Quasisymmetric Optimization of Nonaxisymmetry in Tokamaks

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Predictive 3D optimization reveals a novel approach to modify a nonaxisymmetric magnetic perturbation to be entirely harmless for tokamaks, by essentially restoring quasisymmetry in perturbed particle orbits as much as possible. Such a quasisymmetric magnetic perturbation (QSMP) has been designed and successfully tested in the KSTAR and DIII-D tokamaks, demonstrating no performance degradation despite the large overall amplitudes of nonaxisymmetric fields and strong response otherwise expected in the tested plasmas. The results indicate that a quasisymmetric optimization is a robust path of error field correction across the resonant and nonresonant field spectrum in a tokamak, leveraging the prevailing concept of quasisymmetry for general 3D plasma confinement systems such as stellarators. The optimization becomes, in fact, a simple eigenvalue problem to the so-called torque response matrices if a perturbed equilibrium is calculated consistent with nonaxisymmetric neoclassical transport.

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Magnetic fusion strongly relies on a symmetry in the magnetic field to confine hot and charged particles inside a vessel. It is the toroidal axisymmetry in a tokamak that fundamentally offers good thermal plasma confinement within toroidal magnetic surfaces [1,2], while also providing engineering simplicity. Nonetheless, the axisymmetry can never be perfect in reality and a small nonaxisymmetric error field must be under control as otherwise it can induce unnecessary transport effects such as the toroidal drag of rotating plasmas. The immediate proof of the value of error field control in tokamaks is to increase the propensity of the plasma to rotate toroidally, which helps the disruption avoidance [3–9] and eases transition to or sustainment of high confinement modes [10-13]. This becomes more important as tokamaks grow in size, since the relative amount of torque that can be applied externally decreases [14]. If the error field cannot be reduced in magnitudes by correcting field, an ideal alternative is to modify the nonaxisymmetry into a symmetry required to conserve the action of particles on magnetic surfaces [15,16] and thereby preserve original confinement as much as possible. This paper reports the first design and experimental demonstration of such a quasisymmetric magnetic perturbation in tokamaks, which illuminates a reliable path of comprehensive error field correction in fusion burning plasmas [17].

Small nonaxisymmetry $\delta \vec{B}$ in the tokamak magnetic field $\vec{B}_0 = B_0 \hat{b}$ can still conserve the action of particles $\mathcal{J} = \oint v_{\parallel} dl$, the integral of the parallel velocity v_{\parallel} along the trajectories dl, if the field strength along the field lines

remains unchanged, i.e., $|(\vec{B}_0 + \delta \vec{B})(\vec{x} + \vec{\xi})| = |\vec{B}_0(\vec{x})|$. The displacement of the field lines $\vec{\xi}$ moves plasmas almost ideally through Faraday's and Ohm's laws, giving the condition for quasisymmetry in a perturbed tokamak [18] as

$$\delta_{\mathcal{L}} \equiv (\hat{b} \cdot \vec{\nabla} \, \vec{\xi} \cdot \hat{b} - \vec{\nabla} \cdot \vec{\xi}) \sim 0, \tag{1}$$

to the leading order in particular on the so-called Boozer coordinates [19]. This condition is, however, not compatible with the perturbed plasma equilibrium $\delta \vec{F}[\vec{\xi}] = 0$ [20] that dictates the $\vec{\xi}$ profiles and thus cannot be satisfied globally across the plasma, as is known generally for 3D magnetic confinement systems [21]. This is also true for the omnigeneity [22,23] $\delta \mathcal{J} \sim 0$, which is less constrained in average than $\delta_{\mathcal{L}} \sim 0$.

The best practice for minimizing the deviation from this symmetry is offered by integrating the calculations of perturbed equilibria into the prediction of its final consequences to confinement, which can be represented by the toroidal drag force $T_{\varphi}(\psi) = \text{Im}[n \int^{\psi} d\vec{x}(\vec{\xi} \cdot \delta \vec{F})]$ [18]. The torque T_{φ} inside a torus at the flux label ψ is due to $\delta \vec{j} \times \delta \vec{B}$ with the nonambipolar current $\delta \vec{j}$ associated with particles radially drifting off magnetic surfaces to conserve the action \mathcal{J} when $\delta_{\mathcal{L}} \neq 0$ [24]. The torque density $\tau_{\varphi}(\psi) = dT_{\varphi}/dV$ with the volume of the torus V by a species with the charge q becomes the direct measure of the additional particle flux due to the nonaxisymmetry, as the number of the particles leaving the torus is increased by



FIG. 1. Quasisymmetric n = 1 configurations tested in the KSTAR (left) #22972 and the DIII-D (right) #178620 high- β tokamak plasmas using their 3 rows of versatile control coils, with the perturbed flux surfaces (amplified visually by ×25 for KSTAR and ×10 for DIII-D), and the illustrated distribution of nonaxisymmetric magnetic fields and coil currents in colors (in red for + and blue for – with contrast proportional to their amplitudes.)

 $\Gamma = (\tau_{\varphi}/q)(dV/d\psi)$. Note that a perturbation is described with the complex Fourier representation $\propto e^{i(m\vartheta - n\varphi)}$ with the *m* poloidal and *n* toroidal mode along the two angles (ϑ, φ) . The unique product of such a self-consistent formulation, implemented in general perturbed equilibrium code (GPEC) [25], is the torque response matrix function $\stackrel{\leftrightarrow}{T}(\psi)$ in the Fourier space, which simplifies the problem of quasisymmetric optimization into a matrix exercise by

$$T_{\varphi}(\psi) = \vec{\Phi}^{\dagger} \cdot \overleftrightarrow{T}(\psi) \cdot \vec{\Phi} = \vec{C}^{\dagger} \cdot \overleftrightarrow{T}_{C}(\psi) \cdot \vec{C} \sim 0.$$
(2)

The matrix \hat{T} can be represented on any basis set as long as it uniquely represents nonaxisymmetric magnetic perturbations available in space. For example, $\vec{\Phi}$ is the perturbed magnetic flux decomposed to Fourier modes on the plasma boundary, and \vec{C} is the amplitude and phase of currents in available nonaxisymmetric coils. Since $\hat{T}^{\dagger} = \hat{T}$ [25], its eigenvector \vec{C}_{\min} with the minimum eigenvalue λ_{\min} is simply the best achievable quasisymmetric magnetic perturbation (QSMP) in a tokamak, as illustrated in Fig. 1 and successfully demonstrated in the two tokamak devices— KSTAR [26] and DIII-D [27].

These two devices were particularly suitable for this test since they both have versatile 3D coils that can generate 3 distinct perturbed field distributions in arbitrary phase for n = 1, which tends to be most amplified by plasma response [28] and thus can magnify the potentially small transport effects driven by QSMPs. Both devices have small uncertainties in nonaxisymmetric machine errors, either due to an intrinsically low level [29] or with an established correction algorithm [8]. For each target plasma, $\hat{T}_C(\psi)$ is a mere 3×3 complex matrix function but still has all the information of the toroidal torque that can be produced by the coils for the given *n*. Figure 1 shows the perturbed flux surfaces and field distributions in the KSTAR and DIII-D target plasmas, with the coil configurations and perturbations designed using \vec{C}_{min} from the GPEC $\stackrel{\leftrightarrow}{T}_{C}(\psi = \psi_{b})$, where ψ_{b} is the numerical plasma boundary, i.e., minimizing the total integrated torque down to the theoretical minimum λ_{\min} .

QSMPs were then contrasted to the other two distinct types of nonaxsymmetric fields-a resonant magnetic perturbation (RMP) [30] and nonresonant magnetic perturbation (NRMP) [31], as introduced in Fig. 2 with each of the predicted torque profiles. As clearly shown in Figs. 2(a-1), the RMP strongly resonates with the plasmas at the rational surfaces q = m/n, where the safety factor q is the ratio of toroidal to poloidal circuits of the magnetic field lines, with locally concentrated torque density making the stairlike jumps in the integrated torque, Figs. 2(a-2) and 2(b). The NRMPs' effect is widely spread throughout the entire region, resulting in a gradual and smooth increase of the integrated torque from the core to the edge. This classification is important for practical purposes. The goal of the RMP optimization is to create a local resonant response without NRMP effects to control instabilities such as edge-localized-modes (ELMs) [32-38], whereas the goal of the NRMP optimization is to purposely create the torque to control the rotation profile [31,39-42] in a particular region but without RMP response. Note that the RMP response includes not only the toroidal drag, or rotational damping, but also a bifurcation into magnetic islands due to the local toroidal torque which can consequently lead to other transport effects such as density pumping [43] or disruptive instabilities such as a locked mode [3]. A QSMP suppresses both effects, requiring at least 3 rows of coils like KSTAR or DIII-D for a successful demonstration-one coil to produce a strong proxy error, another coil to minimize the RMP and yet another to further minimize the NRMP components. An ultimate goal of 3D tokamak optimization would be to leave only QSMPs everywhere except a region where the applied RMP or NRMP is judiciously designed to take an effect for the control purposes.

The optimization of various nonaxisymmetric fields becomes comprehensive only with a kinetic calculation integrated into perturbed equilibria. As indicated



FIG. 2. Comparison of the (a-1) predicted torque density, (a-2) integrated torque profiles in the KSTAR, and (b) DIII-D discharges by QSMPs (blue), NRMPs (green), and RMPs (red). The RMP produces torque mainly through the field resonances, whereas the NRMP induces torque and transport broadly across the region. The QSMP optimization leads to the suppression of both effects as well as the kinetic orbit-resonant effect, as pronounced in the (a-2) RMP application. In very high- β plasmas like the studied DIII-D case, the field resonance is shifted and split due to the kinetic effects which can strongly change the originally optimized spectrum as implied by the revisited QSMP (light blue).

in Fig. 2(a-2), the QSMP also minimizes the orbit-resonant effect which becomes strong when $\vec{E} \times \vec{B}$ rotation ω_E is low, i.e., $\omega_E \sim 0$ or more generally for any particle that cycles to a closed orbit by $(\ell \pm nq)\omega_b + n(\omega_E + \omega_B) \sim 0$, where ω_b is the bounce frequency and ω_B is the magnetic precession frequency with an integer ℓ [44]. In highperformance scenarios like the studied DIII-D cases, the field resonance m - nq = 0 is also largely shifted and split due to local kinetic effects as indicated in Fig. 2(b) by stairlike jumps in both sides to the rational surface. The orbital kinetics is then combined with perturbed equilibria where the amplitude and distribution of $\vec{\xi}$ are simultaneously optimized in a QSMP, as illustrated in Fig. 3 for the KSTAR case. Figure 3(a) in comparison to 3(b) implies the



FIG. 3. Comparison of the (a) field strength averaged on magnetic surfaces (up) and the (b) same but normalized by overall response (down), by the QSMP, NRMP, and RMP applied to the KSTAR discharge. Note that here the RMP and NRMP have the same $|\vec{C}|$, i.e., the rms sum of 3 rows of coil currents, whereas the QSMP is based on a higher $|\vec{C}|$ up to the maximum allowed in the experiments.

importance of the reduction of overall plasma response as roughly represented by ξ_{max} at each surface. The strong plasma response to a small 3D field makes it challenging to intuitively understand the QSMP optimizing process in a tokamak, requiring extended investigations in the future.

These model predictions have been validated then by the measured transport in experimental KSTAR and DIII-D discharges. The KSTAR discharge was assisted by neutral beam injection (NBI) with heating power $P_{nb} \sim 3$ MW and estimated torque $T_{nb} \sim 2.9$ Nm, operating the plasma current $I_P = 0.5$ MA, the toroidal field at the magnetic axis $B_{T0} = 1.8$ T, which produced $\beta_N \sim 1.8$, normalized thermal to magnetic pressure [45], and a safety factor at



FIG. 4. Impact of QSMP, NRMP, and RMP shown by the time traces in a single dedicated KSTAR discharge; (a) 3D coil configurations with 3 amplitudes and phases (rad) for top, middle, bottom row of in-vessel coils, (b) \bar{n}_e measured by two-color interferometer (TCI) and T_e measured by electron-cyclotron emission (ECE) at $R \sim 1.98$ m, and (c) ω_{φ} measured by charge-exchange recombination spectros-copy (CERS) at $R \sim 2.0$ m.

 $\psi = 0.95$, $q_{95} \sim 5$, line-averaged density $\bar{n}_e \sim 3.4 \times 10^{19} \text{ m}^{-3}$, ion and electron temperature $T_i \sim 2.2$ and $T_e \sim 2.3 \text{ keV}$, and toroidal rotation $\omega_{\varphi} \sim 100 \text{ krad/s}$ at the core. Figure 4 shows time traces of the n = 1 field amplitudes and phases in 3 rows of coils (top, middle, bottom coils), \bar{n}_e , T_e , and ω_{φ} slightly off the center at $R \sim 2m$. The RMP induced perturbations in all transport channels of particle, energy, and momentum as is clear by density pumping, temperature degradation, and rotational damping. In contrast, the QSMP did not bring any visible effect, despite the maximum KSTAR 3D coil currents up to $\sim 5 \text{ kA}$.

The benign nature of QSMP was also clearly evinced in DIII-D, compared with NRMP or RMP. The DIII-D experiment targeted high-performance discharges to have a plasma very sensitive to residual nonaxisymmetric fields through the well-known increase of plasma amplification along with β_N [28,46]. The co-NBIs up to $P_{nb} \sim 8.5$ MW on $I_P = 1.2$ MA, $B_{T0} = 1.8$ T injected torque $T_{nb} \sim 6.7$ Nm and increased $\beta_N > 3.0$ with $q_{95} = 4.3$, $\bar{n}_e \sim 5.0 \times 10^{19}$ m⁻³, $T_i \sim 6$ keV, $T_e \sim 4.3$ keV, and $\omega_{\varphi} \sim 80$ krad/s at the core of the target discharges. Figure 5 shows the density and rotation profile changes due to QSMP, NRMP, and RMP in the DIII-D plasmas. Again, the plasma was strongly degraded in all channels and eventually disrupted with a locked mode by the RMP, degraded in rotation by the NRMP, but not influenced in any way by the OSMP despite the maximum coil currents.

The predictive optimization by GPEC torque response matrix has also been validated quantitatively as far as the



FIG. 5. Impact of QSMP, NRMP, and RMP fields on the n_e and ω_{φ} profiles as measured before (solid in black) and after (dash in blue, and dashed-dot in red) the perturbations. Note that the QSMP or NRMP was ramped to its desired maximum at t = 3.05 s but RMP was slowly ramped until it caused a locking and disruption. Note the profiles were taken from OMFIT profile toolkit [47].

total integrated torque is concerned, as shown in Fig. 6. The predictions here include uncertainties in calculating nontrapped (passing) particle effects, in addition to trapped particle effects, which have been extensively verified [44,48]. The torque measurements are simply based on the changes of total angular momentum L of the plasmas, using the mean of $T_{\varphi} = T_{\text{NBI}} \times (\Delta L/L)$ and $T_{\varphi} = dL/dt$ with error bars used to show the deviation between the two methods. These methods ignore momentum transport across the region, which is largely uncertain but can be critical in the future to validate the predicted torque density with rotational damping profiles in detail.

Robustness of the QSMP optimization is also noticeable. Coil configuration optimizations performed well despite nonexact reproduction of the reference discharge used in the predictive modeling. For example, the DIII-D QSMP was designed based on a $\beta_N \sim 2.0$ plasma (#173383) and applied to the high- $\beta_N > 3.0$ (#178620-22), but did not show any degradation in experiments. The difference in the prediction from the re-optimized OSMP for the new target is not entirely ignorable as shown by "QSMP rev." in Fig. 2(b), but mainly through the edge profiles which are subjected to relatively low accuracy. The same QSMP configuration was even applied to a plasma during the L-Htransition [49] with marginal power $P_{nb} \sim 1$ MW and $T_{nb} \sim 0.83$ Nm (#178609-10) and did not show any impact on the transition. This target was disrupted by a NRMP, similarly to the recent observations in the COMPASS tokamak where large NRMPs were left due to highfield-side nonaxisymmetric error fields compensated by low-field-side RMP correction [50].

A practical implication of these observations for the error field correction (EFC) problem is that the QSMP indeed encapsulates an ideal and safe form of nonaxisymmetry. An EFC coil configuration containing a fixed EF source in \vec{C} can be optimized as quasisymmetric as this will simultaneously minimize the negative impact of both the resonant and resonant EF components. The quality of the nonresonant correction can then be quantitatively measured by GPEC torque response matrix. The torque response



FIG. 6. Comparison of the predicted and measured total torques by QSMP, NRMP, RMP in the (a) KSTAR and (b) DIII-D discharges.



FIG. 7. Structure of the integrated torque response matrix \tilde{T} calculated at the plasma boundary for the (a) KSTAR (10⁻³ Nm/G²) and (b) DIII-D (10⁻² Nm/G²) plasmas. The solid circle indicates the dominant mode group with m > nq, and the second circle represents the second nonresonant mode group with m < nq.

matrices T with respect to the full poloidal modes $\vec{\Phi}$ on the boundary, as shown in Fig. 7, typify the second mode group with m < nq which is mostly nonresonant but still degrading, in addition the primary mode group with m > nq which is typically known as the dominant Kink modes [6,46,51]. These components of the EF would naturally be controlled in addition to the resonant components when using a QSMP optimization scheme for EFC.

In summary, new GPEC predictive schemes enabled the first design and demonstration of quasisymmetric magnetic perturbations in tokamaks. Both KSTAR and DIII-D experiments show quiescence of QSMPs in all transport channels despite the large amplitude of perturbations, rendering a group of safe nonaxisymmetric fields. The studies illuminate the feasibility of prevailing concept of quasisymmetry even in a perturbed tokamak, and also a robust path of comprehensive error field correction. It is not yet clear if there is any utility of QSMPs for a tokamak, e.g., heat flux distributions to the divertors, or if 3D stability also remains unchanged, which should be further investigated in the future.

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