

Can *Ab Initio* Theory Explain the Phenomenon of Parity Inversion in ^{11}Be ?

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The weakly bound exotic ^{11}Be nucleus, famous for its ground-state parity inversion and distinct $n + ^{10}\text{Be}$ halo structure, is investigated from first principles using chiral two- and three-nucleon forces. An explicit treatment of continuum effects is found to be indispensable. We study the sensitivity of the ^{11}Be spectrum to the details of the three-nucleon force and demonstrate that only certain chiral interactions are capable of reproducing the parity inversion. With such interactions, the extremely large $E1$ transition between the bound states is reproduced. We compare our photodisintegration calculations to conflicting experimental data and predict a distinct dip around the $3/2^-$ resonance energy. Finally, we predict low-lying $3/2^+$ and $9/2^+$ resonances that are not or not sufficiently measured in experiments.

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The theoretical understanding of exotic neutron-rich nuclei constitutes a tremendous challenge. These systems often cannot be explained by mean-field approaches and contradict the regular shell structure. The spectrum of ^{11}Be has some very peculiar features. The $1/2^+$ ground state (g.s.) is loosely bound by 502 keV with respect to the $n + ^{10}\text{Be}$ threshold and is separated by only 320 keV from its parity-inverted $1/2^-$ partner [1], which would be the expected g.s. in the standard shell-model picture. Such parity inversion, already noticed by Talmi and Unna [2] in the early 1960s, is one of the best examples of the disappearance of the $N = 8$ magic number with an increasing neutron to proton ratio. The next ($n + n + ^9\text{Be}$) breakup threshold appears at 7.31 MeV [3], such that the rich resonance structure at low energies is dominated by the $n + ^{10}\text{Be}$ dynamics. Peculiar also is the electric-dipole transition strength between the two bound states, which has attracted much attention since its first measurement in 1971 [4] and was remeasured in 1983 [5] and 2014 [6]. It is the strongest known transition between low-lying states, attributed to the halo character of ^{11}Be .

An accurate description of this complex spectrum is anticipated to be sensitive to the details of the nuclear force [7], such that a precise knowledge of the nucleon-nucleon (NN) interaction, desirably obtained from first principles, is crucial. Moreover, the inclusion of three-nucleon ($3N$) effects has been found to be indispensable for an accurate description of nuclear systems [8,9]. The chiral effective field theory constitutes one of the most promising candidates for deriving the nuclear interaction. Formulated by Weinberg [10–12], it is based on the fundamental symmetries of QCD and uses pions and nucleons as relevant degrees of freedom. Within this theory, NN , $3N$, and higher many-body interactions arise in a natural hierarchy

[10–16]. The details of these interactions depend on the specific choices made during the construction. In particular, the way the interactions are constrained to experimental data can have a strong impact [17].

In this Letter, we tackle the question if *ab initio* calculations can provide an accurate description of the ^{11}Be spectrum and reproduce the experimental ground state. Pioneering *ab initio* investigations of ^{11}Be did not account for the important effects of $3N$ forces and were incomplete in the treatment of either long- [18] or short-range [19,20] correlations, both of which are crucial to arrive at an accurate description of this system.

In this Letter, we report the first complete *ab initio* calculations of the ^{11}Be nucleus using the framework of the no-core shell model with continuum (NCSMC) [21–23], which combines the capability to describe the extended $n + ^{10}\text{Be}$ configurations of Refs. [19,20] with a robust treatment of many-body short-range correlations. We adopt a family of chiral interactions in which the NN component is constrained, in a traditional sense, to two-nucleon properties [24] and the $3N$ force is fitted in three- and sometimes four-body systems [25–28]. In addition, we also employ a newer chiral interaction, obtained from a simultaneous fit of NN and $3N$ components to nucleon-nucleon scattering data and selected properties of nuclei as complex as ^{25}O [29–31].

Many-body approach.—The general idea of the NCSMC is to represent the A -nucleon wave function as the generalized cluster expansion [21–23]

$$|\Psi_A^{J^\pi T}\rangle = \sum_\lambda c_\lambda^{J^\pi T} |A\lambda J^\pi T\rangle + \sum_\nu \int dr r^2 \frac{\gamma_\nu^{J^\pi T}(r)}{r} \mathcal{A}_\nu |\Phi_\nu^{J^\pi T}\rangle. \quad (1)$$

The first term consists of an expansion over the no-core shell model (NCSM) eigenstates of the compound system $|A\lambda J^\pi T\rangle$ (here ^{11}Be) indexed by λ . These states are expanded in a finite harmonic oscillator basis, and thus well suited to cover the localized correlations of the A -body system, but are inappropriate to describe clustering and scattering properties. The latter properties are addressed by the second term corresponding to an expansion over the antisymmetrized cluster channels $\mathcal{A}_\nu|\Phi_{\nu r}^{J^\pi T}\rangle$ [20], which describe the two clusters (here $n + ^{10}\text{Be}$) in relative motion. Here r denotes the relative distance of the clusters, and ν is a collective index for the relevant quantum numbers. The expansion coefficients $c_\lambda^{J^\pi T}$ and the continuous relative-motion amplitudes $\gamma_\nu^{J^\pi T}(r)$ are obtained as a solution of the generalized eigenvalue problem derived by representing the Schrödinger equation in the model space of expansion (1) as detailed in Refs. [20,22,23]. The resulting NCSMC equations are solved by the coupled-channel R -matrix method on a Lagrange mesh [32–34]. The resonance energies and widths are deduced from the complex poles of the S matrix, via the R -matrix approach extended to complex energies and momenta [35,36].

The inclusion of the $3N$ force is computationally highly demanding and restricts the current application range of the NCSMC. For nuclei with $A > 5$, we rely on an on-the-fly computing of the uncoupled densities discussed in Ref. [37]. The present NCSMC calculations are performed including the first three eigenstates (0^+ , 2_1^+ , 2_2^+) of the ^{10}Be target, entering the cluster states in (1) and at least the first four negative- and three positive-parity eigenstates of ^{11}Be . Such eigenstates are obtained within the NCSM, except in the largest model spaces where, to reduce the dimension of the problem, we use the importance-truncated NCSM [38,39].

Analysis of spectroscopy.—We start by using an interaction and parameter set established in numerous studies [28,37,40–42] and investigate the convergence with respect to the model-space size N_{max} . We use the traditionally fitted chiral interaction where we choose the cutoff in the $3N$ regularization to be $\Lambda_{3N} = 400$ MeV, indicated by $NN + 3N(400)$. To accelerate the convergence of the many-body approach, the interactions are softened via the similarity renormalization group (SRG) [43–45] as described in Refs. [28,42] (see Supplemental Material for details [46]). Note that both the SRG-induced and initial $3N$ forces are treated explicitly at all steps of the calculations.

Without continuum effects, i.e., using the conventional NCSM, a converged ^{11}Be spectrum cannot be obtained within accessible model spaces as demonstrated in Fig. 1. All states are unbound with respect to the $n + ^{10}\text{Be}$ threshold. The positive-parity states converge especially slowly; their excitation energy is too high compared to the experiment. Once continuum effects are taken into account through the inclusion of the $n + ^{10}\text{Be}$ cluster states in the model space, the convergence improves drastically, even though the computed threshold energy of $n + ^{10}\text{Be}$ is not

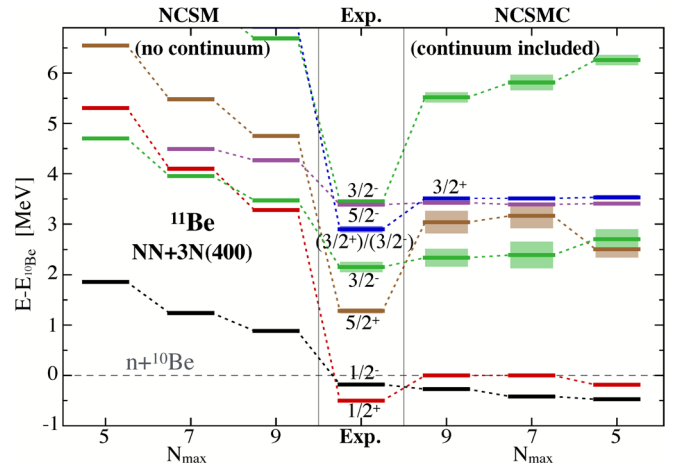


FIG. 1. Spectrum of ^{11}Be with respect to the $n + ^{10}\text{Be}$ threshold. The NCSM (left) and NCSMC (right) calculations are carried out for different model-space sizes ($N_{\text{max}} = 5, 7, 9$). Light boxes of experimental and NCSMC spectra indicate resonance widths. Experimental energies are taken from Ref. [1]. See the text and Supplemental Material for details of the calculations [46].

fully converged, yet. At $N_{\text{max}} = 9$, this energy is -58.4 MeV and increases by 2.3 and 6.2 MeV for the $N_{\text{max}} = 7$ and 5 model spaces, respectively. The extrapolated value of $-60.9(10)$ MeV is underbound with respect to the experimental energy of -64.976 MeV [3]. For the negative parity, the NCSMC achieves an overall quite reasonable description, especially for the three lowest states. On the other hand, the $1/2^+$ state is barely bound and the parity inversion of the bound states is not reproduced. Similarly, the $3/2_1^-$ and $5/2^+$ states are inverted compared to the experiment. The $3/2_2^-$ excitation energy is about 2 MeV larger than the experimental one. Other decay channels (and hence cluster states) presently not included may play a role at such high energies.

We first analyze the sensitivity of the spectrum to the $3N$ interaction in Fig. 2. From left to right, we use exclusively the chiral NN interaction (including SRG-induced $3N$ contributions), the $3N$ interaction with a 500 MeV cutoff, where parts of the two-pion exchange contribution are suppressed ($c_3 = 0$), and the full $3N$ contributions using the cutoffs $\Lambda_{3N} = 500, 450, 400,$ and 350 MeV as introduced in Ref. [28]. The illustrated spectra are expected to show a similar convergence pattern as in the case of the $NN + 3N(400)$ interaction. The omitted SRG-induced beyond- $3N$ contributions are expected to impact the ^{11}Be spectrum only for the $NN + 3N(500)$ interaction, while the remaining spectra are anticipated to be unaffected [27,28,42]. We find the two-pion exchange term to cause the dominant $3N$ effects in the ^{11}Be spectrum. The $3N$ interactions generally increase the excitation energies of both $3/2^-$ resonances, corresponding to the increase in excitation energy of the 2^+ states in ^{10}Be . Neither the inversion of the $1/2^+$ and $1/2^-$ states nor that of the $3/2_1^-$ and $5/2^+$ states can be explained by the adopted $3N$ force versions. Decreasing the $3N$ cutoff initially reduces the

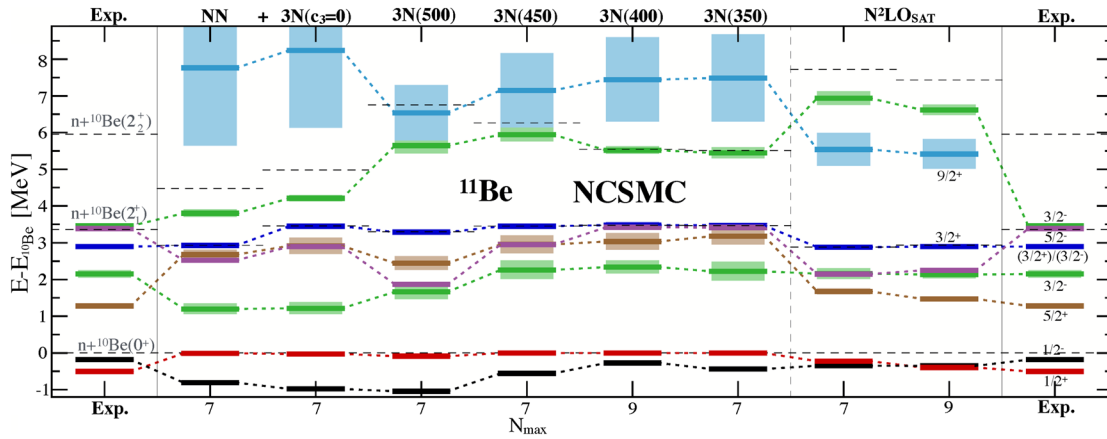


FIG. 2. NCSMC spectrum of ^{11}Be with respect to the $n + ^{10}\text{Be}$ threshold. Dashed black lines indicate the energies of the ^{10}Be states. Light boxes indicate resonance widths. Experimental energies are taken from Refs. [1,51].

bound-state splitting, but below $\Lambda_{3N} = 400$ MeV the influence of the $3N$ interaction is too strongly reduced such that the spectra approach the pure NN result. On the contrary, the converged spectrum with the simultaneously fitted $NN + 3N$ interaction, named $N^2\text{LO}_{\text{SAT}}$ [29], successfully achieves the parity inversions between the $3/2^-_1$ and $5/2^+$ resonances and, albeit marginally, for the bound states. The low-lying spectrum is significantly improved and agrees well with the experiment, presumably due to the more accurate description of long-range properties caused by the fit of the interaction to radii of p -shell nuclei. On the other hand, the strongly overestimated splitting between the $3/2^-_2$ and $5/2^-$ states hints at deficiencies of this interaction, which might originate from a too large splitting of the $p_{1/2}$ - $p_{3/2}$ subshells.

In addition to the resonances observed in the experiment, all theoretical spectra predict a low-lying $9/2^+$ resonance suggested in Refs. [52,53]. For the $N^2\text{LO}_{\text{SAT}}$ interaction, the resonance energy is close to the one predicted by the Gamow shell model [54], although our *ab initio* calculations predict a broader width. Another interesting property is the position of the $3/2^+$ resonance that is strongly influenced by the 2^+_1 state of ^{10}Be . For all theoretical calculations the energies of these correlated states are almost degenerate, while in the experiment the 2^+_1 state in ^{10}Be is about 470 keV above the tentative $3/2^+$ state and coincides with the $3/2^-_2$ and $5/2^-$ resonances.

Nuclear structure and reaction properties.—Except for the two bound states, all the energy levels of Fig. 3 correspond to $n + ^{10}\text{Be}$ scattering states. The corresponding phase shifts obtained with the $N^2\text{LO}_{\text{SAT}}$ interaction are presented in Fig. 3 (see Supplemental Material for further details [46]). The overall proximity of the $N_{\text{max}} = 7$ and 9 results confirms the good convergence with respect to the model space. The states observed in ^{11}Be are typically dominated by a single $n + ^{10}\text{Be}$ partial wave, but the illustrated eigenphase shifts of the $3/2^+$ state consist of a superposition of the $^4S_{3/2}$ and $^2D_{3/2}$ partial waves. The parity of this resonance is experimentally not uniquely extracted

[1], while all *ab initio* calculations concordantly predict it to be positive. The bound-state energies as well as the resonance energies and widths for different interactions and both many-body approaches are summarized in Table I. In the case of the $NN + 3N(400)$ interaction, however, the fast $3/2^+$ phase shift variation near the $n + ^{10}\text{Be}(2^+_1)$ threshold does not correspond to a pole of the scattering matrix, such that this state is not a resonance in the conventional sense and a width could not be extracted reliably. The theoretical widths tend to overestimate the experimental value, but overall the agreement is reasonable, especially for the $N^2\text{LO}_{\text{SAT}}$ interaction. Experimentally, only an upper bound could be determined for the $5/2^-$ resonance width, and the theoretical calculations predict an extremely narrow resonance.

Although the bulk properties of the spectrum are already well described, accurate predictions of observables, such as electric-dipole ($E1$) transitions, which probe the structure of the nucleus, can be quite sensitive to the energies of the involved states with respect to the threshold. Based on our analysis, the discrepancies between the theoretical and experimental energy spectra can be mostly attributed to deficiencies in the nuclear force. Therefore, it can be beneficial to loosen the first-principles paradigm to remedy the insufficiencies in the nuclear force and provide accurate predictions for complex observables using the structure

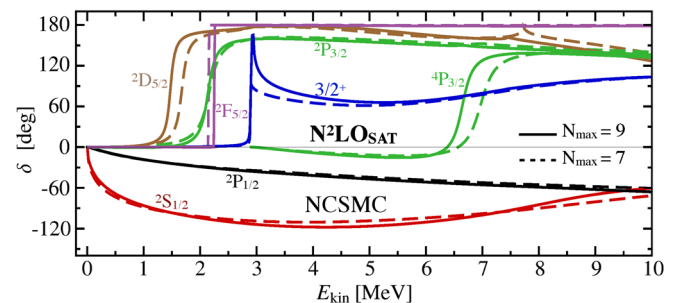


FIG. 3. The $n + ^{10}\text{Be}$ phase shifts as a function of the kinetic energy in the center-of-mass frame. NCSMC phase shifts for the $N^2\text{LO}_{\text{SAT}}$ interaction are compared for two model spaces indicated by N_{max} .

TABLE I. Excitation spectrum of ^{11}Be with respect to the $n + ^{10}\text{Be}$ threshold. Energies and widths are in MeV. The calculations are carried out at $N_{\max} = 9$.

J^π	NCSMC				NCSMC-pheno				Experiment	
	$NN + 3N(400)$		$N^2\text{LO}_{\text{SAT}}$		$N^2\text{LO}_{\text{SAT}}$				E	Γ
	E	Γ	E	Γ	E	Γ	E	Γ		
$1/2^+$	-0.001	...	-0.40	...	-0.50	...	-0.50	...	-0.50	...
$1/2^-$	-0.27	...	-0.35	...	-0.18	...	-0.18	...	-0.18	...
$5/2^+$	3.03	0.44	1.47	0.12	1.31	0.10	1.28	0.1		
$3/2^-$	2.34	0.35	2.14	0.21	2.15	0.19	2.15	0.21		
$3/2^+$	3.48	...	2.90	0.014	2.92	0.06	2.898	0.122		
$5/2^-$	3.43	0.001	2.25	0.0001	3.30	0.0002	3.3874	<0.008		
$3/2_2^-$	5.52	0.20	6.62	0.29	5.72	0.19	3.45	0.01		
$9/2^+$	7.44	2.30	5.42	0.80	5.59	0.62		

information of the *ab initio* approach. In the following, we use a phenomenology-inspired approach indicated by NCSMC-pheno that has been already applied in Refs. [36,55]. In this approach, we adjust the ^{10}Be and ^{11}Be excitation energies of the NCSM eigenstates entering expansion (1) to reproduce the experimental energies of the first low-lying states. Note that the obtained NCSMC-pheno energies are fitted to the experiment, while the theoretical widths, quoted in Table I, are predictions.

An intuitive interpretation of the ^{11}Be g.s. wave function is provided in Fig. 4 by the overlap of the full solution for the g.s. $|\Psi_{\nu}^{J^{\pi}T}\rangle$ in (1) with the cluster portion $|\Phi_{\nu,r}^{J^{\pi}T}\rangle$ given by $r\langle\Phi_{\nu,r}^{J^{\pi}T}|\mathcal{A}_{\nu}|\Psi_{\nu}^{J^{\pi}T}\rangle$. A clearly extended halo structure beyond 20 fm can be identified for the S wave of the $^{10}\text{Be}(0^+) + n$ relative motion. The phenomenological energy adjustment only slightly influences the asymptotic behavior of the S wave, as seen by comparing the solid and dashed black curves, while other partial waves are even indistinguishable on the plot resolution. The corresponding spectroscopic factors for the NCSMC-pheno approach, obtained by integrating the squared cluster form factors in Fig. 4, are $S = 0.90$ (S wave) and $S = 0.16$ (D wave). The S -wave asymptotic normalization coefficient is $0.786 \text{ fm}^{-1/2}$.

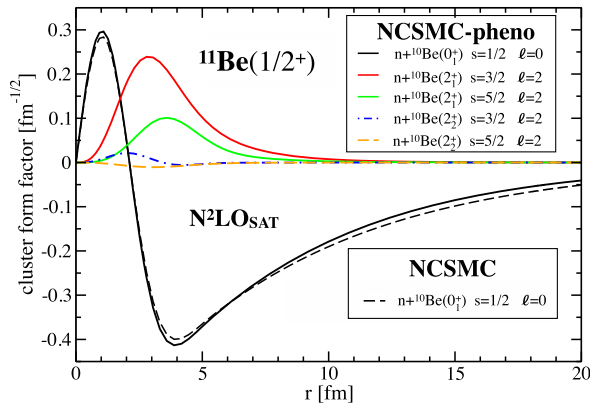


FIG. 4. Comparison of the cluster form factors with the $N^2\text{LO}_{\text{SAT}}$ interaction at $N_{\max} = 9$. Note the coupling between the ^{10}Be target and neutron in the cluster state $|\Phi_{\nu,r}^{J^{\pi}T}\rangle \sim [({}^{10}\text{Be}: J_1^{\pi} T_1) | n: 1/2^+ 1/2^- \rangle^{ST} Y_{\ell}(\hat{r})]^{J^{\pi}T}$.

TABLE II. Reduced transition probability $B(E1: 1/2^- \rightarrow 1/2^+)$ between ^{11}Be bound states in $e^2 \text{ fm}^2$.

	NCSM	NCSMC	NCSMC-pheno	Experiment
$NN + 3N(400)$	0.0005	...	0.146	
$N^2\text{LO}_{\text{SAT}}$	0.0005	0.127	0.117	0.102(2) [6]

The $B(E1)$ transitions are summarized in Table II. Calculations without continuum effects predict the wrong g.s. and underestimate the $E1$ strength by several orders of magnitude. For the NCSMC calculations with the $NN + 3N(400)$ interaction, the $1/2^+$ state is very weakly bound, leading to an unrealistic $E1$ transition. The $N^2\text{LO}_{\text{SAT}}$ interaction successfully reproduces the strong $E1$ transition, albeit the latest measurement [6] is slightly overestimated, even after the phenomenological energy adjustment. There might be small effects arising from a formally necessary SRG evolution of the transition operator. Works along these lines for ^4He suggest a slight reduction of the dipole strength [56,57]. A similar effect would bring the calculated $E1$ transition in better agreement with the experiment [6].

Finally, we study the photodisintegration of the ^{11}Be g.s. into $n + ^{10}\text{Be}$ in Fig. 5. This is proportional to dipole strength distribution $dB(E1)/dE$. In all approaches, a peak of nonresonant nature (see Fig. 3) is present at about 800 keV above the $n + ^{10}\text{Be}$ threshold, particularly pronounced in the $3/2^-$ partial wave. The strong peak for the NCSMC with the $N^2\text{LO}_{\text{SAT}}$ interaction is caused by the slightly extended S -wave tail in Fig. 4 and hence the underestimated binding energy of the $1/2^+$ state. The theoretical predictions are compared to indirect measurements of the photodissociation process extracted from the scattering experiments of ^{11}Be on lead [58–60] and carbon

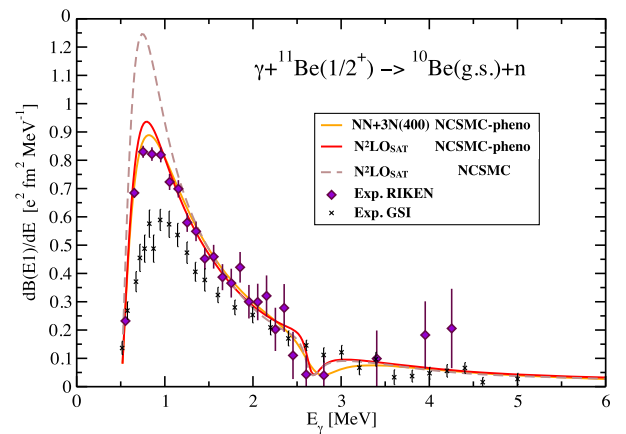


FIG. 5. Dipole strength distribution $dB(E1)/dE$ of the photodisintegration process as a function of the photon energy. Theoretical dipole strength distributions for two chiral interactions with (solid line) and without (dashed line) the phenomenological energy adjustment are compared to the experimental measurements at GSI [58,61] (black dots) and RIKEN [58–60] (violet dots).

[58,61] targets. Our phenomenological adjusted calculations show good agreement with the RIKEN data [58–60]. Based on the analysis in Refs. [56,57], it is doubtful that the missing SRG evolution of the $E1$ -transition operator could explain the $\sim 30\%$ discrepancy with the GSI data [58,61]. A dip in the dipole strength distribution is present at about 2.7 MeV, due to the $3/2_1^-$ resonance. At this energy, the $E1$ matrix element between the ^{11}Be g.s. wave function and the $3/2^-$ partial wave of the $n + ^{10}\text{Be}$ scattering wave function changes its sign. Because of large uncertainties, the experimental data neither confirm nor exclude such a dip. A similar feature, but much less pronounced, can be noticed in microscopic cluster calculations [62] (see Supplemental Material for details [46]).

Conclusions.—We have demonstrated that the inclusion of continuum effects is crucial for a description of the ^{11}Be system and, further, that the spectrum is extremely sensitive to the details of the nuclear $NN + 3N$ interactions and constitutes an important benchmark for future forces. In particular, the parity inversion of the bound states could be achieved only by the $N^2\text{LO}_{\text{SAT}}$ interaction that provides accurate predictions of nuclear radii and matter saturation properties [29,30]. An interesting related endeavor is the investigation of the mirror system $p + ^{10}\text{C}$. New experiments have been performed for the elastic scattering process [63] that will be analyzed with the NCSMC.

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