

Sound Propagation and Quantum-Limited Damping in a Two-Dimensional Fermi Gas

Markus Bohlen^{1,2,3}, Lennart Sobirey¹, Niclas Luick¹, Hauke Biss^{1,2}, Tilman Enss^{1,4},
 Thomas Lompe^{1,*} and Henning Moritz^{1,2}

¹*Institut für Laserphysik, Universität Hamburg, Luruper Chaussee 149, Hamburg 22761, Germany*

²*The Hamburg Centre for Ultrafast Imaging, Universität Hamburg, Luruper Chaussee 149, Hamburg 22761, Germany*

³*Laboratoire Kastler Brossel, ENS-Université PSL, CNRS, Sorbonne Université,
 Collège de France, 24 rue Lhomond, Paris 75005, France*

⁴*Intitut für Theoretische Physik, Universität Heidelberg, Philosophenweg 19, Heidelberg 69120, Germany*

 (Received 9 March 2020; revised manuscript received 26 April 2020; accepted 22 May 2020; published 16 June 2020)

Strongly interacting two-dimensional Fermi systems are one of the great remaining challenges in many-body physics due to the interplay of strong local correlations and enhanced long-range fluctuations. Here, we probe the thermodynamic and transport properties of a 2D Fermi gas across the BEC-BCS crossover by studying the propagation and damping of sound modes. We excite particle currents by imprinting a phase step onto homogeneous Fermi gases trapped in a box potential and extract the speed of sound from the frequency of the resulting density oscillations. We measure the speed of sound across the BEC-BCS crossover and compare the resulting dynamic measurement of the equation of state both to a static measurement based on recording density profiles and to quantum Monte Carlo calculations and find reasonable agreement between all three. We also measure the damping of the sound mode, which is determined by the shear and bulk viscosities as well as the thermal conductivity of the gas. We find that the damping is minimal in the strongly interacting regime and the diffusivity approaches the universal quantum bound \hbar/m of a perfect fluid.

DOI: [10.1103/PhysRevLett.124.240403](https://doi.org/10.1103/PhysRevLett.124.240403)

Strongly interacting fermionic systems appear in many different areas of physics, yet understanding their behavior remains challenging. A powerful experimental method to gain access to their thermodynamic and transport properties is to study collective excitations such as sound modes. The speed of sound is determined by the compressibility of the medium, giving access to its equation of state. The damping of sound modes in the hydrodynamic regime is caused by the diffusion of heat as well as longitudinal and transverse momentum, and thus depends on the transport coefficients of the medium, i.e., thermal conductivity, bulk, and shear viscosity. In hydrodynamic systems which support well-defined quasiparticle excitations such as fermionic quasiparticles in a normal Fermi liquid or phonon excitations in a superfluid, kinetic theory predicts that the damping rate is proportional to the quasiparticle lifetimes. Long-lived quasiparticles can transport heat or momentum over long distances and therefore smooth out density and pressure variations very efficiently, leading to strong attenuation of sound waves. In contrast, no well-defined quasiparticles

exist in the strongly correlated regime. Here, particles scatter with a mean free path comparable to the average interparticle spacing, leading to lower diffusivities and hence lower damping rates. A lower bound for the diffusivities $D \gtrsim \hbar/m$ and thus quantum-limited transport has been predicted and observed in several transport channels, including shear viscosity in ultracold 2D [1–4] and 3D [5–7] Fermi gases as well as spin diffusion in 2D [2,4,8,9] and 3D Fermi gases [10–14]. In measurements of sound propagation, this limit was observed in the sound diffusion of a unitary 3D Fermi gas [15].

Several hypotheses have been brought forward to provide an explanation for quantum-limited transport [16]: one, motivated by holographic duality [17], is that it occurs near scale invariant points in the phase diagram. The unitary 3D Fermi gas is an example that seems to support this hypothesis since it is strongly interacting as well as scale invariant and exhibits quantum-limited shear and spin diffusion. In contrast, 2D Fermi gases exhibit a quantum scale anomaly that breaks scale invariance [18–21]. Here, we investigate the propagation and damping of sound in a strongly interacting 2D Fermi gas and thereby probe a crucial test case for this hypothesis. We observe that the damping approaches the quantum limit $D \approx \hbar/m$ in the strongly interacting regime, where scale invariance is most dramatically violated, showing that scale invariance or quantum criticality is in fact not required for quantum-limited transport. Similar observations

Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI.

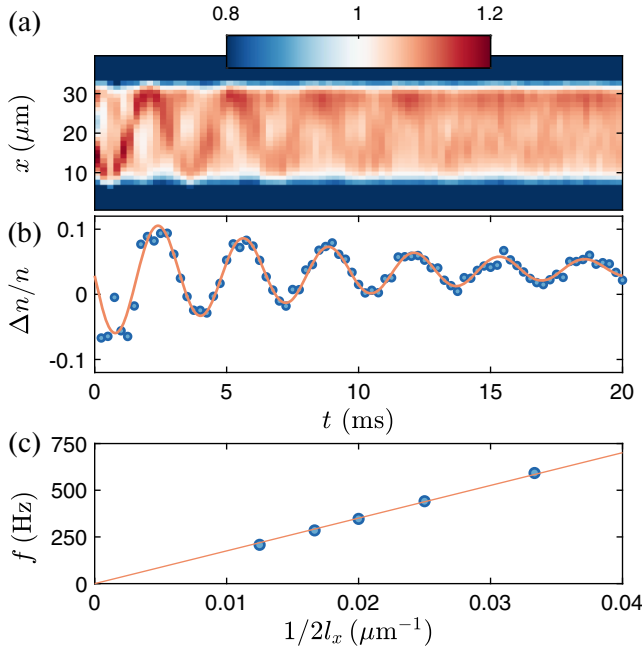


FIG. 1. Propagation of a sound wave in a box potential: (a) Density profiles $n(x, t)/n(t)$ averaged along the direction perpendicular to the sound propagation and normalized to the average density $n(t)$ within the box. A density wave propagating through the box is visible. Each profile $n(x, t)/n(t)$ is the average of 120 individual realizations. Note that the color scale has been chosen to enhance the visibility of the sound wave. (b) Relative density imbalance between the two sides of the box for the same data set. The solid line shows a damped sinusoidal fit to the data. (c) Frequency of the density oscillation as a function of the inverse box length. The slope of the linear fit (solid line) corresponds to the speed of sound. In (b) and (c), the statistical errors are smaller than the marker size. Each data point in (c) is the average of 23 realizations.

were made for transverse spin diffusion in [9]. Our results confirm a scenario of incoherent transport that has emerged in recent years from the study of anomalous transport in high-temperature superconductors and other “bad metals” [22–24] and links quantum-limited transport to strong correlations.

We perform our studies of sound propagation with an ultracold gas of ${}^6\text{Li}$ atoms in a spin-balanced mixture of the lowest two hyperfine states, trapped in a two-dimensional box potential [25,26]. The gas is vertically confined in a single node of a repulsive optical lattice with trap frequency $\omega_z/2\pi = 8.4(3)$ kHz. At our densities of about $n_{\uparrow/\downarrow} \equiv n \approx 1 \mu\text{m}^{-2}$ per spin state, the chemical potential μ is smaller than the vertical level spacing $\hbar\omega_z$, which ensures that our gas is in the quasi-2D regime. The confinement in the horizontal plane is created using a digital micromirror device illuminated with blue detuned light ($\lambda = 532$ nm), trapping the gas in a two-dimensional box with a typical size of $l_x \times l_y = 30 \times 40 \mu\text{m}^2$. According to the temperature determination performed in [26], our system is

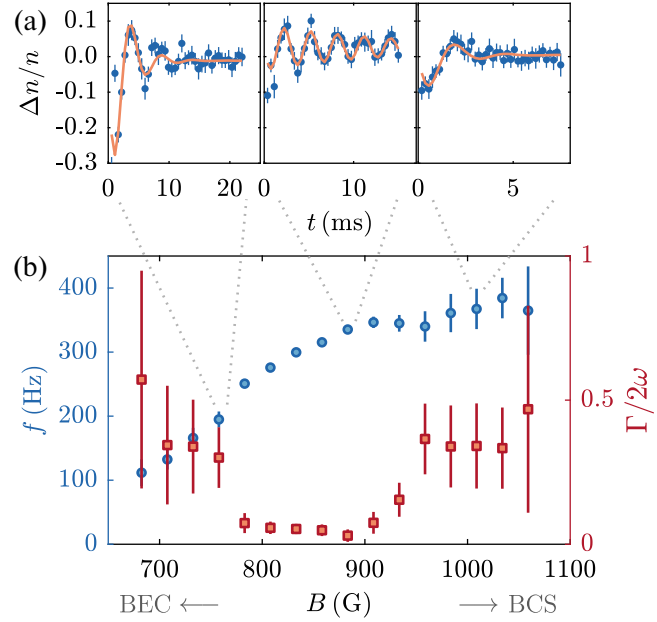


FIG. 2. (a) Oscillations in the density imbalance at $B = 758$ G, $B = 883$ G, and $B = 1009$ G. Solid lines represent damped sinusoidal fits. (b) Frequency (blue circles) and damping (red squares) of sound oscillations as a function of magnetic field. The frequency increases smoothly from the BEC to the BCS side and starts to saturate at high magnetic fields. The damping shows a clear minimum in the strongly interacting regime and increases strongly towards either side. Each data point is the average of 39 realizations.

in the low-temperature regime with $k_B T/E_F \leq 0.1$, where $E_F = \hbar^2 k_F^2/2m$ is the Fermi energy, $k_F = (4\pi n)^{1/2}$ the Fermi momentum and m the atomic mass of ${}^6\text{Li}$.

For our experiments, we build on the experimental procedure developed in [27], where sound propagation was studied in weakly interacting 2D Bose gases. To excite a sound mode in the box we follow the approach of [26] and imprint a relative phase between two halves of the system by illuminating one side with a spatially homogeneous optical potential for a short duration $\tau < \hbar/E_F$. We then observe the resulting density oscillations by imaging the density distribution after different hold times using *in situ* absorption imaging. An example of such an oscillation is shown in Fig. 1(a). A sound wave traveling back and forth between the two sides of the box is clearly visible in the density profile. To extract the oscillation frequency $f = \omega/2\pi$ and the damping rate Γ of this sound wave, we calculate the relative particle imbalance $\Delta n/n = 2(n_t - n_b)/(n_t + n_b)$ from the densities n_t and n_b in the top and bottom halves of the box and fit it with a damped sinusoidal of the form $A(t) = A_0 \cos(\omega t + \phi) \exp(-\Gamma t/2) + b$ [see Fig. 1(b)] [28]. We measure the oscillation frequency for different boxes with lengths between $l_x = 15 \mu\text{m}$ and $l_x = 40 \mu\text{m}$ and find that it is proportional to the inverse of the box length

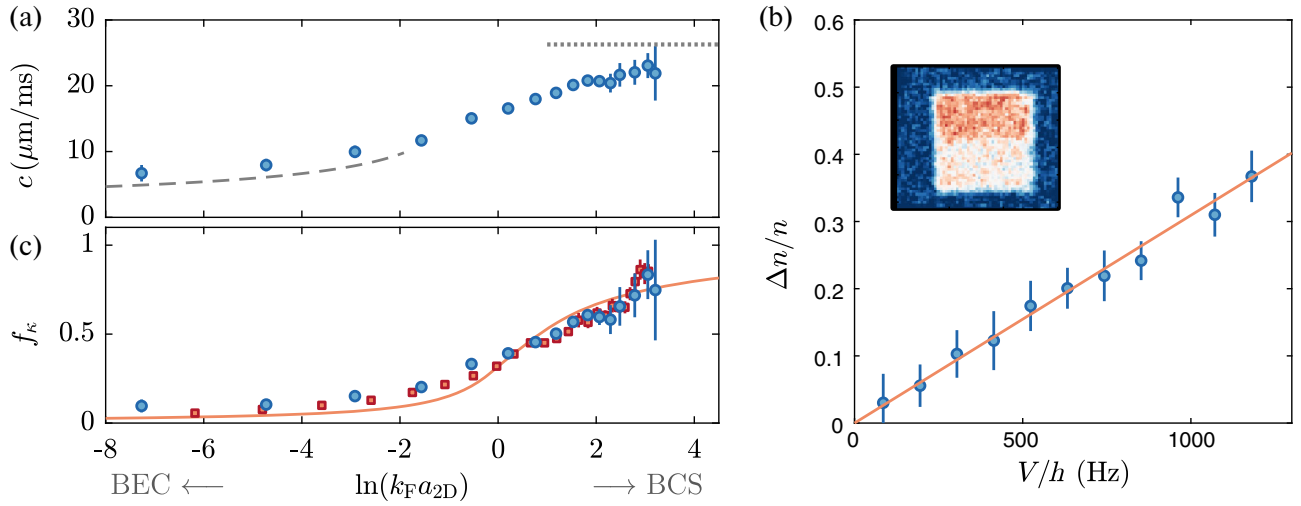


FIG. 3. (a) Speed of sound across the BEC-BCS crossover. Gray lines represent the two theoretical limits: in the BEC regime, Bogoliubov theory predicts $\mu = gn$ and hence $c_B = (gn/2m)^{1/2}$, where g is the interaction parameter between bound dimers defined as in [26,36]. On the BCS side, $\mu \rightarrow E_F$ yields a constant sound velocity $c_F = v_F/\sqrt{2}$ where $v_F = \hbar k_F/m$ is the Fermi velocity. (b) Static measurement of the compressibility. A repulsive potential V is imprinted onto one half of the box resulting in a density imbalance $\Delta n/n$ (blue points). We extract the compressibility from the initial slope of the data points according to $1/n^2\kappa = \lim_{\Delta n \rightarrow 0} V/\Delta n$ in a local density approximation. Each data point and the inset are averages of 20 realizations. (c) Comparison between the compressibility scaling functions f_κ obtained from the speed of sound (blue circles), the density response to an imprinted static potential (red squares) and QMC calculations [37,38].

[see Fig. 1(c)]. This confirms that we observe a sound wave traveling at a constant velocity $c = 2l_x f$ and that edge effects are negligible.

To probe the speed of sound as a function of interaction strength, we perform measurements in a box with $l_x = 30 \mu\text{m}$ at magnetic fields around the Feshbach resonance. Examples of the resulting oscillations as well as the evolution of the oscillation frequency as a function of magnetic field are shown in Fig. 2. As the field is varied from the BEC side to the BCS side of the crossover, the oscillation frequency increases, which is expected since the compressibility of a Fermi gas is much lower than that of a weakly repulsive Bose gas. On the Fermi side, the gas is thus stiffer with respect to density fluctuations and sound waves propagate faster than on the Bose side.

We plot the speed of sound extracted from the oscillation frequencies as a function of the 2D interaction parameter $\ln(k_F a_{2D})$ [29] in Fig. 3(a). In a superfluid gas, two-fluid hydrodynamics predict the occurrence of two sound modes which propagate at different velocities, as observed in [32]. These modes generally mix density and entropy degrees of freedom. For strongly interacting 2D superfluids however, density and entropy excitations have been predicted to be well decoupled [33,34], and hence the sound mode we observe should correspond to an almost pure density wave. In this case, the velocity of a sound wave is given by

$$c = \sqrt{\left. \frac{n}{m} \frac{\partial \mu}{\partial n} \right|_s} \quad (1)$$

and is directly related to the isentropic compressibility $\kappa = (1/n^2)(\partial n/\partial \mu)|_s$ [35]. This relation gives us simple zero-temperature expressions for the speed of sound in the BEC and BCS limits of the crossover, which are in good agreement with our data [dashed and dotted lines in Fig. 3(a)].

For a quantitative analysis we use Eq. (1) to extract the compressibility of our gas from our measurement of the speed of sound. From this, we then determine the dimensionless inverse compressibility scaling function $f_\kappa = 1/nE_F\kappa$ of a two-dimensional Fermi gas.

In addition to this dynamic measurement of the equation of state (EOS), we also perform a static measurement of the compressibility EOS by determining the density response of our system to a static repulsive potential, similar to the work performed in [25,31,39,40] [see Fig. 3(b)]. This results in two independent measurements of f_κ , which show good agreement with each other [see Fig. 3(c)].

Finally we compare our data to theory by extracting f_κ from quantum Monte Carlo (QMC) calculations of the ground state energy E_0 of a homogeneous 2D Fermi gas [37,38]. On the BCS side, the experimental results agree well with the theoretical prediction. On the BEC side, both the static and the dynamic measurements lie above the zero-temperature prediction. This difference is consistent with the predicted increase of the sound velocity at finite temperature [41] and with a corresponding decrease of the compressibility at finite temperature observed in [31], which increases the value of f_κ .

Very recent simulations of the sound velocity in a 2D Bose gas [42] indicate that the density and entropy modes remain coupled even for relatively strongly interacting Bose gases, leading to sound velocities which differ from the Bogoliubov prediction. This should be observable as a difference between the static and dynamic measurements of the compressibility. However, if such a difference exists in our system, it is smaller than the uncertainty of our measurement.

We now turn our attention to the damping of the sound waves. In our strongly correlated system, the mean free path l_{mfp} of the particles is much smaller than the oscillation wavelength and their collision rate is high with respect to the oscillation frequency [43]. Hence the system is in the hydrodynamic regime. In this regime, the spatial variations in density and temperature that constitute a sound wave lead to diffusive currents of longitudinal momentum, transverse momentum and heat, whose magnitudes are proportional to the bulk and shear viscosities ζ and η and to the heat conductivity β [44,45]. These diffusive currents smooth out the density and temperature variations and thus damp the sound wave according to the sound diffusion constant

$$D_s = \frac{\eta}{\rho} + \frac{\zeta}{\rho} + \beta \frac{c_p - c_v}{c_p c_v} = \Gamma/k_0^2, \quad (2)$$

where $k_0 = \pi/l_x$ is the wave vector of the sound wave and c_p and c_v are the heat capacities at constant pressure and volume. The evolution of D_s across the BEC-BCS crossover is shown in Fig. 4. It exhibits a broad minimum in the crossover regime $-1 < \ln(k_F a_{2D}) < 2$ and increases steeply towards the BEC and BCS limits.

Before comparing our data to theory, we note that making quantitative predictions for transport coefficients of strongly interacting 2D Fermi gases in the low-temperature regime is still a major theoretical challenge. Approaches such as Fermi liquid theory and BCS theory [45] are only accurate at weak coupling. Results obtained for the high-temperature regime ($T \geq T_F$) indicate that the shear viscosity and heat conductivity have a minimum in the strongly correlated regime [2–4] whereas the bulk viscosity is maximal near resonance yet contributes much less to the damping [46–48]. In total, high-temperature theory predicts a minimum of the sound diffusion in the crossover regime. Although our measurements are performed in the low-temperature regime, the observed behavior is in qualitative agreement with an extrapolation of the high-temperature result to the low-temperature regime.

A prediction for a lower bound of D_s in the strongly interacting regime can be obtained via a simple scaling argument: in kinetic theory, the diffusion coefficient is given by the mean free path and the velocity via $D_s \sim v l_{\text{mfp}}$. For a strongly interacting degenerate gas the mean free path l_{mfp} is on the order of the interparticle separation $n^{-1/2}$

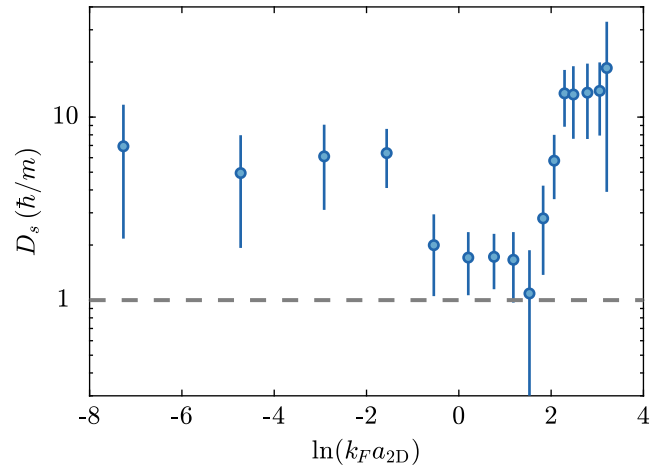


FIG. 4. Sound diffusion coefficient across the BEC-BCS crossover. In the strongly correlated regime, the diffusion coefficient reaches a minimum which agrees well with the universal quantum bound for diffusion at \hbar/m (dashed line).

and the velocity on the order of the Fermi velocity $v \sim v_F \sim \hbar n^{1/2}/m$, resulting in a diffusion coefficient $D_s \sim \hbar/m$. Since the interparticle separation is a lower limit for the mean free path, this yields a generic lower bound for the damping. This lower limit is in agreement with our measured diffusion coefficient of $D_s \approx 1.8(2)\hbar/m$ in the strongly correlated regime. Thus our strongly interacting 2D Fermi gas is a nearly perfect fluid despite the fact that scale invariance is broken and that the system is not at a quantum critical point.

In this Letter, we have studied the propagation and damping of sound waves in a homogeneous 2D Fermi gas across the BEC-BCS crossover. We have extracted the compressibility EOS from a measurement of the speed of sound and find good agreement with $T = 0$ QMC calculations. We have measured the sound diffusion constant as a function of the interaction strength and find universal sound diffusion $D_s \sim \hbar/m$ and quantum-limited transport in the strongly interacting regime. This lower limit is reached at interactions where scale invariance is violated most severely [9,21], but where the mean free path is comparable to the particle spacing. Since sound diffusion is the sum of momentum and heat diffusion, we thus find upper bounds of order \hbar/m on each diffusion channel individually in the crossover regime. This demonstrates that the 2D Fermi gas realizes a nearly perfect fluid [17,49] and provides a benchmark against which future theoretical predictions can be validated.

An interesting extension of our measurements would be to study the temperature dependence of D_s as done in unitary 3D Fermi gases [15]. In the fermionic regime, this would allow us to observe whether there is a maximum of D_s at the critical temperature of superfluidity, similar to measurements in ^3He [50]. In the deep BEC regime, control

over the temperature of the gas would enable studies of second sound in a strongly interacting Bose gas [34,42].

We thank L. Mathey, V. Singh, A. Sinatra, Y. Castin, and N. Defenu for stimulating discussions. We also thank K. Morgener, K. Hueck, and W. Weimer for their work in the early stages of the experiment. This work is supported by the European Union's Seventh Framework Programme (Grant No. FP7/2007-2013) under Grant Agreement No. 335431 and by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) in the framework of SFB 925 and "SFB 1225" (ISOQUANT), the excellence cluster "Advanced Imaging of Matter"—EXC 2056—Project No. 390715994 and under Germany's Excellence Strategy EXC-2181/1-390900948 (the Heidelberg STRUCTURES Excellence Cluster). M. B. acknowledges support by Labex ICFP of ENS Paris.

*tlompe@physik.uni-hamburg.de

- [1] E. Vogt, M. Feld, B. Fröhlich, D. Pertot, M. Koschorreck, and M. Köhl, *Phys. Rev. Lett.* **108**, 070404 (2012).
- [2] G. M. Bruun, *Phys. Rev. A* **85**, 013636 (2012).
- [3] T. Schäfer, *Phys. Rev. A* **85**, 033623 (2012).
- [4] T. Enss, C. Küppersbusch, and L. Fritz, *Phys. Rev. A* **86**, 013617 (2012).
- [5] P. Massignan, G. M. Bruun, and H. Smith, *Phys. Rev. A* **71**, 033607 (2005).
- [6] T. Enss, R. Haussmann, and W. Zwerger, *Ann. Phys. (Amsterdam)* **326**, 770 (2011).
- [7] C. Cao, E. Elliott, J. Joseph, H. Wu, J. Petricka, T. Schäfer, and J. E. Thomas, *Science* **331**, 58 (2011).
- [8] M. Koschorreck, D. Pertot, E. Vogt, and M. Köhl, *Nat. Phys.* **9**, 405 (2013).
- [9] C. Luciuk, S. Smale, F. Böttcher, H. Sharum, B. A. Olsen, S. Trotzky, T. Enss, and J. H. Thywissen, *Phys. Rev. Lett.* **118**, 130405 (2017).
- [10] A. Sommer, M. Ku, G. Roati, and M. W. Zwierlein, *Nature (London)* **472**, 201 (2011).
- [11] G. M. Bruun, *New J. Phys.* **13**, 035005 (2011).
- [12] T. Enss and R. Haussmann, *Phys. Rev. Lett.* **109**, 195303 (2012).
- [13] A. B. Bardon, S. Beattie, C. Luciuk, W. Cairncross, D. Fine, N. S. Cheng, G. J. A. Edge, E. Taylor, S. Zhang, S. Trotzky, and J. H. Thywissen, *Science* **344**, 722 (2014).
- [14] G. Valtolina, F. Scazza, A. Amico, A. Burchianti, A. Recati, T. Enss, M. Inguscio, M. Zaccanti, and G. Roati, *Nat. Phys.* **13**, 704 (2017).
- [15] P. B. Patel, Z. Yan, B. Mukherjee, R. J. Fletcher, J. Struck, and M. W. Zwierlein, *arXiv:1909.02555v2*.
- [16] T. Enss and J. H. Thywissen, *Annu. Rev. Condens. Matter Phys.* **10**, 85 (2019).
- [17] P. K. Kovtun, D. T. Son, and A. O. Starinets, *Phys. Rev. Lett.* **94**, 111601 (2005).
- [18] M. Olshanii, H. Perrin, and V. Lorent, *Phys. Rev. Lett.* **105**, 095302 (2010).
- [19] M. Holten, L. Bayha, A. C. Klein, P. A. Murthy, P. M. Preiss, and S. Jochim, *Phys. Rev. Lett.* **121**, 120401 (2018).
- [20] T. Peppler, P. Dyke, M. Zamorano, I. Herrera, S. Hoinka, and C. J. Vale, *Phys. Rev. Lett.* **121**, 120402 (2018).
- [21] P. A. Murthy, N. Defenu, L. Bayha, M. Holten, P. M. Preiss, T. Enss, and S. Jochim, *Science* **365**, 268 (2019).
- [22] J. A. N. Bruin, H. Sakai, R. S. Perry, and A. P. Mackenzie, *Science* **339**, 804 (2013).
- [23] S. A. Hartnoll, *Nat. Phys.* **11**, 54 (2015).
- [24] S. Hartnoll, A. Lucas, and S. Sachdev, *Holographic Quantum Matter* (The MIT Press, Cambridge, 2018).
- [25] K. Hueck, N. Luick, L. Sobirey, J. Siegl, T. Lompe, and H. Moritz, *Phys. Rev. Lett.* **120**, 060402 (2018).
- [26] N. Luick, L. Sobirey, M. Bohlen, V. P. Singh, L. Mathey, T. Lompe, and H. Moritz, *arXiv:1908.09776v1*.
- [27] J. L. Ville, R. Saint-Jalm, E. Le Cerf, M. Aidelsburger, S. Nascimbène, J. Dalibard, and J. Beugnon, *Phys. Rev. Lett.* **121**, 145301 (2018).
- [28] Note the factor 1/2 in the exponential of the fit function, which takes into account that Γ is the damping rate of the oscillation energy, which is proportional to the square of the oscillation amplitude.
- [29] The 2D scattering length is defined as $a_{2D} = a_{2D}^{(0)} \exp[-0.5\Delta w(\mu/\hbar\omega_z)]$. Here, $a_{2D}^{(0)} = l_z \sqrt{\pi/0.905} \exp(-\sqrt{\pi/2}l_z/a_{3D})$ is the 2D scattering length for dilute gases, with the 3D-scattering length a_{3D} , the harmonic oscillator length in the strongly confined direction $l_z = \sqrt{\hbar/m\omega_z}$ and a positive scaling function $\Delta w(\mu/\hbar\omega_z) \lesssim 2.3$ which accounts for the energy dependence of 2D scattering [30,31].
- [30] D. S. Petrov and G. V. Shlyapnikov, *Phys. Rev. A* **64**, 012706 (2001).
- [31] I. Boettcher, L. Bayha, D. Kedar, P. A. Murthy, M. Neidig, M. G. Ries, A. N. Wenz, G. Zürn, S. Jochim, and T. Enss, *Phys. Rev. Lett.* **116**, 045303 (2016).
- [32] L. A. Sidorenkov, M. K. Tey, R. Grimm, Y. H. Hou, L. Pitaevskii, and S. Stringari, *Nature (London)* **498**, 78 (2013).
- [33] H. Hu, P. Dyke, C. J. Vale, and X.-J. Liu, *New J. Phys.* **16**, 083023 (2014).
- [34] M. Ota and S. Stringari, *Phys. Rev. A* **97**, 033604 (2018).
- [35] We use the adiabatic compressibility since the sound frequency is large compared to the damping ($\omega \geq \Gamma$).
- [36] A. V. Turlapov and M. Y. Kagan, *J. Phys. Condens. Matter* **29**, 383004 (2017).
- [37] H. Shi, S. Chiesa, and S. Zhang, *Phys. Rev. A* **92**, 033603 (2015).
- [38] We obtain f_κ from QMC data for the ground state energy E_0 of the homogeneous 2D Fermi gas [37]. The dimensionless energy scaling function is given by $f(x) = (E_0 + NE_B/2)/(NE_F/2) = E_0/(NE_F/2) + 2e^{-2x}$, with $x = \ln(k_F a_{2D})$. It describes the ground state energy of the homogeneous gas relative to the binding energy $E_B = \hbar^2/ma_{2D}^2$ [31] of the Fermion pairs. From this function, we obtain $f_\kappa = (V^2/NE_F)(\partial^2 E/\partial V^2) = f(x) + 3/4f'(x) + 1/8f''(x)$ by differentiation.
- [39] V. Makhalov, K. Martiyanov, and A. Turlapov, *Phys. Rev. Lett.* **112**, 045301 (2014).
- [40] K. Fenech, P. Dyke, T. Peppler, M. G. Lingham, S. Hoinka, H. Hu, and C. J. Vale, *Phys. Rev. Lett.* **116**, 045302 (2016).
- [41] G. Bighin and L. Salasnich, *Phys. Rev. B* **93**, 014519 (2016).

- [42] V. P. Singh and L. Mathey, *Phys. Rev. Research* **2**, 023336 (2020).
- [43] Within kinetic theory, the mean free path is estimated as $l_{\text{mfp}} = 1/n\sigma \simeq 0.63n^{-1/2}[1 + 4\ln^2(k_{\text{F}}a_{2\text{D}})/\pi^2]$. For our system, one obtains $l_{\text{mfp}} \leq 16 \mu\text{m} < 2l_x$. Hydrodynamic estimates for the relaxation length $l = D_s/c$ and relaxation time $\tau = l/c$ yield $\Gamma/\omega \sim \omega\tau \ll 1$. Thus, both of these estimates suggest that hydrodynamic conditions are satisfied for our system.
- [44] L. D. Landau and E. M. Lifshitz, *Course of Theoretical Physics—Vol. 6: Fluid Mechanics* (Pergamon Press, Oxford, 1987).
- [45] H. Smith and H. Jensen, *Transport Phenomena* (Oxford Science Publications/Clarendon Press, Oxford, 1989).
- [46] T. Enss, *Phys. Rev. Lett.* **123**, 205301 (2019).
- [47] Y. Nishida, *Ann. Phys. (Amsterdam)* **410**, 167949 (2019).
- [48] J. Hofmann, *Phys. Rev. A* **101**, 013620 (2020).
- [49] T. Schäfer and D. Teaney, *Rep. Prog. Phys.* **72**, 126001 (2009).
- [50] G. Eska, K. Neumaier, W. Schoepe, K. Uhlig, W. Wiedemann, and P. Wölfle, *Phys. Rev. Lett.* **44**, 1337 (1980).