $n_r$  are the number of times the population was driven to the excited state during interrogation on the blue- and red-detuned HWHM and n = 20 is the total number of interrogations [23]. If the initial state detection determined that the population was in the  $D_{5/2}$  state, the interrogation is not



FIG. 2. Allan deviation of the Ra<sup>+</sup> optical clock measured over  $\approx 100\,000$  s. The fractional stability (blue line) with a 3 ms interrogation time is  $1.1 \times 10^{-13}/\sqrt{\tau}$ . The quantum projection noise limit that accounts for the motional decoherence and line shape is calculated using the method described in [23]. The inset shows the  $|S_{1/2}, m = -1/2\rangle \rightarrow |D_{5/2}, m = -1/2\rangle$  Zeeman transition averaged over the entire measurement. The HWHM lock points are magnified by 200× on both axes. Error bars represent one standard deviation. The proportion of the population driven to the excited state is limited by decoherence due to thermal motion. The Fourier-limited linewidth of the measured transition corresponds to a 2.7 ms interrogation time.

used in the error signal calculation. The shift of the center detuning of each Zeeman transition is updated from the previous detuning using the error signal and the measured drift rate of the optical cavity. Both of these values are updated throughout the experiment based on the shift of the clock transition center frequency, see Supplemental Material [25]. The center frequency of the  $7s^2S_{1/2} \rightarrow$  $6d^2D_{5/2}$  transition is derived from an average of the three Zeeman pairs (C1, C2, and C3) following each interrogation cycle. The total interrogation cycle time for the three pairs of Zeeman transitions is 10 s, where the 20 interrogation cycles of the HWHM and peak maximum takes ~6.1 s, the single interrogation cycle of the six detunings around the peak takes ~0.6 s, and the pulse programming and data saving takes ~3 s.

The measured Ra<sup>+</sup> clock instability is shown in Fig. 2. An Allan deviation is obtained from the frequency difference of the three Zeeman pairs: (C1, C2), (C2, C3), and (C1, C3). The average of these three Allan deviations is divided by  $\sqrt{6}$  to obtain the self-referenced fractional frequency stability of  $\sigma(\tau) = 1.1 \times 10^{-13}/\sqrt{\tau}$ , where  $\tau$  is the averaging time in seconds [23].

A summary of systematic frequency shifts and uncertainties is shown in Table I. The overall frequency instability is currently limited by the clock interrogation time and the dead time in the total interrogation cycle. The 3 ms interrogation time on the clock transition is mainly limited by decoherence due to short-term ambient magnetic field

TABLE I. Fractional frequency shifts  $(\Delta \nu / \nu)$  and uncertainties of the <sup>226</sup>Ra<sup>+</sup> 7s<sup>2</sup>S<sub>1/2</sub>  $\rightarrow$  6d<sup>2</sup>D<sub>5/2</sub> clock.

Effect	Shift	Uncertainty
Clock laser Stark shift	$1.7 \times 10^{-15}$	$9 \times 10^{-16}$
Blackbody radiation	$4.3 \times 10^{-16}$	$4 \times 10^{-17}$
Magnetic field drift	0	$2 \times 10^{-18}$
Background gas collisions	0	$6 \times 10^{-19}$
Secular motion	$-6.0 \times 10^{-19}$	$6 \times 10^{-19}$
Excess micromotion	$-4.2 \times 10^{-18}$	$5 \times 10^{-19}$
Quadratic Zeeman	$4.2151 \times 10^{-16}$	$1.2 \times 10^{-19}$
Electric quadrupole	0	$3 \times 10^{-20}$
Total	$2.5 \times 10^{-15}$	$9 \times 10^{-16}$

noise. The 728 nm clock laser intensity used to drive a  $\pi$ -pulse with a 3 ms interrogation time is 0.5(3) kW/m<sup>2</sup>, which leads to a probe-induced ac Stark shift of  $\Delta \nu / \nu = (1.7 \pm 0.9) \times 10^{-15}$ . This shift can be reduced by several orders of magnitude by implementing upgrades to the apparatus, such as magnetic field shielding and a trap that can support stronger radial confinement, which would enable interrogation times that approach the  $D_{5/2}$  excited state lifetime of  $\tau \sim 300$  ms [30]. Additionally, techniques such as hyper-Ramsey spectroscopy [31] or frequency stepping [32] could reduce this shift. All other laser beams (468, 802, 1079 nm) are turned off using double-pass AOMs during the clock interrogation pulse. To ensure that there is no leakage light present through the AOMs, they are also backed with mechanical shutters. During each interrogation cycle, the mechanical shutters are closed before the clock laser pulse.

Blackbody radiation generated by the finite temperature of the trapping environment causes an ac Stark shift on the clock transition, which depends on the DSSP of the transition and the effective temperature of the BBR at the location of the ion. The BBR-induced frequency shift evaluated using the theoretical DSSP,  $\Delta \alpha_0 =$ is -22.2(1.7) a.u. [17] and the effective temperature of the BBR field at the ion's location,  $T_{BBR} = 295(4)$  K [33]. To determine the ambient effective temperature and uncertainty observed by the ion, we measured the maximum temperature differential (3 K) of the vacuum chamber and performed a numerical simulation, using a finite element method, to estimate the maximum temperature rise (0.3 K)of the ion trap due to trap drive heating. The resulting BBR-induced frequency shift is evaluated as  $\Delta \nu / \nu =$  $(4.3 \pm 0.4) \times 10^{-16}$ . At the current level of precision, the total uncertainty in the BBR shift is dominated by the uncertainty in the DSSP, and, based on previous work in  $Ca^+$  and  $Sr^+$ , the dynamic correction to the DSSP is negligible compared to the current theoretical uncertainty [17,34].

During clock operation, we average the frequencies of symmetric Zeeman pairs to synthesize a clock frequency that is first-order insensitive to magnetic fields. However, we have observed that magnetic field fluctuations at the location of the ion can be significant during the dead time between probing individual transitions in a Zeeman pair. This effect has been observed in previous single ion clocks based on Ca<sup>+</sup> and can lead to a frequency shift due to a residual magnetic field drift between clock probes [35,36]. The longest dead time between probings of a Zeeman pair is 50 ms, which is largely due to synchronizing the measurement with the 60 Hz ac power line. Given an average magnetic field drift rate of  $(0 \pm 7) \times 10^{-13}$  T/s observed in our system, and the maximum Zeeman shift sensitivity among all transitions used,  $2.8 \times 10^{10}$  Hz/T, the pair averaged frequency shift is estimated to be  $\Delta \nu / \nu = (0 \pm 2) \times 10^{-18}$ .

Collisions between the Ra<sup>+</sup> ion and background gas molecules (i.e., H<sub>2</sub>) can lead to a phase shift during the clock probe pulse. Here, we bound the corresponding clock frequency shift by assuming a worst case estimate of the phase shift of  $\pm \pi/2$ , which occurs in the middle of a Rabi pulse. In this case, a collision with a background gas molecule leads to a frequency shift of  $0.15R_{coll}$ , where  $R_{coll}$ is the background gas collision rate [37]. We measure  $R_{coll}$ in our trap to be  $0.0013(4) \text{ s}^{-1}$  using the technique described in [38], which corresponds to a fractional frequency shift due to background gas collisions of  $\Delta \nu/\nu = (0 \pm 6) \times 10^{-19}$ .

Frequency shifts due to ion motion are characterized as that due to excess micromotion (EMM), due to the rf drive, and secular (thermal) motion. Ion motion leads to frequency shifts due to relativistic time dilation and the ac Stark effect [26]. Here, the time-dilation shift is the dominant source of frequency shift and uncertainty and is expressed as  $\Delta \nu / \nu = -v^2 / (2c^2)$ , where v is the speed of the ion in the laboratory frame and c is the speed of light in vacuum. The EMM-induced frequency shift is evaluated by measuring the amplitude of the ion motion at the trap drive frequency,  $\Omega_{\rm rf}/2\pi$  [25]. The frequency shift due to secular motion is evaluated by characterizing the ion temperature during clock operation [24,25]. The frequency shift due to secular motion is  $\Delta \nu / \nu = (-6.0 \pm 0.6) \times 10^{-19}$ , and EMM-induced frequency shift is  $\Delta \nu / \nu =$ the  $(-3.9 \pm 0.5) \times 10^{-18}$ . The clock frequency shifts and uncertainties due to ion motion can be reduced by using an ion trap design that minimizes residual rf fields and supports higher secular motion frequencies. Trap improvements and operation at the "magic" rf drive frequency (6.2 MHz) are expected to reduce both the magnitude and uncertainty of motional frequency shifts [17].

Additional systematic shifts, including the quadratic Zeeman shift and the electric quadrupole shift and their uncertainties are constrained at the low  $10^{-19}$  level (fractional), see the Supplemental Material [25].

The ratio of Landé *g*-factors,  $g_D/g_S$ , is directly obtained from the clock measurement data [27]. From a single clock measurement, such as shown in Fig. 2, we determine three



FIG. 3. The three *g*-factor ratios calculated from the 3 ms interrogation time clock measurement data presented in Fig. 2. The red triangle in the inset represents the weighted average of these data,  $g_D/g_S = 0.598\ 805\ 25(3)$ . The circle markers are weighted averages of ~2000 s of clock data with a 250  $\mu$ s interrogation time taken at a range of magnetic fields. The shorter interrogation and measurement time results in a larger uncertainty. The gray fill represents the full standard deviation of the five clock measurements, which we assign as the uncertainty for the *q*-factor ratio measurement.

ratios of Landé q-factors from the frequency division of the three Zeeman pairs, see Fig. 3(a). The weighted average of these three ratios gives a value for  $g_D/g_S$ . The reported  $g_D/g_S$  ratio is calculated from a weighted average of five measurements at different magnetic fields. The assigned uncertainty is the standard deviation of the measurements, resulting in  $g_D/g_S = 0.598\,805\,3(11)$ , see Fig. 3. Because of the rf trapping field, an ac magnetic field is present at the trap frequency,  $B_{trap}$ , at the location of the ion, which shifts the measured  $g_D/g_S$  [39]. By performing direct spectroscopy of individual Zeeman transitions with the rf trapping frequency set to the ground state magnetic sublevel splitting, we are able to set an upper bound of  $B_{\rm trap} \leq 7 \times 10^{-8}$  T. The systematic shift due to the maximum  $B_{\text{trap}}$  value is significantly smaller than the statistical uncertainty of  $g_D/g_S$  for all magnetic fields where the Landé g-factor ratio was measured. To improve upon this initial measurement, the  $S_{1/2}$  state Landé g-factor in Ra<sup>+</sup> could be directly measured to high precision in a Penning trap [40] or in a comparison with a co-trapped ion magnetometer [41], which would, in turn, give the  $D_{5/2}$ state Landé q-factor based on the ratio measured here.

In conclusion, we have demonstrated the operation of a  $^{226}$ Ra<sup>+</sup> ion clock with a total systematic uncertainty of  $\Delta \nu / \nu = 9 \times 10^{-16}$  and a frequency instability of  $\sigma(\tau) = 1.1 \times 10^{-13} / \sqrt{\tau}$ . The current clock performance is primarily limited by (1) short-term magnetic field noise at the ion's location, which limits the clock interrogation time, (2) the uncertainty in the DSSP that dominates the uncertainty in the frequency shift due to BBR, and (3) limitations in the trap design that lead to motional

decoherence. The ambient magnetic field noise can be reduced by adding magnetic field shielding, as has been done with  ${}^{40}Ca^+$  [35] and  ${}^{88}Sr^+$  [24] and motional decoherence can be reduced by using an improved trap design [2,42]. Reduced magnetic field sensitivity could be realized with radium-225, which has first-order magnetic field insensitive states due to its I = 1/2 nuclear spin. The 14.9 day half-life of radium-225 can be overcome by using an oven based on the decay of thorium-229  $(\tau_{1/2} \approx 7340 \text{ y})$ , as demonstrated with a 10  $\mu$ Ci oven source [43]. Such a source promises a long-term in vacuo supply of radium-225, as the thorium vapor pressure is more than a trillion times smaller than radium [44], which also makes it robust to inadvertently exhausting the atom supply by running the oven at high temperatures [45]. These features, along with the photonic-technology compatible wavelengths of Ra<sup>+</sup> and the low optical power requirements of an ion clock make it an intriguing candidate for a transportable optical clock.

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