

How Different is the Core of ^{25}F from $^{24}\text{O}_{\text{g.s.}}$?

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The structure of a neutron-rich ^{25}F nucleus is investigated by a quasifree ($p, 2p$) knockout reaction at 270A MeV in inverse kinematics. The sum of spectroscopic factors of $\pi 0d_{5/2}$ orbital is found to be 1.0 ± 0.3 . However, the spectroscopic factor with residual ^{24}O nucleus being in the ground state is found to be only 0.36 ± 0.13 , while those in the excited state is 0.65 ± 0.25 . The result shows that the ^{24}O core of ^{25}F nucleus significantly differs from a free ^{24}O nucleus, and the core consists of $\sim 35\%$ $^{24}\text{O}_{\text{g.s.}}$ and $\sim 65\%$ excited ^{24}O . The result may infer that the addition of the $0d_{5/2}$ proton considerably changes neutron structure in ^{25}F from that in ^{24}O , which could be a possible mechanism responsible for the oxygen dripline anomaly.

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In the independent particle picture [1], a nucleon is moving without any correlation with other nucleons. Building upon this, a shell model successfully describes many nuclear properties by introducing residual interactions [2]. The residual interactions perturb the single-particle wave function and cause nucleons to become correlated. Theoretically, the degree of independence of a nucleon of a specific single-particle orbital (SPO) can be characterized using the spectroscopic factor (SF) [3], which is related to the occupancy of the SPO. Using electron-(proton)-induced knockout (transfer) reactions on most stable nuclei, the integrated SFs for a given orbital are limited to 0.6–0.7 [4,5]. The reduction from unity is attributed to the short- and long-range correlations among the nucleons [6].

In the particular case of nuclei with a single valence nucleon and a doubly magic core, the residual interaction between the valence nucleon and the core is weak due to the closed-shell nature of the core. For example, the pairing

correlation is weak [7]. The SFs of ground-state to ground-state transitions are experimentally in the range of 0.8–1.1 for $^{17}\text{F} = p + ^{16}\text{O}_{\text{g.s.}}$ [8–10], $^{41}\text{Sc} = p + ^{40}\text{Ca}_{\text{g.s.}}$ [11,12], $^{49}\text{Sc} = p + ^{48}\text{Ca}_{\text{g.s.}}$ [13], and $^{209}\text{Bi} = p + ^{208}\text{Pb}_{\text{g.s.}}$ [14–16]. Nevertheless, the above SFs are subject to reanalysis in regard to the quenching found in ($e, e'p$) experiments [4].

A ($p, 2p$) quasifree knockout reaction can be used to extract the SF of a proton SPO (π -SPO) [3,17] using experimental cross sections and theoretical single-particle cross sections. The ($p, 2p$) quasifree knockout reaction is regarded as a proton-proton scattering in a nucleus without significant disturbance to other part of the nucleus. With the approximations in Ref. [3,17], the cross section (σ) is proportional to the square of the overlap between a target (AZ) and the knocked-out proton and a residual nucleus [$^{A-1}(Z-1)$] wave functions [3] as

$$\sigma \propto |\langle \pi_j | \otimes \langle ^{A-1}(Z-1)^i | | ^AZ \rangle|^2 = \alpha^i(\nu) \beta^i(\pi_j), \quad (1)$$

where $|\pi_j\rangle$ is the j th π -SPO, $\otimes$ is the spin-isospin coupling and antisymmetrization operator, i indicates the state of the residual nucleus, $\alpha^i(\nu)$ is the overlap of the neutron orbitals, and $\beta^i(\pi_j)$ is the overlap of the proton orbitals. Usually, in proton-removal reactions such as $^{16}\text{O}(p, 2p)$ [18] and $^{40}\text{Ca}(p, 2p)$ [19], the neutron part is assumed to be inert and $\alpha^i(\nu) = 1$. Thus the SF is directly related to the overlap of the proton orbitals.

In the special case where the knocked-out proton is in a SPO to a good approximation, i.e., $\beta^j(\pi_j) \approx 1$, the reaction can be used to investigate the neutron-shell structure via the overlap $\alpha^i(\nu)$. In this Letter, we apply this method to neutron-rich fluorine isotopes of $^{23,25}\text{F}$. The cores of ^{23}F and ^{25}F are ^{22}O and ^{24}O with a proton magic number of 8 and neutron semimagic number of 14 and 16 [20,21], respectively. Particularly, ^{24}O is known to have established doubly magic nature [22,23]. The pn pairing correlation energies of ^{23}F and ^{25}F are small and equal 0.7 MeV and 0.1 MeV, respectively [24]. Therefore, the pn pairing correlation is considered to be weak. In addition, the oxygen dripline anomaly, i.e., the drastic change in the neutron dripline from $N = 16$ for oxygen to $N = 22$ for fluorine, indicates that the structure of the neutron shell may drastically change due to the addition of one $0d_{5/2}$ proton. A previous work reports that the SF extracted from the $^{12}\text{C}(^{25}\text{F}, ^{24}\text{O})$ reaction at 50.4A MeV is as small as 0.4 [25]. No detailed discussion is made in Ref. [25] and it is concluded that experiments with higher precision are necessary in order to infer a change of the structure. On the other hand, the $(p, 2p)$ reaction has demonstrated to be a good spectroscopic tool to investigate single particle properties of stable [5] and unstable nuclei [26,27].

In this Letter, the experimental results for a $(p, 2p)$ proton knockout reaction of $^{23,25}\text{F}$ are presented. The ^{25}F data is compared to the distorted-wave impulse approximation (DWIA) calculations. The overlap between the oxygen core of ^{25}F and the $^{24}\text{O}_{\text{g.s.}}$ is as small as $\sim 35\%$. The data for ^{23}F shows similar feature. However, it is not possible to draw a clear conclusion on ^{23}F because contributions from bound excited states in ^{22}O cannot be ruled out due to insufficient resolution.

The $(p, 2p)$ quasifree knockout experiments with exclusive measurements using ^{25}F and ^{23}F beams were performed at the Radioactive Isotopes Beam Factory operated by RIKEN Nishina Center and Center of Nuclear Study, The University of Tokyo. The primary beam of ^{48}Ca at 345A MeV with an intensity of 200 pnA hit a 30-mm thick ^9Be target, and then a secondary beam was produced and transported through the BigRIPS [28] to the SHARAQ spectrometer [29]. The BigRIPS was tuned to provide a cocktail beam, which included ^{25}F . The particle identification (PID) of the secondary beam was conducted using the ΔE -TOF- $B\rho$ method. The intensity, energy, and purity of ^{25}F were 1.69×10^4 pps, 277A MeV, and 42%,

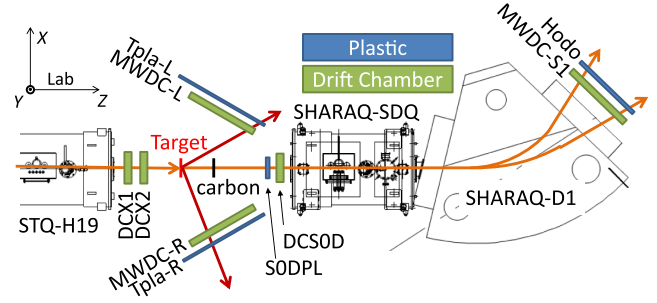


FIG. 1. Illustration of the experimental setup near the target. It is not to scale. Beam (orange) comes from the left and is tracked. Scattered protons (red lines) are detected by plastic scintillators [Tpla-L(R)] and tracked by multiwire drift chambers [MWDC-L(R)]. Residual nuclei are analyzed by downstream detectors with SHARAQ-SDQ and -D1 magnets. See Ref. [26] for details.

respectively. A ^{23}F cocktail beam was also produced and analyzed. The secondary target was a 1-mm-thick C_{10}H_8 crystal [30–33]. The carbon background was subtracted using events from the carbon target placed downstream of the reaction target. Figure 1 shows the detector setup around the target. Details can be found in Ref. [26].

The upstream PID, the proton-proton coincidence, the reaction vertex, and the residues PID were used to identify the reaction channel. The missing four-momentum of the residual ^{24}O was reconstructed using

$$P_O = P_F + P_T - P_1 - P_2, \quad (2)$$

where P are the four-momenta of the oxygen residues (O), the fluorine nucleus (F), the target proton (T), and the two scattered protons (1 and 2). The excitation energy E_x of the residual oxygen was then deduced by

$$E_x = m(P_O) - m_O, \quad (3)$$

where $m(P_O)$ is the invariant mass of oxygen residues P_O , and m_O is the mass of ground state oxygen.

The residual oxygen nucleus can be excited above the neutron-emission thresholds and produces ^{24-n}O isotopes. PID of the reaction fragments was used to select a group of excited states in ^{24}O as shown in Fig. 2(a). The probability for direct production of ^{24-n}O via multinucleon knockout should be much smaller. In the following, the selection is notated as $(^{25}\text{F}, ^{24-n}\text{O})$. Data for ^{23}F were analyzed using the same method.

Figure 2(b) shows the experimental excitation-energy spectrum of the $^{25}\text{F}(p, 2p)$ reaction. Each $(^{25}\text{F}, ^{24-n}\text{O})$ channel was fitted with a single Gaussian to obtain the mean excitation energy and the width. The mean energy of the $(^{25}\text{F}, ^{24}\text{O})$ channel is -0.5 ± 1.1 MeV and is consistent with transition to the ^{24}O ground state. The center of $(^{25}\text{F}, ^{23}\text{O})$ channel is at 6.5 ± 1.4 MeV. The mean energy is located between the one-neutron and the two-neutron

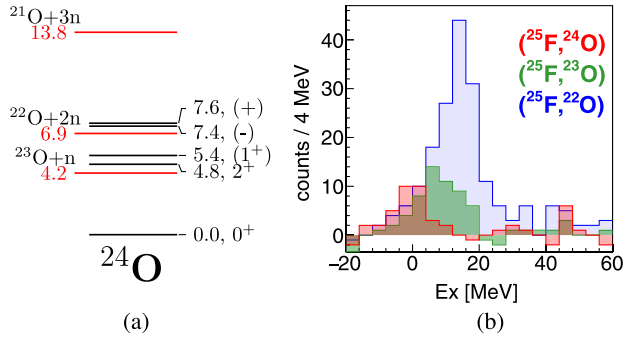


FIG. 2. (a) Energy levels (black lines) and multiple-neutron threshold energies (red lines) of ^{24}O [34]. Unit of energy is MeV. (b) Experimental excitation-energy spectra of ^{24}O from the $^{25}\text{F}(p, 2p)$ reaction.

emission thresholds [Fig. 2(a)] as it should be. The mean energy of the $(^{25}\text{F}, ^{22}\text{O})$ channel is 12.7 ± 0.6 MeV. The counts of $(^{25}\text{F}, ^{24}\text{O})$, $(^{25}\text{F}, ^{23}\text{O})$, and $(^{25}\text{F}, ^{22}\text{O})$ channels were integrated from -20 to 20 MeV, -14 to 26 MeV, and -8 to 32 MeV, respectively. The cross section of each channel is obtained from dividing the integrated counts by the total luminosity, detector efficiency and acceptance. Table I lists the experimental results along with those of $^{23}\text{F}(p, 2p)$ reaction.

The orbital of the knocked-out proton for each channel can be identified by comparing the Fermi momentum distribution of the knocked-out proton to the DWIA calculation and the parity of the known states of the oxygen residues. The Fermi momentum is reconstructed using the momenta of the incident fluorine and the two protons as $\vec{k}_{\text{Fermi}} = \vec{k}_1 + \vec{k}_2 - \vec{k}_{\text{F}}/A_{\text{F}}$, where A_{F} is the mass of the fluorine nucleus. Additionally, the estimated shell-gap energy between $\pi 0d_{5/2}$ and $\pi 0p_{1/2}$ orbits could also support the orbital assignment.

To compare the experimental momentum distribution and extract the SF (S_{exp}), DWIA calculations were conducted using the codes PIKOE [35] with a microscopic folding potential based on the Melbourne G -matrix interactions [36] and nuclear densities calculated with the single particle potential by Bohr and Mottelson [37]. The calculations use the single proton wave function from the

Woods-Saxon potential with a half-potential radius and a diffuseness parameter of $1.27A^{1/3}$ fm and 0.67 fm, respectively [37]. These Wood-Saxon parameters were chosen to be consistent with the optical potential used in the reaction analysis [26]. The potential depth is calculated by matching the separation energy. A Coulomb radius of $1.25A^{1/3}$ fm is used.

The theoretical cross section (σ_{th}) for a unit SF integrated over the detector acceptance is shown in Table I, together with the experimentally integrated cross section (σ_{exp}). The error of the DWIA-integrated cross section was evaluated by taking the energy-dependence of the cross section and the uncertainty of the Wood-Saxon parameters into account. Finally, dividing the experimentally integrated cross section by the theoretical integrated cross section, the SF (S_{exp}) was obtained.

Figure 3 shows the experimental and theoretical proton momentum distributions of the $(^{25}\text{F}, ^{24}\text{O})$ and $(^{25}\text{F}, ^{23}\text{O})$ channels. Because the significant contribution of the s orbital is not seen, one can consider that the protons are knocked out from the $0d_{5/2}$ orbital in both channels. Since ^{24}O does not have a bound excited state, this channel contains only the ground state. The parity of the ^{24}O ground state is positive, and the momentum distribution [Fig. 3(a)] shows that the $(^{25}\text{F}, ^{24}\text{O})$ channel is due to the knockout of $0d_{5/2}$ proton.

The momentum distribution for the $(^{25}\text{F}, ^{23}\text{O})$ channel [Fig. 3(b)] is consistent with that for the knockout of $0d_{5/2}$ orbital. Moreover, the parities of the known states are positive [Fig. 2(a)]. These support the idea that the channel is mainly due to knockout of $0d_{5/2}$ proton. Considering the mean excitation energy for the $(^{25}\text{F}, ^{22}\text{O})$ channel is 12.7 ± 0.6 MeV, which is comparable to the $\pi 0d_{5/2} - \pi 0p_{1/2}$ shell gap of 12.7 MeV evaluated using proton separation energies of ^{25}F and ^{24}O , this channel is attributed to the $0p_{1/2}$ proton knockout.

The SF of the $(^{25}\text{F}, ^{24}\text{O})$ channel is found to be 0.36 ± 0.13 , which is significantly smaller than unity. Similarly small spectroscopic factor is found in heavy-ion-induced knockout reaction in Ref. [25], however, because of significant difference seen in reduction factors

TABLE I. Experimental results, integrated cross-sections, and spectroscopic factors. S_{exp} extracted from experimental cross section and theoretical single-particle cross sections. J_{th}^{π} is the spin-parity used for theoretical calculations.

Channel	Mean [MeV]	Width [MeV]	σ_{exp} [μb]	σ_{th} [μb]	J_{th}^{π}	S_{exp}	$S_{\text{th}}(\text{USDB})$	$S_{\text{th}}(\text{SFO})$	$S_{\text{th}}(\text{SPDF-MU})$
$(^{25}\text{F}, ^{24}\text{O})$	$-0.5(1.1)$	$4.8(1.3)$	$53(18)$	$149(24)$	$5/2^+$	$0.36(13)$	1.01	0.90	0.95
$(^{25}\text{F}, ^{23}\text{O})$	$6.5(1.4)$	$6.3(9)$	$81(26)$	$125(26)$	$5/2^+$	$0.65(25)$	0.01	0.07	0.05
$(^{25}\text{F}, ^{22}\text{O})$	$12.7(6)$	$7.6(6)$	$274(71)$	$80(24)$	$1/2^-$	$3.43(1.4)$		2.19	
$(^{23}\text{F}, ^{22}\text{O})$	$1.0(8)$	$6.0(6)$	$61(14)$	$166(28)$	$5/2^+$	$0.37(10)$	1.08	0.92	1.00
$(^{23}\text{F}, ^{21}\text{O})$	$9.5(4)$	$7.9(4)$	$456(67)$	$93(25)$	$1/2^-, 3/2^-$	$4.9(1.5)$		5.21	
$(^{23}\text{F}, ^{20}\text{O})$	$18.0(5)$	$9.7(5)$							

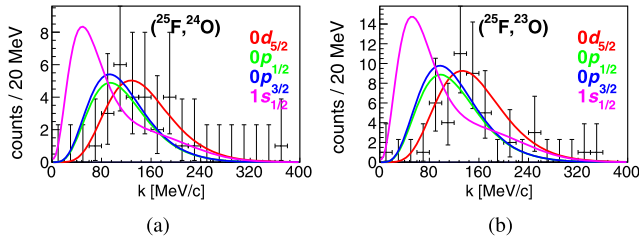


FIG. 3. Experimental proton momentum distribution of different channels. Colored lines are the theoretical distributions. (a) (^{25}F , ^{24}O) channel. (b) (^{25}F , ^{23}O) channel.

by proton-induced and heavy-ion induced reactions, we don't compare our results with those in Ref. [25].

The quenching of the $0d_{5/2}$ proton is not solely responsible for the reduction of proton SF [6]. The SF of 0.65 ± 0.25 for the (^{25}F , ^{23}O) channel, which is due to the $0d_{5/2}$ proton knockout, indicates that part of the proton $0d_{5/2}$ strength is fragmented to the ^{24}O excited states. The sum of the SFs of the $0d_{5/2}$ proton from the ground state to the excited states is 1.0 ± 0.3 . Thus, it is reasonable that the $0d_{5/2}$ proton is primarily in a SPO, and no significant configuration mixing is occurring on the proton side.

Considering the $0d_{5/2}$ proton is in a SPO, the small overlap is due to the difference in the neutron shell structure [Eq. (1)]. The small SF for the (^{25}F , $^{24}\text{O}_{\text{g.s.}}$) channel indicates the small overlap between the oxygen core of ^{25}F and $^{24}\text{O}_{\text{g.s.}}$ [Eq. (1)]. In other words, the core of ^{25}F would significantly differ from $^{24}\text{O}_{\text{g.s.}}$. The SFs show that only $\sim 35\%$ of the ^{25}F core is $^{24}\text{O}_{\text{g.s.}}$ and the remaining $\sim 65\%$ is the ^{24}O excited states.

A strong pn tensor interaction induced by the $0d_{5/2}$ proton in ^{25}F [Fig. 4(a)] may be a plausible mechanisms for the change in the neutron-shell structure. A first-order effect of the tensor interaction by the $0d_{5/2}$ proton [Fig. 4(a)] [38–40] attracts the $0d_{3/2}$ neutrons and repels the $0d_{5/2}$ neutrons. A reduction in the $\nu 0d_{5/2} \rightarrow \nu 0d_{3/2}$ energy gap results in a larger configuration mixing among the neutron orbits, causing a change in the structure of the ^{25}F core from $^{24}\text{O}_{\text{g.s.}}$. It should be noted that a recent γ -ray spectroscopy experiment revealed an additional $1.7 \text{ MeV } 1/2^+$ level in ^{25}F [41]. This may indicate the disappearance of $N = 16$ magicity and be related to the configuration mixing.

Shell model calculations with $0, 1$, and $2\hbar\omega$ excitation were carried out to clarify whether the SFs are explained by present nuclear theories. The calculations use the OXBASH [42] with the USDB (sd model space) [43], SFO (psd model space) [44], and SDPF-MU ($sdpf$ model space) [45] interactions. The results of the ground-state SF (Table I) are in the range of 0.9 – 1.0 , contradicting with the experimental results (S_{exp}).

The contradiction could be attributed to nuclear correlations that are not fully taken into account in the shell model calculations employed above. One possibility is

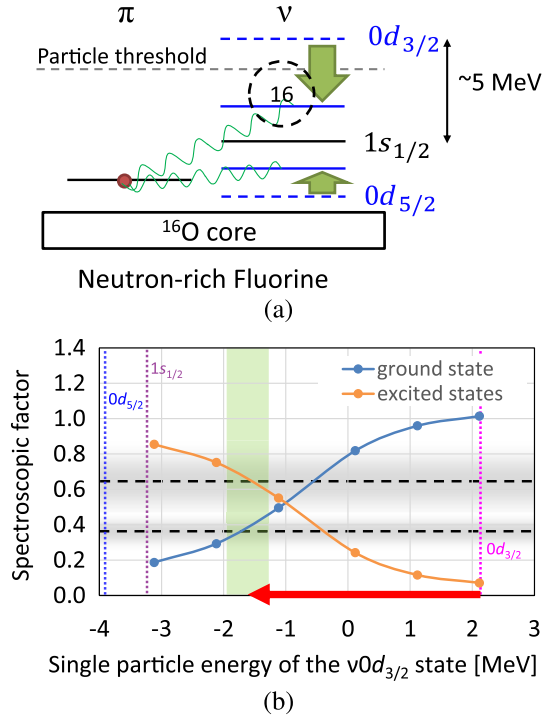


FIG. 4. (a) Mechanism of the Type-I shell evolution driven by the tensor force [38–40]. Blue dashed lines are the energy levels of the d orbits of oxygen. Blue solid lines are the energy levels of the d orbits of fluorine. The wavy green lines represent the pn tensor interaction. The $1s_{1/2}$ orbital is assumed to be unaffected by the $0d_{5/2}$ proton. The energy gap between $0d_{3/2}$ and $1s_{1/2}$ orbits in ^{24}O is $\sim 5 \text{ MeV}$. (b) Modified shell model calculation based on USBD interaction. Vertical dotted lines are the original SPEs. Two black dashed lines and the gradients are SFs and their errors for (^{25}F , ^{24}O) and (^{25}F , ^{23}O) channels. When the energy of $0d_{3/2}$ SPO becomes lower, the ground state spectroscopic factor reduces. The red arrow indicates the reduction of the SPE of the $0d_{3/2}$ orbital. See main text for detail.

stronger tensor correlation in the region. Although the effective interactions including the tensor component successfully reproduce many of the experimental results, the lack of data in the very neutron-rich oxygen and fluorine region may limit the accuracy. Reference [41] found that 60% of ^{25}F ground state is one-particle state from $N^2\text{LO}$ calculation using constraints from the latest measurement of the level scheme. This suggests the $3N$ force is important.

As a sensitivity test for the possibility of a stronger pn tensor interaction, shell model calculations based on USDB interaction with a modified $\nu 0d_{3/2}$ single-particle energy (SPE) have been explored. Since the pn tensor interaction lowers the $\nu 0d_{3/2}$ SPE [Fig. 4(a)], the $\nu 0d_{3/2}$ SPE may be a suitable parameter to represent the tensor force strength. To reproduce the results of the present work, the $\nu 0d_{3/2}$ SPE must be lowered by 3 – 4 MeV [Fig. 4(b)]. This suggests a stronger pn tensor interaction in the structure

of neutron-rich fluorine and oxygen isotopes. A more sophisticated self-consistent modification of all matrix elements would be needed to properly understand the effect of the tensor force, while out of the scope of the present experimental work.

A sudden change in the neutron-shell structure due to the $0d_{5/2}$ proton may provide insight into the oxygen neutron dripline anomaly. The pn tensor interaction lowers the energy of the $\nu 0d_{3/2}$ orbital. This may pave the path for a long fluorine neutron dripline and extend the dripline from $N = 16$ for oxygen to $N = 22$ for fluorine. The $3N$ force can also play a considerable role in describing the nuclear structure of fluorine isotopes [41,46]. The present work suggests that the effects of the pn tensor interaction in the widely used effective interactions may be too weak to reproduce the observed difference between the ^{25}F core and $^{24}\text{O}_{\text{g.s.}}$. Together with the experiments discussed in Ref. [39,47–49], the mechanism on how the $0d_{5/2}$ proton changes the neutron-shell structure may be revealed.

In conclusion, the neutron-shell structure of ^{25}F is investigated using the $(p, 2p)$ quasifree knockout reaction at 270A MeV in inverse kinematics. The $0d_{5/2}$ proton knockout from ^{25}F populates the ^{24}O ground state with a smaller probability than the ^{24}O excited states. This result indicates that the oxygen core of ^{25}F is considerably different from $^{24}\text{O}_{\text{g.s.}}$, and has a larger overlap with the excited states of ^{24}O . The change in the neutron-shell structure due to the $0d_{5/2}$ proton may be responsible for the small overlap between ^{25}F and $^{24}\text{O}_{\text{g.s.}}$. A comparison with the shell model calculations indicates that the USDB, SFO, and SFPD-MU interactions are insufficient to reproduce the present results. A stronger tensor force or other mechanism such as the $3N$ force effects, or both, might be needed to explain the experimental results. More experimental and theoretical studies are necessary to clarify the mechanism for the change in the core of neutron-rich fluorine from the ground state of oxygen isotopes.

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- [1] V. R. Pandharipande, I. Sick, and P. K. A. deWitt Huberts, *Rev. Mod. Phys.* **69**, 981 (1997).
- [2] E. Caurier, G. Martínez-Pinedo, F. Nowacki, A. Poves, and A. P. Zuker, *Rev. Mod. Phys.* **77**, 427 (2005).
- [3] N. K. Glendenning, *Direct Nuclear Reaction* (World Scientific Publishing Co, Pte. Ltd., Singapore, 2004).
- [4] G. J. Kramer, H. P. Blok, and L. Lapikás, *Nucl. Phys.* **A679**, 267 (2001).
- [5] T. Wakasa, K. Ogata, and T. Noro, *Prog. Part. Nucl. Phys.* **96**, 32 (2017).
- [6] L. Lapikás *et al.*, *Nucl. Phys.* **A553**, 297 (1993).
- [7] S. Frauendorf *et al.*, *Nucl. Phys.* **A78**, 24 (2014).
- [8] C. J. Oliver, P. D. Forsyth, J. L. Hutton, G. Kaye, and J. R. Mines, *Nucl. Phys.* **A127**, 567 (1969).
- [9] H. T. Fortune, L. R. Medsker, J. D. Garrett, and H. G. Bingham, *Phys. Rev. C* **12**, 1723 (1975).
- [10] M. Yasue *et al.*, *Phys. Rev. C* **46**, 1242 (1992).
- [11] H. G. Leighton, G. Roy, D. P. Gurd, and T. B. Grandy, *Nucl. Phys.* **A109**, 218 (1968).
- [12] D. H. Youngblood, R. L. Kozub, R. A. Kenefick, and J. C. Hiebert, *Phys. Rev. C* **2**, 477 (1970).
- [13] R. M. Britton, and D. L. Watson, *Nucl. Phys.* **A272**, 91 (1976).
- [14] B. Berthier *et al.*, *Phys. Lett. B* **182**, 15 (1986).
- [15] S. Gales, C. P. Massolo, S. Fortier, J. P. Schapira, P. Martin, and V. Comparat, *Phys. Rev. C* **31**, 94 (1985).
- [16] D. Branford *et al.*, *Phys. Rev. C* **63**, 014310 (2000).
- [17] G. Jacob, and T. A. J. Maris, *Rev. Mod. Phys.* **38**, 121 (1966).
- [18] W. J. McDonald *et al.*, *Nucl. Phys.* **A456**, 577 (1986).
- [19] Y. Yasuda *et al.*, *Phys. Rev. C* **81**, 044315 (2010).
- [20] A. Ozawa, *Phys. Rev. Lett.* **84**, 5493 (2000).
- [21] B. Fernández-Domínguez, *Phys. Rev. C* **84**, 011301(R) (2011).
- [22] C. Nociforo *et al.*, *AIP Conf. Proc.* **1165**, 90 (2009).
- [23] R. V. F. Janssens, *Nature (London)* **459**, 1069 (2009).
- [24] K. Kaneko and M. Hasegawa, *Phys. Rev. C* **69**, 061302(R) (2004).
- [25] M. Thoennessen *et al.*, *Phys. Rev. C* **68**, 044318 (2003).
- [26] S. Kawase *et al.*, *Prog. Theor. Exp. Phys.* **(2018)**, 021D01.
- [27] L. Atar *et al.*, *Phys. Rev. Lett.* **120**, 052501 (2018).
- [28] T. Kubo *et al.*, *Nucl. Instrum. Methods Phys. Res., Sect. B* **204**, 97 (2003).
- [29] T. Uesaka *et al.*, *Prog. Theor. Exp. Phys.* **(2012)**, 03C007.

- [30] T. Uesaka, M. Hatano, T. Wakui, H. Sakai, and A. Tamii, *Nucl. Instrum. Methods Phys. Res., Sect. A* **526**, 186 (2004).
- [31] T. Wakui, M. Hatano, H. Sakai, T. Uesaka, and A. Tamii, *Nucl. Instrum. Methods Phys. Res., Sect. A* **550**, 521 (2005).
- [32] T. L. Tang *et al.*, *CNS Annu. Rep.* **2012**, 59 (2013), <https://www.cns.s.u-tokyo.ac.jp/archive/annual/ann12.pdf>.
- [33] T. L. Tang *et al.*, *CNS Annu. Rep.* **2013**, 11 (2014), <https://www.cns.s.u-tokyo.ac.jp/archive/annual/ann13.pdf>.
- [34] National Nuclear Data Center, information extracted from the evaluated Nuclear Structure Data File (ENSDF).
- [35] K. Ogata, K. Yoshida, and Y. Chazono, Computer Code PIKOE.
- [36] K. Amos *et al.*, in *Advances in Nuclear Physics* (Plenum, New York, 2000), Vol. 25, p. 275.
- [37] A. Bohr and B. R. Mottelson, *Nuclear Structure* (Benjamin, New York, 1969), Vol. I.
- [38] T. Otsuka, T. Suzuki, R. Fujimoto, H. Grawe, and Y. Akaishi, *Phys. Rev. Lett.* **95**, 232502 (2005).
- [39] T. Otsuka, T. Suzuki, J. D. Holt, A. Schwenk, and Y. Akaishi, *Phys. Rev. Lett.* **105**, 032501 (2010).
- [40] T. Otsuka, and Y. Tsunoda, *J. Phys. G* **43**, 024009 (2016).
- [41] Z. Vajta *et al.*, *Phys. Rev. C* **89**, 054323 (2014).
- [42] B. A. Brown *et al.*, MSU-NSCL Report No. 1289.
- [43] B. A. Brown and W. A. Richter, *Phys. Rev. C* **74**, 034315 (2006).
- [44] T. Suzuki, R. Fujimoto, and T. Otsuka, *Phys. Rev. C* **67**, 044302 (2003).
- [45] Y. A. Utsuno, T. Otsuka, B. Alex Brown, M. Honma, T. Mizusaki, and N. Shimizu, *Phys. Rev. C* **86**, 051301(R) (2012).
- [46] V. Somà *et al.*, *EPJ Web Conf.* **66**, 02005 (2014).
- [47] T. Otsuka, *Phys. Scr.* **T152**, 014007 (2013).
- [48] B. A. Brown, *Prog. Part. Nucl. Phys.* **47**, 517 (2001).
- [49] T. Baumann, A. Spyrou, and M. Thoennessen, *Rep. Prog. Phys.* **75**, 036301 (2012).