## Ultrahigh-Density Spin-Polarized H and D Observed via Magnetization Quantum Beats

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We measure nuclear and electron spin-polarized H and D densities of at least  $10^{19}$  cm<sup>-3</sup> with ~10 ns lifetimes, from the photodissociation of HBr and DI with circularly polarized UV light pulses. This density is ~6 orders of magnitude higher than that produced by conventional continuous-production methods and, surprisingly, at least 100 times higher than expected densities for this photodissociation method. We observe the hyperfine quantum beating of the H and D magnetization with a pickup coil, i.e., the respective 0.7 and 3 ns periodic transfer of polarization from the electrons to the nuclei and back. The  $10^{19}$  cm<sup>-3</sup> spin-polarized H and D density is sufficient for laser-driven ion acceleration of spin-polarized electrons, protons, or deuterons, the preparation of nuclear-spin-polarized molecules, and the demonstration of spin-polarized D-T or D-<sup>3</sup>He laser fusion, for which a reactivity enhancement of ~50% is expected.

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High-density spin-polarized hydrogen (SPH) isotopes are crucial for the measurement of spin-dependent effects in atomic, particle, nuclear, and plasma physics [1–3]. However, many applications are limited or precluded by the inability to produce high densities: Polarized laser fusion and laser ion acceleration of hydrogen isotopes require densities of at least  $10^{18}$  and  $10^{19}$  cm<sup>-3</sup>, respectively. In contrast, conventional methods such as spin-exchange optical pumping (SEOP) or Stern-Gerlach spin separation produce low densities of only ~ $10^{13}$  [4,5] and ~ $10^{12}$  cm<sup>-3</sup> [1], respectively.

Recently, our group has demonstrated the production of highly spin-polarized deuterium (SPD) from the photodissociation of DI with circularly polarized UV light [6]. The ability to produce SPD densities of  $10^{18}$  cm<sup>-3</sup> with lifetimes of ~1 ns was projected (equivalent to ~ $10^{17}$  cm<sup>-3</sup> with lifetimes of 10 ns), assuming SPH depolarization rates similar to those from collisions with alkali atoms (depolarization rates from halogen atoms are not known).

Here, we demonstrate the production of spin-polarized H (SPH) and D (SPD) densities of at least  $10^{19}$  cm<sup>-3</sup>, with ~10 ns lifetimes, from the photodissociation of HBr, DI with 0.15 ns, 213 and 266 nm laser pulses, respectively. These SPH densities are at least 100 times higher than projected for depolarization from alkali atoms [6–9], as the SPH depolarization rates from halogen atoms are at least 100 times smaller than expected. In addition, we determine that the SPD is depolarized via a DI-D intermediate species, which helps explain the long ~10 ns polarization lifetimes, as the depolarization rate unexpectedly saturates at high pressures. Therefore, even higher densities are possible.

The  $10^{19}$  cm<sup>-3</sup> SPH or SPD densities allow at least three new applications: (1) the demonstration and study of polarized laser fusion [9] using >5 kJ pulses offered at several laser facilities [10–12]; (2) polarized ion acceleration with SPH densities of  $10^{19}$ – $10^{21}$  cm<sup>-3</sup> for wavelengths of 10–1  $\mu$ m, respectively [13]; (3) maximizing the production of spin-polarized molecules in the NMR detection volume, for signal enhancement requiring gas densities of >10<sup>19</sup> cm<sup>-3</sup>.

Our approach to creating ultrahigh densities of spinpolarized atoms is to take advantage of the ultrafast  $(\sim 100 \text{ fs})$  timescales of the UV photodissociation. Such a rapid process generates, nearly instantaneously, highly electronically polarized atoms [14-20] at the original density of the parent molecules, before there is time for depolarization, allowing extremely high densities. Subsequently, the hyperfine interaction transfers polarization from the electronic to the nuclear spin in  $\sim 1$  ns [21]. which is  $\sim 6$  orders of magnitude faster than the polarization step of conventional methods [4,22]; therefore, highly nuclear-spin-polarized atoms can also be produced at ultrahigh density, on nanosecond timescales. However, spinpolarized atom densities higher than  $10^{12}$  cm<sup>-3</sup> have not yet been verified from photodissociation, because the optical detection methods used so far fail at a high density [17].

The rapid production of large numbers of spin-polarized H or D atoms, and the polarization transfer between the electrons and nuclei, creates a large time-dependent electron magnetization  $M_e(t) = 2n\langle m_s(t) \rangle$ . The expectation values of the *m*-state projections for the electronic  $\langle m_s(t) \rangle$  and nuclear spin  $\langle m_I(t) \rangle$ , for H and D, are given, for  $t \ge 0$ , by [21,23,24]

$$\langle m_s(t)\rangle = \frac{1}{2}e^{-t/\tau_p}[1 - \alpha \sin^2(\omega t/2)], \qquad (1)$$

$$\langle m_I(t)\rangle = \frac{1}{2}e^{-t/\tau_p}[\alpha \sin^2(\omega t/2)], \qquad (2)$$

where  $\alpha = 1$  for H,  $\alpha = 32/27$  for D, and  $\omega = 2\pi\nu$  is the angular hyperfine frequency for H or D [25,26]. The timedependent magnetization creates a current in a pickup coil (2 mm diameter, 5 mm long, 4.5 turn) through the voltage (EMF) (see Fig. 1), which is used to determine the number of spin-polarized atoms generated by the photodissociation, similar to recent experiments by Milner, Korobenko, and Milner in the measurement of electronspin-polarized O<sub>2</sub> molecules [27].

We vary the photodissociation laser intensity by several orders of magnitude, by drastically changing the focusing conditions, and show that nearly all of the molecules in the laser focus can be dissociated, leading to densities of  $10^{19}$  cm<sup>-3</sup>. Finally, we study the depolarization-rate dependence on the pressure and elucidate how the dominant depolarization mechanism explains the surprisingly long polarization lifetimes.

The photodissociation of 125 mbar DI at 266 nm produces an EMF trace [Fig. 2(a)] that starts with a sharp peak, from the magnetization produced by the 150 ps rising edge of the laser pulse, followed by a damped oscillation at the deuterium (D) hyperfine frequency with lifetime  $\tau_p \sim 20$  ns; the fast Fourier transform (FFT) shows a strong peak at  $\nu_D = 327$  MHz (inset). The signal is consistent with  $n = 2.5 \times 10^{13}$  SPD and the expected value of  $p_z(e) = 0.24$  [6]. We note that the peak near 1.1 GHz and below in Fig. 2(a) (inset) is due to a large background noise peak related to laser ionization of iodine atoms, which is not completely nulled by the light-polarization subtraction using the PEM. In addition, the peak near 1.4 GHz is caused by SPH from the photodissociation of HI contamination.



FIG. 1. Experimental setup: The photoelastic modulator (PEM) and quarter-wave plate  $(\lambda/4)$  alternate laser polarization between right circularly polarized (RCP) and left circularly polarized (LCP) on a shot-to-shot basis at a 10 Hz repetition rate. The laser is focused through the pickup coil, producing an ~2 mm diameter beam ( $f_1$ = 50 mm) or a focused beam ( $f_2$ = 25 mm,  $4 < r < 200 \ \mu$ m).

A similar damped oscillation, with a higher beating frequency, is observed from photodissociating 70 mbar HBr at 213 nm [Fig. 2(b)]; the FFT shows a strong peak at  $\nu_{\rm H} = 1.42$  GHz (inset). There is no evidence in the EMF signals from polarized I( ${}^{2}P_{J}$ ) or Br( ${}^{2}P_{J}$ ) photofragments (arrows in Fig. 2 insets); we conclude that they are depolarized almost instantly and give no EMF signal.

We compare the dependence of the EMF signal on the laser-pulse energy [Fig. 3(a)] for 200 mbar DI, for two focusing conditions. The  $\sim$ 2 mm laser beam gives an EMF signal that is nearly linear with the pulse energy [Fig. 3(a), orange circles]; the focused beam, while yielding signals nearly as large, shows the onset of the saturation of the DI photodissociation [Fig. 3(b), blue circles]. The lines are simulations of the dissociation process using Beer's law,



FIG. 2. Raw data, theoretical prediction, and FFT of magnetization hyperfine quantum beats. (a) EMF for 125 mbar DI in 875 mbar SF<sub>6</sub>, with  $\tau_p \sim 20$  ns. (b) EMF for 70 mbar HBr in 930 mbar SF<sub>6</sub> with  $\tau_p \sim 40$  ns.

taking saturation into account, and the DI dissociation cross section of  $2 \times 10^{19}$  cm<sup>2</sup> at 266 nm [28]. This comparison is made clearer in Figs. 3(b) and 3(c): The 2 mm beam fills the coil, for a nearly uniform density of ~10<sup>16</sup> SPD cm<sup>-3</sup> [Fig. 3(b)]; in contrast, for the focused beam, a similar number of SPD atoms are concentrated in a much smaller volume [Fig. 3(c)], and the SPD density reaches the original parent-molecule density of  $0.5 \times 10^{19}$  cm<sup>-3</sup> (red). The good fit of the simulations indicates that ionization or other losses are negligible, within the experimental error.

Figure 3(d) shows the EMF dependence on the pulse energy (using  $f_2$ = 25 mm) for 400 mbar DI. The conditions of the experimental point (iii) give the SPD density plot [Fig. 3(e)], which reaches  $10^{19}$  SPD cm<sup>-3</sup> (red). Finally, densities of  $10^{19}$  SPD cm<sup>-3</sup> for volumes of ~0.3 cm<sup>-3</sup> can be produced [Fig. 3(f)], in which high-power lasers can be focused for polarized laser-fusion studies.

We elucidate the SPD depolarization mechanism at a high pressure, by measuring the dependence of the D<sup>↑</sup> depolarization rate  $K = 1/\tau_p$  (where D<sup>↑</sup> denotes polarized D atoms) on the DI pressure [Fig. 4(a)]. We see a linear dependence at a low pressure, which however curves towards a constant value at high pressures. This behavior is not consistent with depolarization caused by DI collisions:

$$D^{\uparrow} + DI \xrightarrow{k} D + DI, \qquad (3)$$

which predicts a plot of *K* vs [DI] with slope *k* and not the curving behavior in Fig. 4(a). We find that the simplest process that explains this behavior is the following set of three reactions involving the intermediate molecular species DI-D<sup>↑</sup>, formed by collisions of D<sup>↑</sup> with DI:

$$D^{\uparrow} + DI \stackrel{k_1}{\underset{k_{-1}}{\longrightarrow}} DI - D^{\uparrow}$$
(4)

followed by intramolecular depolarization:

$$\text{DI-D}^{\uparrow} \xrightarrow{\kappa_d} \text{DI-D}$$
 (5)

or by dissociation of DI-D<sup> $\uparrow$ </sup> via collisions with DI:

$$\mathrm{DI}\text{-}\mathrm{D}^{\uparrow} + \mathrm{DI} \xrightarrow{\kappa_2} \mathrm{D}^{\uparrow} + 2\mathrm{DI} \tag{6}$$

or a third body *X*:

$$\mathrm{DI}\text{-}\mathrm{D}^{\uparrow} + X \xrightarrow{k_2^X} \mathrm{D}^{\uparrow} + \mathrm{DI} + X.$$
 (7)

These reactions, assuming the steady-state approximation  $d[\text{DI-D}^{\uparrow}]/dt = 0)$ , yield the depolarization rate *K*:

$$K = \frac{k_1 k_d [\text{DI}]}{k_{-1} + k_d + k_2 [\text{DI}] + k_2^X [X]}.$$
 (8)

For [X] = 0, Eq. (8) fits the data in Fig. 4(a) well, as it predicts linear behavior for small [DI] and tends to a constant value ( $K = k_1 k_d / k_2$ ) for large [DI]. Equation (8) predicts that the addition of inert gas X, for constant [DI], will decrease the depolarization rate, as [X] is only in the denominator. Indeed, such behavior is shown by SF<sub>6</sub> in Fig. 4(b) and fit well by Eq. (8). Therefore, the addition of an inert gas lengthens the polarization lifetime, likely allowing even higher densities than  $10^{19}$  cm<sup>-3</sup>.

Finally, we investigate  $D^{\uparrow}$  depolarization by the other photodissociation products,  $I({}^{2}P_{J})$  atoms, due to

$$\mathbf{D}^{\uparrow} + I \xrightarrow{k^{\mathrm{I}}} \mathbf{D} + \mathbf{I}^{\uparrow}. \tag{9}$$

The dependence of *K* on the laser pulse energy is measured, for both focusing conditions, from 3 to 7 mJ/pulse [Fig. 4(c)]. For the highest pulse energies and focusing in the coil, average I-atom densities of  $2 \times 10^{18}$  cm<sup>-3</sup> are produced within the laser beam. However, no significant effect on *K* is observed, which allows us to put an upper limit on the I-atom depolarization rate  $k^{I} < 10^{-11}$  cm<sup>3</sup> s<sup>-1</sup>, which implies that still higher SPD densities are possible than reported here (needing more UV pulse energy).

We propose the production of various nuclear-spinpolarized molecules, through SPH reactions, on nanosecond timescales, for pump-probe NMR detection with signal enhancement. In contrast, current methods, such as SEOP [1,29] and dynamic nuclear polarization (DNP) [30] operate on timescales of minutes or hours and are less suitable for pump-probe experiments. The hydrogen isotopes can be easily reacted to form a wide variety of biologically compatible molecules, such as small hydrocarbons and alcohols, as well as radicals. For a typical reaction cross section of the order of 1  $Å^2$  and a (thermalized) speed for the polarized H or D atoms of a few thousand meters per second, reactant densities of a few 10<sup>19</sup> cm<sup>-3</sup> yield reaction rates of the order of  $10^8 \text{ s}^{-1}$ , so that all the polarized H and D atoms can react within the polarization lifetime of  $\sim 10$  ns. Examples of such reactions are given by [31]

$$H + C_2 H_4 \xrightarrow{k_3} C_2 H_5 \left( k_3 = 1.4 \times 10^{-12} \frac{\text{cm}^3 \text{ s}^{-1}}{\text{molecule}} \right)$$
 (10)

and

$$H + C_2 H_5 \xrightarrow{k_4} C_2 H_6 \left( k_4 = 6.0 \times 10^{-11} \frac{\text{cm}^3 \text{ s}^{-1}}{\text{molecule}} \right)$$
(11)

with H-atom reaction lifetimes given by  $1/k_3[C_2H_4]$  and  $1/k_4[C_2H_5]$ , respectively. The conditions we have demonstrated here are necessary to maximize the NMR signals, as the photodissociation laser pulse will be entirely absorbed within the NMR detection region of length  $\approx 1$  cm, only for HI and HBr densities in excess of  $10^{19}$  cm<sup>-3</sup>. Furthermore,



FIG. 3. Signal pulse-energy dependence and corresponding SPD density plots. (a) Signal (points) and Beer-law simulation (lines) of the pulse-energy dependence for 200 mbar DI for an  $\sim$ 2 mm laser beam (orange) and for a focused beam (blue). SPD density plots for (b) 4 mJ pulse energy and  $\sim$ 2 mm beam (i) and (c) 4.5 mJ pulse energy and focused beam (ii). (d) Signal dependence on the pulse energy, for 400 mbar DI and a focused beam (blue circles) and Beer-law simulation (blue line). SPD density plots for (e) 4 mJ pulse energy and a focused beam (iii) and (f) 100 mJ pulse energy and an  $\sim$ 100  $\mu$ m beam. Error bars are 2 $\sigma$  standard deviations derived from replicate measurements.

the SPH atoms or spin-polarized molecules can be easily adsorbed at surfaces; this will offer much need sensitivity in NMR of surfaces [32], which can be important for studying complex surface-related processes, such as catalysis [33].

This production of at least  $10^{19}$  SPH/SPD cm<sup>-3</sup> densities is sufficient for the  $\lambda = 10 \ \mu$ m laser ion acceleration [13] of spin-polarized protons, deuterons, or electrons, adding the control of spin to this method of particle acceleration.

Polarized laser fusion, using densities of at least  $10^{19}$  SPD cm<sup>-3</sup> and  $10^{20}$  cm<sup>-3</sup> of polarized <sup>3</sup>He, and at least 5 kJ/pulse focused to ~10  $\mu$ m [10–12], will yield well above  $10^4$  neutrons for the D-<sup>3</sup>He and D-D fusion reactions, needed for polarized fusion studies; well above  $10^6$  neutrons will be produced using the 2 MJ/pulse NIF laser [6].

For the D-T or D-<sup>3</sup>He nuclear fusion reactions, the angular distribution of the neutron or proton products  $D(\theta, \phi)$  about the quantization axis, as a function of the nuclear vector polarizations  $p_z$  of D, T, or <sup>3</sup>He, is well approximated by [34]

$$D(\theta,\phi) = \frac{\sigma_0}{3} [(2+p) - (2p+p_{zz})P_2(\cos\theta)]/4\pi, \quad (12)$$

where  $p = p_z(D)p_z(Y)$ , Y = T or <sup>3</sup>He,  $p_z$  is the nuclear vector polarization,  $p_{zz}$  is the tensor polarization for D nuclei,  $\sigma_0$  is the fusion cross section through the intermediate <sup>5</sup>He or <sup>5</sup>Li  $\frac{3}{2}$ <sup>+</sup> state for the D-T and D-<sup>3</sup>He reactions, respectively, and  $P_2(x)$  is the second Legendre polynomial.



FIG. 4. Depolarization-rate dependence. (a) On DI pressure, fit with Eq. (8). (b) On SF<sub>6</sub> partial pressure (250 mbar DI), fit with Eq. (8). (c) On pulse energy (250 mbar DI) for both focusing conditions (Fig. 3). Error bars are  $2\sigma$  standard errors from the nonlinear fit of EMF traces.

The first term in Eq. (12) is proportional to the integrated product signal, so that for maximal nuclear polarization, with p = 1, the product integrated intensity is increased by 50% compared to p = 0; also, in this case  $p_{zz} = 1$ , and hence  $D(\theta, \phi) \sim 1 - P_2(\cos \theta) \sim \sin^2 \theta$ .

For the D-<sup>3</sup>He reaction performed with  $p_z({}^{3}\text{He}) = 0.76$ [7,35],  $p_z(D, t = 1.5 \text{ ns}) = 0.12$  (reported here), and  $p_{zz}(D) = 0$ , we predict a 14% variation in the angular distribution (between  $\theta = 0^{\circ}$  and 90°) and a 4.5% increase in the integrated intensity, whereas if bond alignment is used prior to dissociation [36],  $p_z(D, t = 1.5 \text{ ns}) = 0.5 \text{ can}$  be produced [6], leading to a 70% variation in the product angular distribution and a 19% increase in the integrated intensity. In contrast, the effect of polarization in the D-D reaction is poorly understood, with predictions ranging from suppression to enhancement [3]. The measurement of the polarized fusion reactions will answer the two outstanding problems of polarized fusion of the past decades [3,37]: determining whether nuclear polarization survives the plasma long enough to benefit fusion reactivity and elucidating the effect of nuclear polarization in the D-D reactions [38].

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