Long-Range Interactions and Symmetry Breaking in Quantum Gases through Optical Feedback

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We consider a quasi-two-dimensional atomic Bose-Einstein condensate interacting with a near-resonant laser field that is backreflected onto the condensate by a planar mirror. We show that this single-mirror optical feedback leads to an unusual type of effective interaction between the ultracold atoms giving rise to a rich spectrum of ground states. In particular, we find that it can cause the spontaneous contraction of the quasi-two-dimensional condensate to form a self-bound one-dimensional chain of mesoscopic quantum droplets, and demonstrate that the observation of this exotic effect is within reach of current experiments.

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Ultracold atomic gases have emerged as a unique platform for exploring the rich physics of quantum many-body systems in and out of equilibrium [1-5]. These new capabilities are based on the exquisite control of cold atoms by external fields and in particular the ability to control and tune atomic interactions. Most prominently, the use of Feshbach resonances [6], induced by magnetic or optical fields, makes it possible to vary the strength of zerorange collisional interactions between cold atoms, which is essential for their use in quantum simulations. The generation and control of finite-range interactions is significantly expanding the scope of such capabilities and therefore has been a frontier of cold atom research in recent years. Among the most promising systems are cold ion crystals [7], cold molecules [8], Rydberg atoms [9], and dipolar quantum gases [10], which have led to a number of recent breakthroughs, from the simulation of quantum spin models [11-16] to the discovery of exotic quantum-fluid phenomena [17–19]. Alternatively, effective interactions can be induced by another quantum system coupled to the cold atoms. Examples include polaron interactions in degenerate gases [20-22] and photon-mediated interactions induced by interfacing atoms with nanoscale photonic structures [23,24] or optical cavities [25-33]. These and similar atom-photon interfaces offer unprecedented control capabilities for the emerging interactions [24,29,33] and provide a unique platform for observing new phases of quantum matter [26-28,30,32,34,35] and fascinating collective optomechanical phenomena [36–38].

Here, we consider one of the simplest possible setups, namely a light field coupled to an atomic gas via a mirror [see Fig. 1(a)]. We show that such a single-mirror optical feedback [38–45] induces an unusual type of atomic interaction that leads to equally exotic collective behavior of the optically driven quantum gas. In particular, we find that it can cause the spontaneous contraction of a quasi-two-dimensional Bose-Einstein condensate (BEC) into a

self-bound one-dimensional chain of mesoscopic quantum droplets. Despite the simplicity of the setup, the system's ground-state phase diagram indicates rich behavior, from quantum-droplet solutions and the aforementioned droplet chains to extended density-wave states. The found structures exhibit an intrinsic emerging length scale and, in contrast to purely repulsive systems, such as dipolar condensates [17] or other long-range interacting systems [46–48], are self-confined and do not rely on external in-plane trapping. Numerical simulations of the condensate dynamics under realistic conditions and including scattering-induced atom



FIG. 1. (a) Schematic illustration of the considered setup in which a quasi-2D BEC is illuminated by a laser light that is backreflected by a mirror and thereby generates optical feedback in the degenerate atoms. The atoms are driven by the incoming $(\hat{\mathcal{E}}_{+})$ and backreflected $(\hat{\mathcal{E}}_{-})$ light field according to the depicted level scheme. The resulting multiple light scattering generates an effective atomic interaction as shown in (b). The blue and green lines depict the potential for kd = 20 and for $d \gg k^{-1}$, respectively, where d is the distance between the BEC and the mirror and $k = 2\pi/\lambda$ is the wave number of the optical field. Panel (c) shows the potential energy resulting from the average interaction between two Gaussian clouds separated by a distance r, both with a rms radius of $\sigma = 0.5$. The peculiar form of the interaction can stabilize a 1D lattice of quantum droplets that is illustrated in (d), along with the typical lattice spacings. All graphs use scaled dimensionless units described in the text.

losses show that such states should be observable with present experimental capabilities.

As illustrated in Fig. 1(a), we consider a quasi-2D BEC placed in front of a mirror [43,44] at a distance d. Incident laser light propagates through the condensate, is backreflected from the mirror, and then traverses the BEC a second time. It is the optical feedback associated with the second encounter that can generate a nonlinear effect for the atoms. In classical terms, the light beam's effect can be intuitively understood as follows. As the light field propagates through the atomic cloud, it imparts an energy shift onto the atoms and simultaneously acquires a phase shift which depends on the optical depth and therefore the local density of the atoms. Diffraction of the beam on its way to and from the mirror partly converts the beam's phase modulation into an amplitude modulation. The backreflected modulated intensity therefore generates a light shift that depends on the atomic density. This optomechanical nonlinearity was found to trigger a dynamical instability and pattern formation for sufficiently high laser intensities [40-43], as observed in experiments with atomic vapor [38,44].

In order to formulate a quantum theory in the limit of small light intensities, we describe the forward and backward propagating fields by the slowly varying electric field operators [49] $\hat{\mathcal{E}}^{\dagger}_{+}$ and $\hat{\mathcal{E}}^{\dagger}_{-}$, respectively. These two paraxial fields couple the electronic ground state $|g\rangle$ of the atoms to two excited states $|\pm\rangle$. This configuration can be realized by using circularly polarized light and placing a quarterwave plate between the BEC and the mirror. In this way, the two light fields traverse the BEC with opposite circular polarization and drive separate atomic transitions, thereby avoiding interference effects. The underlying level scheme, which can, e.g., be realized with alkaline atoms, is depicted in Fig. 1(a). Within the rotating wave approximation, the coupled atom-photon system can be described by the following Heisenberg equations [50]:

$$i\frac{\partial\hat{\Psi}_{\pm}}{\partial t} = -\left[\Delta + \frac{\hbar}{2m}\left(\frac{\partial^2}{\partial z^2} + \nabla_{\perp}^2\right)\right]\hat{\Psi}_{\pm} - \frac{\mu}{2\hbar}\hat{\Psi}_g\hat{\mathcal{E}}_{\pm},\quad(1a)$$

$$i\frac{\partial\hat{\Psi}_{g}}{\partial t} = -\frac{\hbar\nabla^{2}}{2m}\hat{\Psi}_{g} + g_{3\mathrm{D}}\hat{\Psi}_{g}^{\dagger}\hat{\Psi}_{g}\hat{\Psi}_{g} - \frac{\mu}{2\hbar}\left(\hat{\mathcal{E}}_{+}^{\dagger}\hat{\Psi}_{+} + \hat{\mathcal{E}}_{-}^{\dagger}\hat{\Psi}_{-}\right),$$
(1b)

$$i\frac{\partial\hat{\mathcal{E}}_{\pm}}{\partial z} = \mp \frac{1}{2k} \left(\frac{\partial^2}{\partial z^2} + \nabla_{\perp}^2\right) \hat{\mathcal{E}}_{\pm} \mp \frac{k\mu}{2\varepsilon_0} \left(\hat{\Psi}_g^{\dagger}\hat{\Psi}_{\pm} + \hat{\Psi}_{\pm}^{\dagger}\hat{\Psi}_g\right),$$
(1c)

for the two light fields $\hat{\mathcal{E}}_{\pm}$ and the field operators, $\hat{\Psi}_g(\mathbf{r}, z)$ and $\hat{\Psi}_{\pm}(\mathbf{r}, z)$, of the condensate atoms in the three respective electronic states. Here, *z* defines the light propagation axis and $\mathbf{r} = (x, y)$, such that $\nabla_{\perp}^2 = (\partial^2 / \partial x^2) + (\partial^2 / \partial y^2)$. Moreover, *m* denotes the atomic mass, ε_0 is the vacuum permittivity, k is the wave number of the optical field, and $g_{3D} = (4\pi\hbar a/m)$ denotes the strength of the zero-range interaction between ground-state atoms, due to collisions with a scattering length a. Additional interaction terms due to collisions involving excited-state atoms can be neglected, since their density is much smaller than that of the ground-state atoms, as discussed below. For simplicity, but without loss of generality [52], we assume equal laser detunings Δ and dipole matrix elements μ for the two transitions.

For sufficiently large detunings Δ , we can neglect the kinetic energy in Eq. (1a) and adiabatically eliminate the excited-state dynamics, which gives $\hat{\Psi}_{\pm} = -(\mu/2\hbar\Delta)$ $\hat{\Psi}_g \hat{\mathcal{E}}_{\pm}$. Considering a quasi-2D condensate, the remaining atomic field operator can be factorized as $\hat{\Psi}_g(\mathbf{r}, z) =$ $\hat{\psi}(\mathbf{r})\psi_z(z)$, with $\int |\psi_z(z)|^2 dz = 1$ [53,54]. We consider a longitudinal density profile that is finite for $0 < z < \ell_z$ [cf. Fig. 1(a)], such that $\int_0^{\ell_z} |\psi_z(z)|^2 dz = 1$. Substituting this expression and the adiabatic solution for $\hat{\Psi}_{\pm}$ into Eqs. (1b) and (1c) gives

$$i\frac{\partial\hat{\psi}(\mathbf{r})}{\partial t} = -\frac{\hbar}{2m}\nabla_{\perp}^{2}\hat{\psi} + g_{2\mathrm{D}}\hat{\psi}^{\dagger}\hat{\psi}\,\hat{\psi} + \hat{V}\,\hat{\psi},\qquad(2\mathrm{a})$$

$$i\frac{\partial\hat{\mathcal{E}}_{\pm}(\mathbf{r},z)}{\partial z} = \mp \frac{1}{2k} \left(\frac{\partial^2}{\partial z^2} + \nabla_{\perp}^2\right) \hat{\mathcal{E}}_{\pm} \pm \frac{k\mu^2}{2\varepsilon_0\hbar\Delta} |\psi_z|^2 \hat{\psi}^{\dagger} \hat{\psi} \hat{\mathcal{E}}_{\pm},$$
(2b)

where $g_{2D} = g_{3D} \int |\psi_z(z)|^4 dz$ is the quasi-2D interaction [53,54] and $\hat{V} = (\mu^2/4\hbar^2\Delta) \int |\psi_z|^2 (\hat{\mathcal{E}}_+^{\dagger}\hat{\mathcal{E}}_+ + \hat{\mathcal{E}}_-^{\dagger}\hat{\mathcal{E}}_-) dz$. For a sufficiently short longitudinal extent of the BEC, we can solve the field propagation through the condensate by neglecting diffraction in Eq. (2b) [43,44] and obtain

$$\hat{\mathcal{E}}_{+}(\mathbf{r},z) = e^{-i(k\mu^{2}/2\varepsilon_{0}\hbar\Delta)\hat{\psi}^{\dagger}(\mathbf{r})\hat{\psi}(\mathbf{r})\int_{0}^{z}|\psi_{z}(z')|^{2}dz'}\hat{\mathcal{E}}_{0}, \quad (3)$$

where $\hat{\mathcal{E}}_0$ describes the incoming light field. On the contrary, light propagation between the condensate and the mirror is entirely determined by diffraction and yields for the backreflected amplitude at $z = \ell_z$

$$\hat{\mathcal{E}}_{-}(\mathbf{r}, \mathscr{C}_{z}) = \frac{1}{2\pi} \int \tilde{\mathcal{E}}_{+}(\mathbf{p}) \Phi^{*}(\mathbf{p}) e^{-i\mathbf{p}\cdot\mathbf{r}} d^{2}\mathbf{p}, \qquad (4)$$

where $\tilde{\mathcal{E}}_{+}(\mathbf{p})$ denotes the Fourier transform of $\hat{\mathcal{E}}_{+}(\mathbf{r}, \ell_z)$, $\Phi(\mathbf{p}) = e^{2d(ik-\sqrt{\mathbf{p}^2-k^2})}$, and *d* is the distance between the BEC and the mirror, as indicated in Fig. 1(a). From Eqs. (3) and (4) we obtain for the last term in Eq. (2a),

$$\hat{V}(\mathbf{r}) = \frac{\Omega^2}{4\Delta} + \frac{\Omega^2}{16\pi^2 \Delta} \left| \int e^{-i(3\pi\Gamma/2k^2\Delta)\hat{\psi}^{\dagger}(\mathbf{r}')\hat{\psi}(\mathbf{r}')} f(\mathbf{r} - \mathbf{r}') d^2 \mathbf{r}' \right|^2,$$
(5)

where $\Omega = (\mu \mathcal{E}_0/\hbar)$ is the Rabi frequency of the incident field, $\Gamma = (k^3 \mu^2/3\pi \varepsilon_0 \hbar)$ denotes the spontaneous decay rate of the excited states, and $f(\mathbf{r}) = (1/2\pi) \int \Phi^*(\mathbf{p}) e^{-i\mathbf{p}\cdot\mathbf{r}} d^2\mathbf{p}$. Finally, expanding the exponent in Eq. (5), assuming $(3\pi\Gamma/2k^2\Delta)\langle\hat{\psi}^{\dagger}\hat{\psi}\rangle \ll 1$, and rotating out the constant term, we obtain a closed effective Heisenberg equation for the atoms,

$$i\frac{\partial}{\partial t}\hat{\psi}(\mathbf{r}) = -\frac{1}{2}\nabla_{\perp}^{2}\hat{\psi}(\mathbf{r}) + g\hat{\psi}^{\dagger}(\mathbf{r})\hat{\psi}(\mathbf{r})\hat{\psi}(\mathbf{r}) + 2\alpha\beta\int\hat{\psi}^{\dagger}(\mathbf{r}')\hat{\psi}(\mathbf{r}')U(\mathbf{r}-\mathbf{r}')d^{2}\mathbf{r}'\hat{\psi}(\mathbf{r}), \quad (6)$$

which contains an induced effective interaction potential $U(\mathbf{r}) = 2\text{Im}[f(\mathbf{r})]$. We have scaled space and time by $\sqrt{d/k}$ and $md/\hbar k$, respectively, giving the dimensionless parameters $\alpha = (md\Omega^2/16\pi\hbar k\Delta)$, $\beta = (3\pi\Gamma/2kd\Delta)$, and $g = g_{2D}(m/\hbar)$. It follows from the above considerations that the excited-state population is negligibly small as long as $\Delta \gg \Omega$; thus, $\hat{\psi}$ can be used as the atomic field operator, regardless of their electronic state.

The characteristic shape of the interaction is shown in Fig. 1(b). The potential oscillates with a growing frequency and a slowly damped amplitude as the interatomic distance increases. Simple insights can be gained for large mirror distances $d \gg k^{-1}$. In this limit, the interaction potential takes on the form $U(\mathbf{r}) = -\cos(r^2/4)$, which features persistent oscillations, with consecutive minima at $r_n =$ $\sqrt{8n\pi}$ (n = 0, 1, 2, ...). Even though this approximation starts to deviate significantly at large distances, it still provides a good description of the resulting BEC dynamics, as we shall see below. This is due to the finite extent of any emerging density patterns in the BEC, which tends to smear out such fine long-distance details, as illustrated in Fig. 1(c). At short distances, the interaction is attractive and forms a potential well with a length scale $\sim \sqrt{d/k}$ that can be made significantly larger than the wavelength of the applied laser field. Interestingly, though, its Fourier transform vanishes at zero momentum such that the induced interaction potential does not promote phonon excitations in the Bogoliubov spectrum of the condensate. In practice, one requires a short distance d in order to reach sufficiently small length scales $\sqrt{d/k}$ that are compatible with the typical size of BECs. Experimentally, this can be achieved by optically projecting a distant mirror into close proximity of the condensate [50,55].

Within mean field theory, we approximate $\hat{\psi}(\mathbf{r}, t) \approx \psi(\mathbf{r}, t) = \langle \hat{\psi}(\mathbf{r}, t) \rangle$ by the condensate wave function $\psi(\mathbf{r}, t)$ that determines the particle density $|\psi(\mathbf{r}, t)|^2$ [56]. Specifically, we explore the ground states by imaginary time evolution of the underlying Gross-Pitaevskii equation resulting from Eq. (6) for a fixed particle number $N = \int |\psi(\mathbf{r})|^2 d^2 \mathbf{r}$. Depending on the two parameters $\alpha\beta N$ and gN, we find different ground states [Fig. 2(a)], from an



FIG. 2. (a)–(d) Ground-state phase diagram of the driven BEC, determined by the competition between the zero-range and finiterange interaction with strengths g and $\alpha\beta$, respectively. Panels (b)–(d) provide a closer look at the thresholds beyond which a new phase can be stabilized. Panels (e)–(g) illustrate the different solutions and depict the density profile of the (e) single-droplet state $(gN/10^4 = 0.9)$, (f) droplet chain state $(gN/10^4 = 1.475)$, and (g) droplet lattice state $(gN/10^4 = 1.625)$ for $\alpha\beta N/10^3 = 1$.

infinitely extended flat BEC for strong zero-range interactions to a single localized quantum droplet [Fig. 2(e)] for dominating nonlocal interactions $U(\mathbf{r})$. In between these limiting cases, there exist two-dimensional regular structures as exemplarily shown in Fig. 2(g) and onedimensional droplet chains as depicted in Fig. 2(f).

The formed quantum droplet is bound by the shortdistance well of the induced interaction potential [Fig. 1(b)] and therefore has a typical size of $\sim \sqrt{d/k}$, i.e., of order ~ 1 in the used scaled units. As the strength q of the zero-range interaction increases, the size of the droplet increases beyond the first minimum of the finite-range interaction potential, which eventually leads to the formation of richer structures. Starting from the single-droplet solution, we see that the one-dimensional droplet chains appear in a substantial range of parameters in phase diagram [Fig. 2(a)], and are energetically favored by the long-range interaction as compared to extended 2D droplet arrays. The particular \sqrt{n} scaling of the location of the *n*th potential minimum leads to a local double-peak structure, resembling a dimer chain, which matches the position of the first few potential minima as illustrated in Fig. 1(d). The found emergence of a one-dimensional structure out of a 2D geometry is indeed remarkable considering the isotropic nature of the interaction potential, and can be traced back to its long-ranged oscillatory form. Upon further increase of g, local repulsion starts to dominate and eventually leads to a completely delocalized structureless state with constant density. In between these two phases, we find two-dimensional structures with broken translational symmetry in the form of two-dimensional droplet lattices. Similar to the droplet chains, each site features a finer structure that emerges from



FIG. 3. Longitudinal density profile $\rho_{\parallel}(x_{\parallel})$ in the droplet-chain phase with increasing strength *g* of the zero-range interaction for $\alpha\beta N/10^3 = 1.5$. All profiles are normalized by the maximum density $\rho_{\parallel}^{(max)}$ at the smallest interaction strength $gN/10^4 = 1.8$.

the particular \sqrt{n} scaling of the potential minima, as discussed above.

Returning to the one-dimensional structure, the size of the emerging droplet chain is controlled by both interaction parameters. Upon increasing gN, the droplet chain grows with a stepwise rising number of sites, as shown in Fig. 3. Here, $\rho_{\parallel}(x_{\parallel})$ is the longitudinal density, obtained by integrating the 2D density $|\psi(\mathbf{r})|^2$ over the coordinate transverse to the chain axis. As the strength qN of the local repulsion is increased, the site number grows, alternating between even and odd chain sizes, accompanied by a gradual decrease of the overall density. Beyond a critical length, the chain eventually dissolves into the delocalized state or is replaced by the 2D droplet lattice state discussed above. By simultaneously increasing the strength $\alpha\beta N$ of the light-induced interaction close to this phase boundary, the chain keeps extending continually and approaches the thermodynamic limit as $N \to \infty$. Note, however, that a sole increase of the atom number N for fixed values of $\alpha\beta$ and q drives the system into the Thomas-Fermi limit in which kinetic energy becomes irrelevant and the formed structure is entirely determined by the competition of the two interactions. In this case, the emerging density profile becomes independent of N and a further increase of the particle number simply leads to a linear growth of the overall density.

The kinetic energy, however, drives the transitions between the different states. Their energy crossings, shown in Fig. 4(a), indicate that the transitions are of first order. This is corroborated [50] by the apparent discontinuity of the average density $\bar{\rho} = N^{-1} \int |\psi(\mathbf{r})|^4 d^2 \mathbf{r}$ at the transition points, as well as the multistability and hysteresis behavior depicted in Fig. 4(b). The appearance of all nontrivial phases involves a threshold strength of the nonlocal light-induced interaction. While the formation of the self-bound quantum droplet only requires a relatively small value of $\alpha\beta N \approx 0.5$ for vanishing local repulsion g = 0 [Fig. 2(b)], the emergence of the droplet chain and droplet lattice states requires significantly larger values of $\alpha\beta N \approx 50$ and $\alpha\beta N \approx 675$, as shown in Figs. 2(c) and 2(d), respectively.



FIG. 4. Ground-state energy E (a) and average density $\bar{\rho}$ (b) of the two different indicated solutions as a function of gN for $\alpha\beta N/10^3 = 0.5$, whereby thick lines mark the ground state and thin lines otherwise. The corresponding transition, marked by the vertical dotted line at gN = 6130, is of first order, which leads to characteristic hysteresis behavior. As illustrated in (b), both solutions coexist until one of them loses stability at the critical points marked by the open circles. The apparent drop of the average density originates from the development of a ring structure, as illustrated by the two insets that show the amplitude $|\psi(\mathbf{r})|$ for gN = 5500 (left) and gN = 6100 (right). In contrast to the first-order droplet-chain transition, the ring structure retains rotational symmetry and emerges through a continuous crossover.

In order to explore observable signatures of the described states in potential experiments, we have studied the real dynamics of the system under relevant experimental conditions. The main challenge stems from spontaneous photon emission on the two optically driven transitions, which causes condensate loss and thereby limits the observation time. In the considered limit of a large detuning, the dissipation rate can be determined from $\Gamma_{sc} = (\Gamma \Omega^2 / 2\Delta^2)$, i.e., the decay rate Γ multiplied by the small excited-state population $\Omega^2/2\Delta^2$. Within our scaled units, the dimensionless condensate loss rate is given by $\tilde{\Gamma}_{sc} = \Gamma_{sc}(md/\hbar k) = 16kd\alpha\beta/3$. The corresponding timescale for condensate loss should be significantly longer than the typical dynamical time for structure formation. Since the latter scales with the interaction strength $\alpha\beta N$, a high atomic density provides favorable conditions. Moreover, the actual parameters are chosen such that $|\Delta| \gg \Gamma, \Omega; \ell_z < d$ and $\beta |\psi(\mathbf{r})|^2 = (3\pi^{3/2}\Gamma/2k^2\Delta)\rho_0 \ell_z \ll 1$ to ensure the validity of the effective theory Eq. (6). In the last inequality, ρ_0 denotes the atomic peak density.

These constraints can be satisfied without fundamental difficulty as demonstrated in Fig. 5, where we show the dynamics of a quasi-2D rubidium BEC in the presence of atom losses with a rate $\tilde{\Gamma}_{sc}$ under realistic experimental conditions [1,54]. The simulations start from an initial Thomas-Fermi profile [56] $|\psi(t=0)|^2 = \rho_0[1 - (x^2/\sigma_x^2) - (y^2/\sigma_y^2)]e^{-z^2/\ell_z^2}$ for the BEC in a harmonic trap. Upon turning off the in-plane confinement and simultaneously turning on the driving field $\hat{\mathcal{E}}_0$, the system indeed undergoes a rapid dynamical formation of structures on a timescale of a few milliseconds before atom loss starts to significantly deplete the condensate and decrease its



FIG. 5. Time evolution of a laser-driven rubidium BEC (from left to right) for different initial density profiles depicted in the leftmost column. The simulations account for scattering-induced atom loss and are performed for $\Omega/\Delta = 2.5 \times 10^{-3}$, $d = 10\lambda$, $\lambda = 780$ nm, and a scattering length tuned to a = 0.62 nm via a Feshbach resonance [6]. The atomic density distribution has a longitudinal width of $\ell_z = 1 \ \mu m$ and follows an initial Thomas-Fermi profile with $\rho_0 = 2.8 \times 10^{14} \text{ cm}^{-3}$ (see text for details). The rightmost column shows the final density for the approximate interaction potential $U = -\cos(r^2/4)$, which is virtually identical to the exact results.

density. Depending on the initial aspect ratio σ_x/σ_y , the BEC relaxes towards different states that reflect the ground-state physics discussed above.

In conclusion, we have shown that coupling light to a BEC within a single-mirror feedback configuration leads to interesting effective interactions between the atoms. Its long-range and oscillatory behavior stands out from other types of interactions that are currently considered in ultracold atomic quantum gases [9,17]. This peculiar shape was found to cause surprising behavior such as a transition to one-dimensional chains of quantum droplets from a twodimensional condensate. Recently, there has been significant work on the formation of quantum droplets and their regular structures [17,18]. The present 2D system provides the first instance that promotes such regular structures in a self-stabilized fashion without external confinement. Our simulations show that this behavior should be within experimental reach which, in light of the comparable technological simplicity of the considered setup, suggests an intriguing alternative route to long-range interactions in atomic quantum gases. Given the peculiar nature of the found effective interactions, the consequences of strong laser driving beyond the small-phase regime, effects of strong interactions and quantum fluctuations, as well as the possibility of supersolidity in the present system all present exciting future questions to be explored.

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