## Chiral Anomaly and Giant Magnetochiral Anisotropy in Noncentrosymmetric Weyl Semimetals

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We theoretically propose that giant magnetochiral anisotropy is achieved in Weyl semimetals in noncentrosymmetric crystals as a consequence of the chiral anomaly. The magnetochiral anisotropy is the nonlinearity of the resistivity  $\rho$  that depends on the current I and the magnetic field B as  $\rho = \rho_0(1 + \gamma I \cdot B)$ , and can be applied to rectifier devices controlled by B. We derive the formula for the coefficient  $\gamma$  in noncentrosymmetric Weyl semimetals. The obtained formula for  $\gamma$  shows that the magnetochiral anisotropy is strongly enhanced when the chemical potential is tuned to Weyl points, and that noncentrosymmetric Weyl semimetals such as TaAs can exhibit much larger magnetochiral anisotropy than that observed in other materials so far.

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Relativistic electronic states in solids recently have attracted intense interest [1]. They include two-dimensional Dirac electrons in graphene [2], surface states of threedimensional topological insulators [3,4], band crossing in three-dimensional ferromagnetic metals behaving as magnetic monopoles [5], and Weyl semimetals [6,7]. In particular, the magnetotransport phenomena in Weyl semimetals have been actively studied in the context of chiral anomaly [1,7]. Symmetries play a crucial role in the appearance of relativistic electrons. Time-reversal symmetry T and the spatial inversion symmetry P are the most fundamental, in which the energy dispersion of the Bloch electrons satisfies the following constraints:  $\varepsilon_{\sigma}(\mathbf{k}) =$  $\varepsilon_{\bar{\sigma}}(-k)$  ( $\bar{\sigma}$  means the opposite spin to  $\sigma$ ) in the presence of T symmetry, while P symmetry imposes the relation  $\varepsilon_{\sigma}(\mathbf{k}) = \varepsilon_{\sigma}(-\mathbf{k})$ . When both T and P symmetries are present, the Kramers degeneracy occurs at every k point and the band crossings are described by a  $4 \times 4$ Hamiltonian. In this case, additional symmetry such as point group symmetry is required to realize stable massless Dirac electrons [8]. This Kramers degeneracy at each kpoint is lifted by the broken T [5] or P combined with the relativistic spin-orbit interaction. This results in the band crossing described by the  $2 \times 2$  Hamiltonian expanded as  $H(\mathbf{k}) = \sum_{\alpha=0}^{3} h_{\alpha}(\mathbf{k}) \sigma^{\alpha}$  near the crossing point  $\mathbf{k}_{0}$  (Weyl point). Here,  $\sigma^0$  is the unit matrix while  $\boldsymbol{\sigma} = (\sigma^1, \sigma^2, \sigma^3)$  are the Pauli matrices. Expanding  $h_{\alpha}(\mathbf{k})$  with respect to  $\mathbf{k} - \mathbf{k}_0$ up to the linear order, one obtains the Weyl fermion (WF). After an appropriate coordinate transformation and neglecting  $h_0(\mathbf{k})$ , which simply gives the shift of the energy, one obtains

$$H(\mathbf{k}) = \eta v_F \hbar \mathbf{k} \cdot \boldsymbol{\sigma},\tag{1}$$

with the Fermi velocity  $v_F$ , where  $\eta = \pm 1$  determines the chirality. Weyl semimetals are realized when the WFs are the only low-energy excitations at the Fermi energy and the transport properties are governed by WFs.

From the symmetry point of view, Weyl semimetals are classified according to the symmetries, i.e., whether *T* or *P* is broken. Magnetic materials break *T* symmetry and are able to support the Weyl semimetals. One example is the pyrochlore antiferromagnets where the pairs of Weyl electrons appear along the four equivalent directions in momentum space [1,9]. In this system, *P* symmetry is intact for the single crystal, and the WFs with opposite chiralities are located at  $k_0$  and  $-k_0$ . The other class is the non-centrosymmetric Weyl semimetals, which include a recently discovered material realization of TaAs [10–12]. In this Letter, we focus on the latter noncentrosymmetric Weyl semimetals.

The WF is characterized by the Berry curvature b(k) in momentum space. The Berry curvature b for the lowerenergy state for Eq. (1) is given by

$$\boldsymbol{b}(\boldsymbol{k}) = \eta \frac{\boldsymbol{k}}{2|\boldsymbol{k}|^3},\tag{2}$$

which corresponds to that of monopole (antimonopole) for  $\eta = 1$  ( $\eta = -1$ ). Namely, the integral of b(k) over the surface enclosing the Weyl point is a topological index which gives stability to the WFs. In this case, the only way to destroy them is the pair annihilation of two WFs with  $\eta = 1$  and  $\eta = -1$ . Now, the time-reversal symmetry *T* connects the electronic states at *k* and -k. As for the Berry curvature b(k), *T* imposes the relation b(-k) = -b(k). This relation indicates that WF at  $k_0$  is always accompanied by its partner WF at  $-k_0$  with the same chirality. This is

because the surface integral of b(k) around  $k_0$  is the same as that around  $-k_0$ , as seen in Fig. 1. There is also a theorem by Nielsen and Ninomiya [13,14] that the WFs with opposite chiralities are always paired. Therefore, it is concluded that there must be at least another pair of WFs at  $k_1$  and  $-k_1$  with the opposite chirality. This means that in the Weyl semimetals with broken *P* symmetry, there are at least four WFs, two of which have  $\eta = 1$  at  $\pm k_0$  and the other two have  $\eta = -1$  at  $\pm k_1$ . This situation is schematically shown in Fig. 1.

Electromagnetic responses of WFs have unique features that originate from the Landau levels (LLs) formed by the magnetic field **B**. In the presence of **B**, so called "zero modes" with the one-dimensional dispersion along the direction of **B** are formed by the zeroth LLs. They allow electrons to be pumped with the applied electric field **E** from one Weyl node to another Weyl node of opposite chirality. Specifically, application of both **E** and **B** in a parallel way increases the imbalance of electron numbers  $n_{\eta}$  between the WF with opposite chiralities [15]. This is expressed for  $\nu$  pairs of WF and anti-WFs by the equation [16,17]

$$\frac{dQ^5}{dt} = \frac{2\nu}{(2\pi)^2} \frac{e^2}{\hbar^2} \boldsymbol{E} \cdot \boldsymbol{B},\tag{3}$$



FIG. 1. Schematic picture of Weyl fermions in noncentrosymmetric system. Time-reversal symmetry connects the flow of the Berry curvature b(k) at k to that at -k as b(-k) = -b(k). This means that the Weyl fermions at k and -k have the same chirality; i.e., both are monopoles or antimonopoles. Therefore, there must be at least four Weyl fermions in noncentrosymmetric Weyl semimetals with time-reversal symmetry, i.e., two pairs of WFs and anti-WFs, respectively. When both the magnetic (B) and electric (E) fields are applied, the charge transfer between Weyl points occurs between monopoles and antimonopoles due to chiral anomaly. This phenomenon is shown by the shift of the chemical potentials (arrows) in the figure, which drives the system into a nonequilibrium state. Anisotropy between WFs and anti-WFs (which is allowed by the broken inversion symmetry) leads to nonreciprocal current response in this nonequilibrium state induced by the chiral anomaly.

where  $Q^5 = n_{\eta=1} - n_{\eta=-1}$ . In solids, there exists the relaxation due to impurity or phonon scattering with which a nonequilibrium steady state is realized with

$$Q^{5} = \frac{\nu e^{2} \tau_{\text{inter}}}{4\pi^{2} \hbar^{2}} \boldsymbol{E} \cdot \boldsymbol{B}, \qquad (4)$$

where  $\tau_{inter}$  is the relaxation time of electrons for the inter-Weyl-node scattering. This imbalance of electron numbers between WFs and anti-WFs leads to the chemical potential difference  $\mu^5$  between different chiralities. The chiral magnetic effect discussed in Refs. [18,19] is expressed by the equation for the current density J as  $J = -(e^2/h^2)\mu^5 B$ . This effect is derived from the axion electrodynamics action  $L_{ax} \propto \theta(r, t) \boldsymbol{E} \cdot \boldsymbol{B}$ , which is obtained from the Fujikawa Jacobian with  $\theta(r, t)$  being the angle corresponding to the chiral gauge transformation [20]. Using Eq. (4) with this equation for the chiral magnetic effect, one obtains  $J = -(e^4 v^3/8\pi^2 \hbar \epsilon^2) \tau_{\text{inter}} \times$  $(E \cdot B)B$ , where  $\epsilon$  is the chemical potential measured from the Weyl point. This describes the magnetotransport, i.e., the linear response to the electric field E that is modified by the external magnetic field. Such current response  $J \propto B^2 E$  is allowed in both T-broken and P-broken Weyl semimetals [18]. In a similar manner, we can consider another current response  $J \propto BE^2$  in the case of *P*-broken Weyl semimetals, as we discuss below.

One of the interesting effects in noncentrosymmetric systems is the nonreciprocal response, i.e., the propagation of light or the flow of current that depends on the direction, with the external magnetic field **B** or the spontaneous magnetization **M** that breaks T symmetry [21–25]. The time-reversal symmetry in the microscopic dynamics leads to the Onsager reciprocal relation, which imposes a condition on the conductivity tensor  $\sigma_{ij}$  as

$$\sigma_{ij}(\boldsymbol{k},\boldsymbol{B}) = \sigma_{ji}(-\boldsymbol{k},-\boldsymbol{B}), \qquad (5)$$

with the wave vector k, and governs the form of the nonreciprocal responses. A well-known example of nonreciprocal responses is the optical magnetochiral dichroism that is realized when the magnetic field  $\boldsymbol{B}$  (or magnetization M) and the electric polarization P form the toroidal moment  $T = P \times B$  (or  $T = P \times M$ ) [21]. In this case, the dielectric constant  $\varepsilon$  depends on the relative direction of the pointing vector S of the light  $(\propto k)$  and the toroidal moment T. Phenomenologically, this can be expressed as  $\varepsilon = \varepsilon_0 +$  $\alpha T \cdot k$ , where k is the wave vector of light. In fact, this nonreciprocal linear response is consistent with the Onsager relation in Eq. (5). Meanwhile, nonreciprocal responses in the transport phenomena have been studied by Rikken et al. [22]. They discussed that the wave vector k can be replaced by the velocity or current of the electrons I in Eq. (5) and, hence, the  $I \cdot B$  term is allowed in the conductivity tensor, which leads to the transport

magnetochiral anisotropy [22–24]. Specifically, the transport magnetochiral anisotropy is the current response  $J \propto BE^2$  and is described by the resistivity  $\rho$  that depends on the current **I** and the external magnetic field **B** as

$$\rho = \rho_0 (1 + \gamma \boldsymbol{I} \cdot \boldsymbol{B}). \tag{6}$$

This effect has been studied for Bi helix [22], molecular solid [23], and carbon nanotubes [24] with chiral structure, where two major microscopic mechanisms have been proposed. One is the magnetic self-field. In the presence of the magnetic self-field, the magnetoresistance is expressed by  $\Delta \rho = \beta B_{\text{eff}}^2$ , where  $B_{\text{eff}}^2$  is the effective magnetic field given by the sum of the external one  $B_{\text{ext}}$ and B' induced by the current I. Because of the helical structure of the materials, the induced B' is parallel to I and produces positive magnetoresistance resulting in Eq. (6). The other mechanism is the scattering of electrons by chiral objects such as crystal defects and phonons. It has also been found that the spin-orbit interaction in Si leads to a different type of magnetochiral anisotropy of the form  $\rho = \rho_0 [1 + \chi \mathbf{E} \cdot (\mathbf{I} \times \mathbf{B})],$  where the external electric field *E* plays the role of the inversion symmetry breaking [25]. The strength of the magnetochiral anisotropy is usually discussed in terms of the coefficient  $\gamma$ . However,  $\gamma$ depends on the cross section A of the sample, and a more intrinsic quantity is  $\gamma' = \gamma A$ . The coefficients  $\gamma$  and  $\gamma'$  have been measured experimentally as  $\gamma \simeq 10^{-3} \text{ T}^{-1} \text{ A}^{-1}$  and  $\gamma' \simeq 10^{-10} \text{ m}^2 \text{ T}^{-1} \text{ A}^{-1}$  in Bi helix [22],  $\gamma \simeq 10^{-3} \text{ T}^{-1} \text{ A}^{-1}$  and  $\gamma' \simeq 10^{-11} \text{ m}^2 \text{ T}^{-1} \text{ A}^{-1}$  in molecular solid [23],  $\gamma \simeq 10^{-1} \text{ T}^{-1} \text{ A}^{-1}$  and  $\gamma' \simeq 10^{-10} \text{ m}^2 \text{ T}^{-1} \text{ A}^{-1}$  in Si [25,26], and  $\gamma \simeq 10^2 \text{ T}^{-1} \text{ A}^{-1}$  and  $\gamma' \simeq 10^{-16} \text{ m}^2 \text{ T}^{-1} \text{ A}^{-1}$ in carbon nanotube [24]. From the viewpoint of the applications of magnetochiral anisotropy as a rectifying function, the larger values of  $\gamma$  and  $\gamma'$  are desirable because it enables more efficient rectifier devices which are controllable with magnetic fields.

Since the Weyl semimetal has been realized in noncentrosymmetric materials such as TaAs, it is an interesting issue to study Weyl semimetals as a platform for the magnetochiral anisotropy. In particular, it is interesting to explore its relationship to the chiral anomaly, which is an origin of various anomalous transport properties. Motivated by this, we now proceed to the prediction of the magnetochiral anisotropy in noncentrosymmetric Weyl semimetals. It turns out that the inversion symmetry breaking and the chiral anomaly play a crucial role in the magnetochiral anisotropy of the Weyl semimetals as follows. In the noncentrosymmetric Weyl semimetals, the WFs with different chiralities are not equivalent and usually form the small electron or hole pockets. In the presence of  $B \cdot E$ , the chiral anomaly triggers changes of the sizes of these inequivalent pockets and, hence, the value of metallic conductivity. This results in nonlinear resistivity proportional to B in noncentrosymmetric Weyl semimetals.

To substantiate the above idea, we consider WFs at  $\pm k_{+}$ and anti-WFs at  $\pm k_{-}$  for which the Fermi velocity is  $v_{\pm}$  and the Fermi energy measured from the Weyl point is  $\epsilon_{\pm}$ , respectively, as schematically illustrated in Fig. 1. The parameters  $v_{\pm}$  and  $\epsilon_{\pm}$  can differ for the WFs and anti-WFs due to the broken inversion symmetry. Contributions to the linear conductivity from the WFs or anti-WFs are written as

$$\sigma_{\pm} = \frac{1}{3} e^2 v_{\pm}^2 \tau_{\text{intra}} D_{\pm}(\epsilon_{\pm}). \tag{7}$$

Here,  $\tau_{\text{intra}}$  is the relaxation time for intra-Weyl-node scattering, which is usually shorter than  $\tau_{\text{inter}}$  [17], and the density of states  $D_{\pm}(\epsilon)$  is given by

$$D_{\pm}(\epsilon) = \frac{\nu \epsilon^2}{2\pi^2 \hbar^3 v_{\pm}^3},\tag{8}$$

where  $\nu$  denotes the number of pairs of WFs or anti-WFs. For example,  $\nu = 12$  for TaAs. This reduces to

$$\sigma_{\pm} = \frac{\nu e^2}{6\pi^2 \hbar^3} \frac{\tau_{\text{intra}} \epsilon_{\pm}^2}{v_{\pm}}.$$
(9)

When the electric field E and the magnetic field B are applied to the sample in a parallel way, electrons are transferred from the WFs to the anti-WFs (or vice versa) due to the chiral anomaly, as shown in Fig. 1. This results in changes of Fermi energies for the WF and the anti-WFs given by  $\Delta \epsilon_{\pm} = \pm Q^5/D_{\pm}(\epsilon_{\pm})$ . As a result, the linear conductivity is also modified as

$$\Delta \sigma_{\pm} = \frac{1}{3} e^2 v_{\pm}^2 \tau_{\text{intra}} \frac{dD_{\pm}(\epsilon)}{d\epsilon} \Delta \epsilon_{\pm}, \qquad (10)$$

which can be explicitly written as

$$\Delta \sigma_{\pm} = \pm \nu \frac{e^4}{6\pi^2 \hbar^2} \frac{v_{\pm}^2 \tau_{\text{intra}} \tau_{\text{inter}}}{\epsilon_{\pm}} \boldsymbol{E} \cdot \boldsymbol{B}.$$
 (11)

These changes of the linear conductivity can become nonvanishing after summing over the WFs and the anti-WFs due to the anisotropy in  $v_{\pm}$  and  $\epsilon_{\pm}$ . In this case, the nonlinear current response  $J \propto (E \cdot B)E$  is realized and supports the nonreciprocal current response: in the presence of the magnetic field B, different magnitude of dc current flows in the case where E and B are parallel compared to the case where E and B are antiparallel. Thus, the noncentrosymmetric Weyl semimetals support the current rectification effect originating from the chiral anomaly.

Now we quantify the nonreciprocal current response in Weyl semimetals by defining the intrinsic nonlinear resistivity coefficient  $\gamma'$  as  $\gamma' = \gamma A$  with the cross section of the sample A. This coefficient  $\gamma'$  does not depend on the cross section of the sample and can be obtained from the conductivity change in the above as

$$\gamma' = -\frac{2\Delta\sigma/(\boldsymbol{E}\cdot\boldsymbol{B})}{\sigma^2}$$
$$= -\frac{12\pi^2\hbar^4\tau_{\text{inter}}}{\nu\tau_{\text{intra}}} \left(\frac{v_+^2}{\epsilon_+} - \frac{v_-^2}{\epsilon_-}\right) \left(\frac{\epsilon_+^2}{v_+} + \frac{\epsilon_-^2}{v_-}\right)^{-2}.$$
 (12)

We see that the expression for  $\gamma'$  is simplified in the following two cases. (i) In the case of  $v_{\pm} = v_0$ , the nonlinear resistivity coefficient  $\gamma'$  further reduces to

$$\gamma' = -\frac{12\pi^2 \hbar^4 v_0^4 \tau_{\text{inter}}}{\nu \tau_{\text{intra}}} \frac{-\epsilon_+ + \epsilon_-}{\epsilon_+ \epsilon_- (\epsilon_+^2 + \epsilon_-^2)^2}, \qquad (13)$$

which is proportional to the energy difference of Weyl points  $(\epsilon_+ - \epsilon_-)$ . (ii) In the case of  $\epsilon_+ = \epsilon_- = \epsilon$ , this reduces to

$$\gamma' = -\frac{12\pi^2 \hbar^4 \tau_{\text{inter}}}{\nu \tau_{\text{intra}}} \frac{(v_+ v_-)^2 (v_+ - v_-)}{(v_+ + v_-)\epsilon^5}, \qquad (14)$$

which is proportional to the Fermi velocity difference  $(v_+ - v_-)$ . Therefore, any asymmetry of band structures between WFs and anti-WFs can support the rectification effect proportional to *B* originating from the chiral anomaly. In both cases, the magnetochiral anisotropy is enhanced when the Weyl points are close to the Fermi energy and the Fermi velocity is large. In particular, we notice by comparing Eq. (14) and Eq. (9) that the enhancement of magnetochiral anisotropy  $\gamma' \propto e^{-5}$  with  $e \to 0$  is larger than that of magnetoresistance  $1/\sigma \propto e^{-2}$ .

Discussions.—We give a crude estimate for the nonlinear ratio  $\gamma$ . In time-reversal symmetric Weyl semimetals such as TaAs [10,11], typical parameters are given by  $v = 4 \times 10^5$  m/s and  $|\epsilon_{\pm}| \sim 10$  meV, and we assume  $\tau_{\text{intra}} \simeq \tau_{\text{inter}}$  for simplicity. In this case, the estimate is given by  $\gamma' \simeq 3 \times 10^{-8} \times \text{m}^2 \text{ T}^{-1} \text{ A}^{-1}$ . This coefficient  $\gamma'$ for Weyl semimetals is larger than that for any of the materials reported in Refs. [21-24]. If we consider the sample of a cross section  $A = 0.1 \text{ mm}^2$ , we obtain the nonlinear coefficient  $\gamma = 0.3 \text{ T}^{-1} \text{ A}^{-1}$ . From the practical point of view, the dimensionless factor  $\eta = \gamma \mathbf{I} \cdot \mathbf{B} =$  $\gamma' J \cdot B$  determines the ratio between the currents of right and left directions. This rectification efficiency  $\eta$  can be of the order of unity in our case for  $J = 10^3 \text{ A/mm}^2$  and B = 0.1 T, while it is typically of the order of  $10^{-4}$ – $10^{-3}$  in the systems in Refs. [21-24]. In this regard, Weyl semimetals which are metals and have large  $\gamma'$  offer an efficient nonreciprocal property in the magnetic field.

Comments are in order for the validity of our semiclassical approach. We used the semiclassical formula Eq. (9) for the conductivity change at each Weyl node in deriving the magnetochiral anisotropy in Weyl semimetals. This description is valid when the Landau level separation  $\Delta \epsilon_{LL}$  is smaller than the level broadening  $h/\tau_{intra}$ . When the Landau level separation becomes larger than the level broadening with a strong magnetic field **B**, the energy bands decouple into separate 1D channels of LLs along the direction of **B**. In this case, the system does not exhibit the magnetochiral anisotropy by applying Ebecause pumping of electrons between left movers and right movers at Weyl or anti-Weyl nodes does not induce change of the conductivity (the conductance is always  $2e^2/h$  for each 1D channel). Thus, the nonvanishing magnetochiral anisotropy requires that the system is in the semiclassical regime  $\Delta \epsilon_{LL} < \hbar / \tau_{intra}$ , which constrains the strength of magnetic field **B**. Since the Landau level separation is given by  $\Delta \epsilon_{LL} \cong 10 \text{ meV}(B/1 \text{ T})$  for the parameters in the above and  $h/\tau_{intra} = 4 \text{ meV}$  for the relaxation time  $\tau_{intra} = 1$  ps, the magnetic field of B < 0.4 T justifies the semiclassical approach and supports the large magnetochiral anisotropy in Weyl semimetals. In addition, Weyl fermions realized in materials such as TaAs are not isotropic in the momentum space and show directional anisotropy (i.e., the Fermi velocity  $v_i$  differs for directions i = x, y, z [27]. This modifies the formula for magnetochiral anisotropy, but the qualitative behavior such as the scaling law with  $\epsilon$  remains unchanged [28]. Finally, we note that the effect of electron-electron interaction and disorder is captured by the relaxation times  $\tau_{intra}$  and  $\tau_{inter}$  in the semiclassics. This indicates that the types of interaction or disorder affect the ratio  $\tau_{\text{inter}}/\tau_{\text{intra}}$  that enters in the formula for  $\gamma'$ . Namely, when the long-range (short-range) interaction or long-range (short-range) scatters are dominant,  $\tau_{inter}/\tau_{intra}$  becomes large (small) and enhances (suppresses) the magnetochiral anisotropy. Moreover, the magnetochiral anisotropy ( $\gamma$  and  $\gamma'$ ) becomes even larger than the estimate above due to the factor of  $\tau_{inter}/\tau_{intra}$ because the internode relaxation time  $\tau_{inter}$  is usually larger than intranode relaxation time  $\tau_{intra}$ .

In general, there exist other rectification effects in the presence of the inversion symmetry breaking and timereversal breaking. What is special for the rectification effect proposed here for Weyl semimetals is that it originates from the chiral anomaly of WFs and the direction of the rectification can be controlled by **B**. Namely, although the expression is the same as Eq. (6), the crystal structure determines the direction of the current in the cases of helix [22,24] or molecular solid [23]. In contrast, in the present case, the rectification effect is essentially free from the crystal anisotropy, i.e., determined solely by the relative angle between I and B. Actually, this is the signature of the negative magnetoresistance due to the chiral anomaly [11,29,30]. Since the present magnetochiral anisotropy is the twin effect of this negative magnetoresistance, it is quite natural that the magnetochiral anisotropy shows similar angle dependence. In addition, it is interesting to note that Fermi pockets of the Weyl and anti-Weyl nodes are found to be connected in TaP [31]. Even in this case, we can expect magnetochiral anisotropy since charge transfer is induced between different parts of the Fermi surface by applying both E and B fields as a remnant of the chiral anomaly, which results in the negative magnetoresistance observed in Ref. [31]. Since TaP breaks inversion symmetry, this charge transfer can also lead to a change of the linear conductivity and hence the magnetochiral anisotropy. However, the isotropic form of the coefficient with the  $I \cdot B$  term is modified to some anisotropic form reflecting details of materials in this case.

To summarize, we have theoretically proposed the magnetochiral anisotropy of topological origin, i.e., chiral anomaly of Weyl fermion, in noncentrosymmetric Weyl semimetals. This effect is missing in the centrosymmetric Weyl semimetals with magnetism, since it is prohibited by the inversion symmetry. The magnitude of this effect can be very large,  $\delta \rho / \rho_0 \sim 1$ , and the peculiar angle dependence will be the signature of this effect as in the case of negative magnetoresistance. This effect may be utilized in rectifier devices controlled by the external magnetic field.

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$$\gamma' = -\frac{12\pi^2\hbar^4 \tau_{\text{inter}}}{\nu \tau_{\text{intra}}} \left(\frac{v_{+,z}^2}{\epsilon_+} - \frac{v_{-,z}^2}{\epsilon_-}\right) \left(\frac{\epsilon_+^2 v_{+,z}}{v_{+,x} v_{+,y}} + \frac{\epsilon_-^2 v_{-,z}}{v_{-,x} v_{-,y}}\right)^{-2}.$$

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