## Determination of Surface Recombination Velocities at Contacts in Organic Semiconductor Devices Using Injected Carrier Reservoirs

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A method to determine surface recombination velocities at collecting contacts in interface-limited organic semiconductor devices, based on the extraction of injected carrier reservoirs in a single-carrier sandwich-type structure, is presented. The analytical framework is derived and verified with drift-diffusion simulations. The method is demonstrated on solution-processed organic semiconductor devices with hole-blocking  $TiO_2$ /organic and  $SiO_2$ /organic interfaces, relevant for solar cell and transistor applications, respectively.

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Contacts play a crucial part in thin-film semiconductor devices, such as those based on organic and perovskite semiconductors. Most electronic devices require at least one contact that is either charge collecting or blocking. For instance, in organic field effect transistors, the source and drain constitute collecting contacts, while the gate electrode, covered with an insulating dielectric, needs to be blocking [\[1\]](#page-3-1). Many applications also require selective contacts that are able to efficiently either inject or collect one type of charge carrier while simultaneously blocking the other type. This is of particular importance in organic and perovskite solar cells, where contacts that are able to efficiently collect majority carriers, while simultaneously blocking minority carriers, are desired [2–[9\].](#page-3-2) However, a comprehensive understanding of the processes taking place at the contacts in organic thin-film semiconductor devices is still lacking.

The current of carriers flowing out from the semiconductor (to the electrode) at a collecting contact is generally described in terms of an effective surface recom-bination current [10–[13\]:](#page-3-3)

$$
J_R = qS_R[n_c - n_0],\tag{1}
$$

where  $S_R$  is the associated surface recombination velocity,  $n_c$  is the carrier density at the surface and  $n_0$  is the corresponding equilibrium density, and  $q$  is the elementary charge. The surface recombination velocity is a characteristic for the quality of the surface and can be expressed as  $S_R = \sigma_R v_R N_s$ , where  $\sigma_R$  is an *effective* capture cross section,  $v_R$  is the carrier emission velocity at the contact, and  $N<sub>s</sub>$  is the surface density of recombination centers [\[3,10\]](#page-3-4). At an ideal semiconductor-metal contact, acting as an infinite recombination center ( $\sigma_R N_s \rightarrow 1$ ), the upper limit of  $S_R$  is typically on the order of 10<sup>6</sup> cm/s at temperature  $T = 300$  K in accordance with the thermionic emission theory [\[4,10\]](#page-3-5). A schematic picture of surface recombination for holes at a contact is shown in Fig. [1\(a\)](#page-0-0).

In general, if  $S_R$  is larger than the effective transport velocity  $v_D \sim \mu |F|$  of carriers within the semiconductor layer ( $S_R \gg v_D$ ), the carrier collection is limited by the bulk (diffusion limited) [\[9,14](#page-3-6)–16]. In this case, the contact virtually acts as a perfect collector ( $S_R \rightarrow \infty$ ). Here,  $\mu$  is the carrier mobility and F the electric field. If  $S_R < v_D$ , on the other hand, the charge collection is controlled by kinetics at the contact as the carrier transport becomes limited by the interface [\[9,10,16,17\].](#page-3-6) The surface recombination at a contact that is blocking from the viewpoint of carrier collection is by definition also interface limited ( $S_R \ll v_D$ ). However, the condition  $S_R \ll v_D$  alone does not necessarily fulfill the requirements of a blocking contact. Ideally, a blocking contact with  $S_R = 0$  is achieved by inserting an interlayer that prevents all carriers from leaving the device at the contact ( $\sigma_R N_s \rightarrow 0$ ). In practice, however,

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FIG. 1. (a) Schematic picture of surface recombination at a semiconductor-electrode contact for holes being collected at a metal electrode. In (b) and (c), a schematic picture of the CELIV technique is shown. A linear voltage pulse  $u(t)$  is applied to extract charge carriers at the dc voltage V. From the corresponding extraction current transient  $j(t)$  (corrected for the steady-state current), the extracted charge is obtained from  $Q_{\text{extr}} =$ current), the extracted charge is obtained from  $Q_{\text{extr}} = \int_0^{t_{\text{extr}}}[f(t) - j_0]dt$ , where  $j_0 = (\varepsilon \varepsilon_0/d)(du/dt) = (\varepsilon \varepsilon_0 u_{\text{max}}/dt_{\text{pulse}})$ .

recombination centers (gap states) are likely to always be present within the interface layer ( $\sigma_R N_s \neq 0$ ) [\[2,3,10,13,18\]](#page-3-2), effectively leading to nonzero  $S_R$  [see Fig. [1\(a\)](#page-0-0)]. The surface recombination velocity is thus a key parameter in understanding the processes taking place at the contacts.

In this Letter, a method to determine the surface recombination velocity at limiting contacts in organic semiconductor devices is proposed. The method is based on the analytical derivation of the relationship between the net charge, injected into the semiconductor layer in a single-carrier device structure, and the surface recombination velocity at the collecting contact. By determining the injected charge by charge extraction measurements, the surface recombination velocity is subsequently obtained. The method can be used to investigate properties of (nominally) blocking buffer layers, such as selective electrode interlayers and gate dielectrics, in organic semiconductor devices.

The device under consideration is hole-only consisting of a semiconductor layer, sandwiched between a hole-injecting contact at the anode  $(x = 0)$  and a hole-collecting contact with a finite  $S_R$  for holes at the cathode  $(x = d)$ , where d is the thickness of the semiconductor layer. By applying a dc voltage  $V > V_{bi}$ , where  $V_{bi}$  is the (effective) built-in voltage of the device, holes are readily injected into the semiconductor layer from the injecting anode contact. The net injected charge accumulating in the layer is given by  $\Delta Q = q \int_0^d \Delta p(x) dx$ , where  $\Delta p(x) = p(x) - p_0(x)$  is the difference between the hole density at the applied voltage V and the equilibrium hole density. The surface recombination current at the collecting cathode contact is given by  $J_p|_{\text{cat}} = qS_R\Delta p(d)$ , where  $p(d)$  is the hole density at the cathode interface. The impact of  $S_R$  for holes at the cathode is simulated in Fig. [2.](#page-1-0) For the simulations, a previously developed drift-diffusion-Poisson model is used [\[17\]](#page-3-7). Typical energy level diagrams for the case  $S_R < v_D$  are shown in Fig. [2\(a\).](#page-1-0) In Fig. [2\(b\),](#page-1-0) the simulated  $\Delta Q$  as a function of V at different surface recombination velocities is shown, as depicted by the symbols. At high  $S_R$ , in this case larger than 0.10 cm/s,  $\Delta Q$  is independent of  $S_R$ . This corresponds to the bulk-limited regime  $S_R \gg v_D$ , when  $\Delta Q$  is independent of the kinetics at the cathode interface. Note that, close to flat-band conditions ( $V = V_{\text{bi}}$ ),  $v_D \approx \mu kT/gd$  corresponding to 0.13 cm/s in this case. At smaller  $S_R$ , however, a drastic increase in  $\Delta Q$  with decreasing  $S_R$  and increasing V is obtained.

The behavior in the  $S_R \ll v_D$  limit can be understood as follows. For a planar hole-only device, the steady-state continuity equation requires that  $dJ_D/dx = 0$ , where  $J_D$  is the current density. Hence, the size of the accumulated reservoir of bias-induced holes is controlled by the current density flowing through the device  $J_D(V) = J_p|_{cat} =$  $qS_R\Delta p(d)$ , being dependent on both  $S_R$  and V. As more holes are being transported to the cathode interface than holes leaving the device at the cathode, the injected holes will accumulate at the cathode interface. Under these circumstances ( $S_R \ll v_D$ ), the quasi-Fermi-level  $E_{F_p}$  is flat in the active layer at quasiequilibrium conditions [\[9,10,16\]](#page-3-6). The hole density is given by  $p(x) = N \exp\left(\frac{E_n(x)}{F_n(x)}\right)$  $E_{Fp}/kT$  =  $p(d)$  exp  $(\left[E_v(x) - E_v(d)\right]/kT)$ , where N is the density of transport states,  $k$  is the Boltzmann constant, and  $E<sub>v</sub>(x)$  is the (effective) hole transport level. Upon solving the Poisson equation,

$$
\frac{1}{q}\frac{d^2E_v(x)}{dx^2} = \frac{qp(x)}{\varepsilon\varepsilon_0},\tag{2}
$$

<span id="page-1-1"></span>where  $\varepsilon \varepsilon_0$  is the permittivity, the injected hole density near the cathode interface can be expressed as  $p(x) = \frac{p(d)}{1 + [d - x]/\lambda\sqrt{2}}^2$ , with the Debye length  $\lambda = \sqrt{\varepsilon \varepsilon_0 kT/q^2p(d)}$  [\[10,19,20\].](#page-3-3) In the derivation of  $p(x)$ , it was assumed that a minimum for  $E<sub>v</sub>(x)$  exists within the active layer at a distance ≫λ from the cathode interface. The injected charge, accumulating at the cathode interface, becomes

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FIG. 2. (a) Simulated energy level diagrams at  $V = 0$  (upper) and  $V > V_{bi}$  (lower) are shown for the case  $S_R < v_D$  at the cathode  $(x = d)$ . In (b), the simulated  $\Delta Q$  as a function of applied voltage V for varying  $S_R$  is indicated by symbols. The analytical approximation Eq. [\(3\)](#page-1-1) is depicted by the corresponding solid lines. The current density  $J_D(V)$  is obtained from the simulated JV curve (not shown). The dashed line corresponds to  $\Delta Q = \frac{3}{2}CU$ . In (c), the normalized  $Q_{\text{norm}}/J_{\text{norm}}^{1/2}$  as a function of  $S_R/(\mu kT/qd)$  is shown, where  $Q_{\text{norm}} \equiv \Delta Q/CU$ ,  $J_{\text{norm}} \equiv J_D/J_{\text{SCLC}}$ , and  $\mu kT/qd \approx 0.13 \text{ cm/s}$ . In the simulations we assume  $V_{\text{bi}} = 0.5 \text{ V}$ ,  $d = 200 \text{ nm}$ ,  $\varepsilon = 3$ ,  $T = 300$  K,  $\mu = 10^{-4}$  cm<sup>2</sup>/V s, and an injection barrier of 0.20 eV at the anode.

$$
\Delta Q \approx \sqrt{2\varepsilon \varepsilon_0 kT p(d)} = \sqrt{\frac{2\varepsilon \varepsilon_0 kT}{qS_R}} J_D(V),\tag{3}
$$

for  $p(d) = J_D(V)/qS_R \gg p_0(d)$ . Indeed, upon comparing Eq. [\(3\)](#page-1-1) (solid lines) with the simulated  $\Delta Q$  (symbols) in Fig. [2\(b\),](#page-1-0) an excellent agreement is found for  $V > V_{\text{bi}}$ .

In Fig. [2\(c\),](#page-1-0) the ratio  $\Delta Q/J_D^{1/2}$  is simulated as a function of  $S_R/\tilde{\mu}kT/qd$ ). Note that Eq. [\(3\)](#page-1-1) can be reexpressed as  $\Delta Q \sqrt{J_{\text{SCLC}}/J_D} = 1.5CU \sqrt{\mu kT/qS_Rd}$ , where  $C =$  $\epsilon \epsilon_0/d$  is the geometric capacitance of the semiconductor,  $J_{\text{SCLC}} = 9 \varepsilon \varepsilon_0 \mu U^2 / 8d^3$  is the space-charge-limited current density (see Refs.  $[15,21]$ ), and U is the (effective) potential difference across the layer. Comparing the analytical prediction with the simulations, we see that an excellent agreement is obtained when  $S_R < \mu kT/qd$ . On the other hand, as  $S_R > \mu kT/qd$ , the charge transport is no longer limited by the kinetics at the cathode. In this case, the injected charge instead approaches  $\Delta Q = \frac{3}{2}CU$  as  $J_D \rightarrow J_{\text{SCLC}}$ , as expected from the theory of bulk-limited charge transport [\[21\].](#page-4-0)

Experimentally, the injected charge at V can be quantified by applying a voltage pulse  $u(t)$  of reversed polarity (relative to V) and measuring the induced extraction current transient  $j(t)$ . In this work, we use charge extraction by a linearly increasing voltage (CELIV) pulse to extract the injected charge [\[22](#page-4-1)–24]; a schematic picture is shown in Figs. [1\(b\)](#page-0-0) and [1\(c\).](#page-0-0) For a hole-only device, the extracted charge can generally be expressed as [\[25\]](#page-4-2)

$$
Q_{\text{extr}} \equiv \int_{0}^{t_{\text{extr}}} [j(t) - j_0 - J_D] dt = -\frac{q}{d} \int_{0}^{d} \int_{x}^{d} \Delta p dx' dx, \qquad (4)
$$

<span id="page-2-0"></span>where  $j_0 = C(du/dt)$  and  $t_{\text{extr}}$  is the time at which the injected bias-induced carriers have been extracted. In our case of an injected surface charge of holes at the cathode, we find  $|Q_{\text{extr}}| \approx \Delta Q$ , provided that  $\lambda \ll d$ . As a result, the extracted charge at  $V > V_{bi}$  can be used to determine the surface recombination velocity at the contact via

$$
S_R = \frac{2\varepsilon\varepsilon_0 kT}{qQ_{\text{extr}}^2} J_D(V),\tag{5}
$$

where  $J_D(V)$  is the steady-state current density at  $V > V_{\rm bi}$ , obtained from the dark current-voltage characteristics. The determination of  $S_R$  is limited to the case  $S_R < v_D$ . If  $S_R \gg v_D$ , however, Eq. [\(5\)](#page-2-0) instead gives an effective (bulk-limited) transport velocity  $S_R^{\text{eff}} \approx \mu kT/qd$  at the contact, corresponding to a lower limit estimate of  $S_R$ . In the following, the method is demonstrated on solutionprocessed organic semiconductor devices, employing  $TiO<sub>2</sub>$  and  $SiO<sub>2</sub>$  as electrode buffer layers (for experimental details, see Supplemental Material [\[26\]\)](#page-4-3).

We first demonstrate the method on an inverted organic solar cell device with  $TiO<sub>2</sub>$  as the cathode interlayer.  $TiO<sub>2</sub>$  has been commonly used as an electron-selective (holeblocking) layer in organic, dye-sensitized, and perovskite solar cells [\[2,7,30\].](#page-3-2) The organic semiconductor layer consists of P3HT:PCBM, widely studied in organic solar cell research. The hole-only device structure is ITO/  $TiO<sub>2</sub>(7 nm)/P3HT$ : PCBM/Cu, where Cu is used as the hole-injecting anode. By applying a positive dc bias, holes are accumulated at the  $TiO<sub>2</sub>/P3HT$ : PCBM interface. These charges are subsequently extracted using CELIV. In Figs. [3\(a\)](#page-2-1) and [3\(b\)](#page-2-1), the extracted charge and steady-state current density are shown at different dc voltages V, respectively. The corresponding surface recombination velocities  $S_R$  (symbols), as calculated using Eq. [\(5\)](#page-2-0), are presented in Fig. [3\(c\).](#page-2-1) The analysis yields a surface recombination velocity of  $S_R \approx 6 \times 10^{-6}$  cm/s for holes at the TiO<sub>2</sub>/P3HT: PCBM interface, consistent with find-ings in Ref. [\[24\]](#page-4-4). This is to be compared to  $v_D \sim \mu kT/qd$ estimated to be  $0.06 \text{ cm/s}$ . Introducing the hole-blocking  $TiO<sub>2</sub>$  layer effectively reduces the hole transport velocity by a factor of  $10<sup>4</sup>$  at the cathode contact. However, a small number of holes are still able to leak through the  $TiO<sub>2</sub>$  layer, suggesting that recombination (with electrons in the cathode layer) is taking place at the  $TiO<sub>2</sub>/organic$  contact (cf. Fig. [1](#page-0-0)).

In general, there are also parasitic conductive pathways present for the current to circumvent the device (or the blocking layer), giving rise to additional leakage currents.

<span id="page-2-1"></span>

FIG. 3. In (a) and (b), the extracted charge  $Q_{\text{extr}}$  and steady-state current density J, respectively, are shown for  $TiO<sub>2</sub>/P3HT$ : PCBM (circles) and  $SiO<sub>2</sub>/P3HT$  (squares) interfaces at different V. In (c), the corresponding  $S_R$  for holes is shown, as obtained by Eq. [\(5\)](#page-2-0) (symbols). The open and solid squares indicate  $SiO_2/P3HT$  data that have been uncorrected  $(R_{\rm sh} = \infty)$  and corrected  $(R_{\rm sh} \approx 1050 \Omega \text{ m}^2)$  for the shunt resistance, respectively. The dashed lines in (a) and (c) correspond to  $S_R = 5.8 \times 10^{-6}$  cm/s and  $S_R = 4.5 \times 10^{-9}$  cm/s for TiO<sub>2</sub>/ P3HT∶PCBM and  $SiO<sub>2</sub>/P3HT$ , respectively. In (d), the extracted charge for  $SiO_2/P3HT$  [from (a)] is shown on the linear scale (symbols); the corresponding  $dJ/dV$  [mS/m<sup>2</sup>] as a function of  $dQ_{\text{extr}}^2/dV$  [(C/m<sup>2</sup>)<sup>2</sup>/MV] are shown in the inset.

<span id="page-3-9"></span>These leakage currents are typically described in terms of a finite shunt resistance. Taking this effect into account, the total measured current density is given by

$$
J(V) = J_D(V) + V/R_{\rm sh},\tag{6}
$$

<span id="page-3-10"></span>where  $R_{\rm sh}$  is the effective shunt resistance in units of  $\Omega \cdot m^2$ . Neglecting the presence of a finite shunt resistance leads to an overestimation of  $J_D(V)$  and thereby also  $S_R$ . Based on Eq. [\(6\),](#page-3-9) the effect of shunts can be taken into account by differentiating with respect to V and making use of Eq.  $(5)$ ; one finds

$$
\frac{dJ(V)}{dV} = \frac{1}{R_{\rm sh}} + \frac{qS_R}{2\epsilon\epsilon_0 kT} \frac{d[Q_{\rm extr}^2]}{dV},\tag{7}
$$

assuming  $S_R$  to be independent of V. By plotting  $dJ(V)/dV$  as a function of  $dQ_{\text{extr}}^2/dV$ , the shunt resistance is obtained from the intercept, while  $S_R$  is obtained from the slope. For the TiO<sub>2</sub>/P3HT∶PCBM device, the effect of shunts was found to be insignificant.

In Fig. [3,](#page-2-1) we also included an organic semiconductor device of P3HT with a thin insulating  $SiO<sub>2</sub>$  layer, typically used as a gate dielectric in transistor applications [\[1\]](#page-3-1), at the cathode. The device structure is given by  $\text{ITO}/\text{SiO}_2(5 \text{ nm})/$  $P3HT/MoO<sub>3</sub>/Ag$  with MoO<sub>3</sub>/Ag as the hole-injecting anode. The accumulated charge at the  $SiO<sub>2</sub>/P3HT$  interface is found to be closely given by  $Q_{\text{extr}} = C_i U$  [see Fig. [3\(d\)](#page-2-1)], where  $C_i$  is the geometric capacitance of the  $SiO_2$  layer. Because of the low current densities obtained in this case, shunts will dominate at smaller voltages. Utilizing Eq. [\(7\)](#page-3-10), we obtain  $R_{\rm sh} \approx 1050 \ \Omega \cdot m^2$ . The effect of shunts on the extracted  $S_R$  is demonstrated in Fig. [3\(c\)](#page-2-1). After correcting the current for the shunt, we find  $S_R \approx 5 \times 10^{-9}$  cm/s for holes at the  $SiO_2/P3HT$  interface. It should be noted that if shunts are not accounted for, Eq. [\(5\)](#page-2-0) instead gives an upper limit estimate of  $S_R$ .

The above analysis based on Eq. [\(3\)](#page-1-1) assumes the nondegenerate limit to be valid. At very high carrier concentrations (low  $S_R$  and high V), however, density of states (DOS) filling effects become significant [\[28\]](#page-4-5). Under these conditions, the shape of the DOS can be taken into account via a correction factor  $\eta$ , and we obtain  $S_R = \eta S_R^0$ (see Supplemental Material [\[26\]\)](#page-4-3), where  $S_R^0$  corresponds to the nondegenerate case given by Eq. [\(5\)](#page-2-0). In the case of a Gaussian distribution of states  $[\alpha \exp(-E^2/2\sigma^2)]$ ,  $\eta$  is well approximated by  $\eta \approx 1/\text{erf}([-\ln c]^{2/3} kT/\sigma)$  for  $c \le 0.1$ , where  $c = p(d)/N$  is the DOS occupation and  $\sigma$  is the energetic disorder parameter (see Supplemental Material [\[26\]](#page-4-3)). Concomitantly, with  $\sigma = 69$  meV for P3HT [\[29\]](#page-4-6), *n* is close to 1.5 for  $c = 0.1$  (at 300 K). At smaller c, the nondegenerate limit is eventually approached as  $\eta \to 1$ .

In conclusion, a technique to determine (effective) surface recombination velocities at contacts in thin-film devices is presented. The method is based on using a single-carrier device structure with an injecting contact to inject and accumulate a carrier reservoir at the opposite collecting contact interface. From the size of the injected charge reservoir, determined by charge extraction measurements, the surface recombination velocity for carriers accumulating at the collecting contact can be obtained. The analytical framework behind the method is derived and confirmed by numerical simulations. Furthermore, the method is demonstrated on hole-only organic thin-film devices with different hole-blocking buffer layers.

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