

From Stress Chains to Acoustic Emission

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A numerical scheme using the combined finite-discrete element method is employed to study a model of an earthquake system comprising a granular layer embedded in a formation. When the formation is driven so as to shear the granular layer, a system of stress chains emerges. The stress chains endow the layer with resistance to shear and on failure launch broadcasts into the formation. These broadcasts, received as acoustic emission, provide a remote monitor of the state of the granular layer of the earthquake system.

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Low frequency earthquakes [1], nonvolcanic tremor [2–4], and acoustic emission [5,6] are examples of weak seismic signals that may serve as harbingers of a major seismic event, an earthquake [7]. In a laboratory setting [8], in which stick-slip events are simulated, acoustic emission is detected far from the stick-slip events [9]. Recent machine learning and related studies [10,11] of acoustic emission are able to use it to predict location in the seismic cycle; i.e., the evolution of acoustic emission as a stick-slip scenario unfolds allows one to follow the scenario and anticipate the subsequent earthquake. In all cases, field and laboratory, the signals involved are sourced or detected in a volume remote from the volume that spawns the earthquake. These findings bring to the fore the question of the causal relationship between signals detected on passive, remote monitors and the dynamics of the elastic structures that launch important seismic events. In this Letter we introduce a numerical model that lets us follow this causality, i.e., examine and connect the dynamics in a granular system (fault gouge), to signals detected on passive remote monitors. Thus we show that stress chains [12,13] are the principals in the dynamics of the granular system and that this dynamics is the source of the acoustic emission. The numerical model necessarily combines discrete element method (DEM) to describe grain-grain interactions and finite element method (FEM) to describe elasticity within grains and wave propagation away from the granular system [14–16]. More details about the finite-discrete element method can be found in the Supplemental Material [17].

The numerical model, two dimensional, comprises a gouge layer of approximately $50 \times 1 \text{ cm}^2$ sandwiched between two $50 \times 25 \text{ cm}^2$ pieces of formation [26] (Fig. 1). The gouge layer is filled with particles (disks) of two diameters, 1.2 and 1.6 mm, and each particle is represented by 24 approximately equal size constant strain triangular FEM elements. The particles are in contact with one another and with the formation via a penalty function

based contact interaction algorithm [27]. A normal force N is applied to the bottom edge of the lower formation piece, essentially rigid, that is fixed in x . The top edge of the upper formation piece, also essentially rigid and fixed in y , is driven uniformly at constant velocity V_0 in the x direction. The material density and elastic properties of gouge, formation, and the top (bottom) edge of the formation piece are recorded in Table I of the Supplemental Material [17], in which more details about the model setup are also included.

Typically, the state of the system is set by a choice of V_0 and N : in the example here, $V_0 = 0.50 \text{ mm/sec}$ and $N = 28 \text{ kPa}$. The basic output is the shear and normal forces between the formation and gouge [28]. This is shown in Fig. 2 as a coefficient of friction (black line), $\mu = (\text{shear force})/(\text{normal force})$, versus time.

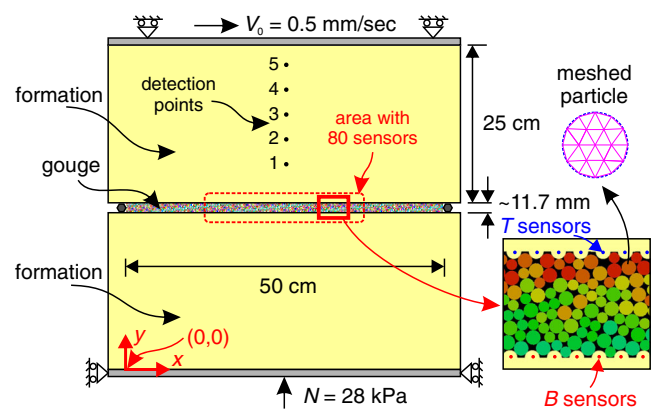


FIG. 1. Model system. The formation and the interior of the particles are described with a FEM scheme. The contacts of gouge particles with one another and with the formation are described with a DEM scheme. The formation has a rough surface profile (lower right). Sensors in the formation surface, adjacent to the gouge, are spaced by 2.4 mm. The elastic properties of gouge and formation are listed in the Supplemental Material [17].

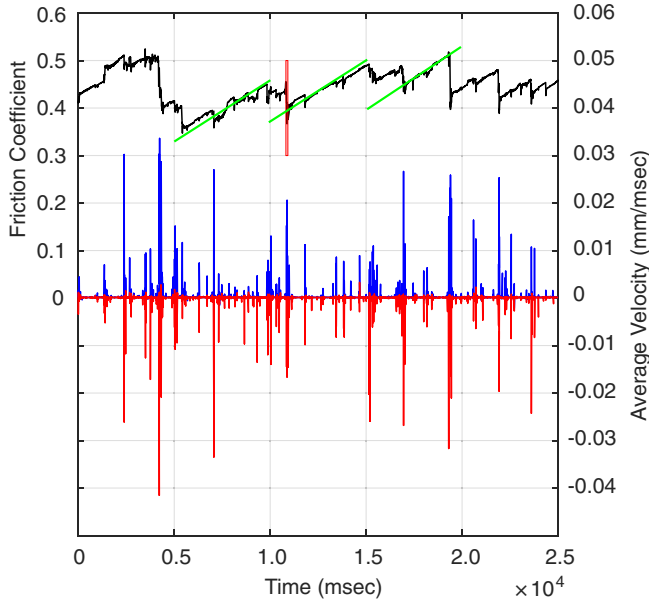


FIG. 2. Primary outputs. The coefficient of friction (black line) as a function of time, left-hand scale. The average velocity of the top (T , blue line) and bottom (B , red line) sensors as a function of time, Eq. (1), right-hand scale. The green lines, all of the same slope, show the average elasticity of the gouge. The stress drop near 11000 msec (marked by red line) is examined in Fig. 3.

This stress-time pattern has several qualities of note. There is on average a linear stress-time relationship that is punctuated by many small and a few large stress drops. Compressive structures form in the gouge that push back against the effort of the upper formation piece to drag the lower formation piece along [12,13]. The three green lines, all with the same slope, illustrate the underlying springlike character of the elasticity of the gouge. Large stress drops occur irregularly in time. The stress values at which large stress drops occur vary markedly; i.e., there is no single stress at which the system fails.

To begin to look at the dynamics of the system we look at the behavior of the formation immediately adjacent to the gouge. At the top of the gouge (T) (at the bottom of the upper formation piece) and at the bottom of the gouge (B) (at the top of the lower formation piece) there are 80 uniformly spaced sensor pairs that detect the motion of the formation, i.e., the velocity of the formation point with which the sensor is identified. In Fig. 2 we plot the average x velocity of 80 T sensors (sensors just above the gouge and near its center) as a function of time, $\bar{V}_X^T(t)$ (blue),

$$\bar{V}_X^T(t) = \frac{1}{80} \sum_{n=1}^{80} V_X^T(t, n), \quad (1)$$

where $V_X^T(t, n)$ is the x component of the velocity of T sensor n at time t . The velocity $\bar{V}_X^T(t)$ has a background value of approximately 0.25 mm/sec ($V_0/2$) from which

there are spikes in velocity that coincide with sharp, large stress changes. In Fig. 2 we also plot the average x velocity of the 80 associated B sensors (sensors just below the gouge and near its center) as a function of time, $\bar{V}_X^B(t)$ (red). The velocity $\bar{V}_X^B(t)$ also has a background velocity of approximately 0.25 mm/sec. From this background there are spikes in $\bar{V}_X^B(t)$ that coincide with sharp, large stress changes. The spikes in $\bar{V}_X^B(t)$ are *opposite* in sign from the spikes in $\bar{V}_X^T(t)$. That is, attending sharp, large stress changes are sharp, large velocity dipoles delivered to the formation. We focus on these velocity dipoles. To characterize them we form the velocity dipole field

$$D(t, n) = \frac{V_X^T(t, n) - V_X^B(t, n)}{2} \quad (2)$$

that has a value at each moment of time t at each sensor n ; see the Supplemental Material [17]. The spectrum of values of $D(t, n)$, shown in Fig. 3(a), is broadly distributed, $10^{-8} < D(t, n) < 0.2$. We use the magnitude of the velocity dipole field to form a detailed picture of the space-time structure of events in the gouge. This is illustrated in Figs. 3(b) and 3(c) for the large stress drop ($\Delta\mu/\mu \approx 0.2$) near 11 000 msec in Fig. 2. Figure 3(b) is an enlargement of the stress drop; Fig. 3(c) shows the space-time points at

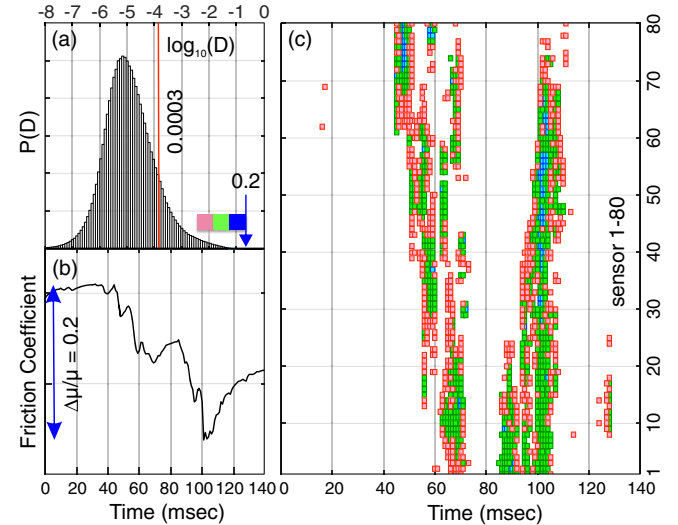


FIG. 3. Spectrum of velocity dipole strengths D . (a) The spectrum of velocity dipole strengths, for all space-time points, Eq. (2), is broadly distributed from 10^{-8} to approximately 0.2. The space-time points (n, t) with large D [in the 3 intervals red, green, blue on the lower right in (a)] are used to identify events. The stress near 11 000 msec in Fig. 2 is shown in detail in (b). Time is measured from 11 000 msec, where $\mu = 0.45$; i.e., time 0 msec here corresponds to time 11 000 msec in Fig. 2. The velocity dipole strength at (n, t) for this time interval is shown in (c), where the time axis is the same as in (b) and n is on the vertical axis. The velocity dipole strength is shown with the color coding from (a).

which the velocity dipole field is large. The sharp drop in Fig. 2 is ragged in close up, Fig. 3(b), and involves a complex set of events throughout much of the gouge, Fig. 3(c). We employ the velocity dipole field to establish the connection between stress chains, that live in the gouge, and the displacement field in the formation, far from the gouge, i.e., stress chains $\rightarrow D(t, n) \rightarrow$ acoustic emission.

To this end, we use the velocity dipole field to locate and examine small, simple events. In Fig. 4(a) there are 3 stress drops of modest size ($\Delta\mu/\mu \approx 0.002$, about 1% of the stress drop in Fig. 3). We look in detail at the third of these stress drops, Fig. 4(a). This stress drop occurs rapidly in time, lasting approximately 3 msec, and locally in space, involving large $D(t, n)$ at about 20 sensors, Fig. 4(b). To see more details we examine $V_X^T(t, n)$ and $V_X^B(t, n)$ separately in Fig. 4(c). We see that while $V_X^T(t, n)$ and $V_X^B(t, n)$ are simultaneous in time, they are structured in space. The B sensors contributing to the velocity dipole field are further along in x than the associated T sensors. The structural feature in the gouge, that upon failure delivers the forces that produce the velocity dipole field in the formation, acts like a strut. It is tethered to the formation so that it can deliver a shear stress that crosses the gouge and gives the gouge (an unconsolidated material) a shear modulus. We characterize the spatial structure of the velocity dipole field associated with small events like that in Fig. 4(b) with a measure of the separation of the points of tether, $\Delta n = -n_X^B - n_X^T$,

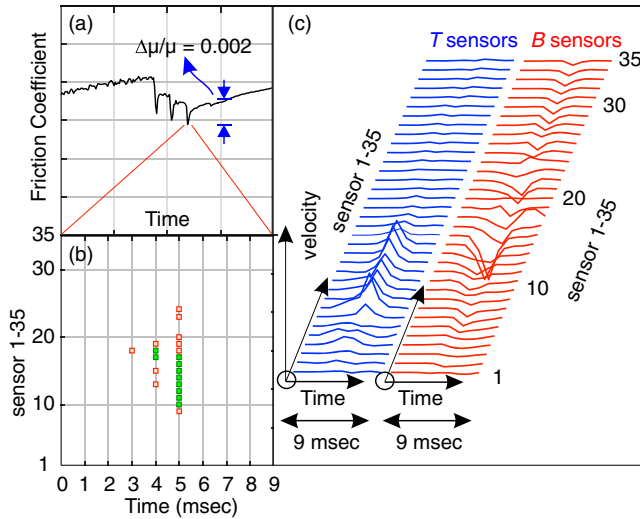


FIG. 4. Details of a small, simple event. (a) Friction coefficient versus time for 3 adjacent small events that have stress drop a few percent of a major event such as the one in Fig. 3(b). These events are near time 25 500 msec, where $\mu = 0.47$. (b) The velocity dipole strengths associated with the third event in (a), on sensors 1–35, color coded from Fig. 3(a), for 9 msec measured from time 25 545 msec. (c) Velocity dipole composition during the 9 msec interval in (b): the velocity of the top sensor set (blue line) and the velocity of the bottom sensor set (red line), displaced to the right for clarity.

$$n_X^* = \frac{\sum_n n d_X^*(n)}{\sum_n d_X^*(n)}, \quad d_X^*(n) = \int dt V_X^*(t, n), \quad (3)$$

where the integral on t and the sum on n are over a domain that surrounds the small event, $d_X^*(n)$ is the displacement of sensor n , and n_X^B (n_X^T) is typically negative (positive). For the spectrum of $r_F = 2.4\Delta n/H$, we find the result shown in Fig. 5, where H is the nominal gouge layer thickness and 2.4 mm is the spacing between sensors. The average value of r_F is ≈ 0.5 , and there are both positive and negative values of r_F .

We turn from examination of the motion of the formation, as evidenced in the behavior of the velocity dipole field, to the examination of forces in the gouge. To do this, for each element in a gouge particle at each time t , we find the maximum principal stress. We take this stress to characterize the force the element is carrying. When the elements carrying large stress are marked with a black dot, an oriented fabric of large stresses that cross the gouge is revealed, Fig. 6. Isolated stress chains are an important component of this fabric. These chains are oriented approximately as suggested by the velocity dipole field; see, e.g., Fig. 4(c). To make a quantitative comparison of the force fabric with the velocity dipole field, we characterize isolated stress chains that cross the gouge with $r_G = \Delta X/H$, where ΔX is the projection of the chain figure onto the x axis. The spectrum of r_G for isolated stress chains is shown in Fig. 5.

The velocity dipole field has been used to examine events that are local in space and time. The two components

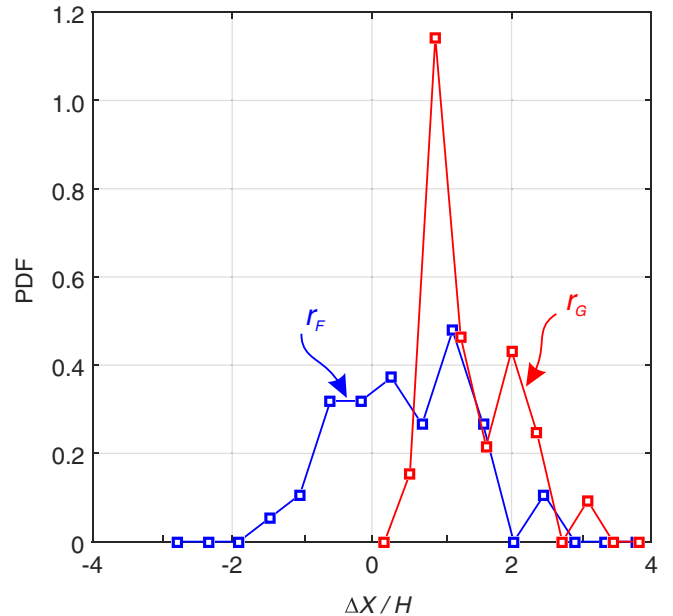


FIG. 5. Probability distribution functions (PDF). Probability distribution function of r_F for the separation of the two components of the velocity dipole field (small events), blue. Probability distribution function of r_G for isolated stress chains, red.

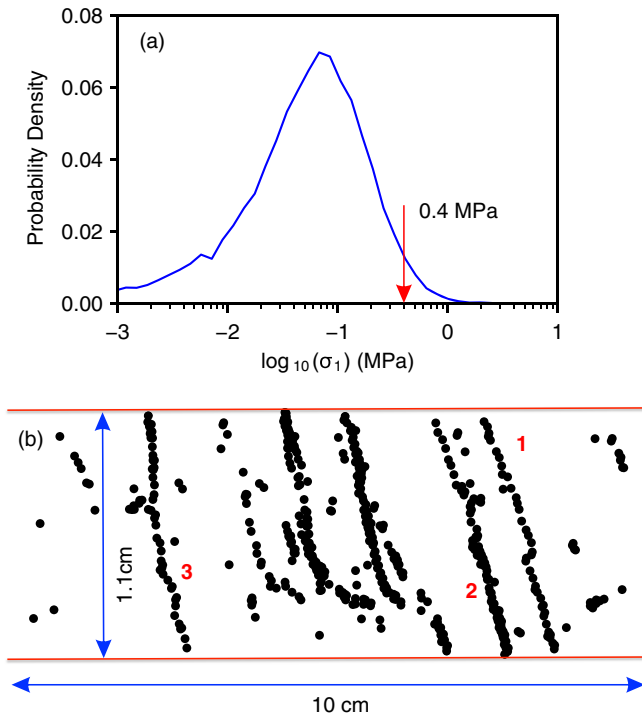


FIG. 6. Stress chains. (a) The spectrum of maximum principal stress of all elements in the gouge. (b) Elements in the FEM description of the particles, with maximum principal stress greater than 0.4 MPa. Each black dot represents the centroid position of the corresponding element. Two chains of elements at the right, 1 and 2, are judged to be isolated as is the chain 3 on the left. These chains are among the chains used to form the PDF of r_G in Fig. 5.

of the velocity dipole field reveal details about the structure in the gouge that produced the event. Often forces are delivered to the T sensors that are upstream from the forces delivered to the B sensors. This orientation mirrors the orientation of the fabric of forces in the gouge, Fig. 6. The most extreme components of this fabric are the isolated linkages that reach from T to B . From Figs. 5 and 6 there are more complex structures in the force fabric. On failure these structures deliver forces to T and B that are not easily identified with a simple geometry. Comparison of the spectrum of r_G and the spectrum of r_F confirms that the geometry of the stress chains is closely related to the geometry of the velocity dipole field.

We complete the argument, stress chain \rightarrow acoustic emission, by examining the motion of points in the formation far from the gouge, i.e., far from the velocity dipole field. This is done in Fig. S4 of the Supplemental Material [17], where it is seen that points in the formation remote from the gouge move much the same way as the velocity dipole field. The causality is stress chain \rightarrow velocity dipole field \rightarrow far field signal, i.e., acoustic emission. The complexity of the numerical model, gouge

plus formation, means that the simulations are quite long. Consequently, the formation does not have true far field points. The explicit near field demonstration in Fig. S4 could be complemented by use of the representation theorems in Aki and Richards [29] that would have the velocity dipole field as the source for broadcast into the formation.

By the evidence of Fig. 6(b) one might estimate the stress chains to be separated by approximately the average of their projection onto the x axis, a number of order H . This suggests that on average about 50 stress chains live in the gouge. A single stress chain on failure releases stress that is a few percent of the stress drop associated with a large slip. This is consistent with a large slip involving almost all of the extant stress chains, compare Figs. 3 and 4. In addition to assigning stress chains responsibility for time-sharp events, we assign the elasticity evidenced in the average rise in stress seen in Fig. 2 to their compression.

To conclude, we have employed a finite-discrete element method to model a sheared gouge layer. The formation adjacent to the gouge and the interior of the particles that comprise the gouge have linear elasticity that is resolved with a FEM treatment. Interactions of gouge particles with one another and with the formation, involving repulsive-only forces, are resolved with a DEM treatment. When at fixed normal force the system is sheared at constant drive velocity, the basic stress-time behavior shows intermittent large stress drops separated by intervals of approximately uniform elastic compression. The principal actors in the gouge are stress chains. Two sets of sensors at the gouge-formation interfaces allow determination of the velocity dipole field which describes the disturbance to the formation caused by the activity in the gouge. The motion of the formation far from the gouge, taken to be the acoustic emission, is monitored. Using the velocity dipole field we establish (a) the linkage between stress chains and the velocity dipole field and (b) the linkage between acoustic emission and the velocity dipole field. That is the relationship between the activity in the gouge and the far field. This is an example of a causal scenario that one might encounter and take advantage of in geophysical systems. Nonvolcanic tremor, low frequency earthquakes, etc., are far fields that may have a role in such a scenario. The great complexity of geophysical elastic systems makes the usefulness of such a scenario problematic. However, the rapid increase in the quality and quantity of reliable geophysical monitoring and the infusion of new, sophisticated analysis methods offer promise that such scenarios are foreseeable.

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- [1] D. R. Shelly, G. C. Beroza, S. Ide, and S. Nakamura, Low-frequency earthquakes in Shikoku, Japan, and their relationship to episodic tremor and slip, *Nature (London)* **442**, 188 (2006).
- [2] R. M. Nadeau and D. Dolenc, Nonvolcanic tremors deep beneath the San Andreas fault, *Science* **307**, 389 (2005).
- [3] G. C. Beroza and S. Ide, Slow earthquakes and nonvolcanic tremor, *Annu. Rev. Earth Planet Sci.* **39**, 271 (2011).
- [4] G. Rogers and H. Dragert, Episodic tremor and slip on the Cascadia subduction zone: The chatter of silent slip, *Science* **300**, 1942 (2003).
- [5] C. H. Scholz, *The Mechanics of Earthquakes and Faulting* (Cambridge University Press, Cambridge, England, 2002).
- [6] B. Rouet-Leduc, C. Hulbert, and P. A. Johnson, Continuous chatter of the Cascadia subduction zone revealed by machine learning, *Nat. Geosci.* **12**, 75 (2019).
- [7] K. Obara and A. Kato, Connecting slow earthquakes to huge earthquakes, *Science* **353**, 253 (2016).
- [8] B. M. Kaproth and C. Marone, Slow earthquakes, preseismic velocity changes, and the origin of slow frictional stick-slip, *Science* **341**, 1229 (2013).
- [9] P. A. Johnson, B. Ferdowsi, B. M. Kaproth, M. Scuderi, M. Griffa, J. Carmeliet, R. A. Guyer, P.-Y. Le Bas, D. T. Trugman, and C. Marone, Acoustic emission and microslip precursors to stick-slip failure in sheared granular material, *Geophys. Res. Lett.* **40**, 5627 (2013).
- [10] B. Rouet-Leduc, C. Hulbert, N. Lubbers, K. Barros, C. J. Humphreys, and P. A. Johnson, Machine learning predicts laboratory earthquakes, *Geophys. Res. Lett.* **44**, 9276 (2017).
- [11] T. A. Brzinski and K. E. Daniels, Sounds of Failure: Passive Acoustic Measurements of Excited Vibrational Modes, *Phys. Rev. Lett.* **120**, 218003 (2018).
- [12] J. F. Peters, M. Muthuswamy, J. Wibowo, and A. Tordesillas, Characterization of force chains in granular material, *Phys. Rev. E* **72**, 041307 (2005).
- [13] K. E. Daniels and N. W. Hayman, Force chains in seismogenic faults visualized with photoelastic granular shear experiments, *J. Geophys. Res. Solid Earth* **113**, B11411 (2008).
- [14] J. K. Morgan and M. S. Boettcher, Numerical simulations of granular shear zones using the distinct element method: I. Shear zone kinematics and the micromechanics of localization, *J. Geophys. Res. Solid Earth* **104**, 2703 (1999).
- [15] O. Dorostkar, R. A. Guyer, P. A. Johnson, C. Marone, and J. Carmeliet, On the micromechanics of slip events in sheared, fluid-saturated fault gouge, *Geophys. Res. Lett.* **44**, 6101 (2017).
- [16] A. A. Munjiza, *The Combined Finite-Discrete Element Method* (John Wiley and Sons, New York, 2004).
- [17] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.123.048003> for more details about the theory of FDEM and model setup, which includes Refs. [18–25].
- [18] M. P. Ciamarra, E. Lippiello, L. de Arcangelis, and C. Godano, Statistics of slipping event sizes in granular seismic fault models, *Europhys. Lett.* **95**, 54002 (2011).
- [19] C. Wang, D. Elsworth, and Y. Fang, Influence of weakening minerals on ensemble strength and slip stability of faults, *J. Geophys. Res. Solid Earth* **122**, 7090 (2017).
- [20] B. Ferdowsi, M. Griffa, R. A. Guyer, P. A. Johnson, C. Marone, and J. Carmeliet, Microslips as precursors of large slip events in the stick-slip dynamics of sheared granular layers: A discrete element model analysis, *Geophys. Res. Lett.* **40**, 4194 (2013).
- [21] A. Munjiza, Discrete elements in transient dynamics of fractured media, Ph.D. thesis, Swansea University, 1992.
- [22] A. Munjiza, E. E. Knight, and E. Rougier, *Large Strain Finite Element Method: A Practical Course* (John Wiley and Sons, New York, 2015).
- [23] R. Guises, J. Xiang, J.-P. Latham, and A. Munjiza, Granular packing: numerical simulation and the characterisation of the effect of particle shape, *Granular Matter* **11**, 281 (2009).
- [24] Z. Lei, E. Rougier, E. E. Knight, and A. Munjiza, A framework for grand scale parallelization of the combined finite discrete element method in 2d, *Comput. Part. Mech.* **1**, 307 (2014).
- [25] E. Knight, E. Rougier, and Z. Lei, Hybrid Optimization Software Suite (HOSS)—Educational Version, Technical Report No. LA-UR-15-27013, Los Alamos National Laboratory, 2015.
- [26] D. A. Geller, R. E. Ecker, K. A. Dahmen, and S. Backhaus, Stick-slip behavior in a continuum-granular experiment, *Phys. Rev. E* **92**, 060201(R) (2015).
- [27] A. A. Munjiza, E. E. Knight, and E. Rougier, *Computational Mechanics of Discontinua* (John Wiley and Sons, New York, 2011).
- [28] K. Gao, B. J. Euser, E. Rougier, R. A. Guyer, Z. Lei, E. E. Knight, J. Carmeliet, and P. A. Johnson, Modeling of stick-slip behavior in sheared granular fault gouge using the combined finite-discrete element method, *J. Geophys. Res. Solid Earth* **123**, 5774 (2018).
- [29] K. Aki and P. Richards, *Quantitative Seismology* (W.H. Freeman, San Francisco, 1980).