## Ultrafast Two-Dimensional Infrared Spectroscopy of a Quasifree Rotor: J Scrambling and Perfectly Anticorrelated Cross Peaks

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Ultrafast two-dimensional infrared (2DIR) spectra of the N<sub>2</sub>O  $\nu_3$  mode in moderately dense SF<sub>6</sub> gas exhibit complex line shapes with diagonal and antidiagonal features in contrast to condensed phase vibrational 2DIR spectroscopy. Observed spectra for this quasifree rotor system are well captured by a model that includes all 36 possible rovibrational pathways and treats P ( $\Delta J = -1$ ) and R ( $\Delta J = +1$ ) branch resonances as distinct Kubo line shape features. Transition frequency correlation decay is due to J scrambling within one to two gas collisions at each density. Studies of supercritical solvation and relaxation at high pressure and temperature are enabled by this methodology.

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Over the last two decades, ultrafast two-dimensional infrared (2DIR) spectroscopy has emerged as one of the leading techniques for investigation of molecular structure and dynamics in condensed phases [\[1,2\]](#page-5-2). 2DIR spectral analysis yields information on molecular fluctuation time scales and mechanisms responsible for IR absorption line shapes, the coupling of resonant intra- or intermolecular modes or the dynamics of chemical exchange between interconverting molecular configurations or species [1–[17\].](#page-5-2) For a single vibrational resonance the 2DIR spectrum consists of two oppositely signed features: ground state bleach and stimulated emission (GSB-SE) contributions centered along the diagonal, and an excited vibrational state absorption (ESA) contribution shifted along the probe frequency axis by the vibrational anharmonicity. Molecular fluctuation time scales due to bath interactions in these condensed phase systems are revealed by the waiting time  $(T_w)$  dependence of the 2DIR line shapes and correspond to the transition frequency-frequency correlation function (FFCF) of a resonantly excited vibrational mode [\[18\]](#page-5-3).

We report here the first observations and analysis of 2DIR spectra of a quasifree quantum rotor in a moderately dense gaseous medium. 2DIR spectra of the resonantly excited  $\nu_3$  asymmetric stretching rovibrational band of N<sub>2</sub>O in SF<sub>6</sub> at two densities  $(\rho^* = \rho/\rho_c = 0.16$  and 0.30;  $\rho_c = 0.74$  g/mL = 5.79 M) have been obtained. Aside from providing a rovibrationally specific framework for understanding the observed complex 2DIR spectral line shapes, these spectra demonstrate a new capability for measuring ultrafast rovibrational relaxation dynamics in the absence of discrete rotational resolution. Furthermore, characterization of the quasifree rotor 2DIR spectrum is required for studies of solvation in higher density solutions where critical point fluctuation dynamics may be evident  $(\rho^* \sim 1)$  and for learning about the onset of liquidlike character ( $\rho^* > 1$ ) as a function of density.

The FTIR (Fourier transform infrared) spectrum of the N<sub>2</sub>O  $\nu_3$  mode at  $T = 313$  K in 26 atm of SF<sub>6</sub> ( $\rho^* = 0.30$ ,  $2.6\%$  N<sub>2</sub>O) is shown in Fig. [1.](#page-0-0) The corresponding spectrum of N<sub>2</sub>O in lower density SF<sub>6</sub> (17 atm,  $\rho^* = 0.16, 4\%$  N<sub>2</sub>O) is slightly narrower. (See Supplemental Material [\[19\]](#page-5-4), Fig. S1). The maxima at 2211 and 2236 cm−<sup>1</sup> correspond to the unresolved  $P (\Delta J = -1)$  and  $R (\Delta J = +1)$  rovibrational branches, respectively, originating from the thermalized ensemble of initial rotational levels, J. The pure  $(\Delta J = 0) 0 \rightarrow 1 \nu_3$  vibrational transition, i.e., the Q branch, would be centered at  $\sim$ 2224 cm<sup>-1</sup> but is formally forbidden for a linear molecule in free space [\[20,21\].](#page-5-5) The rovibrational structure for this single vibrational resonance (Fig. [1\)](#page-0-0) stands in contrast to the single maximum line shape

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FIG. 1. Observed (solid) and modeled (dashed) FTIR spectra of the  $\nu_3$  asymmetric stretching fundamental of N<sub>2</sub>O in  $\rho^* = 0.30$ SF<sub>6</sub>. P and R branch maxima are at 2211 and 2236 cm<sup>-1</sup>.

<span id="page-1-0"></span>

FIG. 2. Experimental and calculated 2DIR spectra of the N<sub>2</sub>O  $\nu_3$  fundamental in  $\rho^* = 0.30$  SF<sub>6</sub> for waiting times (T<sub>w</sub>) of 0.2, 5, and 30 ps. Frequency-frequency correlation functions determined by CLS decay for the bleach diagonal (open circle) and antidiagonal ( filled square) 2DIR features and best fits to an exponential decay and a small constant offset are shown (red). The dominant decay times are  $6.1 \pm 0.3$  ps (diagonal) and  $5.8 \pm 0.4$  ps (antidiagonal).

observed for the N<sub>2</sub>O  $\nu_3$  transition in liquid solutions (See Fig. S1) [\[22\]](#page-5-6).

The corresponding observed 2DIR spectra of the N<sub>2</sub>O  $\nu_3$ mode in SF<sub>6</sub> ( $\rho^* = 0.30$ ) are shown in Fig. [2](#page-1-0) for  $T_w = 0.2$ , 5.0, and 30 ps. These spectra were acquired in a pump-probe configuration [\[23\]](#page-5-7), and thus rephasing and nonrephasing signals are overlapped at the detector. Perpendicularly polarized 85 fs pulses (FWHM 250 cm<sup>-1</sup>) centered at  $\sim$ 2230 cm<sup>-1</sup> were used to acquire these spectra. The rapid scan, phase corrected coherence delay between the first two pump pulses  $(\tau_1)$  was Fourier transformed to give the  $\omega_1$  axis and the dispersed signal on a 32 element array (∼3 cm<sup>-1</sup>/pixel) corresponds to the  $\omega_3$  axis [\[23\]](#page-5-7). (See Supplemental Material [\[19\]](#page-5-4) for additional experimental details). The  $T_w$  dependent 2DIR spectra of the lower density ( $\rho^* = 0.16$ ) N<sub>2</sub>O/SF<sub>6</sub> mixture have a qualitatively similar appearance (Fig. S2 [\[19\]](#page-5-4)). The  $\nu_3$   $\nu = 1$  lifetimes in these solutions, determined by magic angle pump-probe responses,  $(\rho^* = 0.30; 35 \text{ ps and } \sim 1 \text{ ns, and for } \rho^* = 0.16;$ 101 ps and  $\geq$ 10 ns) are much slower than the dynamics revealed in these 2DIR spectra.

The quasifree rotor 2DIR spectra (Fig. [2\)](#page-1-0) exhibit a qualitatively different and considerably more complex spectral signature than seen for 2DIR spectra of isolated vibrational resonances in condensed phases [\[24](#page-5-8)–27]. The sign change and spacing between the center of red and blue overlapping "X"'s at the shorter  $T_w$ 's identifies the red (positive) and blue (negative) 2DIR features resulting from GSB-SE and ESA contributions to the  $N_2O/SF_6$  2DIR spectra. The elongated spectral shape along the diagonal  $(\omega_1 = \omega_3)$  and the parallel component redshifted in the  $ω_3$  direction by the  $ν_3$  1 → 2 transition anharmonicity  $(\sim 28 \text{ cm}^{-1})$  at  $T_w = 0.2 \text{ ps}$ , are the well-known signatures of an inhomogeneously broadened vibrational band in 2DIR spectra. The corresponding antidiagonal features seen in these quasifree rotor spectra are unique relative to previous 2DIR results; however, they are reminiscent of the 2DIR spectrum predicted for two anticorrelated inhomogeneously broadened coupled oscillators [\[28,29\].](#page-5-9) The "X" pattern is evident in a prior 2D rovibronic, low density coherent 4-wave mixing spectroscopy that assists interpretation and simplification of gas phase spectra [\[30\]](#page-5-10).

Dramatic changes are seen in these 2DIR spectra (Figs. [2,](#page-1-0) and S2 of Ref. [\[19\]](#page-5-4)) as a function of  $T_w$ . All the initial ( $T_w = 0.2$  ps) elongated features approach nearly symmetrical shapes at longer  $T_w$ 's which is the well-known signature of transition frequency memory loss, characteristic of spectral diffusion processes in liquid phase environments. Furthermore, the eight spectral features in the 2DIR spectra (4 bleach and 4 absorption types) at the earliest  $T_w$ 's evolve to 4 distinct features at  $T_w \ge 30$  ps.

As shown previously, a change in the aspect ratio of the 2DIR spectral line shapes corresponding to the  $a \rightarrow b$ transition as a function of  $T_w$  closely captures the decay of the FFCF [\[18\]](#page-5-3). Thus, the center line slope (CLS), also plotted in Fig. [2,](#page-1-0) experimentally determines FFCF for both the diagonal and antidiagonal GSB-SE components of the 2DIR spectra. The CLS decay has different signs for the diagonal and antidiagonal components, but both show the same dominant exponential decay constant within experimental error:  $6.1 \pm 0.3$  ps (diagonal) and  $5.8 \pm 0.4$  ps (antidiagonal). Similarly, the CLS decay times for the lower density  $(\rho^* = 0.16)$  sample (Fig. S3) are  $9.4 \pm 0.3$  ps (diagonal) and  $9.5 \pm 0.6$  ps (antidiagonal). However, best fits to all these experimental CLS decays also find a small (∼5% of total amplitude) positive constant component for the diagonal and anti-diagonal 2DIR GSB-SE features. This small residual offset or very slow

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FIG. 3. Twelve (six GSB-SE and six ESA) of the thirty-six density matrix pathways contributing to the 2DIR signal originating in the  $v = 0$ , J rovibrational level are highlighted.

fluctuation component may be attributable to pure vibrational dephasing processes (here due to a static inhomogeneity on the experimental time scale), sample heating effects or consequences of the canceling effects of adjacent, oppositely signed 2DIR contributions.

In order to capture the essential features of the observed quasifree rotor 2DIR spectra, and provide a basis for interpreting the observed  $T_w$  dependence in terms of the underlying rotationally and vibrationally specific collision dynamics, a phenomenological model was developed. The 2DIR signal generated in the  $k_s = k_{\text{probe}}$  direction for the pump-probe experimental configuration employed here is given by

$$
S(k_s; \omega_3, T_w, \omega_1) \propto \text{Re}\left(\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} R_{\text{Tot}}^{(3)}(\tau_3, T_w, \tau_1) \right)
$$

$$
e^{i\omega_1 \tau_1} e^{i\omega_3 \tau_3} d\tau_1 d\tau_3,
$$
 (1)

where  $\tau_1$ ,  $T_w$ , and  $\tau_3$  are the delays between the two pump pulses; the second pump and the probe pulses; and the  $P^{(3)}$ signal detection time, respectively. Since the incident pulse durations (∼85 fs) are much shorter than the dynamics observed here, only the intervals between pulse maxima are used for  $\tau_1$ ,  $T_w$ , and  $\tau_3$ .

For a single vibrational resonance only a three level, optically coupled system, consisting of the ground ( $v = 0$ ), and first and second ( $v = 1, 2$ ) excited vibrational states, is needed to model the 2DIR signal. Consequently, six Liouville pathways, within the rotating wave approximation, due to spatially overlapped rephasing  $(-k_{\text{pump}} + k_{\text{pump}} +$ 

 $k_{\text{probe}}$ ) and nonrephasing ( $+k_{\text{pump}} - k_{\text{pump}} + k_{\text{probe}}$ ) contributions result for well-separated pulses[\[31\].](#page-5-11) However, for an initial rotational level J in  $v = 0$ , i.e.,  $|0J \rangle$ , an eight rovibrational level system,  $|vJ \rangle$ , is required to calculate the 2DIR spectrum of a quantum free rotor. A 2DIR signal pathway originating in  $|0J \rangle = (≡0)$  has two accessible rovibrational levels in the  $v = 1$  excited state rovibrational levels in the  $v = 1$  $(|1J + 1\rangle = 1R$  and  $|1J - 1\rangle = 1P$ , three in the  $v = 2$ second excited state  $(|2J + 2 \rangle) \equiv 2S$ ,  $|2J \rangle \equiv 2Q$ ,  $|2J - 2 \rangle = 2O$  and three in the ground vibrational state  $(|0J + 2 \rangle \equiv 0$ S,  $|0J \rangle \equiv 0$ , and  $|0, J - 2 \rangle \equiv 0$  due to the  $\Delta J = \pm 1$  selection rule for each  $\Delta v = \pm 1$  dipole interaction in this third-order experiment. (See Fig. S4 of Ref. [\[19\]](#page-5-4)). Consequently, there are six rovibrationally explicit Liouville pathways possible for each of the usually considered six types of Liouville pathways contributing to the 2DIR spectrum of an isolated vibrational oscillator [\[1,28\].](#page-5-2) Thus, the *total* third-order response function for the description of a 2DIR spectrum of a rovibrational resonance originating in a single rovibrational level for nonoverlapped pump and probe pulses is modeled as a sum of 36 rovibrationally explicit Liouville pathways:

$$
R_{\text{Tot}}^{(3)}(\tau_3, T_w, \tau_1) = \sum_{n=1}^{36} R_n^{(3)}(\tau_3, T_w, \tau_1). \tag{2}
$$

Twelve such representative pathways showing the temporal evolution from left to right of the density matrix elements contributing to the signal polarization [\[32](#page-5-12)–34] are shown in Fig. [3](#page-2-0), and all 36 of these pathways are summarized in the Supplemental Material [\[19\]](#page-5-4) (Fig. S6).

Expressions for the third-order responses contributing to vibrational 2DIR spectra have been described in detail previously [\[28\]](#page-5-9), thus only those features most salient to their extension to this rovibrational system are summarized here. Each of the 36 contributing rovibrational response functions are a product of four path-specific transition moments, exponential oscillatory phase factors at the resonant transition frequencies during each of the interpulse evolution periods  $(\tau_1, T_w, \tau_3)$ , and a path-specific nonlinear dephasing function [\[35,36\]](#page-5-13). The required dephasing functions can be written as products of exponentiated line shape functions,  $g_{ab}(t)$ , which are defined in terms of the  $a \rightarrow b$ FFCF,  $C_{a,b}(\tau_2 - \tau_1)$ , within the second order cumulant expansion approximation [\[37\]](#page-5-14)

$$
g_{ab}(t) = \int_{0}^{t} d\tau_{2} \int_{0}^{\tau_{2}} d\tau_{1} C_{a,b}(\tau_{2} - \tau_{1}). \tag{3}
$$

The FFCF is determined by the underlying fluctuation dynamics of the system and is one of the key quantities determined by 2DIR spectral analysis [\[1,18\].](#page-5-2) The required rovibrationally explicit FFCFs are given by

<span id="page-3-0"></span>
$$
C_{n\alpha,n'\beta}(t) = \langle \delta\omega_{n0}^{\alpha}(t) \delta\omega_{n'0}^{\beta}(0) \rangle = \zeta_{n\alpha,n'\beta} \Delta_{n0}^{\alpha} \Delta_{n'0}^{\beta} e^{-t/\tau_c}, \quad (4)
$$

where *n*, *n'* refer to vibrational levels 0, 1, or 2, and  $\alpha$ ,  $\beta$  are the corresponding rotational branches. For *n*,  $n' = 1$ ,  $\alpha$ ,  $\beta = P$ , or R ( $\Delta J = -1, +1$ ); for n, n' = 0 or 2,  $\alpha, \beta = 0$ , Q, or S ( $\Delta J = -2$ , 0, or +2). In this stochastic Gaussian line broadening model [\[38\],](#page-5-15) the time dependent fluctuations of the rovibrational transition frequencies, here due to gas collisions,  $\delta \omega_{n0}^{\alpha}$ , are defined relative to some corresponding ensemble averaged value  $\omega_{n0}^{\alpha^o}$ , i.e.,  $\omega_{n0}^{\alpha}(t) = \omega_{n0}^{\alpha^{\circ}} + \delta \omega_{n0}^{\alpha}(t)$ .  $\Delta_{n0}^{\alpha}$  etc. [Eq. [\(4\)](#page-3-0)], are the initial instantaneous widths of the corresponding  $0 \rightarrow n$  rovibrational ( $\alpha$ ) branches, and  $\tau_c$  is the transition energy fluctuation time scale.  $\zeta_{n\alpha,n'\beta}$  is the correlation coefficient [\[28,39,40\]](#page-5-9) describing the relative phasing of the fluctuations or distributions between  $n\alpha$ ,  $n'\beta$  rovibrational branches (see below). The total FFCF decay may result from multiple fluctuation mechanisms [Eq. [\(4\)](#page-3-0)]. Although 14 rovibrationally explicit FFCFs,  $C_{n\alpha,n'\beta}(t)$ , are formally required to calculate the 2DIR spectrum of a free rotor, these may all be given in terms of three, unique  $0 \rightarrow 1$ rovibrational FFCFs:  $C_{1R,1R}(t)$ ,  $C_{1P,1P}(t)$ , and  $C_{1R,1P}(t)$ , assuming negligible fluctuation in vibrational anharmonicity [\[28\];](#page-5-9) see Supplemental Material [\[19\].](#page-5-4)

In order to capture the effects of spectral diffusion within the unresolved  $N_2O \nu_3$  rovibrational branches (Fig. [1\)](#page-0-0)  $\omega_{10}^{R^o}$ and  $\omega_{10}^{P^o}$  are taken as the transition energy at each of the two  $\nu_3$  fundamental absorption branch maxima, and  $\Delta_{10}^P$  and  $\Delta_{10}^R$  are the corresponding inhomogeneous breadths of the P and R branches (Fig. [1](#page-0-0)). The branch maxima correspond to the  $P(15)$  and  $R(15)$  transition frequencies at 313 K and thus  $J = 15$  is taken to be the initial rotational level in the ground vibrational state in this 2DIR rovibrational analysis. This treatment is analogous to modeling the line broadening of a single vibrational oscillator due to solvent fluctuations of the vibrational energy gaps about an ensemble averaged vibrational transition frequency and the loss of frequency memory for a single vibrational oscillator (spectral diffusion). This rovibrational model, equivalently, allows for  $J$  memory loss or  $J$  spectral diffusion [\[37,38\]](#page-5-14) due to bath interactions (collisions).

The ratio of  $1 \rightarrow 2$  and  $0 \rightarrow 1$  vibrational transition moments, given within the Condon approximation, used in this calculation is  $\sqrt{1.6}$  as evident in the observed pumpprobe responses and the rotational contribution to the rovibrational transition dipole is given by  $\sqrt{\max(J, J')}$ , where  $J$  and  $J'$  are the rotational quantum numbers of the rovibrational levels involved in the transition.

By definition,  $\zeta_{n\alpha,n'\beta} = +1$  for autocorrelation functions  $(\alpha = \beta)$ ,  $C_{1R,1R}(t)$  and  $C_{1P,1P}(t)$ . However, for the crosscorrelation functions ( $\alpha \neq \beta$ ),  $\zeta_{1R,1P} = -1$  since for any J value,  $\delta \omega_{10}^R(t) \delta \omega_{10}^P(0) < 0$  (see Eq. S9, Supplemental Material [\[19\]\)](#page-5-4) and, consequently,  $C_{1R,1P}(t)$  is perfectly anticorrelated. Detailed expressions for each of the 36 response functions  $[R_n^{(3)}(\tau_3, T_w, \tau_1)]$  are given in the Supplemental Material [\[19\].](#page-5-4)

Calculated 2DIR spectra for the  $\nu_3$  mode of N<sub>2</sub>O in SF<sub>6</sub>  $(\rho^* = 0.30)$  resulting from the model outlined above are shown in Fig. [2](#page-1-0) as a function of  $T_w$  and closely capture the structure of the experimental 2DIR spectra and their  $T_w$ dependence. The corresponding calculated linear absorption spectrum is shown in Fig. [1](#page-0-0). Similar agreement between observed and calculated 2DIR results are found for the less dense  $\rho^* = 0.16$  solution (Fig. S2). Parameters for these calculated 1D and 2D spectra are summarized in Table [I](#page-3-1) and in the Supplemental Material [\[19\].](#page-5-4) The values of  $\Delta_{10}^P$  and  $\Delta_{10}^R$  were selected to capture the linear spectral shape in the central portion of the rovibrational absorption band (Figs. [1,](#page-0-0) and S1 of Ref. [\[19\]\)](#page-5-4). Given the Gaussian distribution of the instantaneous frequencies inherent to this line broadening model, poor fits in the wings of the experimental asymmetric rovibrational spectrum are expected. However, although not rigorously exact for capturing the shape of the instantaneous transition frequency distribution or any J-specific collision dynamics, the essential features of the observed linear and nonlinear

<span id="page-3-1"></span>TABLE I. Summary of 2DIR experimental results and calculation parameters.

	$SF_6$ Density $\Delta_{10}^R$ (cm <sup>-1</sup> ) <sup>a</sup> $\Delta_{10}^R$ (cm <sup>-1</sup> ) <sup>a</sup> $\tau_c$ (ps) <sup>b</sup> $T_1$ (ps) <sup>c</sup> $Z_{\text{rot}}$				
$\rho^* = 0.16$	17.7	21.4	$9.5 \pm 0.3$	-102	1.4
$\rho^* = 0.30$	19.3	22.4	$6.0 \pm 0.3$	35	16
a					

a FWHM.

<sup>b</sup>Average of diagonal and antidiagonal CLS decay constant. c Fastest component of biexponential lifetime decay.

spectra are well described by this analysis, and can be understood in terms of spectral diffusion and the rovibrationally specific 2DIR pathways (Fig. [3\)](#page-2-0). In particular, the antidiagonal 2DIR spectral features evident for both the GSB-SE and ESA contributions at early times, and the observed J scrambling as a function of  $T_w$  are captured by this treatment. Subsequent more rigorous treatments of these 2DIR observations will have to take a full quantum level specific treatment of coherence loss and J-state changing dynamics into account.

The 36 rovibrational Liouville pathways give rise to twelve unique signal peaks in the 2DIR spectrum in this model. The twelve red (GSB-SE) and blue (ESA) labeled circles on the 2DIR spectral map in Fig. [4](#page-4-0) indicate these signal locations and the number identifies a specific signal pathway from Fig. [3](#page-2-0) contributing to the 2DIR spectrum at that  $(\omega_1, \omega_3)$  position. These signals are centered at the fundamental  $R(\omega_{10}^R)$  and  $P(\omega_{10}^P)$  branch transitions along the  $\omega_1$  axis and at 8 signal frequencies along the  $\omega_3$  detection axis (see Fig. [4](#page-4-0)). However, due to the small dependence of rotational constants on vibrational level ( $B_0 \approx B_1 \approx B_2$ ) and lack of discrete rotational resolution at these densities, only 4 signal frequencies are distinguishable along  $\omega_3$ :  $\omega_{10}^R \approx \omega_{10}^{R'}$ ,  $\omega_{10}^P \approx \omega_{10}^{P'}$ ,  $\omega_{21}^R \approx \omega_{21}^{R'}$ , and  $\omega_{21}^P \approx \omega_{21}^{P'}$  (See Supplemental Material [\[19\]](#page-5-4), Fig. S7). Hence, in contrast to the 2DIR spectra of isolated vibrational resonances in condensed phase environments characterized by a single  $T_w$  dependent GSB-SE and ESA spectral component, the 2DIR spectrum of a free rotor exhibits at least 4 GSB-SE and 4 ESA features. The elongated shapes observed at shorter  $T_w$ 's for these 8 2DIR spectral regions are due to the initial predominant inhomogeneous character due to the ensemble of J-specific allowed rovibrational transitions.

Arguably, the most obvious signature in a 2DIR spectrum of free rotor character are the antidiagonally elongated

<span id="page-4-0"></span>

FIG. 4. 2DIR map that indicates where signal polarization is generated by the 12 density matrix pathways in Fig. [3](#page-2-0) as a function of  $(\omega_1, \omega_3)$ .

spectral features, which result in X-like cross peaks at early times (Figs. [2](#page-1-0) and [4](#page-4-0)). These features result from the inherent perfectly anticorrelated cross-correlation contributions,  $\zeta_{1R,1P} = -1$ , i.e., where  $C_{1R,1P}(t) =$  $\langle \delta \omega_{10}^R(t) \delta \omega_{10}^P(0) \rangle = -\Delta_{10}^R \Delta_{10}^P e^{-t/\tau_c}$ . Such perfectly anticorrelated FFCFs are unique to this quantum rotor description. The diagonally and antidiagonally elongated line shapes at early  $T_w$ 's, symmetrize at longer times as observed both in the experiments and calculations. Only 4 spectral features are evident at longer  $T_w$ 's because the N<sub>2</sub>O  $\nu_3$  vibrational anharmonicity (28 cm−<sup>1</sup>) almost exactly matches the frequency difference between  $P$  and  $R$  branch maxima (25 cm−<sup>1</sup>). Consequently, the symmetrized diagonal GSB-SE contribution of the  $P$  transition (pathway 20) almost exactly cancels the  $(P,R)$  ESA cross–peak (pathway 29), and the cross peak  $(R, P)$  GSB-SE signals (pathways 21, 23) effectively cancel the ESA of the R transitions (pathways 25 and 28). Such intensity cancellation from these same signal polarization pathways results in the two nodes at approximately  $(\omega_{10}^P, \omega_{21}^R)$  and  $(\omega_{10}^R, \omega_{21}^R)$  in the earliest time 2DIR spectra (Fig. [2\)](#page-1-0).

Aside from capturing the 2DIR spectral line shapes for a free rotor, this analysis reveals that the loss of J memory or rotational spectral diffusion due to  $N_2O-SF_6$  interactions is dominated by an exponential decay process with time constants of 9.4 and 6.0 ps at  $\rho^* = 0.16$  and 0.30, respectively. Mean free times between  $N_2O$  and  $SF_6$  collisions  $(\tau_{\text{coll}})$  based on hard sphere calculations are correspondingly 7.0 and 3.8 ps at the experimental state points (see Supplemental Material [\[19\]\)](#page-5-4) [41–[43\].](#page-5-16) Thus, rotational equilibration ( $Z_{\text{rot}} = \tau_c / \tau_{\text{coll}}$ ) occurs within 1 to 2 collisions in these moderately dense gas mixtures;  $Z_{\text{rot}} = 1.4$  $(\rho^* = 0.16)$  and 1.6  $(\rho^* = 0.30)$  and is therefore a highly efficient process at near ambient temperatures. From low pressure emission, state resolved transient absorption or ultrasonic measurements,  $Z_{\text{rot}}$  has been previously typically found to be in the range of 1 or 2 for polar molecules, and 4–5 for nonpolar molecules (hydrides excepted) [\[44,45\].](#page-5-17) Thus, the results of this 2DIR analysis provides quantitative direct time measurements of rotational relaxation that are consistent with these prior low density results. However, the ultrafast nonlinear methodology provides such quantitative relaxation measurements for much higher pressure regimes. These high density 2DIR CLS decays and NMR based determinations of angular momentum correlation times should provide an interesting comparison of these direct and indirect measures of rotational relaxation [\[46,47\]](#page-5-18). This 2DIR methodology for quasifree rotors can be applied to studies of the effects of different types of solvent interactions on rotational relaxation rates, studies of the onset of liquidlike character and dynamics in near critical point regions, as well as reactivity and relaxation in high pressure and high temperature environments.

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