## Absorbing State Phase Transition with Competing Quantum and Classical Fluctuations

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Stochastic processes with absorbing states feature examples of nonequilibrium universal phenomena. While the classical regime has been thoroughly investigated in the past, relatively little is known about the behavior of these nonequilibrium systems in the presence of quantum fluctuations. Here, we theoretically address such a scenario in an open quantum spin model which, in its classical limit, undergoes a directed percolation phase transition. By mapping the problem to a nonequilibrium field theory, we show that the introduction of quantum fluctuations stemming from coherent, rather than statistical, spin flips alters the nature of the transition such that it becomes first order. In the intermediate regime, where classical and quantum dynamics compete on equal terms, we highlight the presence of a bicritical point with universal features different from the directed percolation class in a low dimension. We finally propose how this physics could be explored within gases of interacting atoms excited to Rydberg states.

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Introduction.—Nonequilibrium phenomena can be found in many different contexts, ranging from chemical reactions to disease spreading. Analogously to the equilibrium case, nonequilibrium ensembles can show the emergence of universal behavior, signaling the irrelevance of the microscopic details of the dynamics for macroscopic observables. This occurs when such out-of-equilibrium systems start to act collectively [\[1](#page-4-0)–4]. A distinction can be made, depending on the presence or absence of detailed balance [5–[8\],](#page-4-1) between systems which evolve towards a stationary equilibrium state [\[9\]](#page-4-2) (e.g., quenched systems coupled to thermal baths [\[10\]\)](#page-4-3) or that preserve their nonequilibrium character even in the long time limit, representing flux equilibrium states.

Directed percolation (DP) [\[11\]](#page-4-4) constitutes an instance of a classical phase transition to an absorbing state, i.e., a state which can be reached, but not left by the dynamics, and represents a simple instance of a broader class of intrinsically nonequilibrium phase transitions [\[11](#page-4-4)–14]. Despite its robustness, its experimental observation has thus far been elusive [\[15\],](#page-4-5) with a single exception [\[16,17\].](#page-4-6) However, it was recently suggested to realize and explore DP dynamics in cold gases of atoms excited to high-lying Rydberg states [\[18\]](#page-4-7). In this work, we harness the opportunities that result from the fact that Rydberg gases are actually open quantum systems to go beyond the realm of classical physics (see also Ref. [\[19\]](#page-4-8)), and we establish a generalized absorbing state phase transition in the presence of quantum fluctuations. Driven-dissipative systems indeed constitute an ideal platform for the investigation of the interplay between classical and quantum effects, and they have recently been addressed in a broad range of experiments. The spectrum includes light-driven semiconductor heterostructures [\[20\]](#page-4-9), arrays of driven microcavities [\[21,22\],](#page-4-10) cold atoms in optical

lattices [\[23\],](#page-4-11) cavities [\[24,25\]](#page-4-12), and microtraps [\[26](#page-4-13)–28]. Several of these instances employ excitation of the atoms to high-lying Rydberg orbitals [\[29](#page-4-14)–31] in order to achieve strong interatomic interactions and to study cooperative effects [32–[36\].](#page-5-0)

In these systems, the driving and dissipation not only introduces coherence loss but also explicitly violates the equilibrium conditions at the microscopic level [\[7,37\].](#page-4-15) It is thus a challenge to identify to what extent the nonequilibrium and the quantum nature of the dynamics impact the macroscopic phase diagram and phase transition properties. Oftentimes, upon coarse graining, such systems lose their quantum character and equilibrium conditions are effectively restored [\[38](#page-5-1)–43]. But there are instances where nonequilibrium [\[44,45\]](#page-5-2) and quantum [\[46,47\]](#page-5-3) aspects persist even at an asymptotically large wavelength. The transition we highlight here does not fall into the DP universality class, and its origin can be unambiguously traced back to the presence of coherent dynamics. More precisely, the latter introduces a first-order nonequilibrium phase transition without counterpart in the purely classical DP problem. This discontinuous phase transition terminates in a bicritical point which, even asymptotically at large distances and in dimensions  $d < 2$ , does not feature the symmetries underlying DP, or any equilibrium problem.

Model.—We reproduce a quantum variant of the contact process (for an introduction, see Ref. [\[11\]](#page-4-4)). Basically, it consists of a lattice of "active" and "inactive" sites, where the former can spontaneously decay to inactive, whereas activation can only occur in the proximity of already active sites. Thus, the fully inactive state is absorbing. Specifically, we consider a lattice of quantum two-level systems with spacing  $r$ . On every site  $k$  we define the basis  $|a_k\rangle$  (active) and  $|i_k\rangle$  (inactive), the density of active sites

 $n_k = |a_k\rangle\langle a_k|$  and the ladder operators  $\sigma_k^+ = |a_k\rangle\langle i_k|$  and  $\sigma_k^- = |i_k\rangle\langle a_k|$  . Under the action of Markovian noise  $\sigma_k^- = |i_k\rangle\langle a_k|$ . Under the action of Markovian noise<br>sources the state *a* of the system evolves according sources, the state  $\rho$  of the system evolves according to the Lindblad equation [\[48,49\]](#page-5-4)  $\dot{\rho} = -i[H, \rho] + \sum_{\rho} \mathbf{D}[I_{\rho}]\rho$  (see the sketch in Fig. 1) where  $\sum_{a,k} \mathbf{D}[L_{a,k}] \rho$  (see the sketch in Fig. [1](#page-2-0)), where

$$
H = \Omega \sum_{k} C_{k} \sigma_{k}^{x}, \quad \text{with} \quad C_{k} = \sum_{j \text{ NN } k} n_{j} \tag{1}
$$

is the quantum Hamiltonian,  $\sigma_k^x = \sigma_k^+ + \sigma_k^-$ , and NN k denotes pearest peighbors (NN) of site k:  $\mathbf{D}[X]_Q = X_Q X^{\dagger}$ denotes nearest neighbors (NN) of site k;  $\mathbf{D}[X]\rho = X\rho X^{\dagger} - (X^{\dagger}X\rho + \rho X^{\dagger}X)/2$  is the dissinator and L, are the so- $(X^{\dagger}X\rho + \rho X^{\dagger}X)/2$  is the dissipator and  $L_{a,k}$  are the socalled jump operators, with indices  $a$  (process type) and  $k$ (lattice site). These jump operators are chosen to define a modified contact process [\[11\],](#page-4-4) which is known to feature a DP transition, and include *decay*  $L_{d,k} = \sqrt{\gamma} \sigma_k^{-1}$ <br>( $|a_k \rangle \rightarrow |i_k \rangle$ ) and—for every neighbor *i* of *k—branching*  $(|a_k\rangle \rightarrow |i_k\rangle)$  and—for every neighbor j of k—branching  $L_{b,j,k} = \sqrt{\kappa} n_j \sigma_k^+$  (an active site can activate a neighboring<br>one  $|a_i j_{\lambda}| \to |a_i a_j \rangle$ ) and coagulation  $L_{\lambda,i} = \sqrt{\kappa} n_i \sigma_k^-$  (the one  $|a_j i_k\rangle \rightarrow |a_j a_k\rangle$ ) and coagulation  $L_{c,j,k} = \sqrt{\kappa} n_j \sigma_k^-$  (the inverse process  $|a_j a_k\rangle \rightarrow |a_j i_k\rangle$ ). The "constraint" operator inverse process  $|a_j a_k\rangle \rightarrow |a_j i_k\rangle$ ). The "constraint" operator  $C_k$  in H represents the simplest choice reproducing the requirement of an active site nearby to flip a spin; this makes  $H$  the "minimal quantum equivalent" of the noisy branching or coagulation above. Similar constrained Hamiltonians have been studied in the past, with a focus on quantum glassy behavior [\[19\]](#page-4-8) and many-body localization [\[50,51\]](#page-5-5).

Equations of motion and density path integral.—We infer here the properties of the phase diagram by exploiting an effective path integral description for the density variable  $n_k$  alone. We start by deriving the Heisenberg-Langevin equations of motion (EOMs) [\[52\]](#page-5-6) for the single-site operators  $n_k$ ,  $\sigma_k^x$ , and  $\sigma_k^y = -i\sigma_k^+ + i\sigma_k^-$ . For<br>convenience we introduce the coordination number z (the convenience, we introduce the coordination number  $z$  (the number of nearest neighbors per lattice site) and the shorthand  $P_k^{x/y} = \sigma_k^{x/y} \sum_{j \text{ NN } k} \sigma_j^x$ . In the following, we also measure all times and energies in units of x; i.e., we set measure all times and energies in units of  $\gamma$ ; i.e., we set  $\gamma = 1$ :

<span id="page-1-2"></span>
$$
\dot{n}_k = -n_k + [\Omega \sigma_k^{\mathrm{y}} - \kappa (2n_k - 1)] C_k + \hat{\xi}_k^n, \qquad (2)
$$

$$
\dot{\sigma}_k^x = \Omega P_k^y - \frac{z\kappa + 1}{2} \sigma_k^x - \kappa \sigma_k^x C_k + \hat{\xi}_k^x, \tag{3}
$$

<span id="page-1-3"></span>
$$
\dot{\sigma}_k^y = \Omega P_k^x - \frac{z\kappa + 1}{2} \sigma_k^y - [\Omega(4n_k - 2) + \kappa \sigma_k^y] C_k + \hat{\xi}_k^y. \quad (4)
$$

The quantum noise terms  $\hat{\xi}_k^{\alpha}$  consider the fluctuations of the bath and depend on the structure of the jump operators. They show vanishing averages but nontrivial, Markovian correlations, which, for the present setup, are (in rescaled units)  $\langle \hat{\xi}_k^x \hat{\xi}_{k'}^x \rangle = \langle \hat{\xi}_k^y \rangle$  $\langle k \hat{\xi}^y_k \rangle = \delta_{k,k'}, \langle \hat{\xi}^n_k \hat{\xi}^n_k \rangle = \delta_{k,k'} n_k, \langle \hat{\xi}^x_k \hat{\xi}^y_k \rangle$ unds)  $\langle \xi_k \xi_k^y \rangle - \langle \xi_k \xi_k^y \rangle - \partial k_k^y, \langle \xi_k \xi_k^y \rangle - \partial k_k^y \eta_k^y, \langle \xi_k \xi_k^y \rangle = -i \delta_{k,k'} \sigma_k^+$ , and  $\langle \xi_k^a \xi_k^y \rangle = i \delta_{k,k'} \sigma_k^+$ , up to leading order in the density [53] leading order in the density [\[53\].](#page-5-7)

In the following, we work in the continuum limit  $(k, t) \rightarrow (\vec{x}, t) \equiv X$  and derive an effective path integral

for the density field  $n<sub>X</sub>$  via a Martin-Siggia-Rose construction [\[3,56](#page-4-16)–58], which is presented in the Supplemental Material [\[53\].](#page-5-7) Crucially, the  $\sigma^{x,y}$  fields are gapped and thus can be integrated out perturbatively. The resulting longwavelength field theory depends on the density variable  $n$ alone, and it is obtained by additionally performing a derivative expansion of the action. It reads

<span id="page-1-0"></span>
$$
S_n = \int_X \tilde{n}_X [(\partial_t - D\nabla^2 + \Delta) n_X + u_3 n_X^2 + u_4 n_X^3] - \int_X \left[ \frac{1}{2} \tilde{n}_X^2 n_X + \mu_4 \tilde{n}_X^2 n_X^2 \right] \equiv S_n^{(1)} + S_n^{(2)},
$$
 (5)

where  $D = r^2 \kappa$  represents a diffusion constant and  $\Delta = 1 - z\kappa - [(8z^2\Omega^2)/(z\kappa + 1)^3], \quad u_3 = 2z\{\kappa - [2z\Omega^2/(z\kappa + 1)]\}$  $(z\kappa + 1)$ },  $u_4 = [(8z^2\Omega^2/((z\kappa + 1))]$ , and  $\mu_4 = [2z^2\Omega^2/((z\kappa + 1)^2) + [128z^4\Omega^4/((z\kappa + 1)^6)]$  are the microscopic  $(z\kappa + 1)^2$  +  $[128z^4\Omega^4/(z\kappa + 1)^6]$  are the microscopic<br>coupling constants. The *response field*  $\tilde{n}$  encodes the linear coupling constants. The *response field*  $\tilde{n}$  encodes the linear response properties of *n* under small perturbations.

We emphasize two key properties of the action  $(5)$ : First, the absence of a density-independent Markovian noise level  $\sim T\tilde{n}_X^2$  (necessarily present in classical systems in thermal equilibrium). This is characteristic of DP dynamics, which feature the absence of density fluctuations in the absorbing state  $n<sub>X</sub> = 0$  and, consequently, a multiplicative kernel  $\propto$  n<sub>X</sub>. An additive noise introduced by the dissipative terms  $L_d = \sqrt{\gamma} \sigma^-$  only occurs in the eliminated spin variables  $\sigma^{x,y}$ . Second the presence of a nonzero coherent counting  $\sigma^{x,y}$ . Second, the presence of a nonzero coherent coupling  $\Omega \neq 0$ —i.e., the intrinsic quantum effect—leads to the appearance of nonzero couplings  $u_4$  and  $\mu_4$  as well as a negative contribution to  $u_3$ . This additional quantum scale Ω breaks a fundamental symmetry of the DP class (specified below) and strongly modifies the phase diagram compared to the purely dissipative model (see Fig. [1\)](#page-2-0).

<span id="page-1-1"></span>Effective potential and mean-field phase diagram.—The discussion of the various phases and transitions of the system is considerably simplified by realizing that the deterministic contribution to the action  $S_n^{(1)}$  can be written  $\int_X \tilde{n}_X(\partial_t n_X - D\nabla^2 n_X + {\{\vert \delta\Gamma(n_X) \vert / (\delta n_X) \}})$ , where

$$
\Gamma(n) = \frac{\Delta}{2}n^2 + \frac{u_3}{3}n^3 + \frac{u_4}{4}n^4
$$
 (6)

is a local effective potential. In the absence of fluctuations, Γ characterizes the mean-field phases, which are determined by the properties around its minima.

The corresponding phase diagram is shown in Fig. [1\(b\)](#page-2-0). The active phase is identified by  $\Delta < 0$ ,  $u_4 \ge 0$ , and  $u_3 > 0$ , which leads to a single minimum of the effective potential at finite density. On the other hand, when both  $\Delta$ and  $u_4$  are positive, there is a local minimum of  $\Gamma$  at  $n = 0$ . For negative and sufficiently strong cubic coupling  $u_3 < -2\sqrt{u_4\Delta}$ , there exists a second local minimum at finite density  $n > 0$ . In this regime, the mean-field evolution features two attractive fixed points and the

<span id="page-2-0"></span>

FIG. 1. (a) Fundamental processes. We consider a lattice whose sites admit two states: active (yellow) and inactive (red). Active sites decay to inactive at a rate of  $\gamma$ . Proliferation of active sites is possible through classical (rate κ) and quantum (strength  $\Omega$ ) branching. (b) One-dimensional  $(z = 2)$  phase diagram constructed from the effective action [\(5\)](#page-1-0) in a saddle-point approximation (the color code corresponds to the density of the active sites). All parameters are measured in units of  $\gamma$ . In the classical limit ( $\Omega = 0$ ), the system exhibits a continuous (second-order) directed percolation phase transition between an absorbing state and a finite-density one. This transition extends into the quantum regime (the thick red line) up to the critical point  $\alpha$ . In the quantum limit ( $\kappa = 0$ ) a first-order transition is found which also extends into the classical regime (the dashed yellow line) up to point  $\alpha$ . In the neighborhood of this line, a narrow region of coexistence of two attractive stationary solutions is present, which is not resolved here. The high values of the density reached in the active phase stem from neglecting higher orders of *n* in the action, which would otherwise enforce  $n \leq 1/2$ .

thermodynamic phase is determined within the optimal path approximation in phase space [\[59\].](#page-5-8)

Three different types of phase transitions from the active to the inactive state can be thus identified, their nature depending on the specific choice of parameters and the dimensionality. When the gap  $\Delta$  vanishes with  $u_3$  and  $u_4$ both greater than zero, the system undergoes a secondorder phase transition [see Fig. [2\(a\)\]](#page-2-1), corresponding to a diverging correlation length  $\xi = 1/\sqrt{|\Delta|} \rightarrow \infty$ . Numerical<br>evidence for this transition is presented in Fig. 2(b), which evidence for this transition is presented in Fig. [2\(b\)](#page-2-1), which displays the stationary density of active sites obtained for  $\Omega = 0$  in a chain of 200 sites. For  $\Delta > 0$  and  $u_3 \le -2\sqrt{u_4\Delta}$ , the transition from the active to the inactive phase takes place instead at the finite correlation length  $\xi = 1/\sqrt{|\Delta|} < \infty$ . The form of the effective potential  $\Gamma(n)$  suggests a first-order transition line in this regime  $\Gamma(n)$  suggests a first-order transition line in this regime featuring the coexistence of the zero and finitedensity solutions. This case, however, requires additional care due to the specific form of the noise, as detailed below.

<span id="page-2-1"></span>

FIG. 2. Effective potential and phase transitions. (a) Behavior of the effective potential  $\Gamma(n)$  (arbitrary units) across the secondorder phase transition. Dots mark the minima of  $\Gamma(n)$ . The transition occurs when  $\Delta$  in Eq. [\(6\)](#page-1-1) changes sign. (b) Stationary state density in the classical limit ( $\Omega = 0$ ) as a function of κ (a chain of 200 sites, averaged over  $10<sup>3</sup>$  realizations per point), obtained via Monte Carlo simulations starting from a completely active configuration and stopped at time  $\gamma t = 10^4$ . The data show the characteristic behavior of a continuous phase transition around  $\kappa_c \approx 6.2$ . (c) Effective potential  $\Gamma(n)$  (the dashed lines) and the corresponding "optimal-path" potential  $W(n)$  (the solid lines)—see Eq. [\(7\)](#page-3-0)—across the first-order transition. At the transition point,  $W(n_1 = 0) = W(n_2) = 0$ . (d) Steady-state histogram of the density in the quantum limit  $\kappa = 0$  (12 spins) obtained via a quantum-jump Monte Carlo (QJMC) method, indicating a first-order transition ( $\Omega_c \approx 2$ ) as  $\Omega$  increases. Two stable stationary solutions, one with zero and one with finite density, emerge. The inset displays a section of the histogram taken at  $\Omega = 8$ .

The  $\alpha$  point in Fig. [1\(b\)](#page-2-0) located at  $\Delta = u_3 = 0$  represents a bicritical point at which both the line ( $\Delta > 0$ ,  $u_3 = -2\sqrt{\Delta u_4}$  and the line of continuous transitions<br>  $(\Delta - 0, u_2 > 0)$  terminate. At this point, the quartic  $(\Delta = 0, u_3 > 0)$  terminate. At this point, the quartic potential term  $u_4$  provides the leading nonlinearity.

Fluctuations at the continuous transition.—The competition between quantum and classical dynamics strongly affects the nature of the active-to-inactive transition. In the absence of the coherent coupling,  $u_4$ ,  $\mu_4 = 0$ , the action [\(5\)](#page-1-0) is equivalent to the so-called Reggeon field theory for classical DP [\[60\]](#page-5-9). It features—upon rescaling the fields the characteristic rapidity inversion symmetry, which leaves the system invariant under the transformation  $n \leftrightarrow -\tilde{n}$  and  $t \rightarrow -t$  [\[3,7,59\].](#page-4-16) For  $u_4 > 0$ , this symmetry is broken by the microscopic action. The implications depend on the dimension d: For  $d > 2$ ,  $u_4$  is Renormalization Group (RG) irrelevant and can be discarded in the infrared-dominated dynamics close to the continuous transition. Consequently, in  $d > 2$ , rapidity inversion is restored and the line of continuous transitions displays universal scaling behavior corresponding to classical DP.

At the  $\alpha$  point [the white dot in Fig. [1\(b\)](#page-2-0)],  $u_3 = 0$  and the leading-order coupling becomes  $u_4$ . For  $d > 2$  [\[61\]](#page-5-10), the continuous transition at this point is governed by meanfield scaling behavior since  $u_4$  is RG irrelevant and cannot introduce infrared divergent corrections to the vanishing couplings  $u_3$ ,  $\Delta$ . On the other hand, for  $d < 2$ ,  $u_4$  becomes RG relevant and generates a nontrivial RG flow of  $\Delta$  and  $u_3$ on the entire second-order transition line. This leads to a violation of rapidity inversion which persists at long wavelength and thus drives the system away from the DP critical point to a different nonequilibrium universality class, without specific symmetries. In  $d < 2$ , therefore, only the isolated point  $\kappa = 1/z$ ,  $\Omega = 0$  lies in the DP class, while the presence of quantum fluctuations imprints a new universal scaling behavior on the entire line, including the  $\alpha$ point. In  $d = 2$ , the scaling of the fluctuation corrections to  $u_4$  determines whether this coupling becomes relevant, making the scenario equivalent to  $d < 2$ , or irrelevant, which has to be determined by a RG analysis.

Nonequilibrium discontinuous transition.—For  $(\Delta > 0,$  $u_3 < -2\sqrt{\Delta u_4}$ , the effective potential  $\Gamma$  displays two distinct minima,  $n_1 = 0$  and  $n_2 = (|u_3|/2u_4) +$  $[(u_3^2/4u_4^2) - (\Delta/v)]^{1/2}$ , suggesting a first-order phase tran-<br>sition. The actual transition line lies where the finitesition. The actual transition line lies where the finitedensity minimum becomes statistically preferred. In equilibrium, this would be the point at which the minima of  $\Gamma$  are at the same height. However, the present nonequilibrium noise shows more pronounced fluctuations at larger densities and thus favors  $n_1$  over  $n_2$ . To estimate the steady-state distribution function  $P(n)$ , we apply the optimalpath approximation to the action [\[3,59\];](#page-4-16) this involves treating the coefficient  $\Xi(n) = \frac{1}{2}n + \mu_4 n^2$  of  $\tilde{n}^2$  as a kind of mean-<br>field density-dependent temperature. It vields [53] field, density-dependent temperature. It yields [\[53\]](#page-5-7)

<span id="page-3-0"></span>
$$
P(n) = \frac{1}{Z} e^{-VW(n)}, \quad \text{with} \quad W(n) = \int_0^n dm \frac{\partial \Gamma / \partial m}{\Xi(m)},
$$
\n(7)

with volume V and normalization Z. The potentials  $W(n)$  and  $\Gamma(n)$  both vanish in  $n_1$  and share the finite-density minimum  $n_2$ . In the thermodynamic limit  $V \to \infty$ ,  $P(n) \to \delta(n - n_l)$ , where  $l = 1$ , 2, depending on which one is the global minimum of W, accounting for the physical constraint  $n \geq 0$ . The transition occurs when  $W(n_2) = 0$ , which identifies the nonequilibrium first-order line [the dashed line in Fig. [1\(b\)](#page-2-0)]. Because of the nonequilibrium nature of the fluctuations, this does not coincide with the naive prediction  $\Gamma(n_2) = 0$ , as shown in Fig. [2\(c\)](#page-2-1). In Fig. [2\(d\)](#page-2-1) we report the full-counting statistics of the density  $n$  obtained via QJMC techniques [\[62\]](#page-5-11) for a chain of 12 spins. Despite the presence of strong finite-size effects, a bimodal structure is still highlighted for large values of Ω. This implies that trajectories bunch together around two possible values, the absorbing one and a finite-density one; this constitutes a signature of the aforementioned coexistence.

Realization with Rydberg atoms.—Atoms excited to Rydberg states are employed in current experiments to study many-body effects [\[26,32,34,63](#page-4-13)–71]. Recently, several theoretical studies addressed the semiclassical limit of these systems [\[72,73\],](#page-6-0) connecting their dynamics to that of constrained classical ones [\[73,74\]](#page-6-1). Reasoning along the same lines of Ref. [\[18\]](#page-4-7), we discuss below an implementation which should permit the exploration of the physics discussed above.

The internal structure of Rydberg atoms can be approximated as a ground state  $|GS\rangle \equiv |i\rangle$  (inactive site) and an excited one  $|Ryd\rangle \equiv |a\rangle$  (active site). Rydberg gases feature strong van der Waals interactions in state  $|a > [29-31]$  $|a > [29-31]$  $|a > [29-31]$ , which rapidly decay as  $r^{-6}$  with the interparticle distance r. For the sake of simplicity, we approximate them here as nearest-neighbor terms  $V_{NN}$  in a one-dimensional configuration.

Quantum branching and coagulation is realized via coherent driving by a laser field of Rabi frequency  $\Omega$ and detuning  $\Delta_L$  with respect to the atomic transition frequency; fixing  $\Delta_L = -V_{NN}$  enables an "antiblockade" [\[72,75,76\]](#page-6-0) mechanism which favors the excitation of a Rydberg atom next to an already excited one, e.g.  $|iai \rangle \rightarrow |iaa \rangle$ . Unlike the idealized model above, the constraint requires here a single excitation nearby, and processes such as  $|aia \rangle \rightarrow |aaa \rangle$  are highly suppressed. The Hamiltonian is therefore approximately given by  $H_{\text{Ryd}} = \Omega \sum_{k} C'_{k} \sigma_{k}^{x}$ , where  $C'_{k} = n_{k-1} + n_{k+1} - 2n_{k-1}n_{k+1}$ .<br>To generate the incoherent branching and coagulation

To generate the incoherent branching and coagulation the atoms are coupled (with coupling  $q$ ) to a second equally detuned light field with strong phase noise (dephasing rate  $\lambda \gg q$ ) [\[77\]](#page-6-2); for a correlation length shorter than the interatomic distance, the bath is modeled as independent bosonic modes  $b_k$ ,  $b_k^{\dagger}$  acting on each lattice site. The effective equation of motion for the atoms is obtained by performing second-order perturbation theory in the small parameter  $g/\lambda$  [\[18,78,79\].](#page-4-7) The resulting master equation for the reduced atomic density matrix  $\rho$  is

$$
\dot{\rho} = \frac{4g^2}{\lambda} \sum_{k} (\langle b_{k}^{\dagger} b_{k} \rangle \mathbf{D} [C'_{k} \sigma_{k}^{+}] + \langle b_{k}^{\dagger} b_{k} + 1 \rangle \mathbf{D} [C'_{k} \sigma_{k}^{-}] \rangle \rho.
$$

At sufficiently high  $(\langle b_k^{\dagger} b_k \rangle \gg 1)$  and homogeneous  $(\langle b_k^{\dagger} b_k \rangle \approx \langle b_k^{\dagger} b_k \rangle)$  intensity are seen identify as  $(\langle b_k^{\dagger} b_k \rangle \approx \langle b_m^{\dagger} b_m \rangle)$  intensity, one can identify  $\kappa = (4.2/k_{\perp}^{\dagger} k_{\perp})/l_{\perp}$  looding to the henching and ecosylation  $\left(4g^2\langle b_k^{\dagger}b_k\rangle\right)/\lambda$ , leading to the branching and coagulation jump operators  $L_{b,k}^{\text{Ryd}} = \sqrt{\kappa} C_k' \sigma_k^+$  and  $L_{c,k}^{\text{Ryd}} = \sqrt{\kappa} C_k' \sigma_k^-$ . The final process is radiative decay from the Pydberg state to final process is radiative decay from the Rydberg state to the ground state, with jump operator  $L_{d,k}^{\text{Ryd}} = \sqrt{\gamma} \sigma_k^-$  [\[31\].](#page-5-12)

Although the microscopic formulation of the dynamics is slightly different from the previously discussed model—for example, atoms with more than one excited neighbor are brought off resonance—the resulting phase structure is similar, as the EOMs only differ from Eqs.  $(2)$ – $(4)$  by RG-irrelevant higher-order density terms.

Outlook.—We have investigated the effects of quantum dynamical processes on a prototypical absorbing-state phase transition. We highlighted the emergence of a richer structure in the phase diagram, which includes both a discontinuous and a continuous nonequilibrium transition. In the low dimension  $d < 2$ , the presence of a quantum coherent process leads to a breaking of the only fundamental symmetry of DP in a way that persists at long wavelengths, and thus leads to a phase transition of a different nature. In equilibrium, the interplay between classical (thermal) and quantum fluctuations typically leads to a dimensional crossover [\[2,80\].](#page-4-17) This Letter shows that, out of equilibrium, the picture is not as straightforward and opens the path for further investigations in this field, including the quantitative characterization of the new universality class.

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