Three-Photon Discrete-Energy-Entangled W State in an Optical Fiber

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We experimentally demonstrate the generation of a three-photon discrete-energy-entangled W state using multiphoton-pair generation by spontaneous four-wave mixing in an optical fiber. We show that, by making use of prior information on the photon source, we can verify the state produced by this source without resorting to frequency conversion.

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Multiphoton entangled states are a rich resource for fundamental tests of quantum mechanics [1-4], and they enable an array of powerful quantum communication protocols [5-7]. As the maximally entangled state of one of the two classes of genuine tripartite entanglement, the tripartite *W* state has a form

$$|W\rangle = \frac{1}{\sqrt{3}}(|bba\rangle + |bab\rangle + |abb\rangle), \qquad (1)$$

where $|a\rangle$ and $|b\rangle$ are orthogonal states. Multipartite entanglement is not a trivial generalization of bipartite entanglement [8], which has been extensively studied and demonstrated, and a W state cannot be transformed into a Greenberger-Horne-Zeilinger (GHZ) state [9,10] through local operations and classical communication (LOCC) [11]. Compared to a three-photon GHZ state, the entanglement of a three-photon W state is more robust against such loss, as the remaining two-photon system still retains some entanglement [12,13]. The W states with large numbers of photons enable clear violations of local realism and are more distillable than GHZ states in a noisy channel [14]. Although less studied than the GHZ state, the W state has been shown to have promising applications in quantum teleportation, superdense coding, and quantum key distribution [15–19].

To date, demonstrations of photonic W states have used the polarization degree of freedom (DOF) of photon pairs generated by spontaneous parametric down-conversion [20–24]. Entanglement in polarization is not always optimal for long-distance communication through optical fibers, due to polarization mode dispersion [25]; it was recently proposed [26] that a W state could be generated using the energy DOF, a possibility that has not yet been implemented. As the energy of a photon cannot be easily altered without a strong nonlinearity or modulating field, the propagation of an energy-entangled W state is inherently robust against decoherence. After transmission, if matrix transformations are required for further quantum processing, a wide range of demonstrated single-photon frequency conversion techniques [27-30] can be applied. Thus, it makes sense to study energy as a valuable DOF, even in the context of multipartite states. The scheme for generating a discrete-energy-entangled *W* state can be based on multipair generation in a single nonlinear material, which makes it relatively easy to implement in bulk optics while also potentially realizable in an integrated optics platform for enhanced scalability and efficiency [26,31].

In this work, we demonstrate the generation of a threephoton discrete-energy-entangled *W* state in an optical fiber. Simultaneous generation of two photon pairs through spontaneous four-wave mixing (SFWM) is followed by the energy-resolved detection of one of the photons. This method determines the *W* state that characterizes the other three photons, when postselected on a threefold coincidence. We verify the generation of the *W* state via a reduced density matrix technique [32]. Making use of prior information on the photon source and experiments that mix the channel outputs, we show that a sequence of coincidence measurements is sufficient to determine its density matrix without the need for frequency conversion.

The quantum state of photons generated in optical fibers through SFWM can be written as [26]

$$\begin{split} |\Psi\rangle &= (1 - O(|\beta|^2)) |\text{vac}\rangle + \beta a_B^{\dagger} a_R^{\dagger} |\text{vac}\rangle \\ &+ \frac{\beta^2}{2} (a_B^{\dagger})^2 (a_R^{\dagger})^2 |\text{vac}\rangle + \cdots, \end{split}$$
(2)

where $|\beta|^2$ is the probability of generating a photon pair, and a_B^{\dagger} and a_R^{\dagger} are the creation operators for signal (bluedetuned from the pump, referred to as blue or *B*) and idler (red or *R*) photons. We have truncated the expansion at second order, which corresponds to the creation of two photon pairs. While multipair generation is undesirable for



FIG. 1. (a) Schematic of the experimental setup for generation of the discrete-energy-entangled W state. (b) The setup used to measure coincidences for all possible energy combinations for the three channels j, k, and l, with the filters for measuring the $|Rj, Bk, Rl\rangle$ term shown as an example. The filters are chosen to pass either blue or red photons at each channel for the different projection measurements. (c) Nested interferometers used to measure the reduced density matrix. PMF is for polarizationmaintaining fiber, BP for bandpass filter, BS1-4 for beam splitter, LC for liquid crystal, D for dichroic mirror, RF for red filter, BF for blue filter, and APD for avalanche photodiode.

photon-pair sources, it can be used to produce multipartite entanglement; compared to using two independent photonpair sources, using one optical fiber to generate multipartite entanglement is much easier to implement while still having comparable generation efficiencies. After propagating through a series of beam splitters, shown in Fig. 1(a), the state (2) becomes [26]

$$|\Psi\rangle = \alpha |\Psi_0\rangle + \gamma \frac{1}{\sqrt{2}} [|B\rangle_i \otimes |W_1\rangle + |R\rangle_i \otimes |W_2\rangle], \qquad (3)$$

where $|\Psi_0\rangle$ encompasses all the terms not leading to a single photon per output channel, $|\alpha|^2 + |\gamma|^2 = 1$,

$$|W_1\rangle = \frac{1}{\sqrt{3}} (|RRB\rangle_{jkl} + |RBR\rangle_{jkl} + |BRR\rangle_{jkl}), \quad (4)$$

$$|W_2\rangle = \frac{1}{\sqrt{3}} (|BBR\rangle_{jkl} + |BRB\rangle_{jkl} + |RBB\rangle_{jkl}), \quad (5)$$

and i, j, k, l indicate channels. The second term of Eq. (3) can be taken as the relevant quantum state, assuming that the probability of generating more than two pairs at a time is negligible and that events associated with single pairs, as well as those without a single photon per channel, can be eliminated through the postselection of fourfold

coincidences. Depending on the detected energy of the photon exiting the first channel *i*, the photons exiting the other three channels *j*, *k*, and *l* are in one of the *W* states, $|W_1\rangle$ or $|W_2\rangle$. Note that, in general, among the three terms in (4) or (5), there will be relative phases associated with the different distances of the source from the three detectors (see Supplemental Material [33]). To retain the coherence of the superposition, two conditions must be met: (i) a coherence condition, which requires a typical path length difference ΔL smaller than the coherence length of each photon, i.e., $\Delta L \ll 2\pi/\Delta\kappa$, where $\Delta\kappa$ is the fluctuation of the blue and red photons; (ii) a stability condition, which requires $\delta(\Delta L) \ll 2\pi/\Delta k_0$, where $\delta(\Delta L)$ is the fluctuation of the path length difference, and $\Delta k_0 \equiv k_B - k_R$.

A schematic of our experimental setup is shown in Fig. 1(a). A 1-m polarization-maintaining optical fiber (PMF, PM780-HP) is pumped by a train of about 100-fs pulses with center wavelength 810 nm and repetition rate 80 MHz from a mode-locked Ti:sapphire laser. Pairs of sideband photons are created through SFWM: signal photons at 694 nm and idler photons at 975 nm. The reflection/transmission ratios of the beam splitters BS1-3 are chosen to be 25/75, 33/67, and 50/50, respectively, resulting in each photon having a probability of $\frac{1}{4}$ to arrive at each channel, maximizing the generation efficiency of the W state. Avalanche photodiodes (APDs, SPCM-AQ4C) are placed in each channel to detect the photons. A bandpass filter that only transmits blue is placed in front of detector *i*, such that a fourfold coincidence event corresponds to the postselection of the state $|W_1\rangle$ for the remaining three photons. The estimated photon-pair generation efficiency is about 0.02 per pulse for the minimal power we use in the experiment, which gives relatively low higher-order photon-pair generation but enough for detecting two-pair generation. The coupling efficiency and detector efficiency are 80% (75%) and 55% (11%) for signal (idler) photons. Note that the fourfold coincidence rates are already shown in Fig. 2(b).

With moderate pump power (~20 mW), we first measure fourfold coincidences involving a blue photon in channel *i* and all possible combinations of energies for the other three channels, namely, $|RRR\rangle_{jkl}$, $|RRB\rangle_{jkl}$, $|RBR\rangle_{jkl}$, $|BRR\rangle_{jkl}$, $|RBR\rangle_{jkl}$, $|BRR\rangle_{jkl}$, $|RBR\rangle_{jkl}$, $|BRR\rangle_{jkl}$, and $|BBB\rangle_{jkl}$. Figure 1(b) shows the setup corresponding to the combination $|RBR\rangle_{jkl}$, with bandpass filters used to determine if blue or red photons are detected in each channel. The extracted probabilities are plotted in Fig. 2(a), in which the three terms $|RRB\rangle_{jkl}$, $|RBR\rangle_{jkl}$, and $|BRR\rangle_{jkl}$, associated with the state $|W_1\rangle$, are dominant with approximately 33% probability each. The other terms are small and come from higher-order pair generation and Raman noise; the lack of counts for the $|BBB\rangle_{jkl}$ term indicates there are no contributions from dark counts. Figure 2(b)



FIG. 2. (a) Measured probabilities of all possible energy combinations. Note that $|RRB\rangle_{jkl}$, $|RBR\rangle_{jkl}$, and $|BRR\rangle_{jkl}$ are dominant components with about $\frac{1}{3}$ probability, which is as expected for the $|W_1\rangle$ state. (b) Logarithmic plot of fourfold coincidence measurements as a function of pump power. The black, blue, and red lines are linear least-squares fits for states $|RBR\rangle_{jkl}$, $|RRB\rangle_{jkl}$, and $|BRR\rangle_{jkl}$, with slopes of 4.02 ± 0.04 , 4.06 ± 0.08 , and 4.00 ± 0.03 , respectively.

shows the fourfold coincidence counts for the three dominant terms as a function of the pump power. Leastsquares fits show that, as expected, the fourfold coincidences scale with the fourth power of the pump power, which confirms that these terms arise from two-pair generation. The imbalance between these three terms arises from the imperfection of the beam splitters.

These measurements are not sufficient to completely characterize the postselected three-photon state. Indeed, the appropriate incoherent mixture of $|RBR\rangle_{jkl}$, $|RRB\rangle_{jkl}$, and $|BRR\rangle_{jkl}$ would lead to the same results as state $|W_1\rangle$ of Eq. (4).

To reconstruct the density matrix of the generated state, we make use of a strategy based on the so-called "reduced density matrix approach." It was recently shown that some classes of multipartite entangled states, including three-photon W states, can be determined by constructing a set of reduced density matrices [32]. This approach was tested

experimentally via nuclear magnetic resonance in a molecular sample, where the high fidelities between the results of full quantum state tomography and those deduced from two-particle reduced density matrices were found to be robust against experimental noise [32]. Here we use this method to characterize our photonic state. In our case one needs to reconstruct the three reduced density matrices associated with the detection of a red photon in one of the channels j, k, or l following the detection of a blue photon in channel i.

For example, in the case of the detection of a red photon in channel *j*, the generic density operator ρ^{I} describing the photons exiting channels *k* and *l* for experimental runs involving two photons in those channels [see Fig. 1(c) and the Supplemental Material [33]] is

$$\rho^{\rm I} = \sum_{a,b=1}^{10} |a\rangle \langle a|\rho^{\rm I}|b\rangle \langle b| \equiv \sum_{a,b=1}^{10} |a\rangle \rho^{\rm I}_{ab} \langle b|, \qquad (6)$$

where $|1\rangle = |RR,0\rangle_{kl}$, $|2\rangle = |R,R\rangle_{kl}$, $|3\rangle = |0,RR\rangle_{kl}$, $|4\rangle =$ $|RB,0\rangle_{kl}, |5\rangle = |R,B\rangle_{kl}, |6\rangle = |B,R\rangle_{kl}, |7\rangle = |0,RB\rangle_{kl},$ $|8\rangle = |BB,0\rangle_{kl}, |9\rangle = |B,B\rangle_{kl}, \text{ and } |10\rangle = |0,BB\rangle_{kl}.$ To determine the matrix elements ρ_{ab}^{I} , a traditional quantum state tomography approach would involve projections on linear combinations of the states of different energies [37], which, for the large energy differences of our source, would require frequency conversion [38,39]. However, in our case we can take advantage of prior information on our source: (1) photons are emitted in pairs by nondegenerate SFWM, and (2) the probability for higher-order pair generation is small. Relying on energy conservation, we thus set to zero all the elements corresponding to photon pairs in which both photons have the same energy (i.e., $|1\rangle$, $|2\rangle$, $|3\rangle$, $|8\rangle$, $|9\rangle$, $|10\rangle$). In our case, this procedure leads to a systematic error of about 3% given the coincidence-to-accidentals ratio of 30 [see Fig. 2(a)]. The resulting matrix corresponds to a particular class of states that belong to a much smaller Hilbert space and can be characterized through a sequence of linear measurements (see Supplemental Material [33]). We also notice that, since we demonstrate the generation of an energy-entangled W_1 state in postselection on fourfold coincidences, to reconstruct the state of photons exiting different channels, we only need to determine the elements $\rho_{55}^{\rm I}, \rho_{56}^{\rm I}, \text{ and } \rho_{66}^{\rm I}.$

To determine these elements without frequency conversion, however, we need to go beyond LOCC measurements that would be involved in application protocols of W states with parties at separated sites j, k, l. We build two nested interferometers, as shown in Fig. 1(c). From channel l, blue and red photons travel through an offset Sagnac interferometer closed by a dichroic mirror (D). The phases ϕ_B and ϕ_R acquired along the blue and red paths, respectively, are controlled independently using two liquid crystal (LC) plates. The output from the Sagnac interferometer is combined with that from channel k by a 50/50 beam



FIG. 3. (a) Single-photon spectrum of blue (blue solid line) and red (red dashed line) photons. (b) Single-photon interference counts of blue (blue circles) and red (red triangles) photons after the interferometers as a function of voltage across the liquid crystals. The black circles with arrows indicate the voltages across the liquid crystals that are chosen for phases ϕ_B and ϕ_R .

splitter outputting into two new channels labeled m and n. Dichroic mirrors are placed in channels m and n to separate blue and red photons and facilitate their spectral analysis using four detectors. Finally, bandpass filters are used to suppress pump and Raman noise before detection, which is performed using avalanche photodiodes.

As mentioned before, observing this discrete-energy entangled W state requires that coherence and stability conditions are met. The spectra of the blue and red photons, shown in Fig. 3(a), are measured using a singlephoton-level spectrometer (Andor Shamrock 500i/iDus 420). The measured bandwidths of 2.1 nm (blue) and 4.3 nm (red) allow a value of up to approximately 112 μ m for the path length difference to satisfy the coherence condition. The effective path length difference can be identified by checking the single-photon interference of blue and red photons after the interferometers in Fig. 1(c). Because of differing thicknesses of glass in the paths of the blue and red photons, there is an additional delay for the red photons. We insert a pair of wedges in the path of the blue photons within the Sagnac interferometer to compensate for this delay. The stability condition requires the nested interferometers to be phase stable with fluctuations in the path length $\delta(\Delta L) \ll$ 1.7 µm. The use of an offset Sagnac geometry provides stability for the inner interferometer. A reference diode laser is sent through the nested interferometers for active stabilization of the outer interferometer. The phases ϕ_B and ϕ_R are determined through single-photon interference of blue and red photons as the voltage across the liquid crystals is tuned.

By means of coincidence measurements on photons exiting channels *m* and *n* with phases ϕ_B and ϕ_R set to 0 or $\pi/2$, we find [33] that

$$\operatorname{Re}(\rho_{56}^{\mathrm{I}}) = \frac{1}{2} \left[1 - P_{\mathrm{BR}}^{(m,n)}(0,0) - P_{RB}^{(m,n)}(0,0) - P_{\mathrm{BR}}^{(m,n)}\left(\frac{\pi}{2},\frac{\pi}{2}\right) - P_{\mathrm{RB}}^{(m,n)}\left(\frac{\pi}{2},\frac{\pi}{2}\right) \right],$$

$$\operatorname{Im}(\rho_{56}^{\mathrm{I}}) = \frac{1}{2} \left[P_{\mathrm{BR}}^{(m,n)}\left(0,\frac{\pi}{2}\right) + P_{RB}^{(m,n)}\left(0,\frac{\pi}{2}\right) - P_{\mathrm{BR}}^{(m,n)}\left(\frac{\pi}{2},0\right) - P_{\mathrm{RB}}^{(m,n)}\left(\frac{\pi}{2},0\right) \right],$$
(7)

where $P_{BR}^{(m,n)}(\phi_B, \phi_R)$ is the probability of a coincidence detection of a blue and a red photon exiting channels *m* and *n* when phases ϕ_B and ϕ_R are applied, respectively. The circled voltages in Fig. 3(b) are the experimental set points for the 0 or $\pi/2$ phase as needed in (7), which is derived assuming zero phase difference between the two arms of the outer interferometer. Finally, ρ_{55}^{I} and ρ_{66}^{I} are measured by simply excluding the last 50/50 beam splitter [BS4 in Fig. 1(c)]. A full characterization of the tripartite *W* state is then obtained by iterating the entire procedure on photons exiting from channels *j*,*l* and channels *k*,*j*. In all cases, we postselect upon the detection of a blue photon in *i* and a red photon in the remaining channel.

The real and imaginary parts of the reconstructed reduced density matrices describing the photon pairs exiting from different channels upon the detection of a red photon in channel j, k, or l are shown in Fig. 4. Please note that we did not subtract accidentals in any of the measured terms. The uncertainties characterizing both the phase instability and the Poissonian statistics of the counts are indicated by the error bars. From these results we can reconstruct the density matrix of the generated state, and we confirm that this is the discrete-energy-entangled W state $|W_1\rangle$ in (4) with an estimated fidelity of 92% \pm 6% and an estimated purity of $90\% \pm 10\%$ (see Supplemental Material [33] for the W state density matrix). The fidelity and purity are overestimated due to small but finite counts in some of the zeroed elements; based on Fig. 2(a), the contribution of this systematic error is less than the statistical error of the measured values.



FIG. 4. The real (left) and imaginary (right) parts of the reconstructed reduced density matrices for k,l (top), j,l (middle), and k, j (bottom) channels. The error bars represent the uncertainty due to phase instability and statistical noise.

In summary, we have successfully observed the generation of a discrete-energy-entangled *W* state produced in polarization-maintaining fiber via SFWM. We characterized the state without implementing any frequency conversion, taking advantage of previous information on the source, the reduced density matrix strategy, and experiments that mix the output of different channels. The reconstructed reduced density matrix shows good fidelity to the expected state. With its robustness against noise and loss, we anticipate the discrete-energy-entangled *W* state and this characterization method to find useful applications in future quantum information protocols.

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