## Generalized Phase Sensitivity of Directional Bond Breaking in the Laser-Molecule Interaction

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We establish a generalized picture of the phase sensitivity of laser-induced directional bond breaking using the  $H_2$  molecule as the example. We show that the well-known proton ejection anisotropy measured with few-cycle pulses as a function of their carrier-envelope phases arises as an amplitude modulation of an intrinsic anisotropy that is sensitive to the laser phase at the ionization time and determined by the molecule's electronic structure. Our work furthermore reveals a strong electron-proton correlation that may open up a new approach to experimentally accessing the laser-sub-cycle intramolecular electron dynamics also in larger molecules.

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Bond breaking in molecules with intense laser pulses is a well-established field of science [1–[6\]](#page-4-2). An important step in this field was the demonstration of anisotropic proton ejection during dissociative laser ionization of  $H_2$  using the carrier-envelope phase (CEP) of intense few-cycle pulses [7–[14\]](#page-4-3) or the relative phase between two colors of multicycle pulses [\[15](#page-4-4)–17]. CEP is, however, not the only phase that can determine the directionality of a bondbreaking reaction. A pronounced anisotropy in proton ejection from  $H_2$  can also be observed with single-color many-cycle fields as a function of the laser phase at the instant of ionization [\[18\]](#page-4-5). However, the relation of these two phases for determining the ejection direction of the proton is unclear. Moreover, the fact that the instant of electron emission within a laser cycle can determine the directionality of bond breaking, questions the role of the CEP-dependent laser field shape after the ionization step in the formation of the proton anisotropy.

In this Letter, we establish a unified picture that connects the roles of the laser phase at the instant of ionization (ionization phase) and the CEP in determining the directionality of proton ejection in laser dissociation of  $H<sub>2</sub>$ . We show that the ejection anisotropy due to the ionization phase is an intrinsic property of the molecule that can only be observed in the molecular frame. In contrast, the CEP acts in the lab frame. Our experiments and simulations prove that the connection between the action of the two phases is provided by the CEP modulation of the instantaneous laser field strength at the time of population transfer between electronic states of  $H_2^+$ . Moreover, our experiments reveal a remarkably strong correlation between the outgoing electron and the ejected proton that is due to the intramolecular electron dynamics during dissociation. This finding, together with the one that the CEP sensitivity of bond breaking emerges via field-modulated intrinsic molecular properties may open up a new approach to investigating laser-sub-cycle electronic dynamics and for controlling bond-breaking events also in larger molecules.

The key to these achievements was the combined application of an elliptically polarized few-cycle laser pulse with known CEP and coincidence detection of protons and electrons in our experiments [19–[21\].](#page-4-6) In elliptically polarized light the ionization time,  $t_i$ , is mapped onto the emission angle of the photoelectron by the laser field via  $\mathbf{p}_e = -\mathbf{A}(t_i)$  [\[22,23,24\]](#page-5-0). Atomic units are used throughout. The laser vector potential  $A(t)$  is connected to the laser electric field by  $\mathbf{A}(t) = -\int_{-\infty}^{t} \mathbf{E}(t')dt'$ . Thus, by measuring in coincidence the momenta of the emitted electron  $\mathbf{p}_e$ and the proton ejected upon dissociation  $\mathbf{p}_{H^+}$ , the electric field vector at the time of ionization  $E(t_i)$  and the angle of proton ejection in the lab frame  $\beta$  can be retrieved [\[18,20\]](#page-4-5); see Fig. [1\(a\)](#page-1-0) for a visualization. From  $\beta$  and  $\mathbf{E}(t_i)$  the ionization phase in the molecular frame  $\phi_i^M$  can be unambiguously derived (see sketch). Such retrieval is not straightforwardly possible for linearly polarized pulses.

In our experiments, the laser field in the lab frame is  $\mathbf{E}(t) = f(t)[\hat{E}_z \cos(\omega t + \text{CEP})\mathbf{e}_z + \hat{E}_y \sin(\omega t + \text{CEP})\mathbf{e}_y],$ where the pulse envelope  $f(t)$  with a peak value of 1 had a

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FIG. 1. (a) Evolution of laser electric field vector  $\mathbf{E}(t)$  over time,  $\mathbf{E}(t_i)$  at ionization time  $t_i$  (derived from the electron momentum vector  $\mathbf{p}_e$ ), an example proton vector  $\mathbf{p}_{H^+}$  aligned under  $\beta$  to the z axis of the lab frame, the molecular frame ionization phase  $\phi_i^M$  and the lab frame ionization phase  $\phi_i^L = \omega t_i + CEP$ . (b) Measured proton momentum distribution in the lab frame, integrated over CEP and  $n_{\text{tot}}$ . The two *β* ranges of proton ejection selected for Figs. 2(a), 2(b) are indicated.  $p_{H^+,x}$ . The two  $\beta$  ranges of proton ejection selected for Figs. [2\(a\)](#page-3-0), [2\(b\)](#page-3-0) are indicated. (c) Molecular frame proton anisotropy  $\mathcal{A}_M$  as a function of  $\phi_i^M$  and proton kinetic energy  $E_k$ , integrated over the CEP. (d),(e) Measured difference of proton momentum distributions,  $\Delta M$ , for CEP = 30( $\pm$ 10)° (d) and CEP = 210( $\pm$ 10)° (e), as detailed in the text. Note the linear color scales in (b)–(e). (f) Potential energy curves of H<sub>2</sub> and H<sub>2</sub><sup>+</sup>, dissociation pathways  $n\omega$  for  $n = \{1, 2, 3\}$ , and schematic proton energy distributions for  $n = \{0, 1, 2, 3\}$ .

duration of 4.5 fs (FWHM in intensity), the ellipticity was  $\varepsilon = \hat{E}_{\rm v}/\hat{E}_{\rm z} = 0.85$  and the angular frequency  $\omega$  was given by the spectral center wavelength 750 nm. The peak intensity was 0.8 PW/cm<sup>2</sup> (measured in situ [\[25\]](#page-5-1)). The pulses were focused inside a reaction microscope (background pressure  $\langle 10^{-10} \text{ mbar} \rangle$  onto a supersonic beam of randomly oriented H<sub>2</sub> molecules. Duration and CEPs of the pulses were measured with a stereo electron spectrometer in phase-tagging mode [\[26,27\].](#page-5-2) The value of  $CEP = 0$  was calibrated to the maximum of the  $H_2^+$  yield into  $p_z > 0$ . Protons and electrons created by the laser-molecule interaction were guided to two position and time sensitive detectors by weak electric (20 V/cm) and magnetic fields (9 G) for measuring in coincidence their momenta right after the laser pulse. In the offline data analysis the dissociation channel was selected. Further experimental details can be found in Refs. [\[19](#page-4-6)–21].

The proton momentum distribution in the laser polarization plane,  $\mathcal{M}(p_{H^+,z}, p_{H^+,y})$ , integrated over the third momentum component  $p_{H^+x}$  and all values of the CEP, is shown in Fig. [1\(b\)](#page-1-0). Because the rotational motion of  $H_2^+$  is slow as compared to the dissociation process, the proton momentum  $\mathbf{p}_{H^+}$  encodes the instantaneous orientation of the  $H_2$  molecule before laser interaction [\[20,21\]](#page-4-7). As the molecules are isotropically oriented in the jet, the CEPintegrated momentum distribution reflects the laser intensity distribution of the elliptically polarized pulses and does not show any anisotropy along the radial direction with respect to the origin at any angle  $\beta$ .

To investigate the influence of the CEP on the directionality of the bond-breaking process, we calculated the difference between the proton momentum distributions measured for a given CEP,  $\mathcal{M}$ (CEP), and the CEP-integrated proton momentum distribution,  $M$ . The resulting difference momentum distributions  $\Delta \mathcal{M} = \mathcal{M}(\text{CEP}) - \mathcal{M}$  for CEP = 30° and CEP = 210° are plotted in Figs. [1\(d\)](#page-1-0), [1\(e\)](#page-1-0). The  $\Delta M$ distributions show a pronounced  $\beta$ -dependent antisymmetry about the origin along the radial direction for certain ranges of  $|\mathbf{p}_{H^+}|$  that flips if the CEP is changed by 180° (from 30° to 210°). These  $\Delta M$  distributions constitute, to our knowledge, the first demonstration of a CEP-dependent twodimensional (2D) proton anisotropy in  $H_2^+$  dissociation. Thus far, such 2D control was only demonstrated by the relative phase of 2D two-color laser fields [\[28,29\].](#page-5-3)

Our goal is to relate the CEP-induced anistropy of Figs. [1\(d\),](#page-1-0) [1\(e\)](#page-1-0) to that due to the ionization phase in the molecular frame,  $\phi_i^M$ , introduced by Ref. [\[18\].](#page-4-5) This anisotropy measured in our experiments is shown in Fig. [1\(c\).](#page-1-0) For this plot, we retrieved for each proton in the momentum distribution Fig. [1\(b\)](#page-1-0) the value of  $\beta$  from  $\mathbf{p}_{H^+}$ , and from the electron momentum vector  $\mathbf{p}_e$  we retrieved the lab frame angle  $\phi_i^L$  of the electric field vector  $\mathbf{E}(t_i)$  at ionization<br>time. From  $\phi^L$  and  $\beta$  we calculated for each detected proton time. From  $\phi_i^L$  and  $\beta$  we calculated for each detected proton the angle  $\phi_i^M = \phi_i^L - \beta$ , which is the ionization phase<br>with respect to  $\mathbf{p}_{i,j}$  (modulo  $2\pi$ ) [cf. Fig. 1(a)]. This with respect to  $\mathbf{p}_{H^+}$  (modulo  $2\pi$ ) [cf. Fig. [1\(a\)\]](#page-1-0). This allows to obtain the normalized proton anisotropy in the molecular frame,  $A_M$ . For direct comparability we used the same definition for  $A_M$  as Wu et al. [\[18\]](#page-4-5), namely,  $\mathcal{A}_M(\phi_i^M, E_k, \beta) = [N(\phi_i^M, E_k, \beta) - N(\phi_i^M + 180^\circ, E_k, \beta)]/N(\phi_i^M - E_k, \phi_k)$  $[N(\phi_i^M, E_k, \beta) + N(\phi_i^M + 180^\circ, E_k, \beta)]$ , with  $N(\phi_i^M, E_k, \beta)$ <br>the number of protons ejected along angle  $\beta$  for given values the number of protons ejected along angle  $\beta$  for given values of  $\phi_i^M$  and  $E_k = |\mathbf{p}_{\text{H}^+}|^2/(2m_p)$ , which is the proton kinetic<br>energy (with m the proton mass). This number is compared energy (with  $m<sub>p</sub>$  the proton mass). This number is compared to the number of protons ejected along the same angle  $\beta$  for the opposite ionization phase  $\phi_i^M \to \phi_i^M + 180^\circ$ . Because

 $\phi_i^M$  is defined in the molecular frame, the numbers N can be integrated over  $\beta$ . The resulting anisotropy, integrated over all values of the CEP, is shown in Fig.  $1(c)$ .

Both anisotropies,  $\Delta M$  in Figs. [1\(d\)](#page-1-0), [1\(e\)](#page-1-0) and  $\mathcal{A}_M$  in Fig. [1\(c\),](#page-1-0) are the results of interferences of nuclear wave packets dissociating along different pathways  $n\omega$  on the gerade  $1s\sigma_g$  and ungerade  $2p\sigma_u$  electronic states that are associated with the number of effectively absorbed photons,  $n = \{0, 1, 2, ...\}$  [\[30,31\]](#page-5-4), cf. sketch in Fig. [1\(f\)](#page-1-0). Electronic excitation by electron recollisions, relevant in other works [\[7,10,32\]](#page-4-3), is suppressed in elliptical light. Superposition of the wave packets with a relative phase  $\Delta \varphi$ acquired during pathways associated with odd and even  $n$ dictates the localization of the remaining electron in the dissociating  $H_2^+$  molecule. In turn, the anisotropy of proton ejection A depends on the *n*-dependent kinetic energy  $E_k$ and on  $\Delta\varphi$  according to  $\mathcal{A} \propto \sin(\Delta\varphi)$ . See Supplemental Material [\[33\]](#page-5-5) for an extended description.

Figure [1\(c\)](#page-1-0) shows that for  $E_k > 0.7$  eV in our experiment  $A_M < 0$  for  $0^\circ < \phi_i^M < 180^\circ$ , and  $A_M > 0$ for  $180^{\circ} < \phi_i^M < 360^{\circ}$ . This means that the proton is much more likely ejected against the electron emission direction, i.e.,  $\mathbf{p}_e \cdot \mathbf{p}_{\mathrm{H}^+} < 0$ , than with the electron, independent of the alignment of the molecule in the lab frame. That holds for all values of the CEP, see Supplemental Material [\[33\]](#page-5-5). For  $0.4 < E_k < 0.7$  eV the situation is inverted and the proton is more likely ejected into the same hemisphere as the electron. Our experimental anisotropy for a few-cycle pulse is only qualitatively similar to that of Ref. [\[18\]](#page-4-5) for a multicycle pulse. On a quantitative level we measure much higher values of  $|\mathcal{A}_M|$  (by about a factor of 6) due to the larger intensity and the shorter pulse duration [\[20,21,43,44\]](#page-4-7) in our experiment, and almost no dependence of  $A_M$  on  $E_k$ for  $E_k > 0.7$  eV. The latter we attribute to the much broader spectrum of our laser pulse, which enables transitions between the  $1s\sigma_q$  and  $2p\sigma_u$  states over a much broader range of internuclear distances  $R$  [cf. Fig. [1\(f\)\]](#page-1-0) resulting in averaging over a broader range of  $E_k$ .

The result in Fig. [1\(c\)](#page-1-0), that the ejection direction of a proton with a given  $E_k$  is determined to a large degree only by the direction of electron emission, implies a strong correlation between the outgoing electron and the ejected proton. This correlation is mediated by the laser-sub-cycle intramolecular dynamics of the bound electron. In turn, it may provide experimental access to this dynamics, see Supplemental Material [\[33\]](#page-5-5) for details. Within the abovementioned semiclassical picture of pathway interferences the correlation can be explained as follows. For a given  $E_k$ and photon energy  $\omega$ , the delay  $\Delta t = t_T - t_i$  between ionization time  $t_i$  and the times of transition(s) between the two states at  $t_T = t_{n\omega}$  [cf. Fig. [1\(f\)\]](#page-1-0) is constant for a specific *n* [\[45\].](#page-5-6) In turn, for a given  $t_i$  also the quantum phase difference  $\Delta \varphi(t_i)$  between two pathways with *n* and  $n + 1$  is constant. Therefore, since  $\phi_i^M \propto t_i$ ,  $\sin(\Delta \phi)$  will<br>invert its sign for  $\phi^M \rightarrow \phi^M + 180^\circ$  which entails a change invert its sign for  $\phi_i^M \to \phi_i^M + 180^\circ$ , which entails a change of the anisotropy  $A_M \rightarrow -A_M$ . Thus, for a given photon energy  $\omega$ , the dependence of the proton anisotropy  $\mathcal{A}_M$  on  $\phi_i^M$  is an *intrinsic* property of  $H_2^+$  determined by its potential energy structure.

Even though the high values of the intrinsic anisotropy  $\mathcal{A}_{M}(\phi_{i}^{M}, E_{k})$  in Fig. [1\(c\)](#page-1-0) suggest a promising handle for directional control over the bond-breaking process using the directional control over the bond-breaking process using the phase  $\phi_i^M$ , the anisotropy only appears in the molecular frame and cannot be exploited for lab frame control: The anisotropy changes sign for  $\phi_i^M \rightarrow \phi_i^M + 180^\circ$ . Thus, in a randomly oriented ensemble of symmetric molecules for every proton oriented ensemble of symmetric molecules, for every proton ejection angle  $\beta$  there exists an angle  $\beta' = \beta + 180^{\circ}$  for which the same number of protons are ejected into the opposite direction. As a result, the anisotropy in the molecular frame described in Ref. [\[18\]](#page-4-5) and depicted in Fig. [1\(c\)](#page-1-0) vanishes for integration over  $\phi_i^M$ . Moreover, the quantity  $\phi_i^M$ is accessible only in electron-ion coincidence experiments and can only be measured but not controlled in an experiment. Only a lab frame quantity that can be adjusted using an experimental knob, such as the CEP, can be used for bondbreaking control in the lab frame.

Still, the fact that the proton ejection direction is to a large degree determined by the ionization step, actually questions the role of the CEP-determined laser field's shape during the laser-molecule interaction. To clarify this question, we turn to investigating the connection between the molecular frame anisotropy  $\mathcal{A}_M$ , shown in Fig. [1\(c\),](#page-1-0) and the CEP-dependent lab frame anisotropy, shown in Figs. [1\(d\)](#page-1-0), [1\(e\).](#page-1-0) For this, we first need to connect the molecular frame with the lab frame. To see this connection, we calculate the laser electric field along the molecular axis:  $E_{\text{mol}}(t, \text{CEP}, \beta) =$  $\hat{E}_z f(t) \sqrt{\cos^2 \beta + \epsilon^2 \sin^2 \beta} \cos(\omega t + \text{CEP} - \beta_{\text{eff}})$  with  $\beta_{\text{eff}} =$ <br>ton<sup>-1</sup>(c ton <sup>β</sup>), where c is the pulse ellipticity defined  $\tan^{-1}(\varepsilon \tan \beta)$ , where  $\varepsilon$  is the pulse ellipticity defined above. This relation tells us that for a given ionization time  $t_i$ , the alignment angle  $\beta$  and the CEP lead to equivalent changes of the molecular frame ionization phase  $\phi_i^M = \omega t + C \text{FP} - \beta \approx$  $\omega t_i + \text{CEP} - \beta_{\text{eff}}.$ 

As  $\beta$  and CEP are both lab frame quantities, they connect the molecular frame phase  $\phi_i^M$  with the lab frame. To establish this connection, we turn to the normalized lab frame proton anisotropy,  $A_L$ (CEP,  $E_k$ ,  $\beta$ ), which we define in accordance with  $\Delta M$  in Figs. [1\(d\),](#page-1-0)1(e). After transformation from the Cartesian  $(p_{H^+,z}, p_{H^+,y})$  to the polar coordinates  $(E_k, \beta)$  we obtain  $\mathcal{A}_L$ (CEP,  $E_k$ ,  $\beta$ ) =  $\left[\Delta \mathcal{M}(\text{CEP}, E_k, \beta) - \Delta \mathcal{M}(\text{CEP}, E_k, \beta + 180^\circ) \right] / \left[\mathcal{M}(\text{CEP}, E_k, \beta + \mathcal{M}(\text{CEP}, E_k, \beta + 180^\circ)) \right]$  $[\mathcal{M}(CEP, E_k, \beta) + \mathcal{M}(CEP, E_k, \beta + 180^\circ)].$  The such defined anisotropy is shown in Figs. 2(a) 2(b) for defined anisotropy is shown in Figs. [2\(a\)](#page-3-0), [2\(b\)](#page-3-0) for  $\beta = 0$  and  $\beta = 40^{\circ}$ . Figure [2\(c\)](#page-3-0) shows the anisotropy obtained by integrating over the low and high  $E_k$  regions for which  $A_L$ (CEP,  $E_k$ ,  $\beta$ ) shows opposite CEP dependence. In both  $E_k$  regions, a rotation of the molecule by  $\beta = 40^{\circ}$  results with  $\varepsilon = 0.85$  in a CEP shift of  $\beta_{\text{eff}} =$  $\tan^{-1}[0.85 \tan(40^\circ)] \approx 36^\circ$ , proving the equivalence of  $\beta$ <br>and CEP and CEP.

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FIG. 2. (a), (b) Lab frame anisotropy  $A_L$ (CEP,  $E_k$ ) for proton ejection under  $\beta = 0(\pm 10)^\circ$  (a) and  $\beta = 40(\pm 10)^\circ$  (b). (c)  $A_t$ ejection under  $\beta = 0(\pm 10)^\circ$  (a) and  $\beta = 40(\pm 10)^\circ$  (b). (c)  $\mathcal{A}_L$ <br>over CEP for  $\beta = 0^\circ$  (green) and  $\beta = 40^\circ$  (red), plotted for  $F \to \infty$ over CEP for  $\beta = 0^{\circ}$  (green) and  $\beta = 40^{\circ}$  (red), plotted for  $E_k > 1.5 \text{ eV}$  (full lines) and  $0.6 < E_k < 1.5 \text{ eV}$  (dashed lines)  $\beta_{\alpha} \approx$ 1.5 eV (full lines) and  $0.6 < E_k < 1.5$  eV (dashed lines).  $\beta_{\text{eff}} \approx$ 36° is indicated.

To connect the molecular and lab frame anisotropies  $A_M$ and  $A_L$  we need to use a lab frame counterpart of  $\phi_i^M$ , the phase defining the direction of  $E(t_i)$  in the molecular frame. From Fig. [1\(a\)](#page-1-0) we find the angle of  $\mathbf{E}(t_i)$  in the lab frame as  $\phi_i^L = \phi_i^M + \beta_{\text{eff}} = \omega t_i + \text{CEP}$ . Because of the equivalence of  $\beta = \beta(\beta_{\text{eq}})$  and CEP established in Fig. 2 in equivalence of  $\beta = \beta(\beta_{\text{eff}})$  and CEP established in Fig. [2](#page-3-0), in order to make explicit the influence of the CEP and not to smear out its action, we need to fix the value of  $\beta$ . If  $\beta$  is random, the influence of the CEP in the proton anisotropy gets suppressed. Without loosing generality, we set  $\beta = 0^{\circ}$ , for which the connection between  $\phi_L^L$ <br>and  $\phi_M^M$  becomes particularly simple pamely  $\phi_L^L$ and  $\phi_i^M$  becomes particularly simple, namely  $\phi_i^L$  $\phi_i^M|_{\beta=0}$ . With that, we can straightforwardly adopt the<br>definition of A and obtain  $A \stackrel{\beta=0}{\rightarrow} (AL \stackrel{\frown}{\rightarrow} E)$ definition of  $\mathcal{A}_M$  and obtain  $\mathcal{A}_L^{ \beta=0}(\phi_i^L, \text{CEP}, E_k) =$ <br> $[N(\mathcal{A}^L, \text{CEP}, E_k, \theta = 0) = N(\mathcal{A}^L, \text{CEP}, E_k, \theta = 180^\circ) ]/$  $[N(\phi_i^L, \text{CEP}, E_k, \beta = 0) - N(\phi_i^L, \text{CEP}, E_k, \beta = 180^\circ)]/$ <br> $[N(\phi_i^L, \text{CEP}, E_k, \beta = 0) + N(\phi_i^L, \text{CEP}, E_k, \beta = 180^\circ)]$  $[N(\phi_i^L, \text{CEP}, E_k, \beta = 0) + N(\phi_i^L, \text{CEP}, E_k, \beta = 180^\circ)],$ <br>where we have made explicit the dependence of  $A^{-\beta=0}$ where we have made explicit the dependence of  $A_L^{\beta=0}$  on the CEP. The anisotropy  $A_L^{\beta=0}$  is an equivalent but generalized form of the anisotropy  $A_M$  defined above. We can see this equivalence if we replace  $\phi_i^M \rightarrow \phi_i^L - \beta$  in  $\mathcal{A}_M(\phi_i^M, E_k)$ . For  $\beta = 0$  this is exactly the definition of  $A \stackrel{\beta=0}{\beta=0}$  but with the additional dependence on CEP  $A_L^{\beta=0}$ , but with the additional dependence on CEP. So  $\frac{1}{2}$  or  $\frac{1}{2}$ 

We plot the measured  $A_L^{\beta=0}(\phi_i^L, \text{CEP}, E_k)$ , integrated<br>er CEP in Eig. 3(a) It closely resembles  $A_L(\phi_i^M, E_L)$  that over CEP, in Fig. [3\(a\).](#page-3-1) It closely resembles  $A_M(\phi_i^M, E_k)$  that is integrated over all angles  $\beta$ , shown in Fig. 1(c). Its lab is integrated over all angles  $\beta$ , shown in Fig. [1\(c\)](#page-1-0). Its lab frame counterpart for  $\beta = 0$ ,  $A_L^{\beta=0}(\phi_i^L, \text{CEP}, E_k)$ , finally<br>enables us to investigate the separate actions of the ionizaenables us to investigate the separate actions of the ionization phase  $\phi_i^L$  and the CEP as well as their connection. To this end, we plot  $A_L^{\beta=0}(\phi_i^L, \text{CEP}, E_k)$  in Figs. [3\(b\)](#page-3-1), [3\(c\)](#page-3-1), separated into high and low proton energy ranges that show separated into high and low proton energy ranges that show opposite CEP dependence. The two energy ranges clearly visible in Figs. [2\(a\),](#page-3-0) [2\(b\)](#page-3-0) correspond to the overlap of the  $1\omega$ and  $2\omega$ , and the  $2\omega$  and  $3\omega$  pathways, respectively. The larger peak value of  $A_L$  for  $\beta = 40^\circ$  in Fig. [2](#page-3-0) is attributed to a more favorable population ratio of the interfering dissociation pathways for this angle, due to the  $\beta$  dependence of the intensity along the molecular axis  $|E_{\text{mol}}|^2$ . The distributions<br>in Figs. 3(b), 3(c) show that in both energy regions  $d^L$ in Figs. [3\(b\),](#page-3-1) [3\(c\)](#page-3-1) show that in both energy regions  $\phi_i^L$ has a dominant influence on the proton ejection direction. However, the CEP modulates the value of  $A_L^{\beta=0}$ , evident from its variation along the CEP axis and the corresponding cuts along  $\phi_i^L$  for selected values of the CEP in Figs. [3\(d\)](#page-3-1), [3\(e\).](#page-3-1) In these lineouts the CEP-induced offsets in  $A_L^{\beta=0}(\phi_i^L)$  are clearly visible.<br>Thus the action of the

Thus, the action of the CEP for determining the proton anisotropy is a modulation of the intrinsic anisotropy due to the ionization phase  $\phi_i^L$ . To elucidate the mechanism behind this CEP modulation we developed a simple semiclassical model that calculates the anisotropy-determining phase difference  $\Delta \varphi$  acquired by a vibrational wave packet along the different dissociating pathways. For a qualitative assessment of the physics underlying the measured  $A_L^{\beta=0}(\phi_i^L, CEP, E_k)$  we restricted our model to the low<br>proton energy region where only the Lo and 20 pathways proton energy region where only the  $1\omega$  and  $2\omega$  pathways interfere, see Supplemental Material [\[33\]](#page-5-5) for details. The anisotropy map  $A_L^{p=0}(\phi_i^L, \text{CEP}, E_k)$  predicted by this model,<br>displayed in Fig. 3(f), as well as the lineouts for selected values displayed in Fig. [3\(f\)](#page-3-1), as well as the lineouts for selected values of the CEP, shown in Fig.  $3(g)$ , resemble the measured quantities in Figs. [3\(b\)](#page-3-1) and [3\(d\)](#page-3-1) to a remarkable degree.

<span id="page-3-1"></span>

FIG. 3. (a) Measured proton ejection anisotropy  $A_L^{\beta=0}$  as defined in the text, over the laser phase at ionization time  $\phi_i^L$  and proton kinetic energy  $E_k$ , integrated over the CEP. (b),(c)  $A_L^{\beta=0}$  over  $\phi_i^L$  and CEP for  $0.6 < E_k < 1.5$  eV (b) and  $E_k > 1.5$  eV (c). (d) Lineouts from (b) for three values of the CEP: 30° (red), 120° (green), 240° (blue). (e) Same as (d) with same color code but lineouts from (c). (f) Simulated  $A_L^{\beta=0}$  for  $E_k = 1$  eV corresponding to (b). (g) Lineouts from (f), description as in (d). (h) Evolution of the laser electric field vectors at an example field vector  $\mathbf{E}(t)$  in the lab frame for CEP = 50° (red, full) and CEP = 230° (green, dashed). The laser field vectors at an example transition time  $t_T = t_i + \Delta t$ ,  $\mathbf{E}_T = \mathbf{E}(t_T)$ , are indicated for both field forms

This good agreement, despite the dedicated qualitative character of the model, is due to the correct incorporation of the key mechanism underlying the influence of the CEP on the anisotropy, which is the pronounced variation of the electric field strength with CEP at the times when the  $1s\sigma_g$ and  $2p\sigma_u$  states are coupled by N-photon transitions; see Supplemental Material [\[33\]](#page-5-5) for details. In short, the transition probability  $P$  between the two electronic states is proportional to the field strength along the molecular axis at transition time  $t_T$ , according to  $P \propto |E_{\text{mol}}(t_T)|^{2N}$ . Thus, the CEP variation of the transition probability  $P$ , and therewith that of the anisotropy-determining phase difference  $\Delta \varphi$ , is determined by the CEP modulation of  $E_{\text{mol}}(t_T)$ , cf. the visualization of this field-variation with CEP in Fig. [3\(h\).](#page-3-1) Since the CEP variation of  $E_{\text{mol}}(t_T)$  decreases with the number of cycles in the pulse, the modulation of the proton anisotropy with the CEP, visible in Figs. [3\(d\)](#page-3-1), [3\(e\),](#page-3-1) [3\(g\),](#page-3-1) vanishes for a multicycle pulse. As a result, for a multicycle pulse only the dependence of the anisotropy on the ionization phase  $\phi_i^M$ , which can only be detected in a coincidence experiment, remains.

In conclusion, we investigated the phase sensitivity of bond breaking in dissociative laser ionization of  $H_2$ . We establish a unified picture that relates the well-known CEP dependence of the proton anisotropy in the lab frame measured with few-cycle pulses [7–[14\]](#page-4-3) to an intrinsic proton anisotropy that depends on the laser phase at ionization time. Our work shows that the former anisotropy arises due to a CEP modulation of the latter via the CEP dependence of the transition amplitudes between interfering nuclear pathways. Our experiments also reveal a remarkably strong correlation between the outgoing electron and the ejected proton that is directly connected to the intramolecular electron dynamics during dissociation. We predict that this correlation opens up a new approach to access the laser-sub-cycle electronic dynamics during molecular bond breaking; see Supplemental Material [\[33\]](#page-5-5) for a detailed reasoning.

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