## Absolute Equation-of-State Measurement for Polystyrene from 25 to 60 Mbar Using a Spherically Converging Shock Wave

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We have developed an experimental platform for the National Ignition Facility that uses spherically converging shock waves for absolute equation-of-state (EOS) measurements along the principal Hugoniot. In this Letter, we present one indirect-drive implosion experiment with a polystyrene sample that employs radiographic compression measurements over a range of shock pressures reaching up to 60 Mbar (6 TPa). This significantly exceeds previously published results obtained on the Nova laser [R. Cauble *et al.*, Phys. Rev. Lett. 80, 1248 (1998)] at a strongly improved precision, allowing us to discriminate between different EOS models. We find excellent agreement with Kohn-Sham density-functional-theory-based molecular dynamics simulations.

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Measuring the response of matter to extreme pressures that approach and exceed 100 Mbar (= 10 TPa) is important for our understanding of giant planets [1,2], brown dwarfs [3], and large planetary impacts [4] and in laboratory inertial confinement fusion (ICF) plasmas [5,6]. With the advent of high-power lasers, such high-energydensity conditions can be created in a laboratory setting. We used the National Ignition Facility (NIF) [7] to drive a spherically converging shock wave and measured the equation of state (EOS) of polystyrene along the principal shock Hugoniot-describing the locus of thermodynamic final states accessible via shock compression from a given initial state-for pressures up to 60 Mbar.

Shock compression is the canonical technique to measure the EOS of matter at an elevated pressure. Given a steady shock wave, the conservation of mass, momentum, and energy across the shock discontinuity leads to the Rankine-Hugoniot relations [8]. It follows that the measurement of any two independent mechanical properties uniquely characterizes the shocked state. Such measurements can test and calibrate mechanical EOS models, here in the sense of relations between the mass density, internal energy, and pressure. High-precision EOS measurements based on optical velocimetry, tracking the shock velocity when transiting from a reference material into the sample under study, have been demonstrated [9]. While this impedance matching (IM) method [10,11] is widely used, it relies on an accurate knowledge of the reference material [12]. Extending IM to higher pressures (more than  $\approx 10$  Mbar) is challenging, because (i) reference materials are less well characterized and (ii) the reflectivity at the shock front eventually degrades as the material ahead of the shock front becomes ionized due to radiation from the shock-heated material, limiting the applicability of IM to transit time measurements. An alternative approach is measuring the shock velocity and compression of the shocked state through radiography, which represents an absolute mechanical EOS measurement. This was demonstrated for polystyrene using planar shock waves by Cauble et al. for pressures up to 40 Mbar [13], although the accuracy in their measurements was not good enough to discriminate between today's state-of-the-art EOS models. More recently, spherically converging shock waves in solid spheres have found interesting applications [14–17], because they can act as pressure amplifiers-the shock pressure p increases roughly inversely with radius r $(p \propto 1/r)$  [18]—up into the gigabar range, and they are stable against high-mode perturbations [19].

Here we present the first radiographic EOS measurement of a spherically converging shock wave in the laboratory. A



FIG. 1. The 1D radiography convergent ablator platform [25] (b) is used to measure time-resolved (streaked) radial transmission profiles [(c) shows the raw streak image] of a converging shock wave in a solid plastic sphere of initially 2.3 mm diameter. (a) shows the dimensions and composition of the spherical plastic sphere used in this experiment and the thicknesses of the Ge-doped layers, where doping levels are given in atomic number percent. The temporal laser profiles driving the hohlraum and the backlighter foil are shown in (d) along with the measured hohlraum radiation temperature.

polystyrene sample was used, because a large body of experimental and theoretical work existed [9,13,20-24], high-quality spherical targets were readily available, and experimental requirements could be met by existing NIF target platforms. Our experiments significantly advance the accuracy of high-pressure Hugoniot measurements and extend the data set up to 60 Mbar. The convergent geometry allows us to measure a range of locus points along the Hugoniot in one experiment. Here we present measurement of the principal Hugoniot for polystyrene at pressures from 25 to 60 Mbar; cf. Fig. 1. We adapt the indirect-drive concept to drive a spherical shock into a solid plastic sphere, illustrated in Fig. 1(b). We use a cylindrical gold cavity (hohlraum) with an inner diameter of 5.75 mm, a height of 9.42 mm, and laser entrance holes (LEHs) of 3.38 mm diameter. 168 laser beams enter the hohlraum through the LEHs and generate a symmetric soft x-ray drive by heating the inner hohlraum wall. The plastic sphere is mounted at the center of the hohlraum, which is supported by 45.6-nm-thin plastic membranes. The main sample material, a 1940  $\mu$ m diameter poly( $\alpha$ -methylstyrene) (PaMS, C<sub>9</sub>H<sub>10</sub>) sphere, is overcoated with a 183.8-µm-thick plastic ablator [glowdischarge polymer (GDP)] that contains a graded Ge dopant layer close to the interface with the PaMS sample; see Fig. 1(a) for detailed thickness and dopant levels. The Ge doping serves two purposes: (i) It acts as a preheat shield by attenuating nonthermal Au M-band x rays (2.5-3.5 keV) from the Au hohlraum wall, and (ii) it provides a fiducial for the enclosed sample mass, which can be used as an additional constraint for the radiographic analysis [26,27]. The Hugoniot measurement starts when the shock wave enters the PaMS sample. For the remainder of this Letter, we use polystyrene to refer to PaMS in our experiment.

Heating of the sample prior to shock arrival can limit its compressibility [17]. There are several mechanisms that could cause preheating: (i) gold M-band emission from the hohlraum wall, (ii) hot electrons generated through

laser-plasma-interaction (LPI) instabilities, or (iii) thermal emission from the shock front. To rule out hot electron preheat, we used a near vacuum hohlraum drive that has demonstrated a low level of hot electron generation [28] due to LPI instabilities being almost absent. For this purpose, the target was fielded at room temperature (293 K) with a low-density <sup>4</sup>He hohlraum gas fill of 0.03 mg/cm<sup>3</sup> (p = 0.195 bar). To minimize other preheat sources, we chose a low-energy drive, where 168 laser beams delivered a total of 311 kJ at a wavelength of 351 nm and a peak laser power of 78.0 TW into the hohlraum in a 4-ns-long, nearly square drive pulse [Fig. 1(d)]. The peak hohlraum radiation temperature was measured at  $(203 \pm 3)$  eV at the end of the hohlraum drive by the DANTE diagnostic [29,30] with an Au M-band fraction of only 5% [31]. Hydrodynamics simulations matching these drive observables predict a preheat due to *M*-band emission to be less than 0.3 eV. This low preheat level does not impact the compressibility of the sample and, therefore, the Hugoniot measurement in the pressure range reported here [17].

To track the shock velocity and the compression at the shock front, we use a streaked x-ray radiography platform that was originally developed for ICF capsule implosion velocity measurements [25,32]. Here, the 100-µm-high, horizontal slice of the solid sample at the center of the hohlraum is backlit with a Zn He- $\alpha$  (9.0 keV) area backlighter. The 15- $\mu$ m-thick Zn backlighter foil is driven using four NIF quads, 16 laser beams, with a total of 123 kJ over 7 ns as shown in Fig. 1(d). The backlighter laser pulse has a prepulse to precondition the plasma and increase the conversion efficiency during the main pulse [33]. A  $16-\mu$ m-wide imaging slit was placed at  $103.0 \pm 0.3$  mm from the sample. The one-dimensional image enters the entrance slit of the streak camera cathode, which is located 783 mm downstream of the imaging slit. The spatial resolution for this setup is 18  $\mu$ m. The entrance slit of the streak camera has a height of 500  $\mu$ m. Given the streak duration (9.6 ns), internal



FIG. 2. Measured shock velocity of a converging shock wave in a solid polystyrene sphere, which exceeds 100 km/s near the center of the sphere.

magnification, and detector dimension, the integration time of a given state is 155 ps. Figure 1(c) shows the raw data of the resulting radiograph. The trajectory of the shock wave, which leads to reduced transmission, can clearly be seen. The spherical shock accelerates and converges at the center of the sphere near the end of the streaked data. Also clearly visible is the outer edge of the sphere, which has a radius of 720  $\mu$ m at maximum sample compression. Just inside of the outer radius, the Ge-doped layer is located, which contributes to the sharp appearance of the outer edge and which can be traced throughout the implosion. Outside the compressed capsule region, the shadows of two alignment fiducial wires can be seen, which are placed in front of the cathode. We use them to dewarp the data image and extract the internal magnification of the streak camera, yielding the total magnification of the imaging system of  $M = 9.21 \pm 0.07$ . From the streaked radiograph, the trajectory and the resulting shock velocity  $u_s$  can be directly extracted. Figure 2 shows  $u_s$ as a function of the radius, highlighting the acceleration due to convergence to more than 100 km/s at small radii. Since the thickness of the shock front is on the order of the mean free ion path [34], which is  $\ll 1 \ \mu m$  for conditions encountered in this experiment, the shock can locally be considered steady as in the well-established planar case. Therefore,  $u_s$ can be related to pressure p by the Rankine-Hugoniot relations [8] through

$$p = p_0 + u_s^2 \rho_0 \left( 1 - \frac{\rho_0}{\rho} \right) \tag{1}$$

if the mass density  $\rho$  at the shock front is known. Here  $p_0$  is the ambient pressure, and  $\rho_0 = 1.085 \pm 0.005 \text{ g/cm}^3$  is the initial polystyrene mass density.

States along the shock Hugoniot were deduced by reconstructing the density distribution  $\rho(r, t)$ , locating the locus of the shock front  $r_s(t)$  and, hence, the shock



FIG. 3. Inferred radial mass density profiles at two different times as the shock moves inwards. Inside the shock is the pristine polystyrene sample at a solid density of  $\rho_0 = 1.085 \text{ g/cm}^3$ .

compression  $\rho(r_s(t), t)/\rho_0$ . The shock speed  $u_s(t)$  is obtained by differentiating  $r_s(t)$ , giving a locus of states along the Hugoniot,  $\rho(u_s)$ . The density distribution was reconstructed by profile matching rather than Abel inversion, as this allowed us to use the unshocked region as a strong constraint on the shock compression and is a more natural framework for compensating for low signal levels by smoothing over the time and radius [27,35]. Figure 3 shows two examples of inferred mass density profiles. One can clearly see material piling up behind the shock front as time progresses as a typical feature for a converging shock wave [26].  $\rho(r_s)$  is the density at the shock front, as illustrated in Fig. 3, and represents a fit parameter in the radial density profile function. The increased density feature near the outer edge is due to the Ge-doped layer [cf. Fig. 1(a)] and is used to constrain the enclosed mass in the radiographic analysis. The corresponding measured and fitted sample transmission profiles are shown in Fig. 4.

The sensitivity to the choice of density profile functions was studied, in particular, by fitting the entire time-radiusdensity distribution, compared with fitting shorter slices in time for which the density variation could be represented with simpler functions and fewer parameters. The spatial brightness profile of the x-ray backlighter was included as additional parameters for optimization.

Our analysis accounts for the blurring of the shock front due to its curvature. In order to avoid large blurring near the center of the sphere, we restrict the analysis to shock radii larger than 200  $\mu$ m, which corresponds to a shock pressure of ~60 Mbar. At these pressures and below, for which simulations predict temperatures to not exceed 35 eV, ionization of the carbon *K*-shell electrons can safely be ruled out, justifying the assumption of cold opacities for our analysis. Consistent results were obtained with a fit to the entire ( $r > 200 \ \mu$ m) convergence history of the



FIG. 4. Comparison of the measured and inferred sample transmission profiles that correspond to the inferred mass density profiles shown in Fig. 3.

radiograph, from which compression and pressure along the Hugoniot are inferred. Figure 5 shows the results of this analysis and compares it with previously reported Hugoniot measurements [9,13,20], the Sesame EOS table 7592 [37], and density-functional theory (DFT) simulations [22]. Our NIF results are shown as a probability distribution with contours of the statistical error  $(1\sigma \approx 3.7\%)$  for the compression. The statistical error represents the uncertainty inferred from fitting the time-space density profile to match the streaked radiography image [27]. The systematic error for the compression of 1.0% is dominated by the uncertainty in the spatial scale and background subtraction. Since shock velocity can be measured to a high accuracy  $(\delta u_s/u_s = \pm 1.1\%)$  by smoothing along the trajectory, the uncertainty in compression dominates the uncertainty in shock pressure  $(\delta p/p = \pm 6.9\%)$  per Eq. (1). Figure 5(a) shows a representative single Hugoniot data point with total error bars. We note that all previous work was done with C<sub>1</sub>H<sub>1</sub>, i.e., at a slightly different stoichiometry. The data sets of Ozaki et al. [20] and Barrios et al. [9] were reanalyzed using the latest EOS of the quartz impedance matching standard [12]. We also note that samples with a more complicated phase diagram (such as containing phase changes) might require a more thorough analysis.

Our new experimental measurements between 25 and 60 Mbar are in very good agreement with the Hugoniot curve extracted from Kohn-Sham density-functional theory (KS DFT) molecular dynamics simulations, which use pseudopotentials to treat the 1*s* electrons in carbon [22]. Our data indicate a slightly lower compressibility than predicted by the Sesame EOS table 7592 [37]. With increasing pressures, details of the electronic structure are expected to affect the shape of the Hugoniot curve. The Sesame EOS table does not show this level of detail, as it is derived from the Thomas-Fermi-Dirac model [37–39], which neglects the effects of electronic shell structure in



FIG. 5. Principal Hugoniot measurement of polystyrene (PaMS:  $C_9H_{10}$ ) at the NIF (experiment N140529-001-999). 1 $\sigma$  contours of the *statistical* error are shown. Additionally, the top panel (a) shows one representative NIF data point with *total* error bars. The lower panel (b) sets the new data into context with previous results from planar shock experiments [9,13,20,36], the Sesame 7592 EOS table [37], and Kohn-Sham DFT simulations [22].

atoms. A more nuanced description of electronic excitations including atomic shell structure is possible with the KS DFT. To compare directly with the average-atom Thomas-Fermi-based Sesame 7592, we employ an EOS model for carbon [40] based on the average-atom KS DFT approach, Purgatorio [41,42]. We then use an equal-(P, T), additive-volume mixing scheme [43] to produce a C<sub>9</sub>H<sub>10</sub> EOS by combining this carbon EOS with the hydrogen EOS of Ref. [44]. The Hugoniot curve for the resulting EOS is shown in Fig. 5 labeled as *mix-PC*. Substituting the hydrogen EOS of Ref. [44] for the very different model of Ref. [45] does little to affect the Hugoniot of C<sub>9</sub>H<sub>10</sub> above ~100 Mbar.

The mix-PC curve in Fig. 5(b) shows an inflection just above 100 Mbar, which coincides approximately with the beginning of the *K*-shell ionization in carbon, leading to a

higher heat capacity and increased compressibility. Recent experimental observations show evidence for a larger-thanexpected ionization potential depression in dense plasmas and have challenged the applicability of commonly used ionization models in high-energy density plasmas [46–48]. Future experiments using convergent shocks at higher pressures will probe this interesting physics regime, which will require further improvements in the analysis techniques. These experiments will provide an alternative approach for measuring ionization potential depression. Pressures of several 100 Mbar can be achieved by increasing the hohlraum radiation temperature from 200 to 300 eV (~4× increase in the ablation pressure) and extending the radiography measurement to radii as small as 100  $\mu$ m (2× pressure increase).

In summary, we have successfully measured the principal shock Hugoniot of polystyrene in the pressure range of 25 to 60 Mbar using radiography of a spherically converging shock wave, generated by a symmetric hohlraum drive at the National Ignition Facility. The converging shock samples a range of pressures in a single experiment, rising to several times the ablation pressure of 20 Mbar applied to the outside of the sample. Our Hugoniot data are in good agreement with KS-DFT-based modeling, while the measured curve is slightly stiffer than predicted using the Sesame table 7592. We have demonstrated an experimental capability for absolute EOS measurements in low-Z elements for pressures  $\gg 10$  Mbar. This technique also provides a path towards developing EOS standards at such pressures that can then be used for impedance matching measurements for mid- and high-Z elements.

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