## Electronic-Structure Origin of Cation Disorder in Transition-Metal Oxides

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Cation disorder is an important design criterion for technologically relevant transition-metal (TM) oxides, such as radiation-tolerant ceramics and Li-ion battery electrodes. In this Letter, we use a combination of first-principles calculations, normal mode analysis, and band-structure arguments to pinpoint a specific electronic-structure effect that influences the stability of disordered phases. We find that the electronic configuration of a TM ion determines to what extent the structural energy is affected by site distortions. This mechanism explains the stability of disordered phases with large ionic radius differences and provides a concrete guideline for the discovery of novel disordered compositions.

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Substitutional disorder is a common phenomenon in transition-metal (TM) oxides and is known to affect structural and electronic properties. For example, cation disorder induces structural amorphization in  $La<sub>2</sub>Zr<sub>2</sub>O<sub>7</sub>$  pyrochlores [\[1\]](#page-4-2), controls the magnetoresistance in Fe-Mo perovskites [\[2\]](#page-4-3), and affects the critical temperature of  $La<sub>2</sub>CuO<sub>4</sub>$  superconductors [\[3\]](#page-4-4). In rocksalt-type Li-TM oxides, cation disorder determines the Li-ion conductivity [\[4,5\]](#page-4-5), an important performance measure for Li-ion battery cathodes.

The technological relevance of cation-disordered oxides creates the desire to predict whether a given composition is likely to be disordered. While high-throughput firstprinciples computations are useful to screen specific composition spaces for stable disordered compounds [\[6](#page-4-6)–9], a better understanding of the origin of cation disorder might lead to simple design criteria so that time-consuming computations can be avoided.

For metallic alloys, the Hume-Rothery rules predict that species with similar electronegativity form a solid solution when their atomic radii differ no more than 15% [\[10,11\]](#page-4-7), but this simple heuristic does not directly translate to covalent and ionic materials such as oxides. For example, cation disorder in pyrochlores has been extensively studied [\[12\]](#page-4-8), and while the ionic radii are an important factor for the tendency to disorder [\[13\],](#page-4-9) species-dependent differences in the metal-oxygen bonding [\[14\]](#page-4-10) and electronic-structure effects [\[6\]](#page-4-6) have prevented the formulation of heuristic rules to reliably predict disorder. Likewise, B-site cation disorder in  $A(B'B'')O_3$  perovskites has been linked to the similarity of the ionic radius and charge of the  $B'$  and  $B''$  species, but these two parameters alone cannot explain all experimentally observed trends [\[15,16\].](#page-4-11) On the other hand, cationdisordered Li-TM oxides with a large ionic radius and charge differences are known, e.g.,  $LiNi<sub>0.5</sub>Ti<sub>0.5</sub>O<sub>2</sub>$  [\[17\]](#page-4-12) where the Shannon radii of  $Li^+$ , Ni<sup>2+</sup>, and Ti<sup>4+</sup> are 76, 69, and 61 pm, respectively [\[18\],](#page-4-13) which seems to contradict the present understanding of the origin of cation disorder.

In an ordered structure, a TM has a single or a few local high-symmetry environments, whereas a disordered structure has a large number of distinct low-symmetry environments. Hence, the ability of a TM to disorder will to some extent depend on how it can accommodate such a variety of environments [\[14\].](#page-4-10) We demonstrate, in this Letter, that such an adaptability is determined by the TM's electronic structure. We show that  $d^0$  TMs promote disorder while other *d*-electron configurations, especially the  $d^6$  configuration, strongly prohibit disorder. This mechanism explains the formation of solid solutions with cation species that exhibit considerable ionic radius differences.

As a case study, we focus on the  $Li/TM$  disorder in cation-disordered  $LiTMO<sub>2</sub>$  compounds, which have recently attracted interest as Li-ion battery cathode materials [\[5,19](#page-4-14)–23]. The presence of Li cations with no valence electrons as one of the components simplifies the analysis by focusing on the electronic configuration of the TM.

For all first and second row TMs the ground state  $LiTMO<sub>2</sub>$ structure is either the layered  $\alpha$  – NaFeO<sub>2</sub> structure or the  $\gamma$  – LiFeO<sub>2</sub> structure with the exception of LiMnO<sub>2</sub> which forms an orthorhombic structure [\[8,24\]](#page-4-15). The cation sites in these rocksalt-type Li-TM oxides are octahedral. For a large number of TMs in the LiTMO<sub>2</sub> composition, we calculate the energy and relaxed atomic configuration for the ground state and the disordered structure as represented by a special quasirandom structure (SQS) [\[25,26\]](#page-4-16).

Structures and energies were obtained from spinpolarized density-functional theory (DFT) calculations [\[27](#page-4-17)–29] using the Perdew, Burke, and Ernzerhof functional [\[30,31\]](#page-4-18), projector-augmented wave pseudopotentials [\[32\]](#page-4-19) as implemented in VASP [\[33,34\]](#page-5-0), and k-point meshes with a density of 1000 divided by the number of atoms [\[35\]](#page-5-1). A Hubbard-U correction [\[36](#page-5-2)–39] was employed to correct the DFT self-interaction error (see Table S1 [\[40\]](#page-5-3) in the electronic Supplemental Material [\[40\]](#page-5-3)). All DFT energies and atomic forces were converged to 0.05 meV per atom

and 50 meV  $\AA^{-1}$ , respectively, and the plane-wave cutoff was 520 eV.

To more directly understand the response of the TM electronic states on distortions of the local atomic environment, we represent the displacement of the TM and oxygen atoms from their ideal positions in terms of the 21 normal coordinates of the octahedral  $MO<sub>6</sub>$  structure given in Table S2 [\[40\]](#page-5-3). For the octahedral point group, the normal coordinates (excluding rotations and translations) belong to the five different groups  $\nu_1$  through  $\nu_5$  shown in Fig. [1\(b\)](#page-1-0). The symmetric stretching mode  $\nu_1$  corresponds to an isotropic scaling and does not contribute to any distortion. The asymmetric stretching modes of type  $\nu_2$  are the modes of the Jahn-Teller (JT) distortion [\[43](#page-5-4)–45]. The modes of types  $\nu_3$  and  $\nu_4$  describe bending and twisting, respectively, and the modes in  $\nu_5$  describe the displacement of the cation from the center of the site.

The amplitude of the four symmetry-breaking normal modes around the metal cations in the two ordered ground state structures and disordered SQS are shown in Fig. [1\(a\)](#page-1-0) for all first- and second-row TMs except Mn and Tc. The relative distortions are given by the coefficients of the normal coordinates in the representation of the distorted octahedron D based on an ideal octahedron O,  $D = O + \sum_i c_i \tilde{Q}_i$ , where  $\tilde{Q}_i$  are the normalized normal coordinates of Table S2 [\[40\].](#page-5-3) For each group of normal coordinates, the largest coefficient  $c_i$  is plotted in Fig. [1\(a\)](#page-1-0) and listed in Table S3  $[40]$ . As seen in Fig. [1\(a\),](#page-1-0) the site distortions in most of the ordered layered and  $\gamma$  – LiFeO<sub>2</sub> structures range from 0% to 25% with the exception of LiCuO<sub>2</sub> (layered) and LiAgO<sub>2</sub> ( $\gamma$  – LiFeO<sub>2</sub> structure) which exhibit strong site distortions of type  $\nu_2$  because of the preference of  $d^8$  Cu<sup>3+</sup> and Ag<sup>3+</sup> for square planar coordination. Further, the other ordered compounds exhibit no or only minor distortions ( $\langle 5\% \rangle$ ) in the JT mode ( $\nu_2$ ) and the TM-displacement mode  $(\nu_5)$ . Contributions of the

TM-displacement mode  $(\nu_5)$  are only significant for the second-row TMs Nb, Mo, Ru, and Ag.

The situation is different for the SQS, in which all four types of distortions are present for all of the TMs. In addition, the magnitude of the distortions is, on average, greater, and the contribution of the JT mode is greater than 5% for most of the TMs. Interestingly, the amplitude of the TM-displacement mode  $\nu_5$  is also between 5% and 25% in each SQS. Hence, even cations that reside in nearly undistorted sites in their ground-state structure, e.g.,  $(d<sup>6</sup>)$  $Co<sup>3+</sup>$  and Rh<sup>3+</sup>, will be subject to site distortions in a cation-disordered structure.

To interpret the effect of these site distortions on the energy of the disordered phase we consider the band-sum expression of the total energy [46–[48\],](#page-5-5)  $U = E_{\text{band}} + D$ with  $E_{\text{band}} = \sum_{i}^{\text{occ}} \varepsilon_i$ , where  $\varepsilon_i$  are the eigenvalues of the Kohn-Sham single-electron Hamiltonian (i.e., the energies of the electronic eigenstates), and the sum over the eigenvalues of all occupied electronic states is the band energy  $E_{band}$ . The term  $D$  contains a double-counting correction, electrostatics, and contributions from the exchange-correlation functional, and it is mostly deter-mined by pairwise interactions [\[46\].](#page-5-5)  $E_{band}$  captures the distance and angle-dependent change of the electronic states with the local structural environment [\[46\].](#page-5-5) Hence, to understand the energy trends in disordered structures we ought to analyze the response of  $E_{band}$  on site distortions.

We seek a qualitative picture of band-energy trends for general TM oxides rather than quantitative energies for select compositions (as these can be obtained directly from DFT), so that a simple tight-binding (TB) model of the electronic structure is most appropriate. As such, we construct a model Hamiltonian for an octahedral TM site based on the oxygen  $p$  and TM  $d$  hydrogenlike atomic orbitals in the spirit of the extended Hückel method [\[49\]](#page-5-6),  $H_{ij} = K(H_{ii} + H_{jj})/2 S_{ij}$ , where  $S_{ij} = \int \phi_i(r) \phi_j(r) dr$  is

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FIG. 1. (a) TM site distortion in the LiTMO<sub>2</sub> ground state structures (layered  $\alpha$  – NaFeO<sub>2</sub> structure and  $\gamma$  – LiFeO<sub>2</sub> structure) and in the SQS of all first and second-row TMs except Mn and Tc. The distortions are decomposed into contributions from different normal mode symmetry groups. The first normal mode ( $\nu_1$ ) corresponds to an isotropic scaling and is not considered.  $\nu_2$  is the Jahn-Teller distortion,  $\nu_3$  corresponds to bending distortions,  $\nu_4$  to twisting, and  $\nu_5$  describes the displacement of the TM from the center of the site. (b) Schematic of the normal modes of an octahedral TM site grouped by symmetry (rotations and translations are not shown).

the overlap of orbitals  $\phi_i$  and  $\phi_j$ ,  $K=1.75$  is the Wolfsberg– Helmholtz constant [\[49,50\]](#page-5-6), and the diagonal Hamilton matrix elements  $H_{ii}$  are the ionization potentials (IPs) of the oxygen  $p$  and TM  $d$  valence states. The angular dependence of the overlap integrals is obtained from the tables by Slater and Koster [\[41\]](#page-5-7) for reference integrals with appropriate radial symmetry (see Supplemental Material [\[40\]](#page-5-3)).

Note that the actual choice of the (TM-species dependent) IPs only affects the absolute energy of the electronic states  $\varepsilon_i$  but not the relative change with different distortions, so for the present discussion, we only require that the oxygen  $p$  level lies lower in energy than the TM  $d$  level. Thus, the choice made for the IPs does not limit the generality of the trends discussed in the following.

Figure [2](#page-2-0) shows the change of the electronic states and of  $E_{band}$  that results from distortions in the directions of the JT mode  $(\nu_2)$  and the TM-displacement mode  $(\nu_5)$  predicted by the TB model. The impact of bending  $(\nu_3)$  and twisting  $(\nu_4)$  distortions on  $E_{band}$  (Fig. S5 [\[40\]\)](#page-5-3) is small compared to the JT  $(\nu_2)$  and displacement  $(\nu_5)$  modes. Unlike the bending and twisting modes, the JT distortion and the TM displacement directly affect the TM-O bond length,

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FIG. 2. Change of the electronic states (top) and the band energy (bottom) upon distortion of an octahedral TM site in the direction of (a) the Jahn–Teller mode  $(\nu_2)$  and (b) the TMdisplacement mode  $(\nu_5)$ . The band energies for four electronic configurations are shown:  $d^0$  (blue circles),  $d^4$  high spin (hs, red squares),  $d^6$  low spin (ls, green line), and  $d^8$  (gray dashed line). The energies shown in panel (a) are based on the conventional Jahn–Teller mode (compression or elongation in  $z$  direction) which is a linear combination of the normal coordinates of type  $\nu_2$ shown in Fig. [1\(b\)](#page-1-0). The energy and distortion scales are equal for both normal modes. The labels in the top panels indicate the TM d orbitals that contribute most for distortions along the Cartesian z direction.

explaining the stronger effect of these two modes on the energy levels.

Only the five electronic states corresponding to the TM d orbitals are shown in Fig. [2](#page-2-0), i.e., the two  $e_q$  and three  $t_{2q}$ states in the ideal octahedral crystal field, as the dependence of the lower-lying states on the site distortions is negligible in comparison. The band energies for four d-electron configurations,  $d^0$ ,  $d^4$  (high spin),  $d^6$  (low spin), and  $d^8$  are shown in Fig. [2,](#page-2-0) and the remaining d-electron configurations can be found in Fig.  $S5$  [\[40\].](#page-5-3) Note that  $E_{\text{band}}$ also contains contributions from the lower lying states.

Note that, while the covalent character of the TM-O bond varies with the TM species, the formal TM valence state in oxides usually corresponds to the correct  $d$ -electron count [\[51\]](#page-5-8).

As seen in Fig. [2,](#page-2-0) distortions of the TM site in either JT or TM-displacement mode lower the symmetry such that the degenerate  $e_q$  and  $t_{2q}$  levels split. In the case of the JT mode, the energy of the electronic states changes approximately linearly, whereas TM displacement only gives rise to quadratic and higher-order changes. As a consequence, for TM displacements with amplitudes  $\langle 5\% \rangle$ , the relative change of the electronic states is small compared to the effect of a JT distortion with a comparable amplitude. However, for distortions with amplitudes of  $\geq 10\%$ , the magnitude of the energy change resulting from both normal modes is comparable.

The same general trend is seen in the band energies (Fig. [2\)](#page-2-0), as the JT distortion results in a linear change of  $E_{\text{band}}$ for some d-electron configurations while the effect of the TM displacement is, at most, quadratic. The net energy change for TM displacements with amplitudes  $>10\%$  is, nevertheless, larger than for JT distortions for most d-electron counts. JT distortions can increase or reduce  $E_{band}$  depending on the electronic configuration of the cation. TM displacements result in a steep increase of  $E_{band}$  for TMs with more than four valence  $d$  electrons and slightly stabilize  $d^1$  and  $d^2$  TMs (Fig. S5 [\[40\]\)](#page-5-3). Note that distortions in either JT or TM-displacement mode result in a strong increase of  $E_{band}$  for  $d^6$  (low spin) and  $d^{10}$  configurations. Finally, in the absence of  $t_{2g}$  and  $e_g$  electrons, i.e., for the  $d^0$  configuration,  $E_{band}$  solely depends on the lowerlying oxygen-dominated orbitals that are always occupied. As a result,  $d^0$  TMs are least sensitive with respect to TM site distortions, and the variation of  $E_{band}$  is only minor.

A key conclusion of the original paper by Jahn and Teller [\[43\]](#page-5-4) is that, to first order, only distortions of type  $\nu_2$  can affect the electronic energy. Our results are fully consistent with the JT theorem, as the TM-displacement mode  $(\nu_5)$ only brings about at most second order changes of  $E_{band}$ . When the TM ion is displaced from the center of its octahedral site, one TM-O bond is elongated and a second TM-O bond is compressed, and only the difference of both effects is seen in  $E_{\text{band}}$ .

Most importantly, here, we find that the second-order contributions to the band energy by the TM displacement

<span id="page-3-0"></span>TABLE I. Cation-disordered  $Li_{1+x}TM_{1-x}O_2$  made by conventional solid-state synthesis.  $Li_{1,211}Mo_{0,467}Cr_{0,3}O_2$ , forms in the layered  $(\alpha - \text{NaFeO}_2)$  structure and converts to the disordered (NaCl) structure upon Li extraction and simultaneous oxidation of  $Mo^{5+}$  to  $Mo^{6+}$  [\[5\]](#page-4-14). The other materials form directly in the disordered rocksalt structure.  $d^0$  TM cations are highlighted in bold font.

Composition	TM cations
LiMO <sub>2</sub> (M = Ti, Fe) [24]	$Ti^{3+}$ , $Fe^{3+}$
$Li_{1+r}V_2O_5$ [52]	$V^{3+}$ , $V^{5+}$
$LiM_{0.5}Ti_{0.5}O_2$ (M = Fe, Ni) [17,53]	$M^{2+}$ , Ti <sup>4+</sup>
$Li_{1,211}Mo_{0,467}Cr_{0,3}O_2$ [5] <sup>a</sup>	$Mo^{5+}$ , $Cr^{3+}$
$Li_{1,25}Nb_{0,25}Mn_0$ 5O <sub>2</sub> [19]	$Nb^{5+}$ , Mn <sup>3+</sup>
$Li_{1,3}Nb_{0,3+x}M_{0,4-x}O_2$ (M = Mn, Fe, Co, Ni) [20]	$Nb^{5+}$ , $M^{3+}$
$Li_{1+x}Ti_{2x}Fe_{1-3x}O_2$ [21]	$Ti^{4+}$ , $Fe^{3+}$
$Li_{1.6-4x}Mo_{0.4-x}Ni_{5x}O_2$ [22]	$Mo^{6+}$ , Ni <sup>2+</sup>
$Li_{1,3}Nb_{0,3}V_{0,4}O_2$ [23]	$Nb^{5+}$ , $V^{3+}$
LiCo <sub>0.5</sub> Zr <sub>0.5</sub> O <sub>2</sub> [8]	$Co^{2+}$ , $Zr^{4+}$

<sup>a</sup>Forms in layered structure but disorders upon Li extraction.

are not negligible for the large distortions that occur in cation-disordered Li-TM oxides with amplitudes between 5% and 25% (Fig. [1\)](#page-1-0). Additionally, from the band energies in Fig. [2](#page-2-0) it is obvious that not only JT active TMs are affected by site distortions, as significant energy contributions occur from distortions for any TM ion with more than zero d electrons. Since only the band energy of  $d^0$  TMs is insensitive with respect to distortions, we conclude that  $d^0$ TMs tolerate disordered phases even for relatively large ionic radius differences.

As seen in Fig. S6 [\[40\]](#page-5-3), the DFT band energies of actual  $d^0$ ,  $d^6$ , and  $d^8$  Li-TM oxides (LiYO<sub>2</sub>, LiRhO<sub>2</sub>, and  $LiAgO<sub>2</sub>$ ) precisely follow the trend predicted by the TB model for TM-displacement distortions.

Table [I](#page-3-0) lists published cation-disordered Li-TM oxides that were made by conventional solid-state synthesis  $[5,8,17,19-24,52,53]$  $[5,8,17,19-24,52,53]$ . Indeed, most of the compositions contain one TM species in a formal valence state corresponding to the  $d^0$  electronic configuration: Ti<sup>4+</sup>, V<sup>5+</sup>,  $Zr^{4+}$ , Nb<sup>5+</sup>, or Mo<sup>6+</sup>. The Li-Mo-Cr oxide of Ref. [\[5\]](#page-4-14) forms in the layered structure but becomes cation disordered when Li is extracted and  $Mo^{5+}$  is oxidized to  $d^0$  Mo<sup>6+</sup>. The only cation-disordered compositions that do not contain  $d^0$  TM species are stoichiometric LiTiO<sub>2</sub>  $(d<sup>1</sup> Ti<sup>3+</sup>)$  and LiFeO<sub>2</sub>  $(d<sup>5</sup> Fe<sup>3+</sup>)$  [\[24\].](#page-4-20) In the case of  $LiFeO<sub>2</sub>$ , calorimetry measurements showed that the disordered  $\alpha$  – LiFeO<sub>2</sub> phase is, in fact, significantly higher (~90 meV) in energy than the ordered  $\gamma$  – LiFeO<sub>2</sub> ground state [\[54\]](#page-5-9), and the formation of the  $\alpha$  phase during synthesis has been attributed to kinetic reasons [\[54\]](#page-5-9). A similar mechanism might be responsible for the stabilization of cation-disordered LiTiO<sub>2</sub>. Hence, the literature supports our hypothesis that  $d^0$  cations promote cation disorder.

Finally, to understand how the presence of  $d^0$  cations within a composition with several TM species can stabilize disordered structures, we systematically enumerated atomic configurations of  $LiNi<sub>0.5</sub>Mn<sub>0.5</sub>O<sub>2</sub>$ , which is known to form a layered ground-state structure [\[55\],](#page-5-10) and  $\text{LiNi}_0$ ,  $\text{Ti}_0$ ,  $\text{O}_2$ , which is cation disordered at typical synthesis temperatures [\[17\]](#page-4-12). For both compositions, the DFT energies of 469 symmetrically distinct atomic configurations with up to eight cation sites were computed. Figure [3\(a\)](#page-3-1) shows the number of atomic configurations within an energy range of  $100$  meV/cation above the ground state for both oxides. As seen in the figure, the number of configurations within this energy interval is far greater for  $LiNi<sub>0.5</sub>Ti<sub>0.5</sub>O<sub>2</sub>$  (136 configuration) than for LiNi<sub>0.5</sub>Mn<sub>0.5</sub>O<sub>2</sub> (57 configurations). This means, for the Ti-containing composition, more atomic orderings are thermally accessible at synthesis conditions. The origin of this very different energetic behavior becomes obvious when the TM site distortions are considered: Figures [3\(b\)](#page-3-1) and [3\(c\)](#page-3-1) show the TMdisplacement distortions in the 50 most stable configurations of both materials. As seen in the figure, the  $d^0$  Ti<sup>4+</sup> cations accommodate large site distortions allowing the  $Ni<sup>2+</sup>$  sites to remain close to their preferred geometry. Since  $d^0$  cations are less sensitive with respect to site distortions, the energy of these 50 configurations is within  $40 \text{ meV/cation from the computational ground state. In}$ 

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FIG. 3. (a) Number of LiNi<sub>0.5</sub>Ti<sub>0.5</sub>O<sub>2</sub> and LiNi<sub>0.5</sub>Mn<sub>0.5</sub>O<sub>2</sub> configurations within a 100 meV/cation from the ground state out of 469 distinct configurations with up to four formula units. (b) Energy per cation and TM site distortion of the 50 most stable (b)  $\text{Lin}_{10.5}\text{Ti}_{0.5}\text{O}_2$ and (c) LiNi<sub>0.5</sub>Mn<sub>0.5</sub>O<sub>2</sub> configurations. Only TM-displacement ( $\nu$ <sub>5</sub>) distortions are considered.

contrast, the energy of the  $LiNi<sub>0.5</sub>Mn<sub>0.5</sub>O<sub>2</sub>$  configurations increases rapidly with the relative distortion of the  $d^8$  Ni<sup>2+</sup> and  $d^3$  Mn<sup>4+</sup> sites. Note that some distortion of the Ni and Mn sites is tolerable, as the band energy increases quadratically with the amplitude of  $\nu$ <sub>5</sub> [Fig. [2\(b\)\]](#page-2-0). Hence, not only do  $d^0$  cations have a low energy penalty in distorted sites, their flexibility to distort allows the other TM cations to minimize their distortions.

In conclusion, we identified a specific electronicstructure effect that is responsible for the stabilization of cation-disordered phases in lithium-transition-metal oxides with large cation size differences. We showed that the strong transition-metal site distortions that occur when these compositions disorder give rise to significant secondorder energy contributions. As a consequence,  $d^6$  transition metals are strongly destabilized in cation-disordered phases, whereas  $d^0$  transition metals can tolerate such distortions with very low energy cost. Owing to this tolerance,  $d^0$  species can absorb site distortions in mixed compositions, even when the cation sizes differ significantly. At the example of technologically relevant lithium transition-metal oxides, we show that this insight can function as a concrete guideline for the design of novel cation-disordered compositions. While our numerical data focused on lithium-transition-metal oxides, we believe that the specific mechanism presented here, by which disorder comes at lower energy cost when the TM can accommodate the distorted site more easily, will be more generally applicable to other oxides with octahedral cations.

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