Floquet Engineering of Correlated Tunneling in the Bose-Hubbard Model with Ultracold Atoms

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We report on the experimental implementation of tunable occupation-dependent tunneling in a Bose-Hubbard system of ultracold atoms via time-periodic modulation of the on-site interaction energy. The tunneling rate is inferred from a time-resolved measurement of the lattice site occupation after a quantum quench. We demonstrate coherent control of the tunneling dynamics in the correlated many-body system, including full suppression of tunneling as predicted within the framework of Floquet theory. We find that the tunneling rate explicitly depends on the atom number difference in neighboring lattice sites. Our results may open up ways to realize artificial gauge fields that feature density dependence with ultracold atoms.

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Ultracold atoms in optical lattices provide an excellent platform for highly controlled studies of strongly correlated states of matter, paradigm examples being the observation of a Mott insulator for bosons [\[1\]](#page-4-0) and fermions [\[2,3\].](#page-4-1) At the same time, the unprecedented temporal control over system parameters allows for the investigation of coherent dynamics in the many-body system [\[4,5\]](#page-4-2). Among a plethora of associated phenomena, time-periodic driving of the quantum system opens up particularly exciting possibilities. The effect of such a modulation can often be described within an effective time-independent Floquet-Hamiltonian with novel synthetically engineered properties [6–[8\]](#page-4-3). Pioneering work in this direction has demonstrated the coherent control of the single-particle tunneling amplitude in shaken lattices [\[9\]](#page-4-4), with applications towards shifting phase boun-daries [\[10,11\]](#page-4-5) and transport [\[12,13\],](#page-4-6) observation of magnetic frustration [\[14\]](#page-4-7), and even the realization of artificial gauge potentials [\[15](#page-4-8)–17] and topological band structures [\[18\]](#page-4-9). Here, we go beyond control of the single-particle Hamiltonian by implementing tunable correlated tunneling for which coupling explicitly depends on the presence of other particles in the interacting many-body system [\[19\]](#page-4-10). This opens a new platform for the exploration of phenomena in lattices with occupation-dependent hopping, ranging from a variety of extended Hubbard models with rich phase diagrams for bosons [\[20\]](#page-4-11) and fermions [\[21](#page-4-12)–23] to situations with broken mirror symmetry [\[24\]](#page-4-13) and potentially dynamical synthetic gauge fields [\[25\]](#page-4-14).

Our approach exploits a strongly correlated lattice gas of bosonic cesium (Cs) atoms in the presence of periodically modulated particle-interactions, described by the Bose-Hubbard Hamiltonian [\[26\]](#page-4-15)

$$
\hat{H} = -J \sum_{\langle i,j \rangle} \hat{a}_i^{\dagger} \hat{a}_j + \sum_i \frac{U(t)}{2} \hat{n}_i (\hat{n}_i - 1). \tag{1}
$$

As usual, \hat{a}_i^{\dagger} (\hat{a}_i) are the bosonic creation (annihilation) operators at the *i*th lattice site, $\hat{n}_i = \hat{a}_i^{\dagger} \hat{a}_i$ are the number
operators and *I* is the tunnel matrix element between operators, and J is the tunnel matrix element between neighboring lattice sites. At the heart of the experiments reported in this Letter is a time-dependent, rapidly oscillating on-site interaction energy $U(t)$ of the form $U(t) = U + \delta U \sin(2\pi f_{mod}t)$. For a sufficiently large oscillation frequency $hf_{mod} \gg U, J$, one obtains an effective time-independent description by expanding Eq. [\(1\)](#page-0-0) in a Floquet basis and retaining a single time-averaged Floquet sector [\[19\].](#page-4-10) In striking contrast to shaken lattices, modulated interactions generate dynamics that explicitly depend on the occupation number [\[19,25\],](#page-4-10) so that the modulationinduced tunneling in the effective Hamiltonian,

$$
\hat{H}_{\text{eff}} = -J \sum_{\langle i,j \rangle} \hat{a}_i^{\dagger} J_0 \left(K(\hat{n}_i - \hat{n}_j) \right) \hat{a}_j + \sum_i \frac{U}{2} \hat{n}_i (\hat{n}_i - 1), \tag{2}
$$

is now occupation dependent. Specifically, the amplitudes $J_{\text{eff}} = J \times J_0(K \Delta n)$ of the tunneling processes are determined by the strength of the modulation $K = \delta U/(hf_{\text{mod}})$ via a rescaling with the zeroth-order Bessel function J_0 [Fig. [1\(a\)](#page-1-0)]. One consequence is a suppression of hopping for specific choices of K , which explicitly depends on the particle number difference Δn (after applying \hat{a}) at the lattice sites involved, known as many-body coherent destruction of tunneling [\[27\]](#page-4-16).

We demonstrate the modulation-induced coherent control of occupation-dependent atom tunneling after a quantum quench in the correlated many-body system. Starting from localized bosons prepared in an atomic Mott insulator, we suddenly switch off particle interactions by means of a Feshbach resonance and identify the subsequent delocalization processes as a sensitive probe for hopping in the lattice. This forms the basis for a controlled study of the

FIG. 1. Controlling occupation-dependent tunneling with periodically modulated interactions. (a) Renormalized tunneling rate J_{eff}/J as a function of the modulation strength K for the processes $|1, 1\rangle - |0, 2\rangle$ (solid line) and $|1, 2\rangle - |0, 3\rangle$ (dashed line). Single-particle tunneling $(|1, 0\rangle - |0, 1\rangle)$ is not affected by the modulation (dotted line). (b) Illustration of the experimental measurement protocol. Starting from a Mott insulator with unity filling (top row) the interaction strength is suddenly quenched to zero. The subsequent delocalization of the initially localized atoms, resulting in multiply occupied lattice sites, is controlled via the modulation strength.

many-body tunneling dynamics in the presence of periodically modulated interactions [Fig. [1\(b\)](#page-1-0)].

Our experiments start with a Cs Bose-Einstein condensate [\[28\]](#page-4-17), from which we prepare a three-dimensional (3D) one-atom-per-site Mott insulator in a cubic optical lattice at a scattering length $a_s \approx 230a_0$ [\[29\]](#page-4-18). The lattice depth in all directions is $V_q = 20E_R$ ($q = x, y, z$), where $E_R =$ $h \times 1.325$ kHz is the photon recoil energy. A Feshbach resonance allows us to control a_s and thereby U independent of J [\[33\].](#page-4-19) First, we investigate tunneling dynamics in the lattice after a sudden quench of U to the vicinity of the noninteracting limit. Specifically, starting deep in the Mottinsulating phase with localized atoms, we quickly ramp U to a value in the range $|U/h| \lesssim 200$ Hz and wait for a hold time of $t_h = 50$ ms. Subsequently, the scattering length is rapidly set back to its initial value, which freezes the local site occupancies. We then detect the total number of atoms residing in singly and doubly occupied lattice sites via Feshbach-molecule formation and detection, involving a narrow g-wave Feshbach resonance with a pole at 19.8 G [\[34\]](#page-4-20). The number of atoms in sites occupied by more than two bosons is inferred by means of controlled recombination loss [\[35,36\].](#page-4-21) For this, we quickly ramp the magnetic field to 9.3 G, where a_s is large and negative, inducing fast loss due to three-body recombination [\[37\].](#page-4-22) The sample is held for 10 ms, long enough to lose all particles at sites with occupation number larger than 2, before detecting the remaining atoms. Note that the site occupancies are measured individually in independent realizations of the experiment.

The result of this measurement is shown in Fig. [2\(a\)](#page-1-1). While the total atom number of the sample (circles) remains constant as a function of U, a pronounced resonance for the number of singly occupied lattice sites (triangles) is

FIG. 2. Decay of singly occupied lattice sites after a quench from a Mott insulator with unity filling to noninteracting bosons. (a) Number of atoms in singly (triangles) and doubly (squares) occupied sites, in sites with occupation number ≥ 3 (diamonds), as well as the total number of atoms (circles) as a function of U after a hold time $t_h = 50$ ms for $V_{x,y,z} = 20E_R$. Solid lines show (double-)Gaussian fits to the data. (b) Normalized number of singly occupied sites as a function of t_h after a quench to $U = 0$ for $V_{x,y,z} = 20E_R$ (squares), $25E_R$ (triangles), and $30E_R$ (circles). Solid lines show linear fits to the initial decay. (c) Initial decay rate γ of singly occupied sites after a quench to $U = 0$ as a function of the tunneling rate J in three dimensions (squares) and one dimension (triangles). The dashed lines are linear fits to the data. The shaded area indicates an estimate for γ as extracted from numerical simulations in one dimension [\[29\].](#page-4-18)

observed. The position of the resonance minimum is identified with a vanishing value of U. A Gaussian fit to the data reveals a half-width-at-half-maximum (HWHM) of 68(3) Hz, which is comparable with the calculated lattice bandwidth, $12J/h = 39.6$ Hz. The reduction of the number of lattice sites with unity filling arises from tunnelinginduced delocalization, which is energetically allowed for sufficiently small U . That process is accompanied by the buildup of multiply occupied lattice sites. Accordingly, after the time evolution we observe atoms residing in sites occupied by two (squares) and more than two (diamonds) bosons resonantly enhanced around $U = 0$. For the latter, note the reduced Gaussian HWHM of 34(2) Hz, reflecting the larger on-site energy associated with three particles on the same lattice site.

Next, we study the dynamics after the quench to $U = 0$ for different depths of the optical lattice. In order to provide similar starting conditions for all measurements, the initial Mott-insulating state is now prepared in a deeper potential with $V_{x,y,z} = 30E_R$. The quench in U is done as before, but now it is accompanied by an additional rapid change of the lattice depth to the desired value. After letting the sample evolve for a variable time t_h , the optical lattice and a_s are both ramped back to their initial values, followed by the aforementioned detection scheme for determining site occupancies. In Fig. [2\(b\),](#page-1-1) the normalized number of singly occupied lattice sites as a function of t_h is depicted for three different values of the lattice depth. An initial decay is observed over a time scale that is on the order of the single particle tunneling time, before the signal levels off to a stationary value. The initial decay is quantified by a linear fit, the slope of which delivers a characteristic decay rate γ . In Fig. [2\(c\)](#page-1-1), we show values for γ obtained from such measurements at different lattice depths as a function of the corresponding calculated tunneling rate J (squares). The data suggest a linear dependence, which invites us to exploit the decay of singly occupied sites after the quench as a measure for the tunneling rate in the lattice.

Similarly, we measure the decay of single occupancy in 1D chains by varying only the vertical lattice depth V_z while keeping $V_{x,y}$ fixed at 30 E_R . Here, V_z is kept small compared to $V_{x,y}$ to ensure decoupling of the 1D systems over relevant experimental time scales. The results obtained for γ as a function of J [triangles in Fig. [2\(c\)](#page-1-1)] again obey a linear dependence. A quantitative estimate for γ as extracted from numerical simulations of a single 1D Bose-Hubbard chain [\[29\]](#page-4-18) is found to be in good agreement with the data. We note that for a fixed J we observe a faster decay of single occupancy in three dimensions compared to the 1D case, owing to the increased number of nearest neighbors. This is quantified by the ratio of the slopes $\beta_{3D}/\beta_{1D} = 1.8(1)$, which we obtain from linear fits to the data. The observed ratio is different from 3, as one may expect from the delocalization process of a single atom by counting nearest neighbors. This we attribute to the presence of many particles that all take part simultaneously in the tunneling dynamics. Indeed, a numerical study of a simplified model with multiple atoms in a 3D and 1D configuration predicts a ratio of 1.6 in reasonably good agreement with the measured value [\[29\].](#page-4-18)

Having discussed the bare tunneling dynamics in the many-body system for vanishing particle interaction, we are now in a position to investigate the situation in the presence of a periodically modulated on-site interaction. Starting again from the Mott insulator at $V_{x,y,z} = 20E_R$, we perform the quench to $U = 0$ as before, but now apply an additional sinusoidal modulation with amplitude δU and frequency $f_{\text{mod}} = 120$ Hz during t_h by a periodic oscillation of the magnetic offset field that controls a_s . The normalized number of singly occupied lattice sites as a function of t_h is shown in Fig. [3\(a\)](#page-2-0) for five data sets recorded at increasing values of δU . For zero modulation strength (triangles) we recognize the decay of sites with unity filling as observed before. Increasing δU leads to a substantially slower decay (squares), indicative of a reduced tunneling-induced delocalization of the particles. When further increasing the modulation strength to $\delta U/h = 297(4)$ Hz, the decay is heavily suppressed (diamonds), and essentially allows for a controlled pinning of the particles on their individual lattice sites. For even larger modulation strength, we observe again decay on a comparatively rapid time scale (inverted triangles), while a second strong suppression of tunneling is seen for $\delta U/h$ = $686(23)$ Hz (circles). We stress that the lattice depth is kept at a fixed value for all measurements, and tunneling is thus fully controlled via the modulation of particle interactions.

FIG. 3. Controlling the decay of single occupancy in the presence of modulated interactions after quenching from a Mott insulator with unity filling to $U = 0$. (a) Normalized number of singly occupied lattice sites as a function of t_h after the quench for modulation amplitudes $\delta U/h = 0$ Hz (triangles), 238(3) Hz (squares), 297(4) Hz (diamonds), 476(11) Hz (inverted triangles), and 686(23) Hz (circles) when modulating with $f_{mod} = 120$ Hz. Solid lines show linear fits to the initial decay. (b) Initial decay rate γ of singly occupied sites as a function of δU for $f_{\text{mod}} = 120$ Hz (triangles) and 200 Hz (circles). The dashed lines depict $\gamma_{\delta U=0} \times |J_0(\delta U/(hf_{\rm mod}))|$. The solid lines show numerical results for γ as extracted from a calculation within a 3D lattice of 7 sites in star-type configuration [\[29\]](#page-4-18). For all measurements in this figure $V_{x,y,z} = 20E_R$.

As before, the data are analyzed via a linear fit to the initial decay. From such measurements, we obtain values for the characteristic decay rate γ over a wide range of modulation strengths, and plot them in Fig. [3\(b\)](#page-2-0) as a function of δU for two different values of f_{mod} . We compare the data to the Bessel-function scaling of $|J_{\text{eff}}|$ within the time-independent Floquet-Hamiltonian description of the system (dashed lines). Clear minima in the measured values for γ are found in accordance with the zeros of $J_0[\delta U/(hf_{\text{mod}})]$. This unequivocally demonstrates
a controlled coherent destruction of tunneling in the a controlled coherent destruction of tunneling in the interacting many-body system that entirely relies on the presence of particles in adjacent lattice sites.

Away from these minima, the experimental data lie significantly below a pure rescaling of γ with the Bessel function J_0 . Given the dynamical generation of site occupancies larger than 2 after the quench in combination with the occupation dependence of J_{eff} , one may indeed expect a more sophisticated behavior for the decay of single occupancy in the presence of modulated interactions. We attempt to model these effects via a numerical simulation of the time evolution under the action of H_{eff} within a reduced 3D lattice that consists of 7 sites arranged in a star-type configuration [\[29\].](#page-4-18) The analysis of single occupancy at the central lattice site delivers a measure for the rate of decay, which reproduces the scaling behavior of the measured γ as a function of δU [solid lines in Fig. [3\(b\)\]](#page-2-0).

The occupation dependence of J_{eff} is directly observable in a further experiment, for which we initially prepare a sample of randomly distributed singly and doubly occupied sites at $U/h = 420(20)$ Hz [\[29\]](#page-4-18). We rapidly apply a linear energy offset E per site along the vertical ζ direction by a magnetic force, thereby tilting the lattice. After holding the sample for $t_h = 50$ ms in the tilted configuration, we set E back to zero and detect double occupancy. The number of atoms in doubly occupied sites as a function of E [Fig. [4\(a\)\]](#page-3-0) exhibits two resonances corresponding to resonant tunneling processes of the type $|1, 1\rangle - |2, 0\rangle$ ($E \approx U$) and $|2, 1\rangle - |3, 0\rangle$ ($E \approx 2U$) [\[34,38\].](#page-4-20) We now adjust E to either of the detected resonance positions, thereby selectively addressing one of the two tunneling processes, and additionally modulate U during $[0, t_h]$. The increase
(decrease) of double occupancy C normalized to its value (decrease) of double occupancy C normalized to its value without modulation is shown in Fig. [4\(b\)](#page-3-0) as a function of δU . The data exhibit clear minima in accordance with the zeros of J_{eff} , indicating many-body coherent destruction of tunneling. Moreover, the measurement results follow the qualitative trend expected from the Bessel-function scaling of J_{eff} .

Finally, we investigate the system at unity filling with modulated interactions at nonzero values of U. Again, we

FIG. 4. Modulation control of occupation-dependent tunneling in the tilted lattice. (a) Number of atoms in doubly occupied lattice sites as a function of the tilt E for $a_s = 80a_0$ and $V_{x,y,z} = 20E_R$. The solid line is a double-Gaussian fit to the data. Vertical dashed lines mark the calculated values for U and ²U, the latter corrected for multibody interactions [\[33,39\].](#page-4-19) (b) Normalized resonance peak values $C/C_{\delta U=0}$ for the processes $|1, 1\rangle - |2, 0\rangle$ (triangles) and $|2, 1\rangle - |3, 0\rangle$ (circles) as a function of δU for $f_{\text{mod}} = 120$ Hz. The solid lines show $J_0(\Delta n \times$ $\delta U/(hf_{\text{mod}}))$ with $\Delta n = 1$ and $\Delta n = 2$, respectively. Typical error bars are given for the data point at 380 Hz.

start the experiment from initially localized atoms prepared in a Mott insulator with $V_{x,y,z} = 20E_R$. However, the Mott insulator is now quenched to a finite U in the range -400 Hz $\leq U/h \leq 600$ Hz. As above, we wait for t_h = 50 ms during which the interaction strength is modulated around U, before we detect the number of remaining singly occupied lattice sites. The detected atoms residing in unity-filled sites as a function of U is shown in Fig. [5](#page-3-1) for two different modulation strengths δU . Depending on the value of δU , the range of data shown is restricted by the presence of additional narrow Feshbach resonances that are otherwise crossed during a modulation cycle [\[29\].](#page-4-18)

We observe a pronounced resonance centered around zero on-site interaction energy when $\delta U/h = 290(4)$ Hz, indicative of the tunneling-induced decay of single occupancy. The absence of this resonance for $\delta U/h = 523(14)$ Hz, which is in the vicinity of the Bessel function zero crossing (cf. Fig. [3\)](#page-2-0), reveals the persistence of the coherent destruction of tunneling over an extended range of nonzero interaction strengths. With increasing U, the requirement of rapid modulation $hf_{mod} \gg U, J$ for the Floquet analysis leading to \hat{H}_{eff} breaks down. This is ultimately signaled by resonant formation of particle-hole pairs in the Mott insulator as observed when $U/h \approx f_{mod}$ and $U/h \approx 2f_{mod}$. Modulation of U in this resonant regime $[40]$ thus provides a novel alternative to the more conventional lattice-depthmodulation technique for detecting the Mott gap [\[41\].](#page-4-24)

In summary, we have demonstrated tunable occupationdependent tunneling in a Bose-Hubbard system via periodically driven particle interactions. Our work provides a basis for future studies of interesting many-body phases in correlated hopping models, including insulators with both parity and string order [\[24,42,43\].](#page-4-13) While some of them are expected in the parameter range studied here [\[19\]](#page-4-10), the applicability of our technique can be extended, exploiting narrower Feshbach resonances and faster modulation [\[44\]](#page-4-25).

FIG. 5. Off-resonant and on-resonant tunneling control in the presence of modulated interactions. Number of singly occupied sites as a function of U after $t_h = 50$ ms of modulation at frequency $f_{\text{mod}} = 200$ Hz with amplitudes $\delta U/h = 290(4)$ Hz (squares) and 523(14) Hz (circles). Here, the lattice depth $V_{x,y,z} = 20E_R$. Solid lines show fits to the data using a sum of multiple Gaussians. The data sets are vertically offset for clarity.

Moreover, combining modulated interactions with Ramanassisted hopping may allow for the creation of densitydependent synthetic gauge fields [\[25,45\]](#page-4-14). This work can also be extended to investigate the phase diagram of recently discussed intermediate-time steady states in driven lattice systems [\[46\].](#page-4-26)

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