# Adiabatic Field-Free Alignment of Asymmetric Top Molecules with an Optical Centrifuge 

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#### Abstract

We use an optical centrifuge to align asymmetric top $\mathrm{SO}_{2}$ molecules by adiabatically spinning their most polarizable $\mathrm{O}-\mathrm{O}$ axis. The effective centrifugal potential in the rotating frame confines the sulfur atoms to the plane of the laser-induced rotation, leading to the planar molecular alignment that persists after the molecules are released from the centrifuge. The periodic appearance of the full three-dimensional alignment, typically observed only with linear and symmetric top molecules, is also detected. Together with strong in-plane centrifugal forces, which bend the molecules by up to 10 deg , permanent field-free alignment offers new ways of controlling molecules with laser light.


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Aligning the axes of gas-phase molecules in the laboratory frame has long been recognized as a powerful instrument in the growing number of areas of molecular science. For recent reviews on the impact of molecular alignment on the molecular dynamics, interactions, and spectroscopy, see Refs. [1-3]. Today, linear and symmetric top molecules are routinely aligned in one dimension with a single laser pulse, either long (adiabatic) or short (nonadiabatic) on the time scale of the rotational period, interacting with the induced dipole moment of a molecule [4-6]. Aligning the frame of asymmetric top molecules in three dimensions requires more sophisticated methods, capable of controlling the rotation of a molecule around all three of its distinct rotational axes (for recent reviews, see Refs. [7,8]). Both adiabatic [9,10] and nonadiabatic [11-15] excitation schemes, as well as their combinations [16,17], have been used for the three-dimensional alignment (3DA) of asymmetric rotors.

Adiabatic approaches excel in producing permanent molecular alignment, but only in the presence of a strong laser field, which is often undesirable. Field-free 3DA (FF3DA) has been achieved by means of nonadiabatic excitation with a single elliptically polarized pulse [13] or a series of pulses [12,15]. However, unlike the case of symmetric molecules, where the aligned state is created promptly after the laser pulse and then periodically revives in time, the dynamics of asymmetric rotors exhibit only partial revivals with incommensurate frequencies [18-20]. As a result, the degree of the prompt postpulse FF3DA is not only limited [13], but is also very sensitive to the field ellipticity and strength [19]. Owing to the same complex aperiodic dynamics, enhancing the 3DA with consecutive rotational kicks is inefficient for light molecules with short alignment transients, like $\mathrm{SO}_{2}$ [14], and even for heavier rotors establishing the optimal timing and ellipticity of pulses is not straightforward and may require experiments with feedback-loop based optimization algorithms [15].

In this work, we demonstrate a new approach to aligning asymmetric top molecules with nonresonant laser pulses.

Our method combines the robustness of an adiabatic alignment with field-free conditions of the final aligned state. It is based on the accelerated spinning of molecules with an optical centrifuge-an intense laser pulse, whose linear polarization rotates with gradually increasing angular frequency [21,22]. An optical centrifuge has recently been used for reaching extreme rotational states, known as molecular "superrotors" [23,24], with planar alignment demonstrated in the ensembles of centrifuged linear molecules [25]. Here, we extend this technique to the adiabatic alignment of asymmetric rotors.

The essence of our method is illustrated in Fig. 1. The leading edge of the centrifuge (left plane) adiabatically aligns the molecular axis of maximum polarizability ( $a$ axis of $\mathrm{SO}_{2}$, parallel to the $\mathrm{O}-\mathrm{O}$ axis) along the field direction. As the rotational frequency $\omega$ increases, slowly emerging


FIG. 1. Illustration of the main concept of aligning an asymmetric top molecule $\left(\mathrm{SO}_{2}\right)$ with an optical centrifuge. The left side of the centrifuge pulse (red corkscrew surface) corresponds to its leading edge, linearly polarized along $\vec{E}$. Behind the trailing edge of the centrifuge (right side), the molecular plane is aligned in the plane of the induced rotation. The three axes of $\mathrm{SO}_{2}(a, b$, and $c$ ) are shown in red, green, and blue, respectively. $\theta_{b}$ is the orientation angle measured in this work, as discussed in the text.
centrifugal forces in the rotating frame of reference pull the sulfur atom into the plane of rotation, so as to minimize the effective potential $V_{\text {eff }}=-\frac{1}{2} I \omega^{2}$ by maximizing the molecular moment of inertia $I$ around the rotation axis. For a centrifuged $\mathrm{SO}_{2}$ molecule rotating at $4.5 \times 10^{13} \mathrm{rad} / \mathrm{s}$, the well depth of this centrifugal potential is about 0.9 eV . To produce a comparable potential well via the interaction with the molecular polarizability, e.g., as in the FF3DA schemes with elliptically polarized light, one would need laser powers of the order of $10^{16} \mathrm{~W} / \mathrm{cm}^{2}$, well above the ionization threshold of most molecules.

To observe the field-free rotational dynamics of the centrifuged $\mathrm{SO}_{2}$ molecules, we employed the technique of velocity map imaging (VMI) in a fashion similar to that described in our previous work [26]. Briefly, a supersonic jet of helium-seeded sulfur dioxide is exposed to the field of an optical centrifuge between the plates of a time-of-flight mass spectrometer [Fig. 2(a)]. Rotationally excited molecules are then Coulomb exploded by an ultrashort intense probe pulse ( $40 \mathrm{fs}, \sim 10^{15} \mathrm{~W} / \mathrm{cm}^{2}$ ) of either linear or circular polarization. The momenta of the fragment atomic and molecular ions, bearing the information on the molecular orientation at the moment of explosion, are projected onto the microchannel plate (MCP) detector with a phosphor screen. Centrifuge pulses are produced by combining two oppositely chirped broadband pulses, circularly polarized in the opposite directions [21,22].

Gating the MCP voltage for the arrival of either $\mathrm{S}^{3+}$ or $\mathrm{SO}^{2+}$ ions, we recorded the corresponding VMI images


FIG. 2. (a) Experimental configuration. A supersonically expanded cold molecular ensemble of $\mathrm{SO}_{2}$ is rotationally excited by an optical centrifuge and Coulomb exploded by a femtosecond probe beam between the charged plates of a time-of-flight spectrometer. Ion fragments are collected on a microchannel plate detector (MCP) with a phosphor screen. To determine the inplane angular distribution of the molecules, an opaque mask with a pinhole in the center is placed on top of the screen, with a photomultiplier tube detector (PMT) behind it (see the text for details). (b),(c) Images of $\mathrm{S}^{3+}$ and $\mathrm{SO}^{2+}$ fragments originated from the rotationally cold and centrifuged molecules, respectively.
obtained with linear probe polarization, normal to the plane of the MCP. Because of the symmetry of $\mathrm{SO}_{2}$, the recoil momenta of both species lie in the O-S-O plane of the fragmented molecule and, therefore, define unambiguously the molecular plane at the time of explosion. Without the centrifuge, the observed images exhibited an axial symmetry, expected for the spherically symmetric molecular distribution [Fig. 2(b)]. As we turned the centrifuge on, both images collapsed to the plane of the laser-induced rotation, as shown in Fig. 2(c). The simultaneous collapse of the two distributions for both ion fragments indicates strong planar alignment of $\mathrm{SO}_{2}$ molecules.

At high rotational energies, comparable to the kinetic energy release of the Coulomb explosion, extracting the degree of planar alignment from the velocity map images in Fig. 2(c) is complicated by the additional drift of the ion fragments away from the rotationally unperturbed trajectories [26]. The ultrafast synchronous rotation of the centrifuged molecules results in tilting the Newton sphere of the fragment velocities with respect to the sphere of possible molecular orientations. In the case of $S^{3+}$ ions, preferably ejected orthogonally to the laser field polarization [27], the drift effect leads to the compression of the ion image towards the center. On the other hand, the image of $\mathrm{SO}^{2+}$, preferably ejected along the field polarization, is stretched outwards. This amounts to an underestimated planar alignment factor determined from the $\mathrm{S}^{3+}$ image, $\left\langle\cos ^{2} \theta\right\rangle_{2 \mathrm{D}}=0.64$, and an overestimated value of 0.90 determined from the $\mathrm{SO}^{2+}$ channel.

We studied the rotational dynamics of the aligned molecules within the rotation plane using circularly polarized probe pulses to ensure an isotropic in-plane ionization probability. The in-plane angular distribution of the centrifuged molecules was measured as a function of the delay time between the end of the centrifuge pulse and the probeinduced Coulomb explosion. Similarly to our previous work [26], the distribution was determined by recording the ion signal at a single location on the MCP detector (here, in the center of the phosphor screen) as a function of the release angle of the centrifuge $\theta_{\text {rel }}$ [see Fig. 2(a)]. The latter was found in a separate cross-correlation setup, described in detail in Ref. [26].

With the MCP voltage gated at the arrival of $S^{3+}$ ions, the detected signal is proportional to the number of molecules $F_{\theta_{\text {rel }}}\left(\theta_{b} \equiv 0\right)$ with a zero orientation angle $\theta_{b}$ between the reference time-of-flight axis and the molecular $b$ axis (the one bisecting the O-S-O bond angle, Fig. 1). The dependence of this signal on the release angle $\theta_{\text {rel }}$, included in $F_{\theta_{\text {rel }}}\left(\theta_{b}\right)$ as a parameter, is equivalent to the dependence on $\theta_{b}$ at a fixed $\theta_{\text {rel }} \equiv 0$, i.e., $F_{\theta_{\text {rel }}}(0) \equiv F_{0}\left(-\theta_{b}\right)$. In what follows, we investigate the latter distribution [hereafter referred to as $F\left(\theta_{b}\right)$ ] as a function of the centrifuge-toprobe delay time.

The observed time dependence of $F\left(\theta_{b}\right)$ is shown in Fig. 3(b). Truncating the centrifuge pulse in time enables us


FIG. 3. (a) Periodic revivals of the calculated two-dimensional alignment factor $\beta_{2 \mathrm{D}}=\left\langle\cos ^{2} \theta\right\rangle_{2 \mathrm{D}}-\frac{1}{2}$, determined from (b) the time evolution of the molecular in-plane angular distribution. (c) High resolution time scan around the alignment peak.
to control the final angular frequency of the centrifuged molecules, which in this case was set to $10^{13} \mathrm{rad} / \mathrm{s}$. Because of the centrifuge-induced planar alignment, the number of rotational degrees of freedom of the $\mathrm{SO}_{2}$ molecules is reduced to 1 and their dynamics becomes periodic, similar to the dynamics of a linear rotor. This periodicity, though not apparent from the coarse twodimensional scan, is clearly evident from the extracted alignment factor $\beta_{2 \mathrm{D}}=\left\langle\cos ^{2} \theta\right\rangle_{2 \mathrm{D}}-\frac{1}{2}$ (with $\langle\cdots\rangle_{2 \mathrm{D}}$ being the in-plane average and $\theta$ being measured from the axis of maximum, for a given delay, alignment), plotted in Fig. 3(a). Each peak corresponds to the field-free threedimensional alignment of $\mathrm{SO}_{2}$. We note that although the observed two-dimensional alignment factor in the plane of rotation is not much higher than its isotropic value of 0.5 , the strong molecular confinement to this plane results in rather high values of FF3DA. Using the lower and upper bounds of the achieved planar alignment extracted from the two VMI channels (as discussed above), we arrive at the corresponding estimates of $\left\langle\cos ^{2} \theta_{y b}\right\rangle$ of 0.40 and 0.49 (with $y$ being the axis perpendicular to the MCP plane). These values are comparable with the theoretical predictions for other methods of nonadiabatic three-dimensional alignment $[11,13]$.

The relatively small degree of the observed FF3DA stems from the adiabatic mechanism of the centrifuge spinning, which results in a low number of quantum rotational states in the excited wave packet. As we have shown in a recent work on linear rotors [26], a small number of participating states gives rise to long windows of classical-like rotation around the time of each revival, with the rotational frequency equal to the final frequency of the centrifuge. The same classical-like rotation was observed
here with $\mathrm{SO}_{2}$ molecules when we performed a fine time scan around any of the alignment peaks, as demonstrated in Fig. 3(c).

As expected for the effectively one-dimensional rotation, the alignment peaks are separated by half the revival period $T_{\text {rev }}=2 \pi \hbar\left(d^{2} E / d J^{2}\right)^{-1}$, where $E(J)$ is the rotational energy for a given rotational quantum number $J$ and $\hbar$ is the reduced Planck's constant [28,29]. Using the rigid rotor's energy spectrum $E(J)=\left(\hbar^{2} / 2 I\right) J(J+1)$, with $I$ being the molecular moment of inertia, one finds $T_{\text {rev }}=2 \pi I / \hbar$. At lower centrifuge frequencies, the experimentally detected revival period of 57 ps corresponds to $I=58 \AA^{2}$ in good agreement with the known value for the molecule's largest moment of inertia $I_{c}$ around the axis normal to its plane ( $c$ axis) [30]. These revivals, known as $C$-type transients [31] can be attributed to the beating between a few quantum states $|J, \tau=-J\rangle$, corresponding to the lowest energy for a given $J$.

At higher angular frequencies, the rising centrifugal forces stretch and bend the molecule, distorting the two S-O bonds and the angle between them. This causes the moment of inertia, and hence the revival period, to increase, as is evident from the experimental data in Fig. 4 (blue circles). To describe the effect of the centrifugal distortion on the revival period, we carried out the following classical calculations. For a given rotational state $J$, we minimized the total energy


FIG. 4. Revival period as a function of the rotational frequency of $\mathrm{SO}_{2}$, with the rotational quantum numbers shown along the upper horizontal axis. Experimental data (blue circles) are compared with the results of classical calculations, in which the potential energy surface (PES) is expanded to second and fourth order in the deformation coordinates (dashed and solid lines, respectively). The inset shows the dependence of $\beta_{2 D}$ on the pump-probe delay, used for calculating the revival time at the two angular frequencies $18.8 \mathrm{rad} / \mathrm{ps}$ (magenta) and $39.3 \mathrm{rad} / \mathrm{ps}$ (green), labeled with the correspondingly colored stars in the main plot. The solid lines represent experimental data, while the dashed lines show the fitting functions used to extract the revival period.

$$
E\left(J, r_{1}, r_{2}, \alpha\right)=\frac{\hbar^{2} J^{2}}{2 I_{c}\left(r_{1}, r_{2}, \alpha\right)}+V\left(r_{1}, r_{2}, \alpha\right)
$$

over the S-O bonds lengths $r_{1,2}$ and O-S-O angle $\alpha$. The potential energy surface (PES) $V$ of $\mathrm{SO}_{2}$ was expanded in a Taylor series up to fourth order in the deformations $\delta x_{i}=r_{1}-r_{e}, r_{2}-r_{e}, \alpha-\alpha_{e}$, where $r_{e}$ and $\alpha_{e}$ are the values of $r_{1,2}$ and $\alpha$ for the molecule at rest:

$$
\begin{aligned}
& V\left(r_{1}, r_{2}, \alpha\right) \\
& \quad= \\
& \quad V\left(r_{e}, r_{e}, \alpha_{e}\right)+\frac{1}{2} \sum_{i j} f_{i j} \delta x_{i} \delta x_{j} \\
& \quad+\frac{1}{6} \sum_{i j k} f_{i j k} \delta x_{i} \delta x_{j} \delta x_{k}+\frac{1}{24} \sum_{i j k l} f_{i j k l} \delta x_{i} \delta x_{j} \delta x_{k} \delta x_{l}
\end{aligned}
$$

with the corresponding force constants $f$ taken from Ref. [32]. We then determined the classical angular velocity and the revival period for a given $J$ as

$$
\omega(J)=[E(J+1)-E(J)] / \hbar
$$

and

$$
T_{\mathrm{rev}}=2 \pi \hbar[E(J-1)-2 E(J)+E(J+1)]^{-1}
$$

respectively. The results of these calculations are shown in Fig. 4. Expanding the PES to second order in the deformations $\delta x_{i}$ failed to explain the experimental observations at frequencies higher than $3 \times 10^{13} \mathrm{rad} / \mathrm{s}$ (dashed line). The quartic expansion, on the other hand, proved sufficient (solid line). At the highest achieved rotational frequencies of $4.4 \times 10^{13} \mathrm{rad} / \mathrm{s}$, the calculated bending angle and bond stretching reached $10^{\circ}$ and 10 nm , respectively. Both bonds were found to stretch by an equal amount, as could be anticipated from the symmetry of the system.

In summary, we demonstrated and studied a new mechanism of field-free alignment of asymmetric top molecules with an optical centrifuge. An intuitive classical picture has been presented to explain the observed behavior in the gas of sulfur dioxide. Owing to the adiabaticity of the centrifuge spinning, it leaves $\mathrm{SO}_{2}$ is left rotating with its O-S-O plane aligned with the plane of rotation long after the excitation pulse is gone. This planar alignment reduces the complex rotational dynamics of an asymmetric top to that of a simple linear rotor. Similarly to the latter, centrifuged $\mathrm{SO}_{2}$ molecules exhibit periodic revivals of the transient field-free three-dimensional alignment. The observed FF3DA stems from the slight deviation of the centrifuge action from being fully adiabatic. To enhance the degree of the three-dimensional alignment, one could add a short nonadiabatic rotational kick in the plane of the centrifuge-induced rotation. By measuring the revival period as a function of the rotational frequency, we examined the centrifugal distortion of $\mathrm{SO}_{2}$. At extreme
levels of rotational excitation, available with an optical centrifuge, the molecule bends by up to 10 deg. Both the planar alignment and the tuneable centrifugal bending add to the arsenal of laser-based tools for controlling molecular dynamics.

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[1] Y. Ohshima and H. Hasegawa, Int. Rev. Phys. Chem. 29, 619 (2010).
[2] S. Fleischer, Y. Khodorkovsky, E. Gershnabel, Y. Prior, and I. Sh. Averbukh, Isr. J. Chem. 52, 414 (2012).
[3] M. Lemeshko, R. V. Krems, J. M. Doyle, and S. Kais, Mol. Phys. 111, 1648 (2013).
[4] H. Stapelfeldt and T. Seideman, Rev. Mod. Phys. 75, 543 (2003).
[5] T. Seideman and E. Hamilton, Adv. At. Mol. Opt. Sci. 52, 289 (2005).
[6] V. Kumarappan, S. S. Viftrup, L. Holmegaard, C. Z. Bisgaard, and H. Stapelfeldt, Phys. Scr. 76, C63 (2007).
[7] M. Artamonov and T. Seideman, J. Chem. Phys. 128, 154313 (2008).
[8] M. Artamonov and T. Seideman, Mol. Phys. 110, 885 (2012).
[9] J. J. Larsen, K. Hald, N. Bjerre, H. Stapelfeldt, and T. Seideman, Phys. Rev. Lett. 85, 2470 (2000).
[10] H. Tanji, S. Minemoto, and H. Sakai, Phys. Rev. A 72, 063401 (2005).
[11] J. G. Underwood, B. J. Sussman, and A. Stolow, Phys. Rev. Lett. 94, 143002 (2005).
[12] K. F. Lee, D. M. Villeneuve, P. B. Corkum, A. Stolow, and J. G. Underwood, Phys. Rev. Lett. 97, 173001 (2006).
[13] A. Rouzée, S. Guérin, O. Faucher, and B. Lavorel, Phys. Rev. A 77, 043412 (2008).
[14] S. Pabst and R. Santra, Phys. Rev. A 81, 065401 (2010).
[15] X. Ren, V. Makhija, and V. Kumarappan, Phys. Rev. Lett. 112, 173602 (2014).
[16] S. S. Viftrup, V. Kumarappan, S. Trippel, H. Stapelfeldt, E. Hamilton, and T. Seideman, Phys. Rev. Lett. 99, 143602 (2007).
[17] S. S. Viftrup, V. Kumarappan, L. Holmegaard, C. Z. Bisgaard, H. Stapelfeldt, M. Artamonov, E. Hamilton, and T. Seideman, Phys. Rev. A 79, 023404 (2009).
[18] M. D. Poulsen, E. Péronne, H. Stapelfeldt, C. Z. Bisgaard, S. S. Viftrup, E. Hamilton, and T. Seideman, J. Chem. Phys. 121, 783 (2004).
[19] L. Holmegaard, S. S. Viftrup, V. Kumarappan, C. Z. Bisgaard, H. Stapelfeldt, E. Hamilton, and T. Seideman, Phys. Rev. A 75, 051403 (2007).
[20] L. S. Spector, M. Artamonov, S. Miyabe, T. Martinez, T. Seideman, M. Guehr, and P. H. Bucksbaum, Nat. Commun. 5, 3190 (2014).
[21] J. Karczmarek, J. Wright, P. B. Corkum, and M. Yu. Ivanov, Phys. Rev. Lett. 82, 3420 (1999).
[22] D. M. Villeneuve, S. A. Aseyev, P. Dietrich, M. Spanner, M. Yu. Ivanov, and P. B. Corkum, Phys. Rev. Lett. 85, 542 (2000).
[23] L. Yuan, S. W. Teitelbaum, A. Robinson, and A. S. Mullin, Proc. Natl. Acad. Sci. U.S.A. 108, 6872 (2011).
[24] A. Korobenko, A. A. Milner, and V. Milner, Phys. Rev. Lett. 112, 113004 (2014).
[25] A. Korobenko and V. Milner, J. Phys. B 48, 164004 (2015).
[26] A. Korobenko, A. A. Milner, J. W. Hepburn, and V. Milner, Phys. Chem. Chem. Phys. 16, 4071 (2014).
[27] A. Hishikawa, A. Iwamae, K. Hoshina, M. Kono, and K. Yamanouchi, Chem. Phys. Lett. 282, 283 (1998).
[28] I. Sh. Averbukh and N. F. Perelman, Phys. Lett. A 139, 449 (1989).
[29] T. Seideman, Phys. Rev. Lett. 83, 4971 (1999).
[30] G. Herzberg, Molecular Spectra \& Molecular Structure III (Polyatomic Molecules) (D. Van Nostrand Company, Inc., Princeton, New Jersey, 1966).
[31] P. W. Joireman, L. L. Connell, S. M. Ohline, and P. M. Felker, J. Chem. Phys. 96, 4118 (1992).
[32] J. M. L. Martin, J. Chem. Phys. 108, 2791 (1998).

