

Measuring the Joint Spectral Mode of Photon Pairs Using Intensity InterferometryG. S. Thekkadath^{1,2,*} B. A. Bell,¹ R. B. Patel,^{1,3} M. S. Kim,¹ and I. A. Walmsley¹¹*Department of Physics, Imperial College London, Prince Consort Road, London SW7 2AZ, United Kingdom*²*National Research Council of Canada, 100 Sussex Drive, Ottawa, K1A 0R6, Canada*³*Clarendon Laboratory, University of Oxford, Parks Road, Oxford, OX1 3PU, United Kingdom* (Received 13 July 2021; revised 12 October 2021; accepted 22 December 2021; published 10 January 2022)

The ability to manipulate and measure the time-frequency structure of quantum light is useful for information processing and metrology. Measuring this structure is also important when developing quantum light sources with high modal purity that can interfere with other independent sources. Here, we present and experimentally demonstrate a scheme based on intensity interferometry to measure the joint spectral mode of photon pairs produced by spontaneous parametric down-conversion. We observe correlations in the spectral phase of the photons due to chirp in the pump. We show that our scheme can be combined with stimulated emission tomography to quickly measure their mode using bright classical light. Our scheme does not require phase stability, nonlinearities, or spectral shaping and thus is an experimentally simple way of measuring the modal structure of quantum light.

DOI: [10.1103/PhysRevLett.128.023601](https://doi.org/10.1103/PhysRevLett.128.023601)

The modal structure of light, such as its spatial and spectral shape, is fundamental to its use in probing and manipulating matter and in extracting information from optical beams. For instance, light's time-frequency structure is particularly well-suited for encoding information because it provides a high-dimensional alphabet that is compatible with optical fiber networks [1]. In quantum optics, nonlinear optical processes are used to generate ultrashort pulsed photon pairs and to prepare quantum states such as single photons [2,3], squeezed vacuum [4], and entangled frequency combs [5]. The fast timescale of these quantum states is attractive for quantum information processing [6–8] and metrology [9–12] but poses additional challenges for their characterization [13–15] and manipulation [16–18]. In particular, characterizing their time-frequency structure requires measuring the spectral amplitude and phase of the generated photon pairs [19]. This poses two main challenges.

First, while a photon's spectral amplitude can be measured using a spectrometer, its spectral phase is more challenging to measure. There are self-referencing solutions to determining the spectral phase of an optical pulse [20], but these are often implemented using self-induced or externally controlled optical nonlinear devices [21]. It is not possible to use the former for single photons because of the very weak electric field strengths, and while the latter approach has been demonstrated [22–25], it comes with significant experimental complexity. Alternatively, a purely linear solution is possible by interfering the unknown signal pulse with a reference pulse and performing spectrally resolved detection [26–29]. This generally requires a reference whose mode is known completely (in both spectral amplitude and phase) and which is phase-stable

with respect to the signal. Similar schemes have also been demonstrated without spectrally resolved detection but required scanning the reference in order to reconstruct the spectral mode of the signal [30–34].

The second challenge is that photon pairs can exhibit time-frequency correlations that must be uncovered using joint measurements [35]. This challenge has been partially overcome in experiments measuring the joint spectral [36–39] or temporal [40–42] intensity of the photon pairs. However, these measurements are insensitive to correlations in the spectral phase of the photons. Phase correlations arise when spectrally structured pump fields are used to generate time-frequency entangled photons [23], which have applications in quantum communication [43,44] and sensing [9–12]. They also arise when the pump is chirped and in such cases can degrade the purity of heralded single photons as well as the interference quality between independent sources [45,46]. Such phase correlations must be minimized when preparing the high-purity photons needed for photonic networks [47] and information processors [48,49]. Finally, the joint spectral phase's structure can reveal interesting physics in the photon pair creation process in both atomic systems [50] and nonlinear crystals [51]. All these applications benefit from a full characterization of the time-frequency structure of photon pairs. Recent experiments have demonstrated this either by employing nonlinearities [52,53] or linear techniques that are only applicable to highly correlated pair sources [54–57].

In this Letter, we propose a general scheme to determine the spectral mode of light and demonstrate it experimentally using photon pairs. We interfere the photons with a weak reference pulse and measure spectral

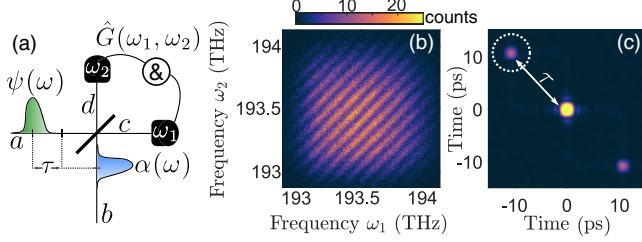


FIG. 1. (a) We combine the unknown signal $\psi(\omega)$ with a reference $\alpha(\omega)$ on a BS and measure spectral intensity correlations $\hat{G}(\omega_1, \omega_2)$ [Eq. (2)]. (b) Example of an experimentally measured $\langle \hat{G}(\omega_1, \omega_2) \rangle$. (c) Fourier transform of $\langle \hat{G}(\omega_1, \omega_2) \rangle$. The interferometric term $\Gamma(\omega_1, \omega_2)$ [Eq. (5)] is isolated using a window function. White dotted line shows 50% contour of a Gaussian window function.

intensity correlations. Our scheme does not require nonlinearities, phase stability, spectral shaping, or complex computational algorithms. It does, however, require *a priori* knowledge of the spectral mode of the reference pulse. Because the reference is simply an attenuated laser, its mode can be measured using conventional self-referencing techniques for classical pulses [58,59].

We begin by describing the single photon case, which is extended later to the biphoton case. We consider for now a signal in a pure single photon pulse $\int d\omega \psi(\omega) \hat{a}_\omega^\dagger |0\rangle$ where \hat{a}_ω^\dagger is a creation operator at frequency ω in input mode a . The goal is to determine its spectral mode $\psi(\omega)$. As shown in Fig. 1(a), the photon is combined with a reference pulse on a beam splitter (BS). The input state of the BS is

$$|\Psi\rangle = \int d\omega \psi(\omega) \hat{a}_\omega^\dagger |0\rangle \otimes \int d\omega' |\alpha(\omega')\rangle, \quad (1)$$

where we assumed the reference is a coherent state with amplitude $\alpha(\omega)$, i.e., $\hat{b}_{\omega_0} \int d\omega' |\alpha(\omega')\rangle = \alpha(\omega_0) \int d\omega' |\alpha(\omega')\rangle$. At the output of the BS, one measures spectral intensity correlations that are described by the observable

$$\hat{G}(\omega_1, \omega_2) \equiv \hat{d}_{\omega_2}^\dagger \hat{c}_{\omega_1}^\dagger \hat{c}_{\omega_1} \hat{d}_{\omega_2}. \quad (2)$$

By repeating measurements of Eq. (2), one determines the expectation value $\langle \hat{G}(\omega_1, \omega_2) \rangle$, which is the second-order cross-correlation function of the two output fields evaluated at ω_1 and ω_2 . We can compute this expectation value with respect to the input state in Eq. (1) by using the BS input-output transformations $\hat{c}_\omega = (\hat{a}_\omega + \hat{b}_\omega)/\sqrt{2}$ and $\hat{d}_\omega = (\hat{a}_\omega - \hat{b}_\omega)/\sqrt{2}$:

$$\begin{aligned} \langle \hat{G}(\omega_1, \omega_2) \rangle &= \langle \Psi | \hat{G}(\omega_1, \omega_2) | \Psi \rangle \\ &= \frac{1}{4} |\alpha(\omega_1)\psi(\omega_2) - \psi(\omega_1)\alpha(\omega_2)|^2 \\ &\quad + \frac{1}{4} |\alpha(\omega_1)\alpha(\omega_2)|^2. \end{aligned} \quad (3)$$

When the reference intensity is at the single photon level, a measurement of Eq. (3) reveals an interference pattern that depends on both the amplitude and phase of the spectral mode of the input fields [Fig. 1(b)]. Similar interference patterns have been measured in experiments performing spectrally resolved Hong-Ou-Mandel interferometry, where both inputs are single photons [29,60–62].

In order to isolate the mode function of the signal from Eq. (3), we use a Fourier filtering technique [26–29]. That is, we delay the reference by τ , i.e., $\alpha(\omega) \rightarrow \alpha(\omega)e^{i\omega\tau}$. Expanding Eq. (3), we obtain

$$\langle \hat{G}(\omega_1, \omega_2) \rangle = \frac{1}{4} [\zeta(\omega_1, \omega_2) - \Gamma(\omega_1, \omega_2) - \Gamma^*(\omega_1, \omega_2)]. \quad (4)$$

The first term, $\zeta(\omega_1, \omega_2) = |\alpha(\omega_1)\psi(\omega_2)|^2 + |\psi(\omega_1)\alpha(\omega_2)|^2 + |\alpha(\omega_1)\alpha(\omega_2)|^2$, depends on the spectral amplitudes of the fields but not their spectral phases. The second term,

$$\Gamma(\omega_1, \omega_2) = \psi(\omega_1)\psi^*(\omega_2)\alpha^*(\omega_1)\alpha(\omega_2)e^{i(\omega_2-\omega_1)\tau}, \quad (5)$$

depends on both quantities. This interference term can be isolated in the Fourier domain. Namely, by performing a two-dimensional Fourier transform \mathcal{F} of Eq. (4), one finds that $\mathcal{F}\{\Gamma(\omega_1, \omega_2)\}$ and $\mathcal{F}\{\Gamma^*(\omega_1, \omega_2)\}$ are symmetrically separated from $\mathcal{F}\{\zeta(\omega_1, \omega_2)\}$ by the temporal delay τ [Fig. 1(c)]. If τ is made larger than the temporal duration of the signal and reference pulses, one can isolate $\Gamma(\omega_1, \omega_2)$ by multiplying $\mathcal{F}\{\langle \hat{G}(\omega_1, \omega_2) \rangle\}$ by a window function (e.g., Gaussian) centered on $\mathcal{F}\{\Gamma(\omega_1, \omega_2)\}$ and taking the inverse Fourier transform [63]. One can then divide the filtered interferogram by the reference spectral mode and a phase term depending on the delay τ , which are both *a priori* known quantities, i.e., $\psi(\omega_1)\psi^*(\omega_2) = \Gamma(\omega_1, \omega_2)/\alpha^*(\omega_1)\alpha(\omega_2)e^{i(\omega_2-\omega_1)\tau}$. This division step imposes that the reference pulse should be at least as spectrally broad as the signal, and thus a characterization of the signal and reference spectra prior to the measurement is required to verify that this condition is met. There are otherwise no special requirements for the reference. The pure signal spectral mode can then be obtained by diagonalizing the matrix $\Phi(\omega_1, \omega_2) = \psi(\omega_1)\psi^*(\omega_2)$, where ω_1 and ω_2 are discrete measurement bins. Suppose instead the signal is in a mixed state of modes $\Phi(\omega_1, \omega_2) = \sum_i p_i \Phi_i(\omega_1, \omega_2)$. Then, one can show that the Fourier filtered $\langle \hat{G}(\omega_1, \omega_2) \rangle$ is determined by $\sum_i p_i \Gamma_i(\omega_1, \omega_2)$ where $\Gamma_i(\omega_1, \omega_2)$ is given by Eq. (5) with $\psi(\omega_1)\psi^*(\omega_2) \rightarrow \Phi_i(\omega_1, \omega_2)$. Then, $\Phi(\omega_1, \omega_2) = \sum_i p_i \Gamma_i(\omega_1, \omega_2)/[\alpha^*(\omega_1)\alpha(\omega_2)e^{i(\omega_2-\omega_1)\tau}]$ and thus modal mixtures can also be obtained without further measurements.

The method outlined above is not restricted to single photons and can be used to determine the spectral mode of any quantum or classical state of light. Moreover, since it

measures spectral intensity correlations rather than the spectral intensity alone, there does not need to be any phase coherence between the reference and signal [65], e.g., these can be phase-randomized coherent states or independent thermal states as in Hanbury Brown and Twiss interferometry. Let us consider the former case as an example. One can replace the creation and annihilation operators in Eq. (2) with the corresponding spectral amplitudes, i.e., $\hat{c}_\omega \rightarrow (\psi(\omega) + \alpha(\omega)e^{i\omega\tau})/\sqrt{2}$ and $\hat{d}_\omega \rightarrow (\psi(\omega) - \alpha(\omega)e^{i\omega\tau})/\sqrt{2}$. Inserting these transformations into Eq. (2) and taking the classical ensemble average, denoted by $\langle \rangle_C$, one finds

$$\langle \hat{G}(\omega_1, \omega_2) \rangle_C = \frac{1}{4} [\zeta(\omega_1, \omega_2) + |\psi(\omega_1)\psi(\omega_2)|^2 - \Gamma(\omega_1, \omega_2) - \Gamma^*(\omega_1, \omega_2)]. \quad (6)$$

Comparing with Eq. (4) where we assumed the signal to be a single photon, an additional spectral phase-insensitive term $|\psi(\omega_1)\psi(\omega_2)|^2$ appears in Eq. (6) due to the intensity fluctuations of the signal, now assumed to be a coherent state. This additional term further limits the visibility of the interference fringes in $\langle \hat{G}(\omega_1, \omega_2) \rangle_C$. In principle, the visibility is limited to 50% for phase-randomized coherent states [66]. A reduced visibility is not an issue so long as $\Gamma(\omega_1, \omega_2)$ is distinguishable from the spectral phase-insensitive terms and any other noise in the Fourier domain, which might require averaging $\langle \hat{G}(\omega_1, \omega_2) \rangle$ over a longer period of time.

We now extend the scheme to measure the biphotons produced by processes like spontaneous parametric down-conversion (SPDC) or four-wave mixing:

$$|\text{SPDC}\rangle = \iint d\omega_1 d\omega_2 f(\omega_1, \omega_2) \hat{a}_{\omega_1}^\dagger \hat{h}_{\omega_2}^\dagger |0\rangle. \quad (7)$$

Here, $f(\omega_1, \omega_2)$ is termed the joint spectral amplitude (JSA) and characterizes the joint spectral mode of the photon pair. Suppose one performs spectrally resolved detection in the herald mode h . By detecting a photon of frequency ω_h , one heralds a signal photon in mode a whose spectral mode is given by $\psi(\omega_1) = f(\omega_1, \omega_h)$. The heralded photon can then be combined with a reference in order to measure $f(\omega_1, \omega_h)$ using the aforementioned procedure. The quantity $f(\omega_1, \omega_h)$ is a cross section of the JSA along $\omega_2 = \omega_h$ and hence this measurement should be repeated for all herald frequencies in order to determine $f(\omega_1, \omega_2)$. One caveat is that there is a phase between each cross section that remains undetermined because of the spectral phase-insensitive detection in mode h . However, one can repeat the measurement using mode a as the herald and mode h as the signal to be combined with the reference. These two measurements unambiguously determine the full JSA [53].

We now turn to our experiment. The experimental setup is shown in Fig. 2. An optical parametric oscillator

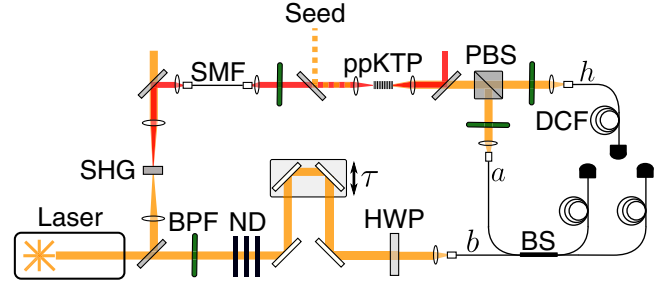


FIG. 2. Experimental setup. The SMF and seed are included only in certain measurements, which are described in the main text. SHG: second-harmonic generation, SMF: single-mode fiber, BPF: bandpass filter ND: neutral-density filter, ppKTP: periodically poled potassium titanyl phosphate, (PBS): (polarizing) beam splitter, HWP: half-wave plate, DCF: dispersion-compensating fiber.

produces pulses (150 fs duration, 1550 nm center wavelength) at a repetition rate of 80 MHz. A small fraction of the power is used as the reference, while the remaining power is used to prepare the pump light for the SPDC source. The pump pulses are frequency-doubled in a lithium niobate crystal and subsequently coupled into a 8-mm-long periodically poled potassium titanyl phosphate (ppKTP) waveguide. A type-II SPDC interaction inside the waveguide produces pairs of photons described by Eq. (7). Our goal is to measure both the amplitude and phase of the JSA $f(\omega_1, \omega_2)$.

We send the down-converted photon in mode h directly into a spectrally resolving single photon detector. The heralded photon in mode a is combined with the reference pulse in a single-mode fiber BS. We use a motorized stage to set a delay of $\tau = 10.00(7)$ ps between the two pulses. We then perform spectrally resolved detection at the output of the BS. Each spectrally resolving single photon detector consists of a dispersion-compensating fiber (DCF) having a dispersion of -997 ps/nm followed by a superconducting nanowire detector. The DCF maps the photon's frequency to its arrival time at the detector, which is recorded using a time-tagging device. The combined detector and time-tagging temporal jitter is roughly 40 ps, resulting in a spectral uncertainty of 40 pm (5 GHz). The combined transmission and detection efficiency of each path is approximately 3% and is mainly limited by the transmission of the DCFs (15%).

We measure roughly 10^5 single photons per second from the SPDC source using 3 mW of pump power. With the reference having approximately 10^6 photons per second, we measure threefold coincidence events at a rate of about 100 per second. We acquire data for a few hours and obtain a three-dimensional histogram $N(\omega_1, \omega_2, \omega_h)$, which is determined by the joint probability to measure frequencies (ω_1, ω_2) at the output of the BS and ω_h in the herald mode. In order to determine $f(\omega_1, \omega_2)$, we process $N(\omega_1, \omega_2, \omega_h)$ in the following manner. First, the measured

frequencies are placed into discrete bins, each having a width of approximately 10 GHz. For the j th herald bin, $N(\omega_1, \omega_2, \omega_{h_j}) = \langle \hat{G}_j(\omega_1, \omega_2) \rangle$ is the cross-correlation function conditioned on having detected the herald photon in the frequency bin ω_{h_j} . An example of this quantity is shown in Fig. 1(b). Second, we use $\langle \hat{G}_j(\omega_1, \omega_2) \rangle$ to determine $f(\omega_1, \omega_{h_j})$ using the Fourier filtering procedure. This process is repeated for all the herald bins, and we obtain the full $f(\omega_1, \omega_2)$. The reference pulse spectrum $|\alpha(\omega)|^2$ is measured by blocking the down-converted photons. We assume that the reference photons are approximately chirpless and so take $\alpha(\omega)$ to be real-valued.

As a first test, we adjust the pump bandwidth using a bandpass filter so that the down-converted photons have an uncorrelated JSA, i.e., $f(\omega_1, \omega_2) = f_1(\omega_1)f_2(\omega_2)$. Bandpass filters are also used after the waveguide to eliminate the sinc sidelobes from the down-converted spectra. We plot the measured $\arg\{f(\omega_1, \omega_2)\}$ and $|f(\omega_1, \omega_2)|$ in Figs. 3(a) and 3(b), respectively. The latter can be compared with a conventional measurement of $|f(\omega_1, \omega_2)|$ where we block the reference and record twofold coincidences [Fig. 3(c)]. To quantify the degree of correlation between the down-converted photons, we perform a Schmidt decomposition of the complex JSA and obtain a Schmidt number of $K = 1.02$. This number is close to unity, which indicates that the down-converted photons are indeed uncorrelated in time and frequency. We also measure the second-order autocorrelation function $g^{(2)}$ of the signal and herald modes with the reference blocked. We find 1.84(2) and 1.85(2), respectively. For an idealized photon pair source, $g_{\text{ideal}}^{(2)} = 1 + 1/K$ [67]. However, in addition to photon pairs, our source also generates uncorrelated single photons (4(2)% of the total counts) due to unguided down-conversion processes in the waveguide.

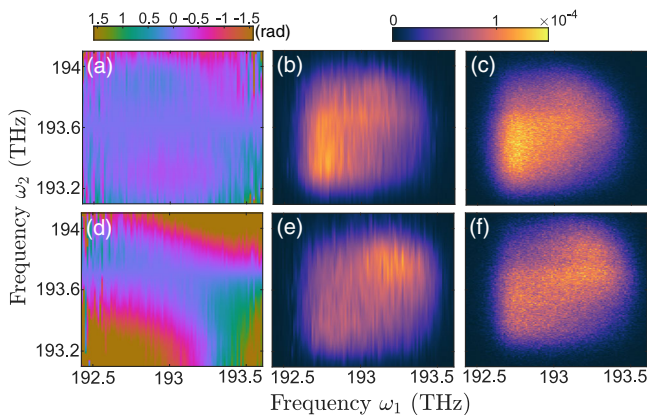


FIG. 3. Measured joint spectral amplitude. Top (bottom) row shows results with a chirpless (chirped) pump. (a) and (d) are the joint spectral phases $\arg\{f(\omega_1, \omega_2)\}$, while (b) and (e) are the amplitudes $|f(\omega_1, \omega_2)|$. (c) and (f) are the amplitudes measured using a conventional phase-insensitive method.

Subtracting the noise photons from the $g^{(2)}$ calculation [63,64], we find 1.98(7) and 1.99(7) in the signal and herald modes, respectively, which agree with the value expected from the Schmidt number, $g_{\text{ideal}}^{(2)} \approx 1.98$.

For a second test, we chirp the pump pulse by coupling it into 5-m-long single-mode fiber. We characterize the chirp using spectral phase interferometry for direct electric-field reconstruction [59]. The chirped pulse is well-described by a quadratic spectral phase, i.e., $|A(\omega_p)|e^{-i(\beta/2)\omega_p^2}$, where $|A(\omega_p)|$ is the spectral amplitude and $\beta = 2.0(4) \times 10^5 \text{ fs}^2$ is the measured group delay dispersion parameter. The pump chirp introduces a correlated phase in the down-converted photons, $f(\omega_1, \omega_2) = f_1(\omega_1)f_2(\omega_2)e^{-i\beta\omega_1\omega_2}$. This correlated phase is visible in the measured $\arg\{f(\omega_1, \omega_2)\}$ [Fig. 3(d)]. Fitting a quadratic function, we find $\beta = 1.69(2) \times 10^5 \text{ fs}^2$, which agrees with the aforementioned value. The slight difference in $|f(\omega_1, \omega_2)|$ [Fig. 3(e)] compared to the chirpless pump case [Fig. 3(b)] is due to self-phase modulation that modifies the pump's spectral amplitude as it propagates inside the fiber. This difference is also apparent in the conventional phase-insensitive measurements [Figs. 3(c) and 3(f)]. The Schmidt number of the measured complex JSA is $K = 1.48$, while it is $K = 1.04$ if one ignores the phase. Thus, the time-frequency correlations of the down-converted photons are mainly caused by the nonuniform spectral phase of the pump. Because of these correlations, the noise-subtracted $g^{(2)}$ of the signal and herald modes decreases to 1.62(6) and 1.68(6), respectively, which agree with the expected $g_{\text{ideal}}^{(2)} \approx 1.67$.

So far, we demonstrated that our scheme can be used to measure both amplitude and phase of the JSA of photon pairs produced by SPDC. One potential drawback of our measurement is that it relies on measuring threefold coincidences, which can lead to slow data acquisition with pair sources that are faint or have low heralding efficiencies. To resolve this issue, we propose a technique to measure the JSA that uses bright classical fields and hence can be much quicker. The technique draws inspiration from stimulated emission tomography [68]. One couples a continuous-wave seed laser with tunable frequency ω_s into the pair source. Through difference frequency generation with the pump, the signal is prepared in a bright coherent state. The spectral mode of this stimulated signal is given by the cross section of the JSA at the seed frequency ω_s , i.e., $f(\omega, \omega_s)$. One can then combine the stimulated signal with the reference and measure $\langle \hat{G}(\omega_1, \omega_2) \rangle$ to determine $f(\omega, \omega_s)$ and repeat this process for different seed frequencies ω_s . Since the signal and reference do not need to be phase-stable, it is not necessary to lock the seed and pump lasers.

We perform a proof-of-principle demonstration of this technique. In addition to the unchirped pump, we couple a seed beam into the SPDC source whose polarization is

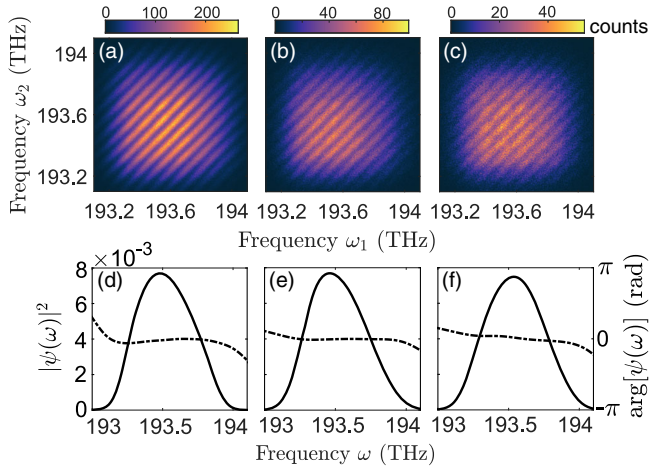


FIG. 4. $\langle \hat{G}(\omega_1, \omega_2) \rangle$ measured using a signal with (a) sub-Poissonian, $g^{(2)} = 0.57(4)$; (b) Poissonian, $g^{(2)} = 1.048(3)$; (c) super-Poissonian, $g^{(2)} = 1.84(2)$ photon statistics. In all three cases, the reference is a coherent state with Poissonian statistics. The fringe visibilities are 0.27(2), 0.17(1), 0.14(1), respectively. Bottom row of plots shows the corresponding $|\psi(\omega)|^2$ (left y-axis scale, solid line) and $\arg[\psi(\omega)]$ (right y-axis scale, dashed line).

aligned with the herald mode. The seed beam is produced by an attenuated continuous-wave laser (1560 nm, 192 THz). We combine the stimulated signal with the reference pulse on a BS and measure $\langle \hat{G}(\omega_1, \omega_2) \rangle$ by recording twofold coincidences. The result is shown in Fig. 4(b). The fringe visibility is reduced compared to the heralded measurement [Fig. 4(a)] due to increased intensity fluctuations of the signal. The benefit is that $\langle \hat{G}(\omega_1, \omega_2) \rangle$ can be measured much more quickly. Using approximately 10^6 photons per second in both the reference and signal (i.e., 0.01 photons per pulse), we obtain 10^4 twofold coincidences per second. This rate was limited by the dead time and dynamic range of the single photon detectors. One could in principle measure $\langle \hat{G}(\omega_1, \omega_2) \rangle$ even more quickly by measuring shot-by-shot correlations between two spectrometers employing regular photodetectors.

For the sake of demonstration, we also measure $\langle \hat{G}(\omega_1, \omega_2) \rangle$ when there is thermal noise in the signal by turning off the seed beam and recording twofold coincidences. This last measurement ignores the herald photon and hence the signal has super-Poissonian photon statistics that further reduce the fringe visibility [Fig. 4(c)]. We determine the spectral modes in the heralded, seeded, and unseeded cases using the Fourier filtering procedure [Figs. 4(d)–4(f)]. The three spectral modes have an average pairwise fidelity $|\int d\omega \psi_1(\omega) \psi_2^*(\omega)|$ of 0.991(4), which demonstrates that our measurement is insensitive to the fringe visibility due to the Fourier filtering.

In summary, we demonstrated a scheme that can determine the joint spectral mode of the photon pairs produced by SPDC or four-wave mixing. By using a combination of intensity interferometry and Fourier filtering, our scheme is

resilient to phase instabilities and intensity fluctuations. An analogous scheme measuring spatial intensity correlations can be used to characterize light’s spatial mode [69,70]. Finally, extending the scheme beyond two photons should be possible by combining each photon with a reference and measuring spectral intensity correlations across all modes.

We thank Single Quantum for loaning us superconducting nanowire detectors. This work was supported by Engineering and Physical Sciences Research Council (P510257); H2020 Marie Skłodowska-Curie Actions (846073); Korea Institute of Science and Technology open research program; National Research Council of Canada.

*Corresponding author.

g.thekkadath@imperial.ac.uk

- [1] G. P. Agrawal, *Fiber-Optic Communication Systems* (John Wiley & Sons, New York, 2012).
- [2] A. I. Lvovsky, H. Hansen, T. Aichele, O. Benson, J. Mlynek, and S. Schiller, *Phys. Rev. Lett.* **87**, 050402 (2001).
- [3] P. J. Mosley, J. S. Lundeen, B. J. Smith, P. Wasylczyk, A. B. U’Ren, C. Silberhorn, and I. A. Walmsley, *Phys. Rev. Lett.* **100**, 133601 (2008).
- [4] R. E. Slusher, P. Grangier, A. LaPorta, B. Yurke, and M. J. Potasek, *Phys. Rev. Lett.* **59**, 2566 (1987).
- [5] J. Roslund, R. M. De Araujo, S. Jiang, C. Fabre, and N. Treps, *Nat. Photonics* **8**, 109 (2014).
- [6] B. Brecht, D. V. Reddy, C. Silberhorn, and M. G. Raymer, *Phys. Rev. X* **5**, 041017 (2015).
- [7] S. Slussarenko and G. J. Pryde, *Appl. Phys. Rev.* **6**, 041303 (2019).
- [8] C. Fabre and N. Treps, *Rev. Mod. Phys.* **92**, 035005 (2020).
- [9] B. Lamine, C. Fabre, and N. Treps, *Phys. Rev. Lett.* **101**, 123601 (2008).
- [10] K. E. Dorfman, F. Schlawin, and S. Mukamel, *Rev. Mod. Phys.* **88**, 045008 (2016).
- [11] A. Lyons, G. C. Knee, E. Bolduc, T. Roger, J. Leach, E. M. Gauger, and D. Faccio, *Sci. Adv.* **4**, eaap9416 (2018).
- [12] V. Ansari, B. Brecht, J. Gil-Lopez, J. M. Donohue, J. Řeháček, Z. c. v. Hradil, L. L. Sánchez-Soto, and C. Silberhorn, *PRX Quantum* **2**, 010301 (2021).
- [13] C. Ren and H. F. Hofmann, *Phys. Rev. A* **84**, 032108 (2011).
- [14] C. Ren and H. F. Hofmann, *Phys. Rev. A* **86**, 043823 (2012).
- [15] I. Gianani, M. Sbroscia, and M. Barbieri, *AVS Quantum Sci.* **2**, 011701 (2020).
- [16] A. Pe’er, B. Dayan, A. A. Friesem, and Y. Silberberg, *Phys. Rev. Lett.* **94**, 073601 (2005).
- [17] A. Eckstein, B. Brecht, and C. Silberhorn, *Opt. Express* **19**, 13770 (2011).
- [18] B. Brecht, A. Eckstein, R. Ricken, V. Quiring, H. Suche, L. Sansoni, and C. Silberhorn, *Phys. Rev. A* **90**, 030302(R) (2014).
- [19] W. Wasilewski, A. I. Lvovsky, K. Banaszek, and C. Radzewicz, *Phys. Rev. A* **73**, 063819 (2006).
- [20] I. A. Walmsley and C. Dorrer, *Adv. Opt. Photonics* **1**, 308 (2009).
- [21] V. Wong and I. A. Walmsley, *Opt. Lett.* **19**, 287 (1994).

- [22] A. O. C. Davis, V. Thiel, M. Karpiński, and B. J. Smith, *Phys. Rev. Lett.* **121**, 083602 (2018).
- [23] V. Ansari, J. M. Donohue, M. Allgaier, L. Sansoni, B. Brecht, J. Roslund, N. Treps, G. Harder, and C. Silberhorn, *Phys. Rev. Lett.* **120**, 213601 (2018).
- [24] S. Zhang, Y. Zhou, Y. Mei, K. Liao, Y.-L. Wen, J. Li, X.-D. Zhang, S. Du, H. Yan, and S.-L. Zhu, *Phys. Rev. Lett.* **123**, 190402 (2019).
- [25] K. Ogawa, T. Okazaki, H. Kobayashi, T. Nakanishi, and A. Tomita, *Opt. Express* **29**, 19403 (2021).
- [26] C. Froehly, A. Lacourt, and J. C. Viénot, *Nouv. Rev. Opt.* **4**, 183 (1973).
- [27] D. N. Fittinghoff, J. L. Bowie, J. N. Sweetser, R. T. Jennings, M. A. Krumbügel, K. W. DeLong, R. Trebino, and I. A. Walmsley, *Opt. Lett.* **21**, 884 (1996).
- [28] M. Beck, C. Dorner, and I. A. Walmsley, *Phys. Rev. Lett.* **87**, 253601 (2001).
- [29] V. Thiel, A. O. Davis, K. Sun, P. D'Ornellas, X.-M. Jin, and B. J. Smith, *Opt. Express* **28**, 19315 (2020).
- [30] W. Wasilewski, P. Kolenderski, and R. Frankowski, *Phys. Rev. Lett.* **99**, 123601 (2007).
- [31] C. Polycarpou, K. N. Casemiro, G. Venturi, A. Zavatta, and M. Bellini, *Phys. Rev. Lett.* **109**, 053602 (2012).
- [32] R. Medeiros de Araújo, J. Roslund, Y. Cai, G. Ferrini, C. Fabre, and N. Treps, *Phys. Rev. A* **89**, 053828 (2014).
- [33] Z. Qin, A. S. Prasad, T. Brannan, A. MacRae, A. Lezama, and A. Lvovsky, *Light Sci. Appl.* **4**, e298 (2015).
- [34] J. Tiedau, V. Shchesnovich, D. Mogilevtsev, V. Ansari, G. Harder, T. Bartley, N. Korolkova, and C. Silberhorn, *New J. Phys.* **20**, 033003 (2018).
- [35] J. D. Franson, *Phys. Rev. Lett.* **62**, 2205 (1989).
- [36] Y.-H. Kim and W. P. Grice, *Opt. Lett.* **30**, 908 (2005).
- [37] W. Wasilewski, P. Wasylczyk, P. Kolenderski, K. Banaszek, and C. Radzewicz, *Opt. Lett.* **31**, 1130 (2006).
- [38] M. Avenhaus, A. Eckstein, P. J. Mosley, and C. Silberhorn, *Opt. Lett.* **34**, 2873 (2009).
- [39] K. Zielnicki, K. Garay-Palmett, D. Cruz-Delgado, H. Cruz-Ramirez, M. F. O'Boyle, B. Fang, V. O. Lorenz, A. B. U'Ren, and P. G. Kwiat, *J. Mod. Opt.* **65**, 1141 (2018).
- [40] O. Kuzucu, F. N. C. Wong, S. Kurimura, and S. Tovstonog, *Phys. Rev. Lett.* **101**, 153602 (2008).
- [41] K. A. O'Donnell and A. B. U'Ren, *Phys. Rev. Lett.* **103**, 123602 (2009).
- [42] J.-P. W. MacLean, J. M. Donohue, and K. J. Resch, *Phys. Rev. Lett.* **120**, 053601 (2018).
- [43] W. Tittel, J. Brendel, H. Zbinden, and N. Gisin, *Phys. Rev. Lett.* **84**, 4737 (2000).
- [44] J. Nunn, L. Wright, C. Söller, L. Zhang, I. Walmsley, and B. Smith, *Opt. Express* **21**, 15959 (2013).
- [45] A. B. U'Ren, C. Silberhorn, R. Erdmann, K. Banaszek, W. P. Grice, I. A. Walmsley, and M. G. Raymer, *Las. Phys.* **15**, 146 (2005).
- [46] B. A. Bell, G. T. Garces, and I. A. Walmsley, *Opt. Express* **28**, 34246 (2020).
- [47] E. Meyer-Scott, N. Montaut, J. Tiedau, L. Sansoni, H. Herrmann, T. J. Bartley, and C. Silberhorn, *Phys. Rev. A* **95**, 061803(R) (2017).
- [48] H.-S. Zhong, H. Wang, Y.-H. Deng, M.-C. Chen, L.-C. Peng, Y.-H. Luo, J. Qin, D. Wu, X. Ding, Y. Hu *et al.*, *Science* **370**, 1460 (2020).
- [49] J. Arrazola, V. Bergholm, K. Brádler, T. Bromley, M. Collins, I. Dhand, A. Fumagalli, T. Gerrits, A. Goussev, L. Helt *et al.*, *Nature (London)* **591**, 54 (2021).
- [50] S. Du, J. Wen, and M. H. Rubin, *JOSA B* **25**, C98 (2008).
- [51] G. Triginer, M. D. Vidrighin, N. Quesada, A. Eckstein, M. Moore, W. S. Kolthammer, J. E. Sipe, and I. A. Walmsley, *Phys. Rev. X* **10**, 031063 (2020).
- [52] J.-P. W. MacLean, S. Schwarz, and K. J. Resch, *Phys. Rev. A* **100**, 033834 (2019).
- [53] A. O. Davis, V. Thiel, and B. J. Smith, *Optica* **7**, 1317 (2020).
- [54] F. A. Beduini, J. A. Zielińska, V. G. Lucivero, Y. A. de Icaza Astiz, and M. W. Mitchell, *Phys. Rev. Lett.* **113**, 183602 (2014).
- [55] P. Chen, C. Shu, X. Guo, M. M. T. Loy, and S. Du, *Phys. Rev. Lett.* **114**, 010401 (2015).
- [56] N. Tischler, A. Büse, L. G. Helt, M. L. Juan, N. Piro, J. Ghosh, M. J. Steel, and G. Molina-Terriza, *Phys. Rev. Lett.* **115**, 193602 (2015).
- [57] I. Jizan, B. Bell, L. G. Helt, A. C. Bedoya, C. Xiong, and B. J. Eggleton, *Opt. Lett.* **41**, 4803 (2016).
- [58] D. J. Kane and R. Trebino, *IEEE J. Quantum Electron.* **29**, 571 (1993).
- [59] C. Iaconis and I. A. Walmsley, *Opt. Lett.* **23**, 792 (1998).
- [60] R.-B. Jin, T. Gerrits, M. Fujiwara, R. Wakabayashi, T. Yamashita, S. Miki, H. Terai, R. Shimizu, M. Takeoka, and M. Sasaki, *Opt. Express* **23**, 28836 (2015).
- [61] T. Gerrits, F. Marsili, V. B. Verma, L. K. Shalm, M. Shaw, R. P. Mirin, and S. W. Nam, *Phys. Rev. A* **91**, 013830 (2015).
- [62] Y. Zhang, D. England, A. Nomerotski, and B. Sussman, *Opt. Express* **29**, 28217 (2021).
- [63] See Supplemental Material, which includes Ref. [64], at <http://link.aps.org/supplemental/10.1103/PhysRevLett.128.023601> for additional details on the window function and the noise photons.
- [64] A. Eckstein, A. Christ, P. J. Mosley, and C. Silberhorn, *Phys. Status Solidi C* **8**, 1216 (2011).
- [65] C. Dorner, D. Kilper, H. Stuart, G. Raybon, and M. Raymer, *IEEE Photonics Technol. Lett.* **15**, 1746 (2003).
- [66] M. O. Scully and M. S. Zubairy, *Quantum Optics* (Cambridge University Press, Cambridge, England, 1999).
- [67] A. Christ, K. Laiho, A. Eckstein, K. N. Casemiro, and C. Silberhorn, *New J. Phys.* **13**, 033027 (2011).
- [68] M. Liscidini and J. E. Sipe, *Phys. Rev. Lett.* **111**, 193602 (2013).
- [69] R. Chrapkiewicz, M. Jachura, K. Banaszek, and W. Wasilewski, *Nat. Photonics* **10**, 576 (2016).
- [70] H. Defienne, B. Ndagano, A. Lyons, and D. Faccio, *Nat. Phys.* **17**, 591 (2021).