Evaluation of the Interplanetary Magnetic Field Strength Using the Cosmic-Ray Shadow of the Sun

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We analyze the Sun's shadow observed with the Tibet-III air shower array and find that the shadow's center deviates northward (southward) from the optical solar disk center in the "away" ("toward") interplanetary magnetic field (IMF) sector. By comparing with numerical simulations based on the solar magnetic field model, we find that the average IMF strength in the away (toward) sector is $1.54 \pm 0.21_{\text{stat}} \pm 0.20_{\text{syst}}$ ($1.62 \pm 0.15_{\text{stat}} \pm 0.22_{\text{syst}}$) times larger than the model prediction. These demonstrate that the observed Sun's shadow is a useful tool for the quantitative evaluation of the average

solar magnetic field.

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Introduction.—The Sun blocks cosmic rays arriving at Earth from the direction of the Sun and casts a shadow in the cosmic-ray intensity. Cosmic rays are positively charged particles, consisting of mostly protons and helium nuclei, and their trajectories are deflected by the magnetic field between the Sun and Earth, depending on the magnetic field strength B and polarity, and on the cosmic ray rigidity. The Tibet air shower (AS) experiment has successfully observed the Sun's shadow at 10 TeV energies and has confirmed, for the first time, the small but the measurable effect of the solar magnetic field on the shadow [1]. The observed intensity deficit in the Sun's shadow shows a clear 11-yr variation decreasing with increasing solar activity. Our numerical simulations succeeded in reproducing this observed feature quantitatively and showed that, during the solar maximum, cosmic rays passing near the solar limb are "scattered" by the strong coronal magnetic field and may appear from the direction of the optical solar disk and reduce the intensity deficit of the Sun's shadow.

While the strong coronal magnetic field affects the intensity deficit in the shadow, the interplanetary magnetic field (IMF) between the Sun and Earth also deflects orbits of TeV cosmic rays. This deflection has actually been observed by the AS experiments as a north-south displacement of the center of the Sun's shadow from the optical center of the Sun [2,3].

These observations indicate that the Sun's shadow can be used as a sensor of the solar magnetic field. The solar magnetic field on the photosphere has been continuously monitored by optical measurements using the Zeeman effect [4], while the local IMF at Earth has been directly observed by the near Earth satellites [5]. The observation of the average IMF between the Sun and Earth, however, still remains difficult. Since the orbital deflection of cosmic rays is proportional to *B*, the observed Sun's shadow can be used for evaluating the large-scale IMF averaged between the Sun and Earth.

In this Letter, we analyze the angular displacement of the shadow's center observed by the Tibet AS array and evaluate the IMF strength $B_{\rm IMF}$ by comparing the observation with detailed numerical simulations based on the potential field model (PFM) of the solar magnetic field, which describes the IMF in terms of the observed photospheric magnetic field. We shall demonstrate that the average $\overline{B_{\rm IMF}}$ is significantly underestimated by the widely used PFM [6].

Experiment and data analysis.—We analyze the Sun's shadow observed between March 2000 and August 2009 by the Tibet-III AS array, which has been operating since late 1999 at Yangbajing (4300 m above sea level) in Tibet, China. The Tibet-III AS array consists of 789 scintillation detectors with a 7.5 m spacing, each with a 0.5 m² detection area, covering an effective area of 37 000 m² [7]. In this Letter, we divide the observed AS events into seven energy bins according to their shower size $\sum \rho_{\rm FT}$,

which is the sum of the number of particles per square meter for each fast-timing (FT) detector and is used as a measure of the primary cosmic-ray energy. For $\sum \rho_{FT}$ we consider the intervals $17.8 < \sum \rho_{FT} \le 31.6$, $31.6 < \sum \rho_{FT} \le 56.2$, $56.2 < \sum \rho_{FT} \le 100$, $100 < \sum \rho_{FT} \le 215$, $215 < \sum \rho_{FT} \le 464$, $464 < \sum \rho_{FT} \le 1000$, and $\sum \rho_{FT} > 1000$. The modal energies of primary cosmic rays corresponding to these energy bins are 4.9, 7.7, 13, 22, 43, 90, and 240 TeV, respectively, and the "window size" Δd , which is the angular distance from the true direction including 68% of the events estimated by MC simulation, is $2.0^{\circ}, 1.4^{\circ}, 0.9^{\circ}, 0.6^{\circ}, 0.4^{\circ}, 0.3^{\circ}$, and 0.2° , respectively. These modal energies of Tibet-III extending below ~ 10 TeV are suitable for analyzing the angular displacement of the Sun's shadow, because the magnetic deflection is expected to be larger for lower energy cosmic rays.

For the analysis of the Sun's shadow, the number of onsource events, $N_{\rm on}$, is defined as the number of AS events arriving from the direction within a circle of $\triangle d$ radius centered at a given point on the celestial sphere. The number of background or off-source events, $\langle N_{\rm off} \rangle$, is calculated by averaging the number of events within each of the eight off-source windows, which are located at the same zenith angle as the on-source window [1]. We then estimate the intensity deficit relative to the number of background events as $D_{\rm obs} = (N_{\rm on} - \langle N_{\rm off} \rangle)/\langle N_{\rm off} \rangle$ at every 0.1° grid of the geocentric solar ecliptic (GSE) longitude and latitude surrounding the optical center of the Sun toward which the GSE-x axis directs from Earth. We confirmed a clear 11-yr variation of D_{obs} , being successfully observed also by the Tibet-III AS array. We will report this elsewhere.

We assign the IMF sector polarity to each day referring to the daily mean GSE-x and GSE-y components of the IMF (B_x, B_y) observed by near Earth satellites [5] and calculate $D_{\rm obs}$ in "away" and "toward" sectors, separately. We assign the away (toward) sector polarity to a day when the IMF observed two days later satisfies $B_x < 0$ and $B_v > 0$ ($B_x > 0$ and $B_v < 0$) and "unknown" to the remaining days. The sector polarity in the solar corona is carried out by the solar wind with an average velocity of ~400 km/s and observed at Earth about four days later. For our assignment of the IMF sector polarity to a day under consideration, therefore, we use the IMF data observed at Earth two days later as an average along the Sun-Earth line on the day. In about 65% of the away or toward days assigned in this way, a different polarity is observed over the following four days, indicating the mixed polarity along the Sun-Earth line. We confirmed, however, that the basic conclusions obtained below in this Letter remain unchanged even by excluding these mixed polarity days from our analyses.

Figure 1 shows $D_{\rm obs}$ in percent deduced from all AS events in the away and toward sectors, each as a function of the GSE latitude and longitude measured from the optical

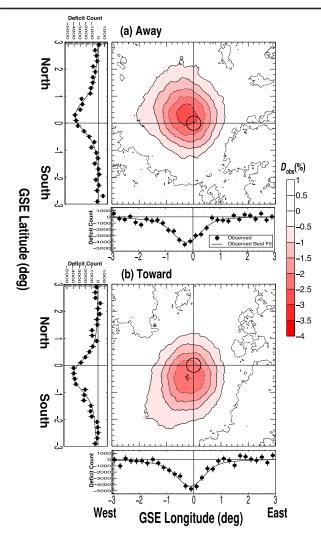


FIG. 1. Two dimensional maps of $D_{\rm obs}$ in the away (a) and toward (b) sectors in 2000–2009. Each panel shows a two dimensional contour of $D_{\rm obs}$ deduced from AS events with $\sum \rho_{\rm FT} > 10$ corresponding to the modal primary energy of ~3 TeV and $\Delta d = 0.9^{\circ}$. In each panel, a small circle centered on the origin indicates the optical solar disk. The significance at the maximum deficit point derived with the Li-Ma formula in the away (toward) sector is -23.9σ (-22.1σ) [9]. The projections of $D_{\rm obs}$ on the horizontal and vertical axes are also attached to each panel.

Sun's center, together with each projection on the vertical [north-south (N-S)] or horizontal [east-west (E-W)] axis. Following the method developed for our analyses of the Moon's shadow [7], we deduce the angular distance of the shadow's center from the optical Sun's center by best fitting the model function to the N-S and E-W projections. It is seen in Fig. 1 that the shadow's center clearly deviates from the optical center of the Sun at the origin of the map. The shadow's center shifts northward (southward) in the away (toward) sector as expected from the deflection in the average positive (negative) B_y along the Sun-Earth line, while the shadow's center shifts westward regardless of the IMF sector polarity. In Fig. 2, the average N-S and E-W

displacement angles in the away and toward sectors are calculated for each energy bin and plotted as functions of R denoting the average rigidity of cosmic rays that are blocked by the Sun. We convert the modal energy of each energy bin to R using the energy spectra and elemental composition of primary cosmic rays reported mainly from the direct measurements [8]. As expected from the magnetic deflection of charged particles, the observed displacement angles displayed by black solid circles are reasonably well fitted by a function $\alpha/(R/10\text{TV})$ of R in teravolts (TV) with a fitting parameter α denoting the displacement angle at 10 TV.

MC simulation.—In order to interpret the observed Sun's shadow, we have carried out detailed MC simulations, tracing orbits of antiparticles shot back from Earth to the Sun in the model magnetic field between the Sun and Earth [1]. For the solar magnetic field in the MC simulations, we use the PFM called the current sheet source surface (CSSS) model [10]. The PFM is unique in the sense that it gives the coronal and interplanetary magnetic field in an integrated manner based on the observed photospheric magnetic field [6]. The CSSS model involves four free parameters, the radius R_{ss} of the source surface where the supersonic solar wind starts blowing, the order n of the spherical harmonic series describing the observed photospheric magnetic field, the radius $R_{\rm cp}(< R_{\rm ss})$ of the spherical surface where the magnetic cusp structure in the helmet streamers appears, and the length scale l_a of the horizontal electric currents in the corona. In our simulations, we set R_{cp} and l_a to 1.7 and 1.0 solar radii (1.7 R_{\odot} and 1.0 R_{\odot}), respectively, and n = 10, which is sufficient to describe the structures relevant to the orbital motion of high-energy particles. We also set $R_{\rm ss}$ to $10R_{\odot}$ which gained recent support from observational evidences [11]. Our simulations with this CSSS model reproduce the observed 11-yr variation of $D_{\rm obs}$ at 10 TeV most successfully [1]. The magnetic field components are calculated at each point in the solar corona between R_{\odot} and $R_{\rm ss}$ in terms of the spherical harmonic coefficients derived from the photospheric magnetic field observations with the spectromagnetograph of the National Solar Observatory at Kitt Peak (KPVT/SOLIS) for every Carrington rotation period (~27.3 d) [4]. We calculate antiparticle orbits by properly rotating the reproduced magnetic field in every Carrington rotation period. The radial coronal field on the source surface is then stretched out to the interplanetary space forming the simple Parkerspiral IMF. For the radial solar wind speed needed for the Parker-spiral IMF, we use the "solar wind speed synoptic chart" estimated from the interplanetary scintillation measurement in each Carrington rotation and averaged over the Carrington longitude [12].

In addition, we assume a stable dipole field for the geomagnetic field [7].

Results and discussions.—In order to compare observations with predictions, we calculate the N-S and E-W

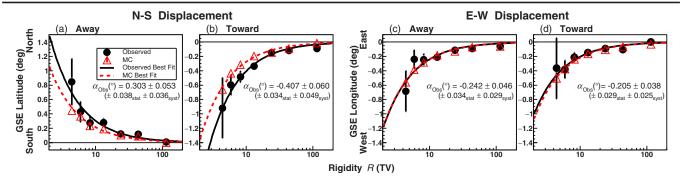


FIG. 2. The rigidity dependences of the N-S [(a),(b)] and E-W [(c),(d)] displacements of the center of the Sun's shadow in away and toward sectors. Black solid circles and red open triangles in each panel show the observed and simulated displacements, respectively, each as a function of the rigidity (R) on the horizontal axis. The error bar of each solid circle indicates the statistical error. Black solid and red broken curves display the function of $\alpha/(R/10 \text{ TV})$ best fitting to black solid circles and red open triangles, respectively. The best-fit parameter α to the observed data is indicated in each panel with systematic errors estimated from the systematic error of the primary energy in our analyses of the Moon's shadow [7].

displacements of the simulated shadow's center in the away and toward sectors for various rigidities *R*. It is seen in the N-S displacement in Figs. 2(a) and 2(b) that the magnitudes of the simulated displacement (red broken curves) are significantly smaller than the observations (black curves) in both sectors, implying a systematic underestimation by the simulations. The simulated E-W displacements in Figs. 2(c) and 2(d), on the other hand, are quite consistent with the observations, implying that the E-W displacements are predominantly arising from the deflection of cosmic ray orbits in the geomagnetic field. We confirmed that the E-W displacement of the Sun's shadow is consistent with the Moon's shadow, when an additional minor deflection in the solar magnetic field is taken into account [7].

We also compare the $B_{\rm IMF}$ observed at Earth with the simulation in Figs. 3(a) and 3(b) and find that the magnitudes of the simulated B_x and B_y are systematically smaller than the observations. By calculating the average B_x and B_y each as a function of the Carrington longitude in every year, we examined the correlations between the simulated and observed B_x and B_y as shown in Figs. 3(c) and 3(d). While the correlation coefficient between the simulated and observed magnetic field component in this figure is 0.93 (0.92) for B_x (B_y) , indicating a high correlation, the regression coefficient is 1.38 ± 0.03 (1.34 ± 0.03) for B_r (B_{ν}) , significantly larger than 1.00, implying the underestimation of the simulated B_x (B_y) on the horizontal axes [13]. This underestimation is observed in every year, while the magnitude of B_x or B_y changes in a positive correlation with the solar activity. We confirmed that the observed average B_z is insignificant in both sectors as expected from the Parker-spiral IMF.

The N-S displacement of the center of Sun's shadow reflects $\overline{B_{\rm IMF}}$ along the cosmic ray orbits between the Sun and Earth, while B_x and B_y in Fig. 3 are the local field components at Earth. The underestimation of the N-S displacement in Fig. 2, therefore, inevitably suggests that

 $\overline{B_{\rm IMF}}$ is underestimated. In order to quantitatively evaluate this underestimation, we simply multiply the simulated B by a constant factor f everywhere in the space outside the geomagnetic field, repeat simulations by changing f, and calculate $\alpha(f)$ best fitting to each simulated displacement. Figure 4 displays $\alpha(f)$ by red open triangles with linear best-fit curves, each as a function of the multiplication factor f. From the intersection between the red curves and black lines showing α for the observed N-S displacement in Fig. 2, we evaluate f best reproducing the observed

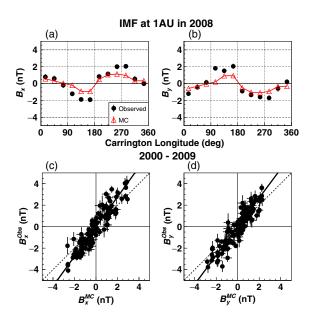


FIG. 3. Comparison between the observed and simulated IMF components at Earth. Black solid circles (red open triangles) in the upper panels display the observed (simulated) B_x (a) and B_y (b), respectively, each as a function of the Carrington longitude. The lower panels show the correlations between the observed and simulated B_x (c) and B_y (d). The regression coefficient (slope of the black solid line) is significantly larger than 1 (slope of the dashed line).

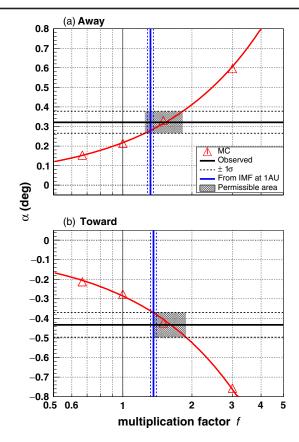


FIG. 4. The parameter α obtained from simulations by changing the multiplication factor f (see text). Red open triangles in (a) and (b) show α in the away and toward sectors, respectively, each as a function of f. The horizontal black line in each panel shows the observed α , while the vertical blue line indicates f deduced from the observed and simulated $B_{\rm IMF}$ at 1 AU. The shaded area in each panel indicates the 1σ region of f allowed by the observed α .

displacement to be $1.54 \pm 0.21_{\rm stat} \pm 0.20_{\rm syst}$ (1.62 \pm 0.15_{stat} \pm 0.22_{syst}) in the away (toward) sector. This is consistent with the regression coefficient, 1.38 ± 0.03 (1.34 \pm 0.03) in the away (toward) sector, derived in Fig. 3. The simulations with *B* multiplied by the best value of *f* also reproduce the observed 11-yr variation of $D_{\rm obs}$ successfully.

The Astrophysical Radiation with Ground-based Observatory at YangBaJing (ARGO-YBJ) experiment reported that the observed N-S displacement is consistent with $B_{\rm IMF}$ observed at Earth [3]. In the present Letter, on the other hand, we find the underestimation of $\overline{B}_{\rm IMF}$ by the PFM. The underestimation of B by the PFM has been recently reported also from simultaneous microwave and EUV observations [14]. They found that the line-of-sight B observed in the lower solar corona is 2–5.4 times larger than B calculated from the PFM and raised a question about the current-free assumption of the PFM in the photosphere and chromosphere. It is also reported, on the other hand, that there are significant differences between the observed photospheric magnetic fields used in the PFMs, although

there is a general qualitative consensus [15]. The difference is arising from the difference in the observation techniques and spatial resolutions. For instance, the average photospheric field strength B_{photo} observed by the Michelson Doppler Imager (MDI) onboard the Solar and Heliospheric Observatory [16] is 1.80 ± 0.20 times larger than $B_{\rm photo}$ observed by the KPVT/SOLIS used in our PFM, during the recent period when both data are available for comparison (see Table 3 of Ref. [15]). Although this ratio is similar to fobtained in this Letter, it should be noted that $\overline{B_{\rm IMF}}$ responsible for the N-S displacement is not simply proportional to B_{photo} in the PFM. Since the nth order harmonic component of the magnetic field at the radial distance ris proportional to $(R_{\odot}/r)^{n+2}$ [17], a more complex and stronger field on the photosphere represented with a larger n diminishes faster with increasing r and only the low order harmonic components dominate the IMF at $r > R_{ss}$. We actually confirmed that the $B_{\rm IMF}$'s at Earth calculated by the PFM using the MDI and KPVT/SOLIS photospheric fields are quite consistent with each other. The underestimation of $\overline{B_{\rm IMF}}$ by the PFM deduced from the observed Sun's shadow is, therefore, more likely due to the current-free assumption of the PFM, which does not hold accurately for the plasma in the solar atmosphere.

In summary, we find that the actual $\overline{B_{\rm IMF}}$ is about 1.5 times larger than the prediction by the PFM, by analyzing the angular displacement of the center of the Sun's shadow. This is unlikely due to the difference between the photospheric magnetic fields used in the PFM, but more likely due to the current-free assumption of the PFM, which does not hold accurately in the plasma in the solar atmosphere. It is concluded that the Sun's shadow observed by the Tibet AS array, combined with other measurements, offers a powerful tool for an accurate measurement of the average solar magnetic field.

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