New Limits on Anomalous Spin-Spin Interactions

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We report the results of a new search for long-range spin-dependent interactions using a Rb^{-2} Ne atomic comagnetometer and a rotatable electron spin source based on a $SmCo₅$ magnet with an iron flux return. By looking for signal correlations with the orientation of the spin source we set new constraints on the product of the pseudoscalar electron and neutron couplings $g_p^e g_p^{\eta}/\hbar c < 1.7 \times 10^{-14}$ and on the product of their axial
couplings $e^e g^{\eta}/\hbar c < 5 \times 10^{-42}$ to a new particle with a mass of less than about 1 ugV. Our measurement $\frac{p}{p}$ couplings $g_A^e g_A^h/\hbar c < 5 \times 10^{-42}$ to a new particle with a mass of less than about 1 μ eV. Our measurements couplings $g_A g_A / nc < 3 \times 10^{-6}$ to a new particle with a mass of less than about 1 μ ev. Our measur improve by about 2 orders of magnitude previous constraints on such spin-dependent interactions.

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Long-range interactions between spin-polarized objects are dominated by photon-mediated magnetic forces. Additional long-range forces may exist if there are new light or massless particles beyond the standard model. For example, such new forces arise from exchange of pseudoscalar axions or axionlike particles [\[1\]](#page-3-1) from spin-1 paraphotons or light Z' bosons $[2,3]$; from exchange of "unparticles" [\[4,5\],](#page-3-3) dynamical breaking of local Lorentz invariance [\[6\],](#page-3-4) or propagating torsion in modified gravity [\[7,8\]](#page-3-5). In many of these models significant long-range interactions appear only when both objects are spin polarized, for example, for axionlike particles without a $\bar{\theta}$ term [\[1\],](#page-3-1) or for paraphotons—massless gauge boson with dimension-6 operator coupling to fermions [\[2\].](#page-3-2) Overall, the search for axion or axionlike particles is of particular interest since they are candidates to explain the unexpected small level of CP violation in QCD or the nature of dark matter.

Experimental searches for anomalous spin-spin interactions were first discussed by Ramsey [\[9\]](#page-3-6) and have been performed using a variety of systems, including atomic comagnetometers [\[10,11\],](#page-3-7) trapped ions [\[12,13\],](#page-3-8) spin-polarized pendulums [\[14,15\]](#page-3-9), polarized geoelectrons [\[16\]](#page-3-10), and NMR spectroscopy [\[17,18\].](#page-3-11) Such experiments typically use a "spin source"—a large collection of spin-polarized fermions and a "spin sensor"—a sensitive system for measurement of the resulting shifts in spin energy levels. Nuclear spin sensors typically have good energy resolution due to long spin coherence times of nuclear spin ensembles. Therefore, it is natural to combine a nuclear spin detector, similar to the one used [\[11\]](#page-3-12), with a permanent magnet spin source that provides the highest density of polarized electron spins, as used in Refs. [\[14,15\]](#page-3-9).

Here we describe such an experiment searching for electron-nuclear spin-dependent forces using a rotatable $SmCo₅$ spin source [\[19\]](#page-3-13) and a ²¹Ne-Rb comagnetometer [\[20\]](#page-3-14). SmCo₅ has a unique property that part of its magnetization is created by angular moment of the electrons, instead of their spins. This allows one to cancel the net magnetic field created by the spin source without canceling an anomalous spin-dependent force. Our experimental arrangement is sensitive to two spin-dependent potentials in the notation of Ref. [\[2\]](#page-3-2), given by

$$
V_2 = \frac{g_A^1 g_A^2}{4\pi} \frac{(\hat{\sigma}_1 \cdot \hat{\sigma}_2)}{r} e^{-r/\lambda},\tag{1}
$$

$$
V_3 = \frac{g_p^1 g_p^2 \hbar^2}{16\pi M_1 M_2 c^2} \left[(\hat{\sigma}_1 \cdot \hat{\sigma}_2) \left(\frac{1}{\lambda r^2} + \frac{1}{r^3} \right) - (\hat{\sigma}_1 \cdot \hat{r}) (\hat{\sigma}_2 \cdot \hat{r}) \left(\frac{1}{\lambda^2 r} + \frac{3}{\lambda r^2} + \frac{3}{r^3} \right) \right] e^{-r/\lambda}.
$$
 (2)

In the above equations, $\hat{\sigma}_i$ is the normalized expectation value of the *i*th particle spin and M_i is its mass, $\lambda = \hbar/mc$ is the Yukawa range of the new particle with mass m mediating the spin-dependent force, and r is the distance between the two spins. We set new limits on the product of electron and neutron pseudoscalar coupling constants $g_p^e g_p^n$ electron and neutron pseudoscalar coupling constants $g_p^r g_p^r$
for V_3 and the product of the axial vector coupling
constants $g_e^e g_e^u$ for V_2 . The interaction potential V_2 can constants $g_A^{\rho} g_A^{\eta}$ for V_2 . The interaction potential V_3 can
also be generated by a vector particle, such as a paraphoton constants $g_A^T g_A^T$ for v_2 . The interaction potential v_3 can
also be generated by a vector particle, such as a paraphoton or Z' boson. Our measurements set new limits on the combinations of their parameters described [\[2\]](#page-3-2). One can also set limits in the product of electron and proton spin couplings using the subleading proton spin polarization in ²¹Ne $[21]$. Our limits are substantially better than can be extracted by combining the results of previous electronelectron and nuclear-nuclear spin force experiments.

The Rb-²¹Ne comagnetometer used in this experiment (Fig. [1](#page-1-0)) is similar to the one in Ref. [\[20\]](#page-3-14). A more detailed explanation of its operation can be found in Refs. [\[20,22](#page-3-14)– [24\].](#page-3-14) At the heart of the comagnetometer is an aluminosilicate GE180 spherical glass-blown cell 1 cm in diameter containing 1.5 amagats of ²¹Ne, 50 Torr of N₂ (to prevent radiation trapping), ⁸⁷Rb and trace amounts of Cs. The cell is heated up to 180° C to create a dense, optically thick

FIG. 1. The experimental setup, adapted from Ref. [\[22\]](#page-4-6). The spin source is placed under the comagnetometer cell with the rotation axis parallel to the probe beam.

vapor of ⁸⁷Rb. The Cs vapor remains optically thin and is optically pumped to create a relatively uniform spin polarization, which is transferred by spin-exchange colli-sions to Rb and then to ²¹Ne [\[25\].](#page-4-1) Cs is optically pumped using 450 mW of circularly polarized light at 895 nm.

The spin polarization of $87Rb$ is measured via Faraday rotation of a linearly polarized probe beam detuned from 795 nm and propagating through the cell in the \hat{x} direction. To measure small optical rotation the linear polarization of the probe beam is modulated at 50 kHz by a photoelastic modulator (PEM) and readout using a lock-in amplifier. Low frequency noise from air currents is greatly reduced by operating the experiment inside a vacuum bell jar at pressure of about 1 Torr. The probe and pump beams are steered to illuminate the center of the cell, which reduces any spurious effects due to the linear dichroism of the cell walls [\[26\].](#page-4-2)

The comagnetometer is operated at a compensation point where the external B_z field is equal and opposite to the sum of the effective magnetic fields created due to spinexchange collisions with polarized $87Rb$ and $21Ne$ [\[26\]](#page-4-2). Automated zeroing routines are used to adjust the magnetic fields inside the shields in the x , y , and z directions. After field zeroing the leading term in the comagnetometer's signal at the compensation point is

$$
S = \kappa \frac{\gamma_e P_z^e}{R_{\text{tot}}} \left[b_y^n - b_y^e + \frac{\Omega_y}{\gamma_n} \right],\tag{3}
$$

where γ_e and γ_n are the gyromagnetic ratios of the free
electron and ²¹Ne respectively P^e is the polarization of ⁸⁷Rb electron and ²¹Ne, respectively, P_z^e is the polarization of ⁸⁷Rb,
 R_{max} is the total relaxation rate of ⁸⁷Rb, and $h^{n,e}$ are the R_{tot} is the total relaxation rate of ⁸⁷Rb, and $b_y^{n,e}$ are the anomalous magnetic fields that couple to the ²¹Ne and ⁸⁷Rb anomalous magnetic fields that couple to the 21 Ne and 87 Rb electron spins in the y direction. Ω_{v} is the gyroscopic rotation around the y axis. The comagnetometer has suppressed sensitivity to ordinary magnetic fields but retains leading order sensitivity to anomalous fields. To calibrate the comagnetometer we measure the response to a slowly modulated B_x field [\[24\].](#page-4-3) We verify the calibration factor by measuring the gyroscopic signal due to a slowly changing tilt of the optical table and compare it to the response of the tilt sensors.

The spin source is made from multiple rectangular blocks of SmCo₅ permanent magnet with $7.6 \times 7.6 \times$ 20.3 cm^3 total volume surrounded by a cylindrical soft iron flux return with an outer diameter of 15.2 cm and length of 22.9 cm. The axis of the spin source is 25 cm away from the center of the comagnetometer cell. The remnant magnetic field outside of the iron cylinder is about 0.6 mT, in good agreement with finite element magnetic field analysis. To further reduce this field, a cosine coil is mounted on the outside of the iron cylinder and three layers of μ -metal shields are added around the spin source. The coil allows us to cancel the residual leakage of the fields by a factor of 10 or alternatively increase the field to check for systematic sensitivity of the comagnetometer. The orientation of the spin source is reversed by rotating the cylinder around its axis using a stepper motor and a timing belt while keeping the outer two magnetic shield layers fixed. The residual magnetic field correlated to the orientation of the spin source is equal to approximately 2.5×10^{-9} T. The comagnetometer apparatus is vibrationally isolated from the mechanical rotation system inside the vacuum bell jar.

Fully magnetized SmCo₅ with $B_0 \approx 1$ T has an electron spin density of 4.5×10^{22} spin/cm³ while soft iron with the same magnetization has a spin density of 8.2×10^{22} spin/cm³ [\[27,28\]](#page-4-4). Hence the spin source posses a large net electron spin while having only a small residual magnetic dipole moment. The presence of net spin in a similar structure had been verified in Ref. [\[27\]](#page-4-4) by observing the gyrocompass signal. The use of magnetic shielding does not screen anomalous spin interactions. Magnetic shielding around the spin source has a similar spin content to the soft-iron flux return. The magnetic shielding around the comagnetometer cannot hide the signal, as discussed in Ref. [\[29\]](#page-4-5), because we compare spin interactions of electron and nuclear spins in the ⁸⁷Rb-Ne comagnetometer. The rotation of the spin source is controlled by a separate computer to minimize possible cross-talk with the main system operating the experiment.

Data are collected in intervals of 250 s during which the spin source is rotated by 180° 19 times every 12 s. String analysis [\[26\]](#page-4-2) is used to calculate the correlation of the comagnetometer signal with spin source orientation, using only the last 2 s to allow the system to settle mechanically after each rotation. The B_z field is adjusted at the end of each interval, while the other field components are zeroed and the comagnetometer sensitivity is calibrated every seven hours.

Figure [2](#page-2-0) shows the results of approximately two weeks of data. Each data point corresponds to a ∼24 h

FIG. 2. Measured correlation for positive polarization (red), negative polarization (black), clockwise spin source rotation (triangles pointing down), counterclockwise ones (triangles pointing up).

measurement. We collected data with clockwise and counterclockwise spin source rotations and for two orientations of the atomic spin polarization. The results of the measurements of $b_y^n - b_y^e$ are summarized in Table [I.](#page-2-1) The
error hars are scaled by the value of reduced y^2 . Extended error bars are scaled by the value of reduced χ^2 . Extended discussion about the method used to obtain uncertainty and reduced χ^2 can be found in Refs. [\[24,30\].](#page-4-3)

To check for possible systematic effects correlated with spin source orientation we monitor the magnetic fields, tilts of the comagnetometer platform, positions of the laser beams, as well as other signals that did not show significant effects. Measurements of the magnetic fields at several positions around the apparatus with a fluxgate magnetometer have average correlated field amplitudes of 8.2×10^{-10} , 2.4×10^{-9} , and 2.6×10^{-10} T for the \hat{x} , \hat{y} , and \hat{z} directions, respectively. The combination of magnetic shielding around the cell and the comagnetometer compensation give an additional suppression of external fields by 5×10^{-8} for \hat{x} and higher suppressions for the \hat{y} and \hat{z} axes. Two four-quadrant photodiodes monitor the positions and powers of the pump and probe beams. A separate set of measurements was used to find the correlation between the rotation of the spin source and the beams' positions for both clockwise and counterclockwise rotations of the spin source in the same analysis window as the main measurement. To estimate sensitivity to beam motion, larger beam motion was induced while monitoring the comagnetometer

TABLE I. Measured correlation for negative polarization (b_{p-}^y) , nositive polarization (b_{p-}^y) , counterclockwise spin source rotation positive polarization (b_{p+}^y) , counterclockwise spin source rotation (b_y^y) , and total correlation $(b_{\text{c}v}^{\mathcal{V}})$, clockwise spin source rotation $(b_{\text{cw}}^{\mathcal{V}})$, and total correlation $(b^{\mathcal{V}})$ $\frac{(b_{\text{tot}}^y)$.

Type	Weighted averaged correlation (aT)	Reduced χ^2
b_{p-}^{y} b_{p+}^{y} b_{c}^{y} b_{c}^{y}	-180 ± 110	1.53
	-9 ± 83	0.743
	-71 ± 89	1.07
	-140 ± 140	1.97
$b_{\text{tot}}^{\text{y}}$	-80 ± 70	1.32

TABLE II. Signal correlation estimated from external sensors.

Sensors	Averaged correlation (aT)
Fluxgate X	-41 ± 1
$Fluxgate$ Y	48 ± 1
Fluxgate Z	$-52+1$
Probe beam position (H)	-14 ± 38
Probe beam position (V)	12 ± 11
Probe beam power	$8 + 10$
Pump beam position (H)	-6.1 ± 16
Pump beam position (V)	$91 + 138$
Pump beam power	-31 ± 26
Tilt rate $Y(\Omega_{v})$	-110 ± 82
Tilt rate $X(\Omega_r)$	-1.4 ± 9
Total	-96 ± 169

signal. A precision tiltmeter mounted on the same vibration-isolation platform as the comagnetometer measured the residual rotation rate of the platform correlated with spin source reversal.

Table [II](#page-2-2) shows the summary of measured systematic effects. The total systematic error from magnetic field leakages, beam positions and power, as well as gyroscopic couplings is constrained with an uncertainty of 169 aT. Our assumption is that systematic effects recorded for the relevant sensor correlations are independent. Hence, we can combine their uncertainties in quadrature to provide an estimate of the overall systematic uncertainty. Hence, we quote the final total anomalous coupling as $b_{\text{tot}}^y =$
-80 + 70 + 169 . This yields at the 95% confidence -80 ± 70 _{stat} ± 169 _{syst}. This yields, at the 95% confidence level, $|b_{\text{tot}}^y| < 400$ aT.
To convert the mean

To convert the measured value of $b_n^y - b_e^y$ to limits on
in-spin interactions, we express the energy shift due to the spin-spin interactions, we express the energy shift due to the anomalous potentials for neutrons, protons, and electrons as $V_n f_n + V_p f_p - V_e = \mu_{21} V_p^b + \mu_B \beta_y^e$, where $f_n = 0.58$
and $f_n = 0.04$ are the fraction of neutron and proton spin and $f_p = 0.04$ are the fraction of neutron and proton spin polarization in ²¹Ne [\[21\]](#page-4-0). The interactions given by Eqs. [\(1\)](#page-0-0), [\(2\)](#page-0-1) are integrated over the distribution of the polarized spins in the $SmCo₅$ magnets and the soft-iron flux return.

The limits on the pseudoscalar and axial coupling constants are summarized in Table [III](#page-2-3) and Figs. [3](#page-3-15)

TABLE III. Experimental limits (95% C.L.) on anomalous spin-spin interaction between two fermions by spin-0 or spin-1 boson exchange with Yukawa range of 10^2 to 10^6 cm.

Coupling	This work	Previous limit	Reference
$g_p^e g_p^n/\hbar c$	1.7×10^{-14}	8.1×10^{-12} 9.0×10^{-13} 5.9×10^{-12}	Direct: $[12]$ $(g_p^e)^2(g_p^n)^2$: [11,15] Only for Yukawa
$g_p^e g_p^e/\hbar c$ $g_A^e g_A^n/\hbar c$ $g_A^eg_A^e/\hbar c$	1.5×10^{-14} 5.0×10^{-42} 8.0×10^{-39}	5.5×10^{-17} 4.8×10^{-40} 7.6×10^{-40}	coupling: [15,33] Direct: $[15]$ $(g_A^e)^2(g_A^n)^2$: [11,14] Direct: [14]

FIG. 3. Constraints (95% C.L.) on the coupling parameter $g_p^ng_p^e$
for two fermions interacting by a pseudoscalar boson \overline{a} for two fermions interacting by a pseudoscalar boson.

and [4](#page-3-17). Only one prior experiment has constrained directly the $g_p^n g_p^e$ combination [\[12\].](#page-3-8) More stringent
limits can be obtained by combining the limit on the drawing the $g_p g_p$ combination [12]. More sumgent
limits can be obtained by combining the limit on $(g_p^e)^2$ from Ref. [\[15\]](#page-3-16) and the limit on $(g_p^h)^2$ from
Ref. [11] If the pseudoscalar particle is coupled to Ref. [\[11\]](#page-3-12). If the pseudoscalar particle is coupled to fermions through a Yukawa interaction (as opposed to the derivative coupling typical for axions), one can also obtain a limit on $(g_p^n)^2$ from two-particle exchange
using equivalence principle experiments [31] Several using equivalence principle experiments [\[31\]](#page-4-7). Several additional limits can be set on combinations of coupling parameters for paraphoton and Z' boson from the expressions for $V_3^{\ell n}$ derived in Ref. [\[2\]](#page-3-2). We also set
limits on the product of axial couplings $a^n a^\ell$ for a limits on the product of axial couplings $g_A^n g_A^e$ for a vector boson exchange improving on previous direct $\frac{d}{dx}$ for the product of axial couplings $g_A^x g_A^x$ for a vector boson exchange, improving on previous direct [\[16\]](#page-3-10) and indirect limits [\[11,14\]](#page-3-12) for a particle with Yukawa range of 1 to 10^6 cm. Several additional constraints on the order of 10^{-10} – 10^{-18} exist for $(g_A)^2/\hbar c$ that extend to much shorter length scales [\[13,18,32\]](#page-3-18).

FIG. 4. Constraints (95% C.L.) on the coupling parameters $g_A^n g_A^e$ for two fermions interacting by a spin-1 boson.

In conclusion, we have improved limits on spin-dependent interactions between electrons and neutrons mediated by a new light pseudoscalar or vector boson by about 2 orders of magnitude. The experimental uncertainties are dominated by mechanical transients which produce the largest systematic errors and force us to use a short integration time and a slow source reversal. The sensitivity can be improved by about 2 orders of magnitude with a better vibration isolation system to reduce the motion associated with the mechanical reversal of the spin source.

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