

Onset of Glacier Tables

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A glacier table consists of a rock supported by a slender column of ice and form naturally on glaciers. We investigate the onset of their formation at a smaller scale in a controlled environment. Depending on the size and thermal conductivity of a cap, it can either form of a table standing on an ice foot, or sink into the ice block. A one-dimension conduction model shows that the differential ice melting is controlled by a competition between two effects: a geometrical amplification, and a heat flux reduction due to the higher temperature of the cap as compared to the ice. Our model captures the transition between the two regimes and identifies a dimensionless number which controls the onset of glacier tables formation.

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Introduction.—Differential ablation in nature is an efficient drive for the formation of spectacular structures or patterns. For instance, the formation of meandering rivers or surface patterns known as rillenkarren can result from dissolution of soluble rocks [1–3]. Furthermore, fairy chimneys appear when a stone protects a narrow column of sedimentary rock from erosion [4,5]. While mechanical ablation is indeed a widely spread mechanism, differential physical phase change may also be an efficient differential ablation process. This is for instance the case in sublimation-driven pattern formation, ranging from penitentes on Earth due to ice sublimation [6–8] to landscape formation on Mars due to carbon dioxide sublimation [9–11] or on Pluto [12]. Differential melting of ice leads to the formation of glacier tables [see Fig. 1(a)], which are structures frequently encountered on Alpine glaciers. They typically consist of a meter-size rock supported by a column of ice [13] and can last several years [14]. Glacier tables form because the ablation rate of the ice is lower under the rock than at the air-ice interface. However, under other circumstances, a stone placed on the ice surface may instead sink in [15]. Dirt layers on a glacier and differential melting can also lead to the formation of dirt cones [16,17] for which shortwave reflection is important [18], as it is for suncups [19,20]. Understanding the dynamics of differential melting on glacier require the modeling of ice melting under various conditions (including under a debris layer) and of the energy balance on a glacier. While the melting of ice submerged in water [21–23] showed the importance of convection and instabilities arising from the density inversion of water, ice melting in air has drawn far less attention. A shielding effect from the water film covering an ice block was ruled out theoretically [24] and the effect of the heat flux from condensation of humid air was recently investigated [25].

The purpose of this Letter is to determine, from a physical point of view, the onset of formation of glacier

tables under a controlled environment. More specifically, we address under which conditions (thermal properties of the material, dimensions and aspect ratio) a cylindrical object placed on an ice surface will initially either sink in or seemingly rise. In order to identify the parameters controlling the ice melting process in air, we first studied the melting of inclined ice plates in a controlled environment (constant temperature, humidity, absence of wind), and we show that ice melting due to convection is the leading factor. We then investigated the behavior of cylindrical caps on a flat ice surface. These experimental results are well fitted using an analytical thermal conduction model, from which a single dimensionless number is shown to control the onset of glacier table formation. Conditions for the formation of natural glacier tables are finally extrapolated from laboratory-scale experiments.

Ice melting in air.—The melting of inclined ice plates in air was studied experimentally under controlled conditions. A slab of clear ice (see Supplemental Material [26]) is laid onto an inclined sheet of Styrofoam, which entirely prevents the ice from melting from underneath. The height of the ice slab $e(x)$ was monitored from series of photographs, taken every 8 min and was extracted using an image-processing PYTHON package (see details in [26]). The local heat flux $q_{\text{total}}(x)$ as a function of the distance x

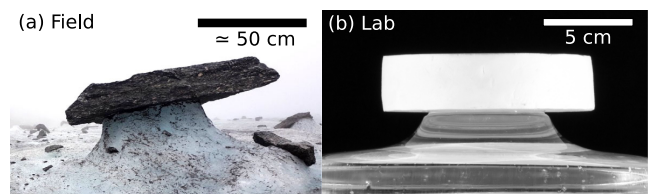


FIG. 1. (a) Picture of a glacier table taken in June 2019 on the Mer de Glace in the French Alps. The table diameter is about 1 m. (b) Artificial glacier table made of extruded polystyrene (XPS), 10 h after being put on a flat ice surface.

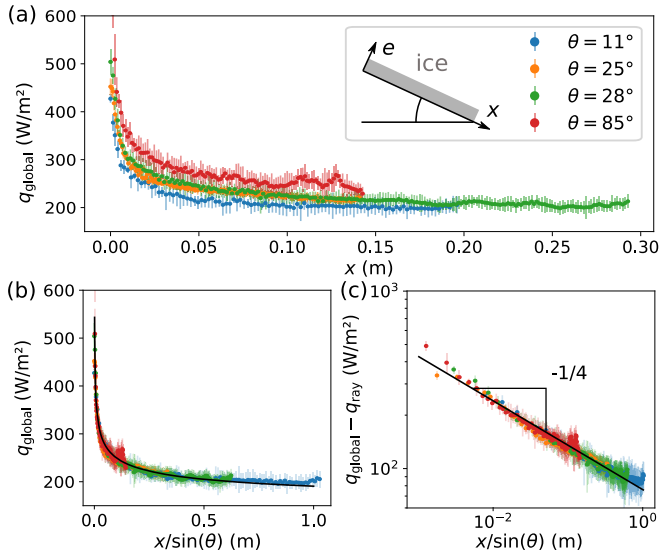


FIG. 2. Heat flux q_{total} received by an ice plate inclined with an angle θ with respect to the horizontal (a) as a function of the distance x from the leading edge and (b) as a function of $x/\sin\theta$. Graph (c) shows $q - q_{\text{ray}}$ as a function of $x/\sin\theta$. The black lines correspond to the expressions of q_{total} (b) and q_{conv} (c) given in Eq. (1) with an adjustable numerical prefactor $A = 0.61$.

from the leading edge of the plate (the highest point from which cold air will flow down the slope), was deduced from the measurement of the local melting rate $v_{\text{ice}}(x) = de(x)/dt = q(x)/\mathcal{L}_{\text{fus}}$ where $\mathcal{L}_{\text{fus}} = 303 \text{ MJ m}^{-3}$ is the enthalpy of fusion of ice. The heat flux profiles are shown in Fig. 2(a) for different inclination angles θ ranging from 11° to 85° . The heat flux is clearly affected by the inclination and strongly increases near the leading edge.

As the ice melts, its surface is covered by a thin film of liquid water. Assuming that this film originates only from the melting of ice and not by condensation, the volumetric flow rate (per unit of width) can be computed from the mean melting rate: $\langle \dot{V}_w \rangle = (1/L) \int_0^L \langle v_{\text{ice}} \rangle x dx = \langle v_{\text{ice}} \rangle L/2 \approx 10^{-7} \text{ m}^3 \text{ s}^{-1}$ where L is the length of the ice plate. Note here that the flow rate $\langle \dot{V}_w \rangle$ and the water velocity vary with x . The typical thickness of the water layer e_w is estimated from the flow rate $\langle \dot{V}_w \rangle$ assuming a free surface flow with a semiparabolic velocity profile [27]

as $e_w = \sqrt[3]{3\nu_w \langle \dot{V}_w \rangle / g} \approx 40 \text{ } \mu\text{m}$, where g is the gravitational acceleration and ν_w is the kinematic viscosity of water. This thickness is in agreement with previous measurements [25]. The maximum typical water velocity v_w at the center of the plate ($x = L/2$) is obtained for a vertical plate ($\theta = 90^\circ$) as $v_w = ge_w^2 / (2\nu_w) \approx 4 \text{ mm s}^{-1}$. On the edges (top and sides) we expect the water flow rate and thus the thickness and velocity to vanish. The typical time of thermal diffusion through the water film $\tau_{\text{diff}} = e_w^2 / D_w \approx 0.01 \text{ s}$ is much smaller than the advection time $\tau_{\text{adv}} = L / (2v_w) \approx 30 \text{ s}$ where D_w is the thermal diffusivity

of water. Therefore the liquid film is not expected to play any role in the energy balance (thermal conduction through the thin film of liquid water is quick) and the incoming heat flux at the ice surface is equal to the local heat flux at the top of the liquid layer (from the ambient air), consistently with previous analysis [24]. Note that the heat flux is two orders of magnitude higher than numerical predictions assuming a leading effect of condensation for a vertical ice plate [25], thus ruling out condensation as the main mechanism governing the melting.

The heat sources in the experiment are infrared radiations coming from the walls at room temperature (q_{ray}) and natural air convection (q_{conv}). The total heat flux is denoted as $q_{\text{total}} = q_{\text{ray}} + q_{\text{conv}}$. The ice is opaque to far infrared radiations which are absorbed in the first tens of micrometers near the surface [28]. For such wavelengths the emissivity of ice and of the chamber walls can be approximated to 1 [29]. The net radiative flux received by the ice is then $q_{\text{ray}} = \sigma(T_{\text{room}}^4 - T_{\text{ice}}^4)$ where σ is the Stefan-Boltzmann constant and $T_{\text{room}} = 295 \text{ K}$ is the room temperature. This gives $q_{\text{ray}} = 110 \text{ W m}^{-2}$ which constitutes, far from the leading edge of the plate, roughly half of the measured heat flux. The convective heat flux may be estimated from numerous studies of natural convective heat transfer between air and a plate with a homogeneous temperature [30–33]. A theoretical assumption [30] states that the laminar convective flow of air on an inclined plate is equivalent to the problem of a vertical plate where the g is replaced by its projection on the plate surface $g \sin\theta$, which was later experimentally verified [31–33]. The analytical calculation of the air boundary layer profile gives a power law dependence of the convective flux with the position [34]:

$$q_{\text{conv}}(x) = A \lambda_{\text{air}} (T_{\text{room}} - T_{\text{ice}})^{5/4} \left(\frac{g \beta_{\text{air}} \sin\theta}{\nu_{\text{air}} D_{\text{air}}} \frac{\sin\theta}{x} \right)^{1/4}, \quad (1)$$

where A is a numerical prefactor, $\lambda_{\text{air}} = 0.025 \text{ W m}^{-1} \text{ K}^{-1}$, $D_{\text{air}} = 2.0 \times 10^{-5} \text{ m}^2 \text{ s}^{-2}$, $\beta_{\text{air}} = 1/T_{\text{air}}$, and $\nu_{\text{air}} = 1.4 \times 10^{-5} \text{ m}^2 \text{ s}^{-2}$ are the thermal conductivity, thermal diffusivity, thermal expansion coefficient, and kinematic viscosity of air [35].

Figure 2(b) shows the evolution of the heat flux as a function of $x/\sin\theta$, and, as expected, all data collapse on one master curve. The black solid line corresponds to $q_{\text{ray}} + q_{\text{conv}}(x/\sin\theta)$ with the room temperature measured independently ($T_{\text{room}} = 21.7^\circ\text{C}$), all thermal parameters being extracted from the literature [35] and an adjusted numerical prefactor $A = 0.61$ very close to the theoretical (0.41) [34] and experimental (0.35–0.56) [31–33] values reported in the literature (see [26] and Refs. [31–34,36,37] therein). The convective heat flux, estimated as $q(x/\sin\theta) - q_{\text{ray}}$, is displayed as a function of $x/\sin\theta$ in Fig. 2(c) and the very good agreement between the

experimental results and the model demonstrates that the melting of an ice sheet in air is controlled both by the infrared radiations coming from the room and by the natural convection of the air. In particular, the smoothing of edges (or corners) that can be observed during the melt of an ice block in air can be attributed to the divergence of the heat flux where the air thermal boundary layer vanishes.

Artificial glacier tables.—We now investigate the formation of artificial glacier tables in a similar controlled environment. As can be seen in Fig. 1(b), a small-scale artificial glacier table can be produced by laying a cylindrical extruded polystyrene (XPS) cap on an ice surface for a few hours. In the following H denotes the height of the cylinder and R its radius. The aspect ratio of the cap is defined as $\beta = H/(2R)$. Experiments using cylinders made of five materials are reported in this Letter: extruded XPS, rigid polyvinyl chloride (PVC), plaster, cement, and granite, with thermal conductivity λ varying over two orders of magnitude (see [26]).

Figure 3 illustrates the evolution of a melting ice sheet on which caps are initially laid. Depending on the thermal properties of the material used, the outcome greatly varies. Indeed, under the XPS cap, the ice ablation rate is almost zero and a table forms. The melting under the PVC cap is clearly visible but the ablation rate stays lower under the cap than at the air interface, thus leading to the formation of a less protruding table. In the case of the granite however, the ablation rate is higher under the cap than at the air interface and the stone sinks into the ice sheet. When the cap forms a table, the ice column underneath it becomes thinner and thinner over time, and the cap eventually falls off. In the present Letter, the focus is on the onset of the formation of the table (the first 2 h), when the bottom of the cap is still fully in contact with the ice, and the morphogenesis of the foot over its lifetime is left for future work. Figure 4 shows the evolution of the vertical position of the

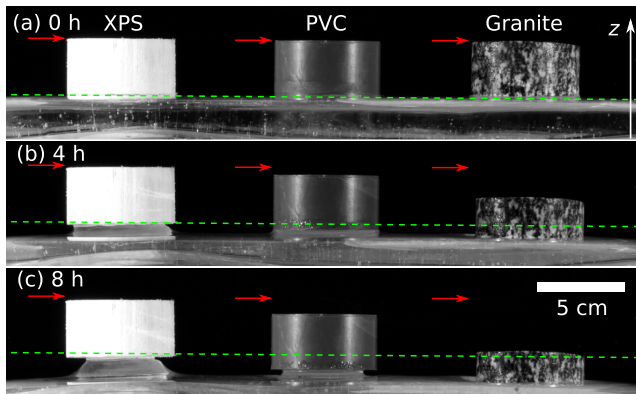


FIG. 3. Cylindrical caps with aspect ratio $\beta = 1/2$ made of XPS, PVC, and granite, in the initial state (a), after 4 h (b) and 8 h (c). The red arrows denote the initial vertical positions of the top of the caps. The green dashed line corresponds to the initial position of the ice surface.

top of caps (for three of the tested materials) along with the position of the ice surface far from the cap. These evolutions are linear meaning that the system quickly reaches a steady state (within minutes) and that the ice ablation rate under the cap (and far from it) is constant over time. The vertical velocity of the cap v_{cap} , and the velocity of the ice at the air interface v_{ice} (far from the cap), are measured from these evolutions, during the same experiment. The ability for a cap to form a table in early stages is estimated from the ratio $v_{\text{cap}}/v_{\text{ice}}$: if this ratio exceeds unity, then the cap sinks into the ice block, whereas, when it is less than unity, a table will initially form. The lower the ratio, the quicker the formation occurs.

The fact that caps of similar sizes but various thermal properties can display such opposite behaviors (forming a table or sinking) shows that there exist two competing effects governing the ice melting under the cap. On the one hand, there is a geometrical amplification effect: the heat flux coming from the environment to the cap, that eventually goes to the ice, is received on a higher surface $S_{\text{air-cap}} = \pi R^2 + 2\pi RH$ than the contact area between the ice and the cap $S_{\text{ice-cap}} = \pi R^2$. The geometrical amplification coefficient expresses $S_{\text{air-cap}}/S_{\text{ice-cap}} = 1 + 4\beta$. On the other hand, there is an attenuation effect of the heat flux because the temperature T_{cap} of the cap-air interface is higher than T_{ice} . This reduces the radiative and the convective heat flux received by the cap compared to the one received by the ice as they both depend on the difference between the surface temperature and T_{room} . In the following we introduce a one-dimensional model that accounts for both effects.

An effective heat transfer coefficient h_{eff} is introduced from a linear expansion of the total heat flux received by the cap from the environment $q_{\text{total}}(T_{\text{cap}}) = q_{\text{ray}}(T_{\text{cap}}) + q_{\text{conv}}(T_{\text{cap}}) = h_{\text{eff}}(T_{\text{room}} - T_{\text{cap}})$, with $h_{\text{eff}} = 4\sigma T_{\text{room}}^3 + h_{\text{conv}}$ when the weak temperature dependence of h_{conv} is neglected. This coefficient, which is independent of the thermal properties of the materials, is therefore the same for the ice and for all caps. The measurements of the ice melting velocity in Fig. 4 lead to

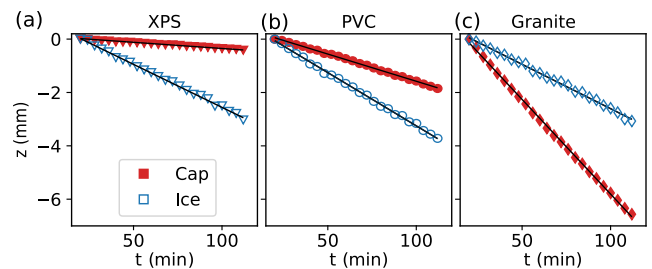


FIG. 4. Vertical position of caps (red solid markers) and of the air-ice interface (blue empty markers, see [26]) as a function of time for caps made of (a) XPS, (b) PVC, and (c) granite with an aspect ratio $\beta = 1/2$ and radius $R = 42, 41,$ and 31 mm respectively.

$h_{\text{eff}} = 9.1 \pm 0.1 \text{ W K}^{-1} \text{ m}^{-2}$, which is consistent with results found in the literature [34].

The heat fluxes received respectively by the cap and by the ice far away from the cap are labeled $q_{\text{air} \rightarrow \text{cap}} = h_{\text{eff}}(T_{\text{room}} - T_{\text{cap}})$ and $q_{\text{air} \rightarrow \text{ice}} = h_{\text{eff}}(T_{\text{room}} - T_{\text{ice}})$. The ice under the cap receives a heat flux $q_{\text{cap} \rightarrow \text{ice}} = (1 + 4\beta)q_{\text{air} \rightarrow \text{cap}}$ due to the geometrical amplification. Moreover, the heat flux going through the cap is computed using a 1D steady-state conduction model: $q_{\text{cap} \rightarrow \text{ice}} = \lambda[(T_{\text{cap}} - T_{\text{ice}})/d]$ where d is a typical length scale. For an infinitely wide cap (i.e., $\beta = 0$), the characteristic length d would directly be given by the height of the cap H . Here, the 3D geometry of the cap is taken into account by assuming that d is proportional to the ratio between the volume of the cap and the surface in contact with air: $d = \eta V_{\text{cap}}/S_{\text{air-cap}} = \eta 2R\beta/(1 + 4\beta)$ where η is a numerical prefactor. This allows one to express temperature difference between the cap and the ice $T_{\text{cap}} - T_{\text{ice}} = (T_{\text{room}} - T_{\text{ice}})/[1 + (\lambda/2\eta\beta h_{\text{eff}}R)]$ and to estimate the ratio between the heat fluxes responsible for the ice melting under the cap and far from the cap. This ratio is also the ratio of the melting velocities under the cap and far from the cap:

$$\frac{v_{\text{cap}}}{v_{\text{ice}}} = \frac{q_{\text{cap} \rightarrow \text{ice}}}{q_{\text{air} \rightarrow \text{ice}}} = \frac{1 + 4\beta}{1 + 2\eta\beta \frac{h_{\text{eff}}R}{\lambda}}. \quad (2)$$

Note that the dimensionless number $h_{\text{eff}}R/\lambda$ which appears in Eq. (2) is the only parameter accounting for the thermal properties of the material. Moreover, as the system quickly reaches a steady state, the only relevant thermal property of a given material is its thermal conductivity, while its heat capacity only plays a role in a rapid transient regime.

The velocities ratio $v_{\text{cap}}/v_{\text{ice}}$ for cylindrical caps made of XPS, PVC, plaster, cement, and granite are shown as a function of $h_{\text{eff}}R/\lambda$ in Fig. 5, for three values of the aspect ratio β . The dimensionless number $h_{\text{eff}}R/\lambda$ varies over three decades by changing the radius R of the cylinder and its thermal conductivities λ —which were measured in the case of PVC, plaster, cement, and granite and taken from

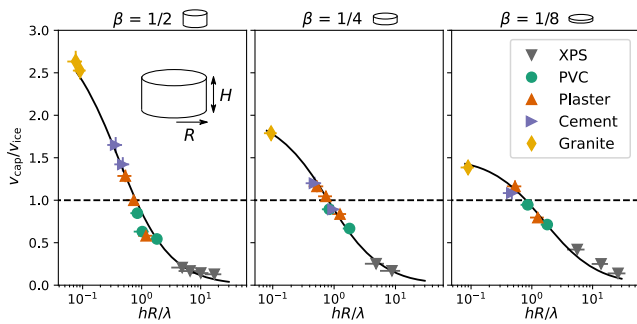


FIG. 5. Ratio $v_{\text{cap}}/v_{\text{ice}}$ as a function of the dimensionless number $h_{\text{eff}}R/\lambda$ for three values of the aspect ratio $\beta = H/(2R)$. The solid black lines correspond to Eq. (2) with $\eta = 2.5$.

the literature for XPS (see [26]). For each aspect ratio β , the two regimes (sinking and table formation) are visible. Note that the transition ($v_{\text{cap}} = v_{\text{ice}}$) is observed to occur experimentally for $(h_{\text{eff}}R/\lambda) = 0.8$, independently of the value of β . In Eq. (2), the transition occurs for $(\eta/2)(h_{\text{eff}}R/\lambda) = 1$ and our experimental observations lead to $\eta = 2.5$. The complete prediction of Eq. (2) is shown as black lines in Fig. 5, in excellent agreement with the experimental data, which validates the simple assumptions of our model.

From an extrapolation of our modeling, it is possible to estimate the critical size of rocks from which a glacier table can form on a glacier. The complexity of the energy balance on a glacier can be tackled using a temperature index model [38], which relies on the observation that the net heat flux is strongly correlated to the temperature of the air above the glacier. Assuming a linear relationship leads to $v_{\text{ice}} = \text{DDF}(T_{\text{air}} - T_{\text{ice}})$. The average degree day factor DDF is reported to vary roughly between 5 and $10 \text{ mm day}^{-1} \text{ K}^{-1}$ [39], which corresponds to an effective heat exchange coefficient $h_{\text{eff}} = \text{DDF} \mathcal{L}_{\text{fus}}/(24 \times 3600) = 20\text{--}40 \text{ W K}^{-1} \text{ m}^{-2}$. For granite rocks, this leads to a critical diameter of $D_{\text{lim}} = 1.6\lambda/h_{\text{eff}} = 10\text{--}20 \text{ cm}$, which is consistent with the observation that the glacier tables usually have a metric size.

Conclusion and perspectives.—We were able to produce small scale artificial glacier tables in a controlled environment in which the mechanisms of the heat transfer were identified. By comparing the experimental results with an analytical heat conduction model, we showed that the table formation in these conditions is controlled by a single dimensionless number, $h_{\text{eff}}R/\lambda$ which takes into account the properties of the material laid on the ice. In the case of a small cap with high thermal conductivity, the geometrical amplification of the heat flux causes the cap to sink into the ice. In contrast, a large cap with low thermal conductivity will form a table as the higher temperature of the cap reduces the net heat flux to the ice below. From this, the critical rock size delimiting these two regimes on a glacier can be estimated to be of the order of tens of centimeters which is consistent with field observations. The question remains on how the direct or indirect solar irradiation, the wind, the diurnal variability, or the porosity of the ice and debris layer can affect this process in natural conditions [38,40–42]. Our approach should also be extended to the study of the overall shape of glacier tables throughout their lifetime. With a more complete understanding, glacier table might be used as proxies to estimate environmental parameters such as effective heat transfer coefficient or glacier ablation.

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