

Observation of Nonlocal Heat Flux Using Thomson Scattering

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Nonlocal heat flux was measured in laser-produced coronal plasmas using a novel Thomson scattering technique. The measured heat flux was smaller than the classical values inferred from the measured plasma conditions in regions with large temperature gradients and agreed with classical values for weak gradients. Vlasov-Fokker-Planck simulations self-consistently calculated the electron distribution functions used to reproduce the measured Thomson scattering spectra and to determine the heat flux. Multigroup nonlocal simulations overestimated the measured heat flux.

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In diverse fields of plasma physics, including astrophysics, inertial confinement fusion, and magnetohydrodynamics, classical thermal transport [1,2] provides the foundation for calculating heat flux [3–7]. The classical theories of thermal transport by Spitzer-Härm (SH) [1] and Braginskii [2] specify the heat flux by a local expression, in terms of the thermal conductivity κ and the electron temperature gradient (e.g., $\mathbf{q}_{\text{SH}} = -\kappa \nabla T_e$). This theory breaks down in the presence of large temperature gradients [8–11], turbulence [12], or return current instabilities [13–16]: classical theory does not include nonlocal effects where energetic electrons travel distances comparable with the temperature scale length before colliding.

Local thermal transport theories [1,2] follow from a perturbative solution of a kinetic equation in terms of the collision parameter $\lambda_{ei}/L_T \ll 1$, where λ_{ei} is the electron (e - i) mean free path and $L_T = |\nabla \ln(T_e)|^{-1}$ is the scale length of the temperature gradient. Nonlocal theories overcome limitations of classical theory by accounting for the range of electron-ion mean free paths associated with different electron velocities. By extending closure relations for hydrodynamic models into the kinetic regime of weak collisions, these theories [17–24] have established the limits of classical transport ($\lambda_{ei}/L_T \sim 10^{-2}$).

In laser-produced plasmas, classical theory predicts unphysically large thermal transport and hydrodynamic simulations of these plasmas require an *ad hoc* limiter on the heat flux to match experimental observables. Historically, these limiters were set by kinetic simulations [17,25–27], integrated experiments [10,11,28,29], or more-focused Thomson scattering (TS) measurements of the local plasma conditions (i.e., electron temperature and density) [8,13,30,31]. More recently, the nonlocal Schurtz, Nicolai, and Busquet (SNB) model [23] was introduced as

a computationally efficient method for calculating the nonlocal heat flux in large-scale multidimensional hydrodynamic simulations. Experiments that attempt to measure nonlocal transport have, however, been limited to indirect observations [8,24,30–32].

In this Letter, we present the first direct measurement of nonlocal heat flux. A novel implementation of collective Thomson scattering measured heat flux by probing the

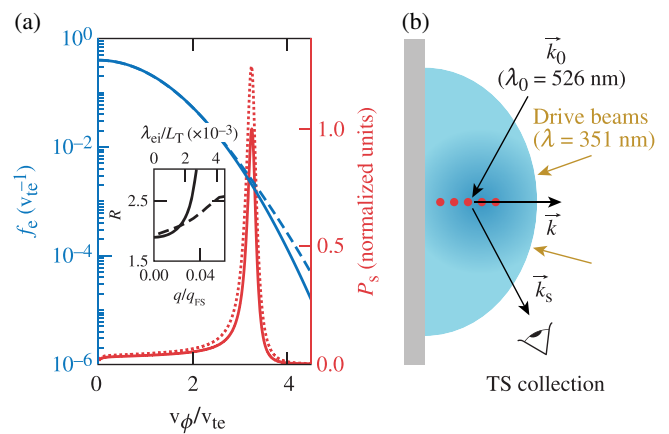


FIG. 1. (a) Calculated Thomson-scattering features (red curve, right axis) from electron plasma waves [Eq. (1)] are shown ($v_\phi = \omega/k$) using a Maxwellian (solid blue curve, left axis) electron distribution function and the non-Maxwellian (dashed blue curve) distribution that accounts for classical SH heat flux ($\lambda_{ei}/L_T = 2.2 \times 10^{-3}$, $q/q_{\text{FS}} = 3\%$). Inset: For a fixed normalized phase velocity, the ratio of the peak scattered power of the up- and downshifted features are shown for calculations that use classical SH (solid curve, top axis) and nonlocal (dashed curve, bottom axis) distribution functions over a range of heat flux. (b) A schematic of the setup is shown.

relative spectral amplitudes of electron plasma waves [Fig. 1(a)]. In addition to the heat flux, the plasma-wave spectrum provided a measurement of the plasma temperature and density profiles. The profiles were used to calculate the classical SH heat flux, which was in good agreement with the measured heat flux far from the target where the temperature scale length was longer than the electron-ion mean free path of heat-carrying electrons ($\lambda_{ei}/L_T \sim 7 \times 10^{-3}$). For steeper gradients, the measured heat flux was up to a factor of 2 smaller than the classical values as a result of nonlocal transport. For the most nonlocal conditions, the SNB model predicted an inhibited heat flux compared with the classical values but still overestimated the measured heat flux by $\sim 40\%$. In the region where classical SH theory agrees with the measured heat flux, the SNB model overestimates the flux.

Figure 1 illustrates the effect of heat flux on the collective Thomson scattering spectrum. Two scattering spectra, calculated with and without SH heat flux, demonstrate the sensitivity of the Thomson scattering spectrum to the shape of the electron distribution function. The SH distribution function was derived from the lowest-order terms in the perturbative solution of the kinetic equation, $f_{\text{SH}}(\mathbf{v}) = f_0^M(\mathbf{v}) + \cos\theta f(\mathbf{v})$, where $f(\mathbf{v}) = \lambda_{ei}/L_T \sqrt{2/9\pi} (\mathbf{v}/v_{te})^4 (4 - \mathbf{v}^2/2v_{te}^2) f_0^M(\mathbf{v})$, $v_{te} = \sqrt{T_e/m_e}$ is the electron thermal velocity, f_0^M is a Maxwellian velocity distribution function, and θ is the angle between electron velocity and the temperature gradient. The Thomson scattering spectra were calculated in the high-frequency limit where the ion dynamics can be ignored [33]

$$S(\mathbf{k}, \omega) = \frac{2\pi}{k} \frac{\tilde{f}_e(\omega/k)}{|\epsilon(\mathbf{k}, \omega)|^2}, \quad (1)$$

where $\epsilon(\mathbf{k}, \omega)$ is the longitudinal plasma dielectric function and the probed wave vector (frequency) is the difference between the incident and scattered wave vectors (frequencies), $\mathbf{k} = \mathbf{k}_i - \mathbf{k}_s$ ($\omega = \omega_i - \omega_s$). The one-dimensional distribution function $\tilde{f}_e(v)$ is determined by integrating the full distribution function over velocities perpendicular to the probed wave vector. At the Langmuir wave resonance defined by $\epsilon(\mathbf{k}, \omega) = 0$, $\omega(k) = \pm\omega_L(k) + i\gamma_L(k)$, where, in general, the Landau damping rate γ_L is proportional to $\partial\tilde{f}_e/\partial v|_{v=\omega_L/k}$ and ω_L is approximately the resonant frequency for Langmuir fluctuations. The collisionless approximation of $S(\mathbf{k}, \omega)$ in Eq. (1) is valid for these experiments as the scale of the probed waves ($\sim 1/k$) is small compared to the electron-ion mean free path such that $k\lambda_{ei} \gg 1$.

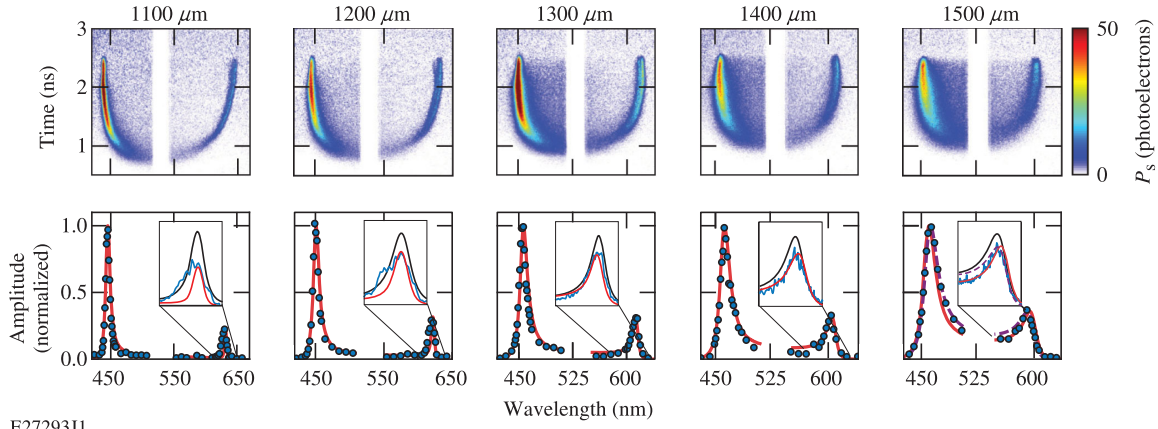
The Fig. 1 inset shows the sensitivity of the amplitude ratio of the up- and downshifted (red- and blueshifted, respectively) scattered peaks to heat flux (normalized to the free-streaming (FS) flux, $q_{FS} = n_e T_e v_{te}$), where SH or nonlocal distribution functions were used to calculate the Thomson scattering spectrum. It is evident from Eq. (1) that

heat flux has two effects on the scattered power near the resonance: (1) the amplitude depends on the number of electrons at the resonance [$\tilde{f}_e(\omega_L/k)$] and (2) the width is given by the slope of the electron distribution function at the resonance $\partial\tilde{f}_e/\partial v|_{v=\omega_L/k}$. Therefore, to maximize the effect of heat flux on the scattered power, the scattering geometry was chosen to probe Langmuir waves propagating along the target normal where the temperature gradient is the largest, $\mathbf{k} \parallel -\nabla T_e$, and with phase velocities near the region of the electron distribution function with the most heat-carrying electrons, $\omega_L/k \gtrsim 3.4v_{te}$. For this geometry, it was demonstrated in theory [34] that the Langmuir fluctuations that contribute to the redshifted peak in the Thomson scattering spectrum experience increased Landau damping, while the oppositely propagating Langmuir waves that contribute to the blueshifted peak become less damped.

The experiment was conducted at the Omega Laser Facility [35] at the University of Rochester's Laboratory for Laser Energetics and used six $\lambda_{3\omega} = 351$ -nm beams to produce a blow off plasma from a planar aluminum target. Each beam had 250 J in a 2-ns flat top pulse. Phase plates [36] were used to set the profile of the laser spot at the target plane to be a high-order super-Gaussian ($n = 4.6$) with a full width at half maximum of 560 μm . The six beams with the smallest angle of incidence ($8^\circ, 29^\circ, 32^\circ, 33^\circ, 35^\circ$, and 40°) were chosen to produce the plasma [Fig. 1(b)]. The Thomson-scattering diagnostic [37] consisted of a 40-J, 2-ns-long, $\lambda_{2\omega} = 526.5$ -nm probe beam with a best-focus diameter of $\sim 50 \mu\text{m}$ [38]. The light scattered from a $50 \times 50 \times 50 - \mu\text{m}$ volume was imaged through a 1/3-m spectrometer onto a streak camera. The spectral dispersion was $0.411 \text{ nm/pxl} \pm 0.4\%$. The system had spectral and temporal resolutions of $0.5 \text{ nm} \pm 5\%$ and $20 \text{ ps} \pm 0.5\%$, respectively. The scattering angle was 60° . The scattering volume was set to five different locations along the target normal ranging from 1.1 to 1.5 mm from the initial target surface. To account for the bremsstrahlung radiation collected by the Thomson-scattering system, a background was established at each location by turning off the Thomson scattering probe beam and was subtracted from the corresponding spectrum.

Figure 2 shows the collective Thomson-scattering spectra measured at each of the probed locations. The data were fit with a fully kinetic Thomson-scattered power spectrum [33] that includes relativistic effects [39] and incorporates a non-Maxwellian electron distribution function to provide a measure of the heat flux, electron temperature, and density [34]. To a good approximation, the relative amplitudes of the electron-plasma wave features are given by heat flux, the frequency of the electron plasma-wave feature by the density, and the width of the plasma wave feature by the electron temperature.

The insets in Fig. 2 compare scattered spectra calculated using non-Maxwellian electron distribution functions,



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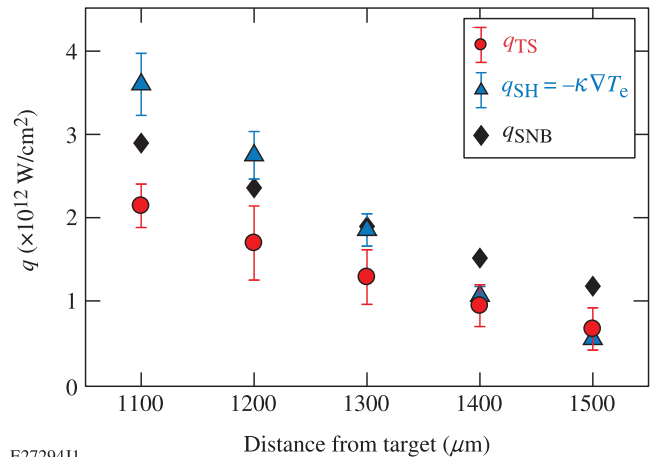
FIG. 2. The measured collective Thomson-scattering spectra (top row) and the corresponding spectral profiles (blue dots) at 1.5 ns (bottom row). The data were fit (red curves) with Eq. (1) using non-Maxwellian electron distribution functions to measure heat flux. Insets: The redshifted features are shown with calculations (black curves) that used the plasma conditions from the fit but a Maxwellian electron distribution function. These spectra recover the location of the scattering features but fail to match their amplitudes. At 1.5 mm, the spectrum was fit (dashed curve) with calculations that use a distribution function consistent with classical SH theory. All spectra are normalized to the peak scattered power.

consistent with thermal transport, with Maxwellian electron distribution functions. The excellent quality of the fits over the complete spectrum indicate the high accuracy of the shape of the distribution functions used. The significant deviation from the measured spectra that occurs when not accounting for the effects of heat flux (i.e., Maxwellian distribution functions) shows the sensitivity of the measurement. The non-Maxwellian distribution functions were determined from a Fokker-Planck simulation [40] where the electron temperature and density profiles were constructed to equal the measured values. Discrepancies between the shape of the measured and calculated spectra at the locations closest to the target suggest that the simulations do not accurately reproduce the electron distribution function far from the resonance and suggest that more work is needed.

Figure 3 shows the resulting heat flux measurements at the five probed locations obtained by integrating the electron distribution functions used to fit the Thomson-scattering (TS) spectrum [$q_{\text{TS}} = \int \frac{1}{2} m v^2 \mathbf{v} f_e(\mathbf{v}) d^3 \mathbf{v}$]. The measured heat flux is compared to classical heat flux values ($q_{\text{SH}} = -\kappa \nabla T_e$) determined by calculating the Spitzer thermal conductivity and the local temperature gradient from the measured plasma profiles (Fig. 4). Excellent agreement between the classical and measured heat flux is observed for the location farthest from the target surface, but for locations closer to the target surface, the measured flux is smaller than the classical values. This difference highlights the nonlocal nature of the thermal transport.

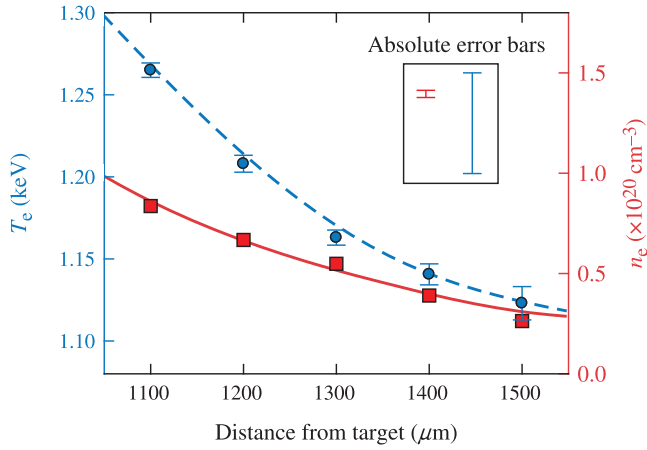
Figure 4 presents the measured electron temperature and density profiles determined from fitting the blueshifted features with the Thomson-scattering power spectrum, assuming Maxwellian electron distribution functions (Fig. 2). The electron temperature decreased from

1.27 ± 0.04 to 1.12 ± 0.04 keV over $400 \mu\text{m}$. The electron temperature gradient at each measurement location was determined by fitting a fifth-order polynomial to the measurements. The uncertainty in the temperature gradient was calculated by varying the data within the relative error bars, which were used to calculate the errors in the classical heat flux (Fig. 3). Over this same distance, the electron density dropped from $8.36 \pm 0.04 \times 10^{19} \text{ cm}^{-3}$ to $2.63 \pm 0.01 \times 10^{19} \text{ cm}^{-3}$. The high signal-to-noise ratio in the measured spectra resulted in excellent χ^2 statistical fits,



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FIG. 3. The heat flux (red points) measured along the target normal is compared with classical heat flux (SH) calculations (blue points) and heat flux values (black points) obtained from the simulations using the SNB model. Both the simulations and calculations were initiated with the measured electron temperatures and densities. For reference, $\lambda_{ei}/L_T = 1.4 \times 10^{-2}$, 1.4×10^{-2} , 1.3×10^{-2} , 1.0×10^{-2} , 7×10^{-3} at 1.1, 1.2, 1.3, 1.4, and 1.5 mm, respectively.



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FIG. 4. Electron temperature (blue dots, left axis) and density (red squares, right axis) measurements at $t = 1.5$ ns. Profiles of electron temperature (dashed blue curve) and density (solid red curve) used in Fokker-Planck simulations. The relative (1σ statistical) error bars are shown with the temperature measurements. The absolute error bars are represented in the inset.

which determined the 1σ statistical relative error bars shown in Fig. 4. The absolute errors in the electron temperature and density were dominated by uncertainties in the spectral dispersion and resolution. Adding these errors in quadrature resulted in a 2% and 3% absolute error in the density and temperature, respectively.

For the measurement farthest from the target surface (1.5 mm), the Thomson scattering spectrum calculated using the electron distribution function determined by classical SH theory, where $\lambda_{ei}/L_T = 7 \times 10^{-3}$, was in good agreement (Fig. 2). This is consistent with the agreement in the measured heat flux at this location presented in Fig. 3. Although the classical SH distribution function allows the amplitudes of the spectral peaks to be reproduced, the fit shows a discrepancy in the width of the redshifted peak suggesting that the shape of the SH electron distribution function moving away from the resonance is incorrect. For locations closer to the target, the electron distribution function predicted by classical theory becomes negative at velocities around the Langmuir wave resonances, and classical theory cannot be used to fit the measured spectrum. This is consistent with the measured heat flux being significantly less than the classical values (Fig. 3). At these locations $\lambda_{ei}/L_T > 10^{-3}$, which confirms, experimentally, the limit of validity previously determined by nonlocal theories [17–22].

To determine the electron distribution functions consistent with nonlocal transport, the $\kappa 2$ Vlasov-Fokker-Planck code [40] was used. $\kappa 2$ uses a Legendre polynomial representation of the electron distribution function, $f(t, x, \mathbf{v}) = \sum_n f_n(t, x, v) P_n(\theta)$ where x is the direction along the target normal. $\kappa 2$ solves for the self-consistent electric field and includes the effects of electron-ion

scattering and electron-electron collisions. To capture the fine detail in the distribution functions at high velocities, close to the Langmuir wave resonances, polynomials up to and including f_8 were required.

In all calculations, the plasma profiles were initially set to the measurements (Fig. 4). The temperature of the region between the target and 500 μm was constant and was varied from 1.2 and 2 keV in different runs. Since the transport is nonlocal, the choice of boundary condition is important to determine heat flow at the edge of the measurement region (i.e., 1.1 mm) but has a small effect at the other measurement positions. Once the initial conditions were set, the $\kappa 2$ code evolved the distribution function in time and, after a few collision times, reached steady state. Over this time, a small amount of heating or cooling was applied to the electrons to help maintain the temperature profile close to the measured (i.e., initial) values. This approximately accounted for the small amount of ongoing thermal compression or expansion in the coronal region. As the hydrodynamic motion is slow compared to the electron thermal transport, it was ignored. For each boundary condition, the electron distribution functions at each measurement position were used in Eq. (1) to calculate Thomson scattering spectra. The boundary condition (1.8 keV) that generated the Thomson scattering spectra with the best match across all locations was used to determine the measured heat flux. A given distribution function produces a unique scattering spectrum, but in practice, signal-to-noise and dynamic range limit measurements to regions around the resonances.

The measured heat flux was compared to calculations that used the multigroup nonlocal SNB model (Fig. 3), initialized with the measured electron temperature and density profiles (Fig. 4). In the nonlocal region, where classical SH theory overestimates the flux, the SNB model calculates a flux that is about halfway between the classical and measured values. In the region where classical transport is valid (1.5 mm), the SNB model overestimates the flux. Furthermore, in the nonlocal transport regions, the electron distribution functions were negative around the electron-plasma wave resonance, which made it impossible to fit the measured Thomson scattering spectrum.

Figure 5 shows the flux contribution of electrons for each of the models at 1.2 mm from the target surface. According to the $\kappa 2$ model, the reduction in heat flux relative to the classical model at this location occurs due to a reduction in the flux of electrons with $v \gtrsim 3.4 v_{te}$. Furthermore, the peak heat flow occurs at a lower velocity ($v_{\kappa 2} \approx 3.5 v_{te}$) relative to the classical result ($v_{SH} \approx 3.7 v_{te}$). The SNB model slightly inhibits the flux but still overpredicts the heat flow. The heat flux at this location is $\sim 60\%$ of the classical value.

In summary, Thomson scattering was used to measure the heat flux directly from the amplitudes of the Langmuir fluctuations and indirectly through the electron temperature and density profiles ($q_{SH} = -\kappa \nabla T_e$). The measured heat

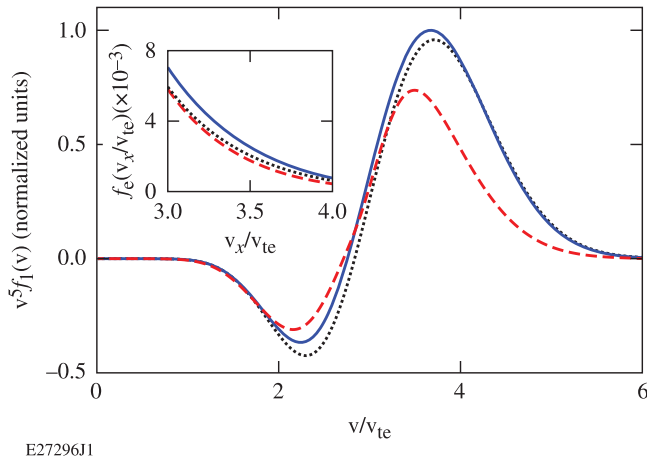


FIG. 5. The velocity-dependent contribution of heat flux is shown at $1200 \mu\text{m}$ for calculations using the Fokker-Planck (dashed red curve), classical (solid blue curve), and SNB (dotted black curve) models. Inset: The corresponding electron distribution functions are shown.

flux agreed with classical SH values when $\lambda_{ei}/L_T < 10^{-3}$, but in the opposite limit ($\lambda_{ei} > 10^{-3}$), the differences were as large as a factor of 2. The multigroup nonlocal SNB model overpredicted the flux in all regions which demonstrates the need to include physics often missing from computationally expedient nonlocal models, most notably high-order polynomials for properly resolving velocity space, the self-consistent electric field, and a Fokker-Planck collision operator.

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