Obtaining Precision Constraints on Modified Gravity with Helioseismology

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We propose helioseismology as a new, precision probe of fifth forces at astrophysical scales, and apply it on the most general scalar-tensor theories for dark energy, known as degenerate higher-order scalar-tensor theories. We explain how the effect of the fifth force on the solar interior leaves an observable imprint on the acoustic oscillations, and under certain assumptions we numerically compute the nonradial pulsation eigenfrequencies within modified gravity. We illustrate its constraining power by showing that helioseismic observations have the potential to improve constraints on the strength of the fifth force by more than 2 orders of magnitude, as $-1.8 \times 10^{-3} \le Y \le 1.2 \times 10^{-3}$ (at 2σ). This in turn would suggest constraints of similar order for the theory's free functions around a cosmological background (α_H , β_1).

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Introduction.—General relativity (GR) has been successful at describing observations at a vast range of scales, but its currently being challenged by crucial cosmological and astrophysical observations: the pressing questions of dark matter and dark energy suggest the possibility of new degrees of freedom and forces, yet to be discovered.

The most popular extensions of GR are theories introducing a new dynamical scalar field coupled to spacetime. Intense efforts over the last years led to the remarkable construction of the most general, covariant theory describing the dynamics of a scalar field kinetically interacting with gravity, collectively labeled as DHOST scalar-tensor theories [1–6]. They correspond to nontrivial generalizations of the popular Horndeski theory of gravity [7], incorporating the archetypal Brans-Dicke theory as a subcase. Their cosmological and astrophysical phenomenology is rich, with their most notable prediction being the change in the propagation speed of gravitational waves as compared to GR. The recent measurement of the speed of tensors [8,9] placed the most stringent constraints on their theory space so far, ruling out a significant part of the allowed kinetic scalar-tensor interactions [10–15].

An intriguing feature of the remaining nontrivial scalarmetric interactions is the prediction of a fifth-force effect within compact objects as (Technically, this is due to the breaking of the Vainshtein screening mechanism in the star, which would otherwise prevent sizable fifth-force effects.) [14,16,17],

$$\nabla^2 \Phi = 4\pi G\rho + G \frac{Y}{4} \nabla^2 \left(\frac{dm}{dr}\right),\tag{1}$$

with Φ the gravitational potential, m(r) the mass enclosed within radius r, and Y the coupling strength of the new force. A Y > 0 (Y < 0) tends to weaken (strengthen) gravity, since $d\rho/dr < 0$ in the stellar interior, while Newtonian gravity is recovered outside the star $(dM/dr \rightarrow 0)$. In a cosmological context, Y relates to the parameters associated with the large-scale structure dynamics of general scalar-tensor theories labeled as α_H and β_1 [14]. Therefore, constraints on Y have direct consequences for gravity at large scales and dark energy modeling. Currently, the upper and lower bound from astrophysics comes from white dwarfs as Y > -0.48 [18] and Y < 0.18 [19], respectively (see also Refs. [20,21]).

Our goal is to explore helioseismology as a highprecision test of fifth forces at local scales (For detailed expositions on helioseismology, see Refs. [22–25].), focusing on theory (1). The solar eigenspectrum traces the finest details of the solar interior, which in combination with the accuracy of the observed frequencies ($\sim 1 \text{ in } 10^5$), provides a powerful probe of the underlying physics. We will explain how the fifth force leaves an observable imprint on the solar eigenspectrum through the subtle deformations of the solar sound speed profile, and employing helioseismic simulations we will illustrate the power of helioseismological constraints in this regard.

Helioseismology as a powerful probe of gravity.—For an intuitive grasp of the way helioseismology traces the interior solar physics, let us consider a key result of the asymptotic (WKB) theory of stellar pulsations, describing the characteristic frequency of an acoustic wave associated to the travel time from the stellar center to the surface (see, e.g., Refs. [22,23]),

$$f_{\text{acoustic}} = \left(\frac{1}{2} \int_0^R \frac{dr}{c_s}\right)^{-1},\tag{2}$$

with *R* the surface radius and $c_s \equiv \sqrt{\partial P / \partial \rho}$ the interior speed of sound, while *P* and ρ stand for the pressure and density profiles. Clearly, solar pulsations probe not only global properties of the star, but also the structure of its interior medium through the shape of the sound speed. Within a helioseismic inversion context, this discrepancy is translated to corrections on physical interior profiles and microphysics assumptions, which can be elegantly formulated as a variational principle (see, e.g., Refs. [25,26]).

Stellar nonradial adiabatic pulsations correspond to small departures from the spherically symmetric equilibrium state, described by a system of fourth-order differential equations for the displacement vector, Lagrangian pressure, and Eulerian gravitational potential field perturbations. Defining $\delta \mathbf{X} = \{\delta \mathbf{r}, \delta P, \delta \Phi, d\delta \Phi/dr\}$ (We consider δP and $\delta \Phi$ as a Lagrangian and Eulerian perturbation, respectively.), we write $\mathcal{L}[P(r), c_s(r); \delta \mathbf{X}] = 0$, with \mathcal{L} a linear differential operator [24]. The eigenspectrum is computed requiring regularity at the center, and that the pressure perturbation vanishes at the surface (free-boundary condition [24]). In a spherical harmonic basis, modes with $l \neq 0$ (l = 0) correspond to nonradial (radial) ones, while the overtone *n* counts the number of radial nodes. Solutions are standing waves formed in the cavity defined by an interior turning point, r_t , and an external turning point. The interior turning point shifts out to the surface for the higherdegree acoustic modes.

Modified gravity.—The modified Poisson equation (1) implies a new hydrostatic equilibrium as

$$\frac{dP}{dr} = -\frac{GM(r)}{r^2}\rho(r) - \frac{GY}{4}\frac{d^2M(r)}{dr^2}\rho(r), \qquad (3)$$

which in turn implies a new pulsation spectrum due to the modified equilibrium structure of the star. Figure 1 (left) shows the fraction change in c_s , $\Delta c_s^2/c_s^2$, under the theory (1), based on a polytrope. Each region of the star is impacted differently, with the effect escalated at two regions: the center, and an interior point $(r \sim 0.3 R_{\odot})$. The effect becomes stronger with |Y|, while a weakening (enhancement) of gravity tends to shift the interior peak towards (away from) the center. In turn, the modified sound-speed profile impacts on the predicted acoustic eigenspectrum. The right of Fig. 1 shows the scaling of eigenfrequencies with Y, numerically computed according to the procedure to be explained later. Frequencies become smaller (larger) for weaker (stronger) gravity, as qualitatively expected considering Eq. (2) in combination with the response of c_s to the fifth force. The effect of Y becomes more pronounced for smaller degrees l (at fixed n), as reflected by the larger slope, as modes with larger degrees probe outer parts of the star, where $\Delta c_s^2/c_s^2$ is declining.

Cowling approximation.—A highly useful approximation widely utilized in asteroseismological studies is the Cowling approximation [28], which accounts to neglecting the Eulerian perturbation of the gravitational potential $\delta \Phi$ for sufficiently large degrees $l \gg 1$, due to its overall suppression by the large factor $\sim (1/(2l+1))$. Therefore, the backreaction of gravity to the density perturbation is not accounted for, and the information about gravity enters implicitly through the background configuration. Since the fifth force acts as a perturbative correction to the Newtonian term, for the perturbed potential, $\delta \Phi = \delta \Phi_N + \delta \Phi_{MG}$, this translates to $|\delta \Phi_{MG}| \ll |\delta \Phi_N|$. We will therefore apply the approximation to the full potential, expected to hold except for possible singular, unphysical configurations. This will allow for an insightful understanding of the problem without loss of accuracy-a study of the full nonradial



FIG. 1. Left: Fractional difference of the solar sound speed between Newtonian and modified gravity for the indicative values of the fifth-force coupling $Y = \{\pm 7 \times 10^{-2}, \pm 3 \times 10^{-2}, \pm 8 \times 10^{-3}\}$, based on the polytrope. Continuous (dashed) curves correspond to weaker (stronger) gravity with Y > 0 (Y < 0). The typical range of turning points of the modes considered are shown with $r_t^{(\min)} = 0.309 R_{\odot}$ and $r_t^{(\max)} = 0.676 R_{\odot}$, corresponding to l = 5 and l = 35 at n = 10. Right: Scaling of polytropic frequencies with Y at fixed overtone n = 10. An order 10% weakening or strengthening of gravity ($|Y| \sim 0.1$) induces a ~0.1% change in the frequencies. The inset shows the dependence of $\partial f / \partial Y$ on overtone and degree [27]. Larger degrees probe outer solar regions where the fifth-force effect decreases, leading to a decreasing $|\partial f / \partial Y|$.

oscillation equations in modified gravity goes beyond our current scope.

Modeling and computation of the pulsation frequencies.—Eigenspectrum computation.—We use the state-of-the-art oscillation suite GYRE [29], a modular code combining advanced shooting or integration schemes to accurately solve the boundary value problem of the pulsation equations on a spatial grid. For the outer boundary condition, we impose that the pressure variation vanishes at $r = R_{\odot}$ ($\delta P = 0$). For a detailed description of the equations see Refs. [24,29,30].

Data set.—We will utilize the helioseismic data of the Global Oscillation Network Group (GONG) [31], with measurements of solar eigenfrequencies between l = 0-120, at the accuracy of 1 part in 10^4 .

Solar modeling and eigenspectrum.—The interior modeling of the star goes hand in hand with the predicted eigenspectrum. In this regard, we first use the code MESA [32–34] (We refer to the Supplemental Material for a brief description of the input physics [35–48].) to produce an evolved model of the present Sun assuming standard gravity. We evolve a 1 M_{\odot} star from its zero-age main sequence, calibrated so that for the solar radius $R/R_{\odot} \sim 10^{-4}$, luminosity $L/L_{\odot} \sim 10^{-3}$, convective radius $R^{cz}/R_{\odot}^{cz} \sim 10^{-1}$ and rms sound speed $|c_s^{rms} - c_{s\odot}^{rms}| \sim 10^{-4}$, after tuning the element abundances, mixing length or overshooting parameters, and choosing the Krishna Swamy atmospheric model.

We proceed computing the acoustic eigenspectrum based on the evolutionary model (Y = 0) with GYRE, considering $5 \le l \le 35$, and scanning for frequencies up to the $n \sim 40$ th overtone. The choice of $l \ge 5$ is for consistency with the Cowling approximation. The numerical computation reveals that agreement between predicted and observed frequencies is at the 0.1% level [49].

Modified gravity.—Aiming at the best balance between simplicity and accuracy, we proceed in two steps: First, we compute the eigenspectrum in modified gravity using as our proxy a polytropic equation of state. The polytrope inevitably omits for a variety of microphysics—this offset is then compensated for at the level of the eigenfrequencies in an effective manner, using the results of our reference evolutionary model at standard gravity (Y = 0).

For the polytropic index, we fix $n_{pol} = 3.069$, which we find to provide the best-fit to the density and pressure profiles of the evolutionary model, so that consistency between both descriptions is ensured. We first construct a set of polytropic models based on Eq. (3) for $-10^{-1} \le |Y| \le 10^{-1}$ and step size $\delta Y = 0.2 \times 10^x$, $x \in \{-6, ..., -1\}$, and proceed solving the pulsation equations with GYRE on a spatial grid of $\sim 7 \times 10^4$ points and $5 \le l \le 35$. The resulting dependence of frequencies on *Y* is shown in Fig. 1.

Comparison between the polytropic (at Y = 0) and evolutionary-model frequencies suggests they disagree by 17.5%–21.5%. We compensate for this offset effectively, through a correction term δf , which accounts for all corrections from a more accurate accounting of the microphysics as

$$f_{\text{theory}}(n,l;Y) = f_{\text{pol.}}(n,l;Y) + \delta f(n,l;Y).$$
(4)

 f_{theory} denotes the predicted and sufficiently accurate frequency, while the polytropic $f_{\text{pol.}}$ is constructed with $n_{\text{pol}} = 3.068$. Since the fifth force is a perturbative correction to the Newtonian term, we can estimate $\delta f(n, l; Y)$ through an expansion around Y = 0 as $\delta f \simeq \delta f_{(0)} + \delta f_{(1)} \equiv$ $\delta f_{(0)} + \{[\partial \delta f(Y)]/\partial Y\}|_{Y=0}Y$. The term $\delta f_{(0)}$ accounts for the neglected microphysics of the polytrope at Y = 0, while $\delta f_{(1)}$ measures their response to the fifth force. Therefore, for Y = 0, f_{theory} identifies with the frequencies computed with the evolutionary model, allowing us to explicitly extract the zeroth-order correction as $\delta f_{(0)} =$ $f_{\text{theory}} - f_{\text{pol.}}(Y = 0)$.

Now, it is straightforward to see that the linear correction $\delta f_{(1)}$ can be written in the suggestive form

$$\delta f_{(1)} \equiv f'_{\text{pol.}} \xi Y, \qquad \xi \equiv \left(\frac{f'_{\text{pol.}} - f'_{\text{theory}}}{f'_{\text{pol.}}}\right)_{Y=0}, \qquad (5)$$

with derivatives evaluated at Y = 0, gradients depending on (n, l), and $\partial f / \partial Y \equiv f'$. In the absence of evolutionary simulations in modified gravity, f'_{theory} is unknown, and we will instead treat ξ as a nuisance parameter. Notice that, since gradients depend on (l, n), Eq. (5) accounts for the appropriate weight for each mode through f'_{pol} , the value of which is known from our numerical simulations. Our goal now is to derive an upper bound for $|\xi|$ that will guide its marginalization range later on. For a numerical estimate, we consider the approximate result from the asymptotic (WKB) analysis for sufficiently low-degree modes (see, e.g., Refs. [22,23]),

$$f = \left(n + \frac{l}{2} + \alpha\right)\bar{f},\tag{6}$$

with $\overline{f} \equiv f_{\text{acoustic}}$ given in Eq. (2), and α a correction due to the phase shift as the wave is reflected at the outer boundary. It is $\alpha \simeq n_{\text{pol}}/2$ for a purely polytropic star, and $\alpha \simeq 0.646$ for perfectly conducting atmospheres (see, e.g., Refs. [22,23] for details).

To estimate $f'_{\text{theory}}(Y)$ in Eq. (5), we first differentiate (6) with respect to Y. In turn, this requires an estimate of the corrected, fundamental frequency $\bar{f}_{\text{theory}}(Y)$. To compute it, we use Eq. (2) under a similar improvement to Eq. (4), but at the level of the sound speed as $c_s(Y) =$ $c_s^{\text{pol.}}(Y) + \delta c_s(Y) \simeq c_s^{\text{pol.}}(Y) + \delta c_s^{(0)}$, truncated at zeroth order. (It is straightforward to see that, expanding the integrand in Eq. (2) with respect to Y, the linear correction $\delta c_s^{(1)}(Y)$ is suppressed by at least one order of magnitude compared to the zeroth-order term.) The polytropic piece acts as a proxy to the fifth-force's effect, while the Y-independent correction $\delta c_s^{(0)}$ is extracted comparing the sound speed profile of our evolutionary model with the polytrope (at Y = 0). Evaluating Eq. (2) under this approximation, and differentiating the result leads to $\partial \bar{f}_{\text{theory}} / \partial Y \simeq -3.425$. For the pure polytrope ($n_{pol} = 3.069$), it is easy to see that $\partial \bar{f}_{\text{pol.}} / \partial Y \simeq -3.053$. We also use $\alpha_{\text{pol.}} = n_{\text{pol}}/2$ and $\alpha_{\text{theory}} = 0.646$, respectively. Now, our numerical solutions for f'_{pol} , show that its magnitude increases with increasing degree at fixed overtone, approximately according to Eq. (6) up to $l \sim 10$, and starts decreasing with l beyond that point (see right of Fig. 1). Therefore, using Eq. (6) and the previous estimates, an upper bound is found substituting the highest overtone in the particular subsample of modes we use for our statistical analysis (see next section), n = 11, for which $l_{\text{critical}} = 9$, yielding $|\xi|_{\text{upper}} \simeq 5.2\%$. We allowed for both positive and negative values in ξ for consistency, given that its exact value is unknown in our analysis.

The constraining power of helioseismology on the fifthforce coupling and its cosmological implications.— Typically, stellar-evolutionary models cannot accurately enough predict the star's eigenspectrum. Within helioseismic inversions, statistically significant differences between theory and observations are translated to background-modeling corrections. In this context, disentangling the subtle effects of the fifth force from such systematics proves a challenging task. A helioseismic-inversion analysis in modified gravity goes beyond the scope of this work -instead, to minimize background-modeling systematics, we select those frequencies differing by no more than $1\sigma_{obs}$, i.e., $|f_{\text{theory}} - f_{\text{obs}}| < \sigma_{\text{obs}}$, when computed with the evolutionary model (at Y = 0). We find this is satisfied in total by 19 modes ranging between l = 10-35 and n = 6-11 [27]. For all modes of this subset we construct a combined likelihood as $\mathcal{L}(Y;\xi) \propto \exp(-\chi^2/2)$, with $\chi^2(Y,\xi;l,n) \equiv$ $\sum_{l,n} [f_{\text{theory}}(Y,\xi;l,n) - f_{\text{observed}}(l,n)]^2 / \sigma_{\text{obs}}^2$, and f_{theory} computed according to the previous section.

Using $|\xi|_{upper} \simeq 5.2\%$, we first marginalize \mathcal{L} over $\xi \in [-0.052, 0.052]$, to find that, $-1.71 \times 10^{-3} \le Y \le 1.15 \times 10^{-3}$ (2 σ). Had we naively assumed the fractional error on the frequency gradients is similar to that for the frequencies between the polytropic and MESA model (~17.5–21.5%), we are led to the extreme case of $|\xi| \simeq 22$. Marginalizing over $|\xi| \le 22$ we find $-1.79 \times 10^{-3} \le Y \le 1.2 \times 10^{-3}$ (2 σ). Clearly, the marginalization range has no practical effect, and using the latter conservative choice for $|\xi|$, we can quote at 2σ

$$-1.8 \times 10^{-3} \le Y \le 1.2 \times 10^{-3}.$$
 (7)

This suggests an improvement by more than 2 orders of magnitude on the previous lower (Y > -0.48 [18]) and upper (Y < 0.14 [19]) bounds from astrophysics, and adds to intense previous efforts to constrain Y [18–20,50–56]. The result (7) should be understood within the context of our data-selection criterion, relying on the modes best



FIG. 2. The implications of Eq. (7) on the cosmologicalparameter space (β_1, α_H) . The region between the blackcontinuous boundaries corresponds to the constraint of Ref. [14], while green-dashed ellipses to the predicted helioseismological bound (7).

described by our reference model. We find that inclusion of a broader set of modes causes tension with Newtonian gravity at 2σ (This is due to a shift in the total likelihood's central value, and not a change in its spread.), until the point when individual likelihoods are in tension with each other too—the latter tension prevents the extraction of a global constraint on Y from all data points, and indicates the need for improved modeling. A detailed helioseismic-inversion treatment in the future would allow for a consistent analysis of all modes, and the distinction between genuine fifthforce effects from background-modeling artifacts [27]. Therefore, Eq. (7) illustrates the constraining power of our approach, and should be regarded as a first, order-ofmagnitude estimate of what would be a thorough helioseismic analysis.

The coupling Y relates to effective theory functions of the original scalar-tensor theory as Ref. [14], $Y = -(2(\alpha_H + \beta_1)^2/\alpha_H + 2\beta_1)$. $\beta_1(t)$ parametrizes the contribution of higher-order scalar-metric kinetic operators in the action, while $\alpha_H(t)$ quantifies the amount of kinetic mixing between the scalar and matter. Their current constraint is due to the Hulse-Taylor pulsar combined with white-dwarf observations, $-8 \times 10^{-2} \le \beta_1 \le 2 \times 10^{-2}$ and $-5 \times 10^{-2} \le \alpha_H \le 2.6 \times 10^{-1}$ [14], while cosmological probes suggest $\mathcal{O}(1)$ constraints [57]. The result (7) implies for both parameters at 2σ as $-1.9 \times 10^{-3} \le \beta_1 \le 5.2 \times 10^{-3}$ and $-2.4 \times 10^{-3} \le \alpha_H \le 3.3 \times 10^{-3}$. The implications of Eq. (7) on the plane of (β_1, α_H) is shown in Fig. 2, and it is to be compared with the similar figure of Ref. [14].

Summary.—We proposed helioseismology as a highprecision test for the most general scalar-tensor theories (DHOST). We showed how the subtle fifth-force effect leaves a characteristic observable imprint on solar pulsations, and demonstrated the constraining power of our approach for the fifth-force coupling strength.

This is the first step towards a complete treatment of helioseismology in modified gravity, begging for further studies in the search of new exciting effects, and the confirmation of our results with a fully consistent approach. In particular, going beyond the Cowling approximation and the inclusion of helioseismic corrections will allow us to probe a broad part of the eigenspectrum. In turn, this calls for the construction of the modified nonlinear pulsations equations, along with accurate solar models in the presence of the fifth force. We leave these issues for future work.

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