



## Possible “Magnéli” Phases and Self-Alloying in the Superconducting Sulfur Hydride

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We theoretically give an infinite number of metastable crystal structures for the superconducting sulfur hydride  $H_xS$  under pressure. Previously predicted crystalline phases of  $H_2S$  and  $H_3S$  have been thought to have important roles for experimentally observed low and high  $T_c$ , respectively. The newly found structures are long-period modulated crystals where slablike  $H_2S$  and  $H_3S$  regions intergrow on a microscopic scale. The extremely small formation enthalpy for the  $H_2S$ - $H_3S$  boundary indicated by first-principles calculations suggests possible alloying of these phases through the formation of local  $H_3S$  regions. The modulated structures and gradual alloying transformations between them not only explain the peculiar pressure dependence of  $T_c$  in sulfur hydride observed experimentally, but also could prevail in the experimental samples under various compression schemes.

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Sulfur hydride has recently been found to become a superconductor at an extremely high pressure around 200 K [1,2]. This is the first achievement of a superconducting transition temperature ( $T_c$ ) exceeding the nitrogen boiling point among the conventional phonon-mediated superconductors [3], and it has broken the long-standing record of 160 K in a mercury cuprate [4–7].

A remarkable feature observed in this superconducting phenomenon is the pressure and annealing-scheme dependences of  $T_c$  [1,2,8]. (i) When the pressure ( $> \sim 100$  GPa) is applied to the  $H_2S$  sample at room temperature and afterwards cooled down, the observed  $T_c$ 's amount to over 150 K, with 203 K being the maximum value (open circle in Fig. 1). (ii) By pressurizing at a temperature around 200 K, on the other hand, the observed  $T_c$  remains low and next rapidly increases (open square in Fig. 1). Although this behavior suggests a variety of structural phases and their peculiar properties, efficient experimental observations have been obstructed by the extremely high pressure. Instead, first-principles calculations have provided insights for the superconducting phases. It is now established that some of the observed values of  $T_c$  with the low- and high- $T$  schemes are well reproduced [9–17] with crystal structures predicted for compositions of  $H_2S$  [9], as well as  $H_5S_2$  [16] and  $H_3S$  [10] (see Fig. 1). However, a consistent understanding of the observed behavior still remains unprecedented. In particular, no clear explanation of the rapid increase of  $T_c$  with the low- $T$  scheme has been given, despite the accumulated first-principles proposals of candidate structures with various compositions of  $H_xS$  [11,14,18,19].

The current theoretical attempts have focused on the possible understanding with a minimal number of distinct

structural phases. Rather, we provide a different view: Not only distinct phases but also their mixture have vital roles. Specifically, we find an infinite number of metastable

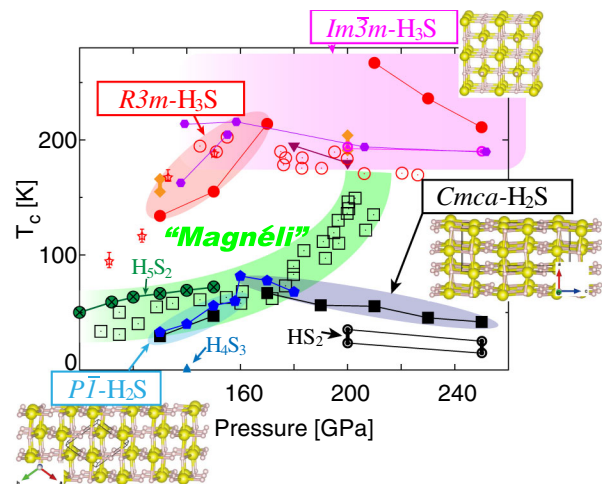


FIG. 1. Experimentally observed  $T_c$  (open circle, square [1], and star with an error bar [8]) compared with the first-principles calculations (solid symbols). The latter data are taken from Refs. [9] (pentagon), [10] (rhombus), [12] (inverted triangle), [13] (circle and square), [14] (double circle), [18] (triangle), [15] (hexagon), and [16] (circle with  $x$  mark). The data points in the shaded areas have been obtained from the corresponding predicted crystal structures [9,10]. Note that  $R3m$ - $H_3S$  is a trigonally distorted variant of  $Im\bar{3}m$ - $H_3S$ . As discussed later, we attribute the pressure dependence of  $T_c$  (open square) to the “Magnéli” phases. The values from Ref. [13] (Refs. [14,15]) includes the plasmon effect (phonon anharmonic effect). The vertical bars connecting the rhombi indicate the  $T_c$  variation with the empirical Coulomb parameter  $\mu^*$  [10,14].

crystal structures having compositions  $H_xS_{1-x}$  with  $2/3 < x < 3/4$ , which have not been reported in the first-principles structure-search studies. They can be understood as long-period modulated crystals formed by stacking the  $H_2S$  and  $H_3S$  slablike structures, which are reminiscent of the Magnéli phases in transition-metal oxides [20]. All these structures are thermodynamically as stable as the complete separation to  $H_2S$  and  $H_3S$  phases. This suggests that the microscopic *intergrowth* of the  $H_2S$  and  $H_3S$  regions requires little activation enthalpy and therefore occurs ubiquitously in the experimental situation, forming, as it were, slab-alloy phases. We also show that the experimentally observed  $T_c$ -pressure curve is reproduced from these alloylike phases.

We begin with a discussion of the hidden similarity between theoretically predicted relevant structures for  $H_2S$  and  $H_3S$ .  $P\bar{1}$ - $H_2S$  and  $Cmca$ - $H_2S$  (Fig. 1) are known to give low  $T_c$  values [9,13,17], which agree relatively well with the experimental values with the low- $T$  annealing for the low-pressure regime.  $Im\bar{3}m$ - $H_3S$  (Fig. 1) has been thought to give the  $T_c$  with the high- $T$  annealing cases [11,14,15,17,21–31], and its presence was recently confirmed with x-ray diffraction measurements [8,18,32,33]. Seen from the  $(1\ 1\ 0)$  direction [ $(1\ 0\ 0)$  direction] in the setup of Ref. [9], one can notice that  $P\bar{1}$ - and  $Cmca$ - $H_2S$  can be decomposed into common unit structures [Figs. 2(a) and 2(b)]: two  $H_2S$  square nets interlaced with each other [Fig. 2(c)]. The units of this shape are bound with each other so that sulfur atoms adopt local fcc-like stacking [Fig. 2(d)] [34]. The  $P\bar{1}$  and  $Cmca$  structures can now be distinguished by the configuration of the interunit bonding. The uniform (alternating) bonding orientation yields the  $P\bar{1}$  ( $Cmca$ ) structure. An important thing is that the  $Im\bar{3}m$ - $H_3S$  structure can also be formed with the present unit by binding them so that the vertical edges are shared [Fig. 3(c)].

The unit-based perspective for  $H_2S$  and  $H_3S$  is indeed helpful for us to construct a group of metastable structures. In a wide variety of materials such as metal oxides, multiple crystalline phases with slightly different stoichiometries emerge depending on the bonding between the unit complexes [35,36]. One such example is the Magnéli phases in molybdenum [20,37,38], tungsten [20,39], titanium [40–43], and vanadium oxides [44–47], where two-dimensional defects (or *crystallographic shear* [48]) of edge- or face-sharing bonding between metal-oxide complexes are periodically formed. In analogy with them, here we consider the possible crystalline phases formed by the structural  $H_2S$  unit.

We first define the three types of interunit bonding [Figs. 3(a)–3(c)]: Bonding  $\alpha$  and  $\bar{\alpha}$  correspond to the two bonding orientations seen in  $Cmca$ - $H_2S$ , respectively, whereas bonding  $\beta$  corresponds to the bond sharing the edge. With this definition, by arranging the units side by side and next assigning any type of bonding for every neighboring pair of units, we can generate a crystal

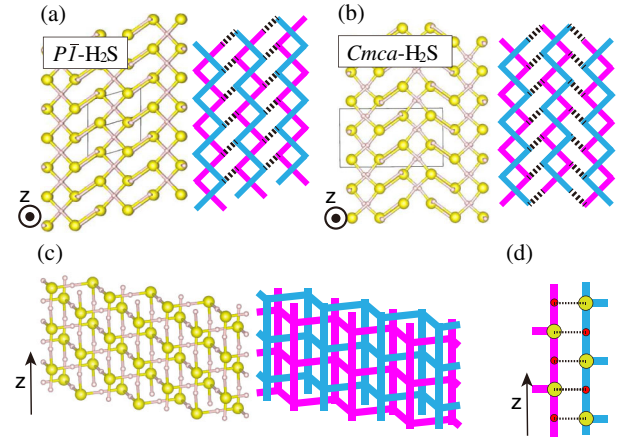


FIG. 2. (a)  $(1\ 1\ 0)$  view of  $P\bar{1}$ - $H_2S$  and (b)  $(1\ 0\ 0)$  view of  $Cmca$ - $H_2S$ , accompanied by their schematic pictures. The unit cells are depicted as thin lines. In the schematic pictures, the bond depicted by (d) is indicated by thick dashed lines. (c) The fundamental unit structure, “interlaced square nets” and its schematic picture. In the latter, sulfur and hydrogen atoms are located at the corners and the centers of the edges, respectively. (d) Bonding structure in (a) and (b), where sulfur and hydrogen atoms are depicted in yellow and red, respectively.

structure formed by the units. In this sense, every circular permutation composed of the desired numbers of  $\alpha$ ,  $\bar{\alpha}$ , and  $\beta$  yields a corresponding long-period modulated crystal structure. Any structures generated in this way have the intermediate composition  $H_xS_{1-x}$  ( $2/3 \leq x < 3/4$ ), whose unit cells are composed of  $H_{4N-k}S_{2N-k}$  with  $N$  and  $k$  being the period of the permutation and the number of  $\beta$ , respectively. The “ $\alpha\beta\bar{\alpha}\beta$ ” structure is exemplified in Fig. 3(d), whose unit-cell formula is  $H_{14}S_6$ . As the number of  $\beta$  increases,  $H_3S$ -like structural regions grow [Figs. 3(d) and 3(e)]. Note that  $P\bar{1}$ - $H_2S$ ,  $Cmca$ - $H_2S$ , and  $Im\bar{3}m$ - $H_3S$  are generated by permutations “ $\alpha$ ” (also “ $\bar{\alpha}$ ”; see Supplemental Material [49]), “ $\alpha\bar{\alpha}$ ,” and “ $\beta$ ,” respectively.

Using the structures thus generated from the permutations of periods 2, 3, and 4 as inputs, we carried out the first-principles structure optimization for various pressures. Our calculations were done using the first-principles code package QUANTUM ESPRESSO [52] with the generalized-gradient approximation for the exchange-correlation potential [53]. The unit-cell compositions of the resulting structures are  $H_7S_3$ ,  $H_{10}S_4$ ,  $H_{11}S_5$ ,  $H_{12}S_6$ ,  $H_{13}S_5$ ,  $H_{14}S_6$ ,  $H_{15}S_7$ , and  $H_{16}S_8$ , respectively. Detailed conditions of the calculations are summarized in Supplemental Material [49]. We have found that the formation enthalpy  $\Delta H(H_xS_{1-x})$  for all the resulting structures satisfies  $\Delta H(H_2S) \gtrsim \Delta H(H_xS_{1-x}) \gtrsim \Delta H(H_3S)$  (Fig. 4). We have also confirmed that all these structures retain the bonding characteristics in their initial structures [Fig. 3(e)]. Namely, every different permutation gives different optimum metastable structures where well-defined bcc- $H_3S$  slab regions emerge. Although we do not examine the  $N \geq 5$  cases here,

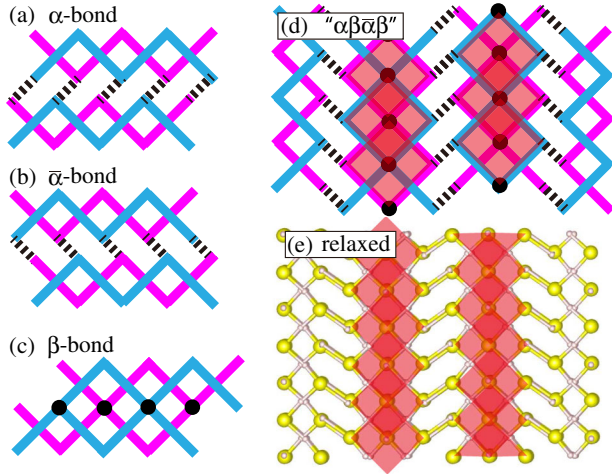


FIG. 3. (a)–(c) Definitions of interunit bonding. (d) Long-period modulated structure generated from permutation " $\alpha\bar{\beta}\bar{\alpha}\beta$ " and (e) its relaxed counterpart (see the main text). The  $Im\bar{3}m$ -H<sub>3</sub>S regions are shaded in red.

an infinite number of metastable structures are expected to be obtained in this way.

Remarkably, the values of the formation enthalpy relative to the complete decomposition into H<sub>2</sub>S and H<sub>3</sub>S are wholly within 50 K per atom [insets in Figs. 4(a)–4(d)]. This dependence is not an indication of a trivial phase separation into H<sub>2</sub>S and H<sub>3</sub>S, because the two regions intergrow in a microscopic scale in the respective structures [see Fig. 3(e)]. A more appropriate interpretation is that the formation enthalpy for the H<sub>2</sub>S-H<sub>3</sub>S boundary is extremely small in these structures.

Let us argue the relevance of the newly found intermediate phases in the experimental situation. We here have to bear in mind that the intermediate structures are *within* the convex hull of the formation enthalpy in the present pressure regime, apart from the narrow range around 110 GPa (Fig. 4 and Ref. [18]). This means that, in the compressed H<sub>2</sub>S system, these phases do not grow as the decomposition residues of the emergence of the H<sub>3</sub>S phase, if annealed with enough time and heat. However, the decomposition paths otherwise depend on the enthalpy barrier from the pristine H<sub>2</sub>S structures. The transition between two metastable structures with slightly different  $x$  occurs through transformations of a small fraction of  $\alpha(\bar{\alpha})$ -type interunit bonds to  $\beta$ . This sporadic character of the bonding transformation and the small formation enthalpy for the H<sub>2</sub>S-H<sub>3</sub>S boundary revealed above suggest that such a transition requires little activation enthalpy. The intermediate crystalline phases should thus be observable if H<sub>x</sub>S systems exhibit either the  $P\bar{1}$ - or  $Cmca$ -H<sub>2</sub>S region and next further compressed at a low temperature.

The possible emergence of the intermediate Magnéli-type phases draws a consistent explanation of the puzzling pressure dependence of  $T_c$  observed experimentally. In the present Magnéli phases,  $T_c$  is expected to increase as

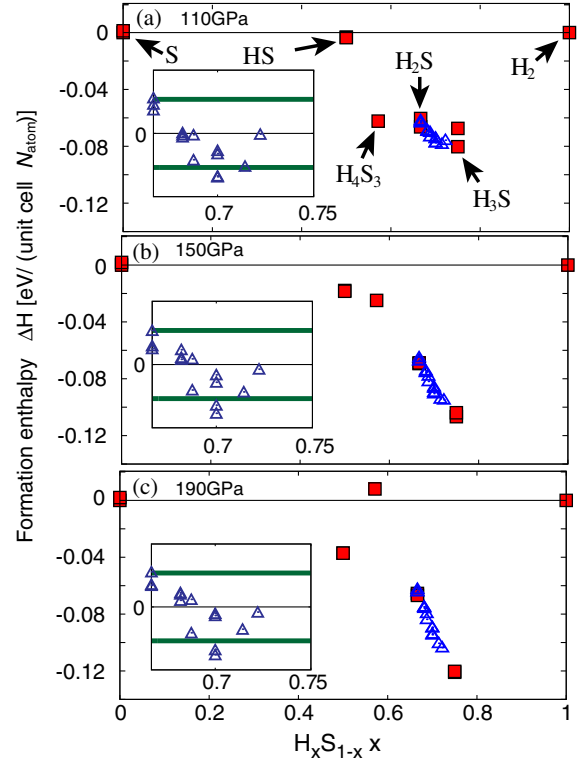


FIG. 4. (a)–(c) Formation enthalpy from first principles at various pressures, where  $N_{\text{atom}}$  denotes the number of atoms in the unit cell. The structures corresponding to the points are summarized in Supplemental Material [49]. The inset panels focus the region between  $x = 2/3$  (H<sub>2</sub>S) and  $x = 3/4$  (H<sub>3</sub>S), where the formation enthalpies are measured with respect to the values for the phase separation of H<sub>2</sub>S and H<sub>3</sub>S. Bold lines indicate  $\pm 50$  K.

the H<sub>3</sub>S regions grow. Indeed, by selecting plausible phases and calculating their superconducting  $T_c$ 's from first principles [13,49,52,56–58,60–62,66,72], we successfully reproduced the experimentally observed  $T_c$  behavior (Fig. 1): 41 K (130 GPa), 80 K (180 GPa), 107 K (190 GPa), and 121 K (200 GPa). Here, the increase of  $T_c$  is due to the enhancement of electron-phonon coupling (see Supplemental Material [49]). The succession of the Magnéli phases with an increasing fraction of the H<sub>3</sub>S region is hence the probable origin of the pressure dependence of  $T_c$  observed with the low- $T$  compression scheme, filling the unsolved gap between the theory and experiments. Although we have selected the  $\alpha\bar{\beta}$ ,  $\alpha\bar{\beta}\bar{\beta}$ ,  $\alpha\bar{\beta}\bar{\beta}\bar{\beta}$ , and  $\alpha(\bar{\beta} \times 9)$  phases for 130, 180, 190, and 200 GPa, respectively, we do not conclude that these specific phases were emerging in the experimental situation in Ref. [1] but were more various Magnéli phases. For example, there has been a recent first-principles calculation that H<sub>5</sub>S<sub>2</sub>, which is actually equivalent to the  $\alpha\bar{\beta}\bar{\beta}$  phase, also yields a good agreement for  $P < 150$  GPa (circle with  $x$  mark in Fig. 1; Ref. [16]).

We can also find a plausible reaction path consistent with the experiment. The calculated formation enthalpies

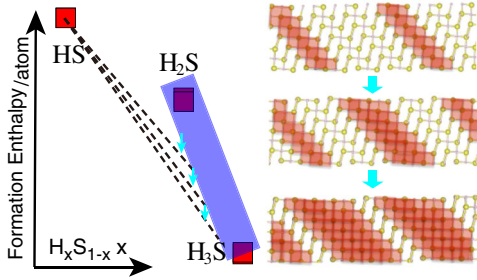


FIG. 5. Schematic picture of a possible transformation path “ $\alpha(\bar{\alpha}) \rightarrow \beta + \text{HS}$ .” The shaded area in the left plot represents the multiple intermediate structures, whereas that in the right indicates the  $\text{H}_3\text{S}$  regions.

for HS and the Magnéli phases decrease with compression compared with those for  $\text{H}_2\text{S}$  [see Figs. 4(a)–4(c)]. This pressure-induced phenomenon would stimulate local reactions forming the  $\text{H}_3\text{S}$  slabs:  $\alpha(\bar{\alpha}) \rightarrow \beta + \text{HS}$  (Fig. 5; see also Supplemental Material [73]). This supports the present scenario: the increase of the  $\text{H}_3\text{S}$  region by compression.

The multiplicity of the metastable phases deduces an interesting speculation: Arbitrary values of  $T_c$  between those of the low- and high- $T_c$  phases in Ref. [1] are observable. The local  $\text{H}_3\text{S}$ -slab formation can also be stimulated by annealing. By carefully controlling the annealing conditions, one would observe various values and their temporal evolution even at fixed pressures.

Here we note a possible characteristic effect in the present  $\text{H}_x\text{S}$  Magnéli phases for future studies. In the titanium-oxide Magnéli phase, it is known that the local electron-lattice coupling is enhanced by two-dimensional defects to form bipolarons (or charge order) [71]. Hydrogen atoms are, in principle, subject to this instability because of their multivalent character. Although we have not found traces of such polaronic phases (see Supplemental Material [49]), in view of the strong electron-phonon coupling, proximity effects of such phases may affect the transport and superconducting properties [74–77].

To facilitate the experimental exploration of the  $\text{H}_x\text{S}$  Magnéli phases, we computed theoretical x-ray diffraction patterns at 150 GPa using the RIETAN package (Ref. [55]; see Supplemental Material [49]). We focus on two distinct groups of structures. When the fraction of the  $\beta$  bond is small and both  $\alpha$  and  $\bar{\alpha}$  bonds are present, multiple minor peaks are generally seen around the diffraction angle of the dominant peak in  $R3m\text{-H}_3\text{S}$  [(110) peak;  $2\theta \approx 11^\circ$  in Fig. 6(a)], as exemplified in Fig. 6(b). This behavior is due to a subtle distortion of the sulfur lattice and apparently difficult to understand with a simple combination of the patterns for the pristine  $R3m\text{-H}_3\text{S}$ ,  $P\bar{1}\text{-H}_2\text{S}$ , and  $\text{Cmca}\text{-H}_2\text{S}$  phases. Experimental “noise” may actually be contributed to by the diffraction peaks from those phases. We also show the simulated patterns when the  $\beta$  bonds are gradually introduced in either the  $P\bar{1}\text{-}$  or  $\text{Cmca}\text{-H}_2\text{S}$  phase in Fig. 6(c). We observe gradual evolutions between the end

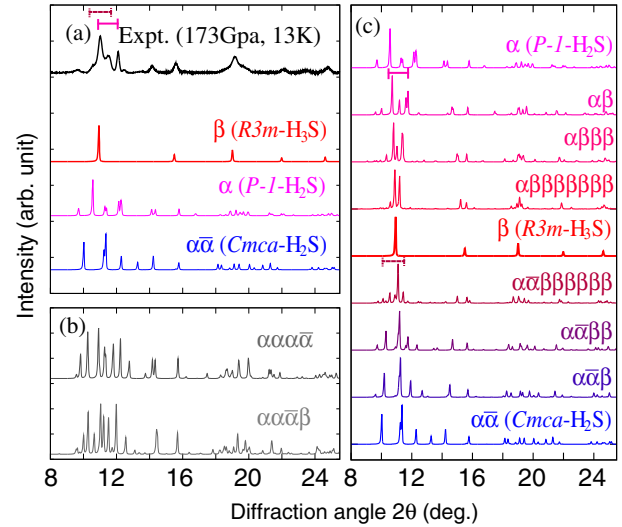


FIG. 6. X-ray diffraction patterns. The simulations were done for the structures optimized at 150 GPa. (a) (Top) Experimentally observed diffraction pattern for  $\text{D}_2\text{S}$  taken from Ref. [8], where the horizontal bars indicate regions where we can find a similarity to the simulated patterns for some Magnéli phases [see (c)]. (Bottom) The simulated patterns for the reference structures. (b) Representative simulated patterns exhibiting multiple diffraction peaks. (c) Patterns obtained from a selected group of structures which are ordered so that the fraction of  $\beta$  bond gradually varies.

points. Remarkably, the intensity of the dominant peak is well retained, while peripheral features such as subpeaks and a peak shift and tail are found. In the previous diffraction experiments [8,18,32], the presence of the  $\text{H}_3\text{S}$  phase has been indicated from the (110) peak, though it was accompanied by subtle subpeaks depending on the experimental protocol. The Magnéli phases of this group may provide a unified understanding of such structures. To demonstrate this, we plotted an experimental pattern quoted from Ref. [8] in Fig. 6(a). The subpeaks and tails around  $10^\circ \lesssim 2\theta \lesssim 12^\circ$  well resembles, for example, those for  $\alpha\beta$  and  $\alpha\bar{\alpha}\beta\beta\beta\beta\beta\beta$ , as indicated in Figs. 6(a) and 6(c).

We additionally assert that not only crystalline Magnéli phases but also their nanoscale stripes can emerge in an ordered and random fashion, similarly to the cases of microsyntactic intergrowth [45] observed in silicon carbide [78] and metallic oxides including the Magnéli materials [45,79–82]. Such structures will appear in reality as an alloylike phase formed by the slabs of the metallic  $\text{H}_2\text{S}$  and  $\text{H}_3\text{S}$ . This alloy phase is a compound analog of the classic superconducting alloys formed by elemental metals [83] but quite different from them. The ingredients of the former alloy— $\text{H}_2\text{S}$  and  $\text{H}_3\text{S}$  slabs—can develop in the common  $\text{H}_2\text{S}$  crystalline phases, and therefore, even in the pristine sample, their alloying occurs in a self-contained manner through structural and stoichiometric transformations. This alloying obviously smears the experimental diffraction pattern, which could appear to be amorphouslike behavior.

In summary, we have provided an interpretation based on the common structural unit for the known crystal structures of low- and high- $T_c$   $H_2S$  and  $H_3S$  and thereby found metastable Magnéli-type structures formed by their layered microsyntactic intergrowth. The experimentally observed pressure dependence of  $T_c$  is reasonably explained with pressure-induced gradual transformations through such alloy phases. The present finding gives new insight into the high- $T_c$  superconducting phenomena in sulfur hydride that the microscopic mixture of the phases can be ubiquitous.

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